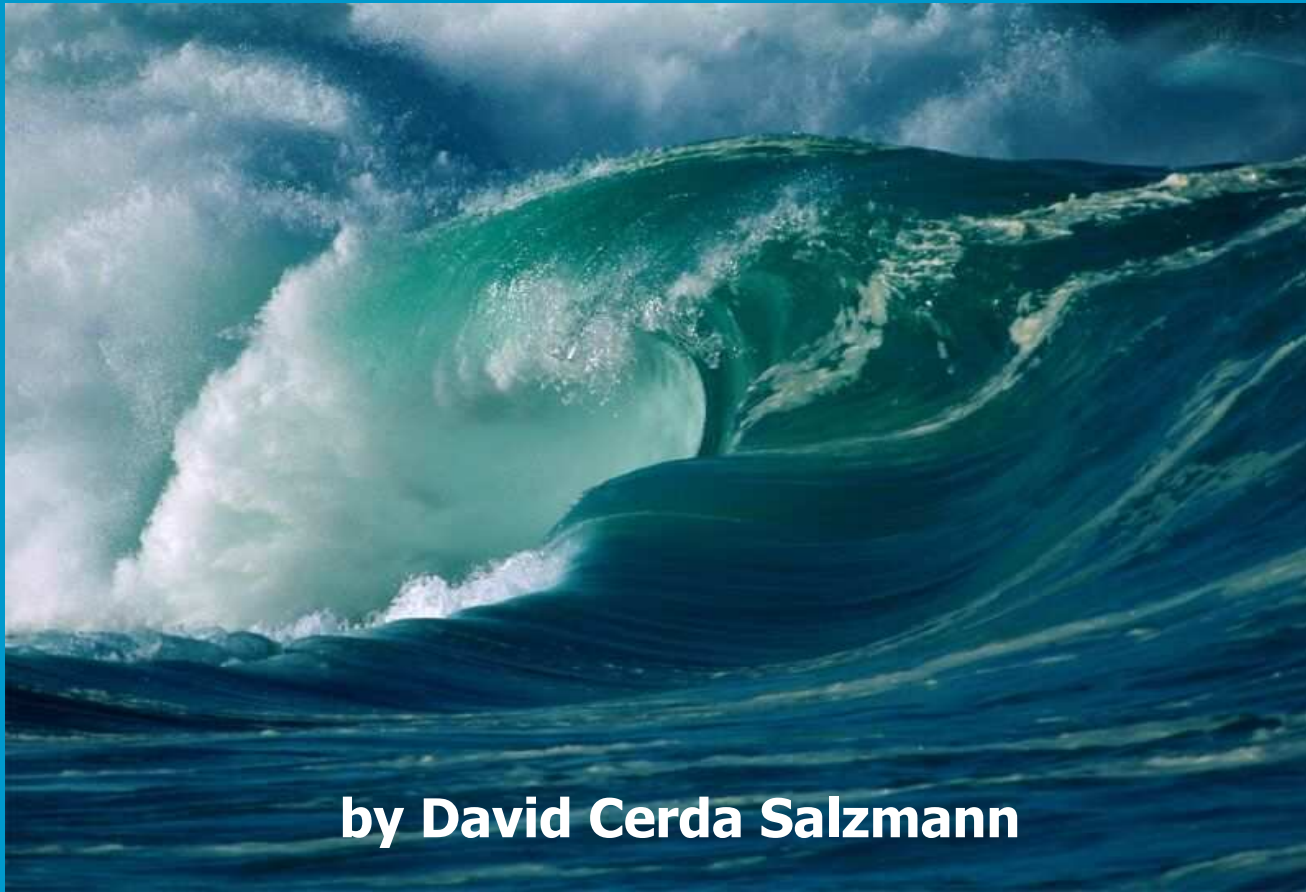
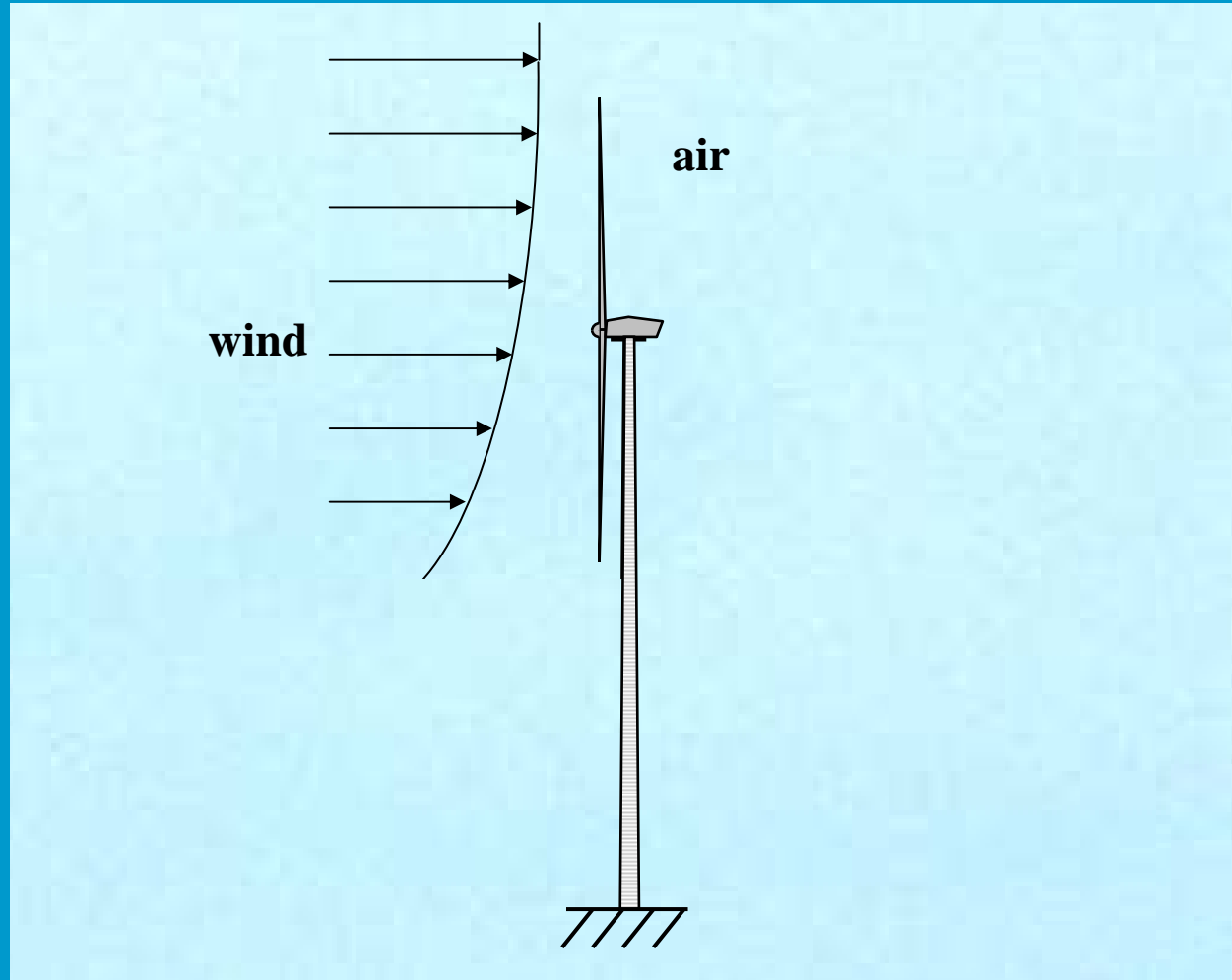


Waves & Current

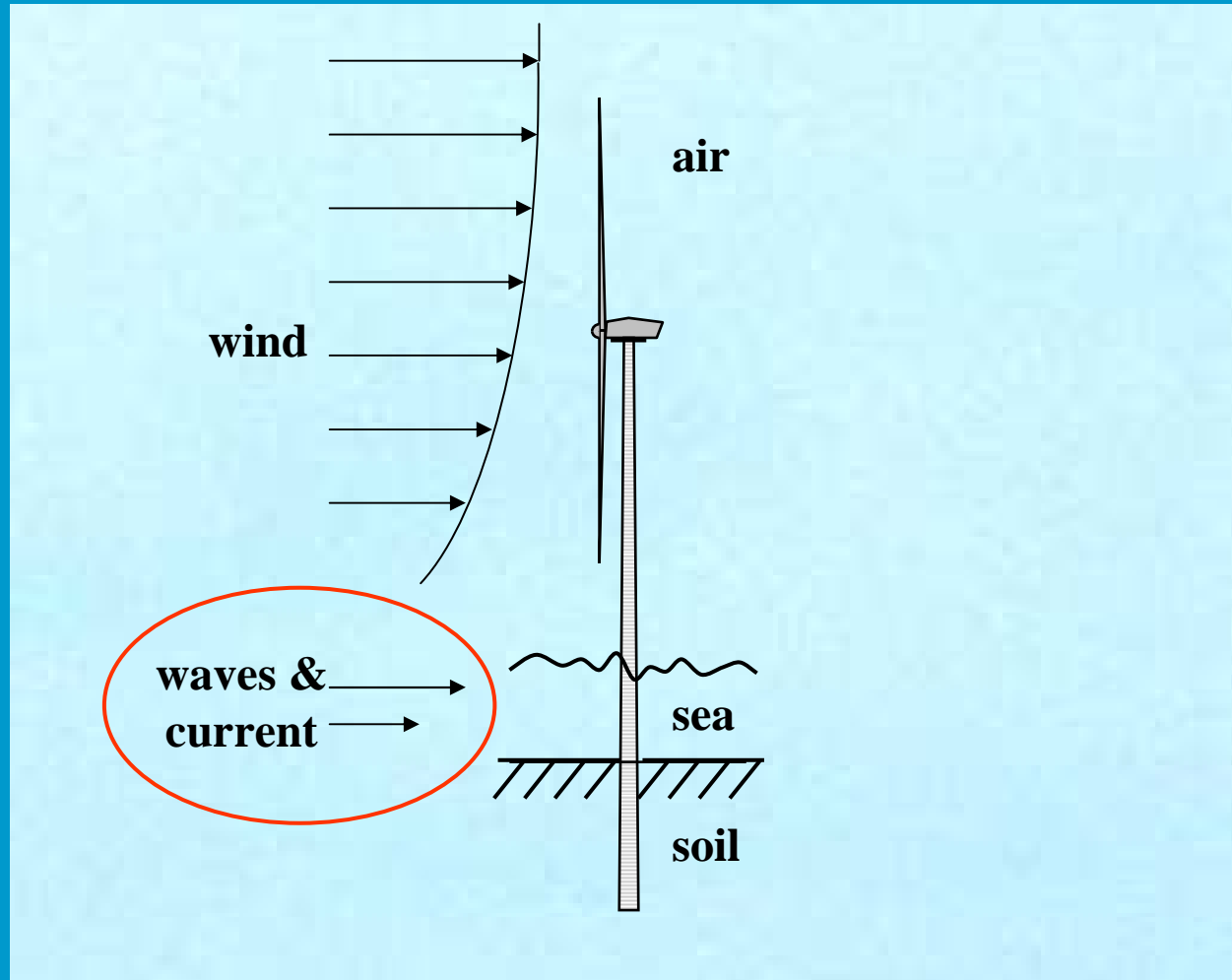


by David Cerda Salzmänn

Environmental Loads: Onshore



Environmental Loads: Offshore



Waves

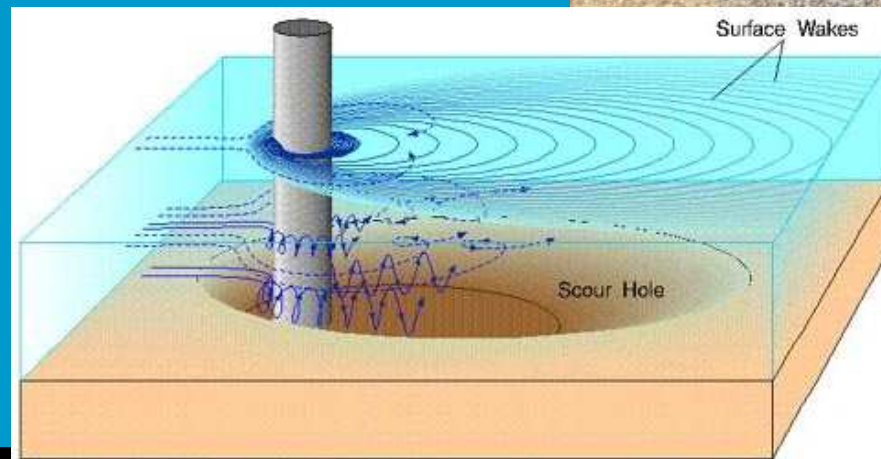
Consider waves for:

- Extremes
- Fatigue
- Installation & Maintenance

Current

Consider current for:

- Extremes
- Fatigue
- Installation & Maintenance
- Scour



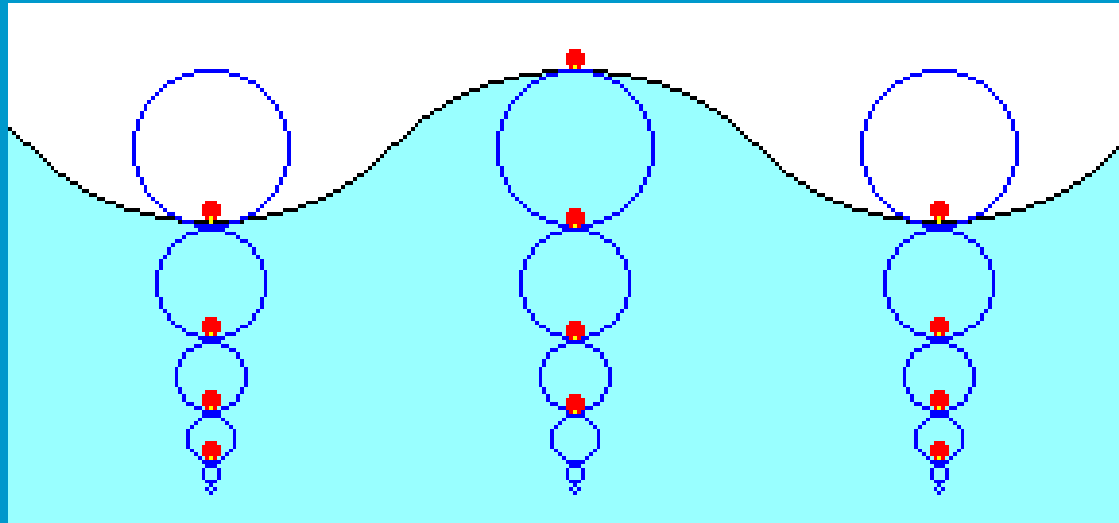
In this lecture...

- What data do you need
- What do you use it for
- Next hour: where to get data from

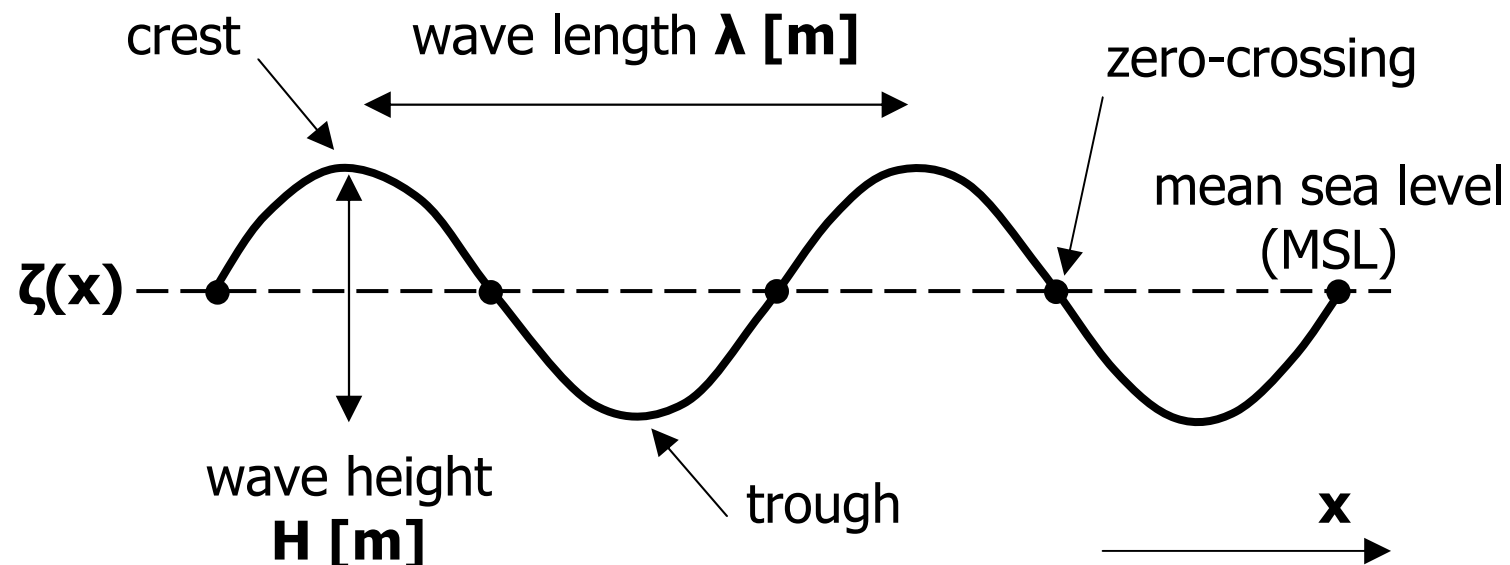
Ocean Surface Waves

Definition:

“Perturbations that propagate through water”

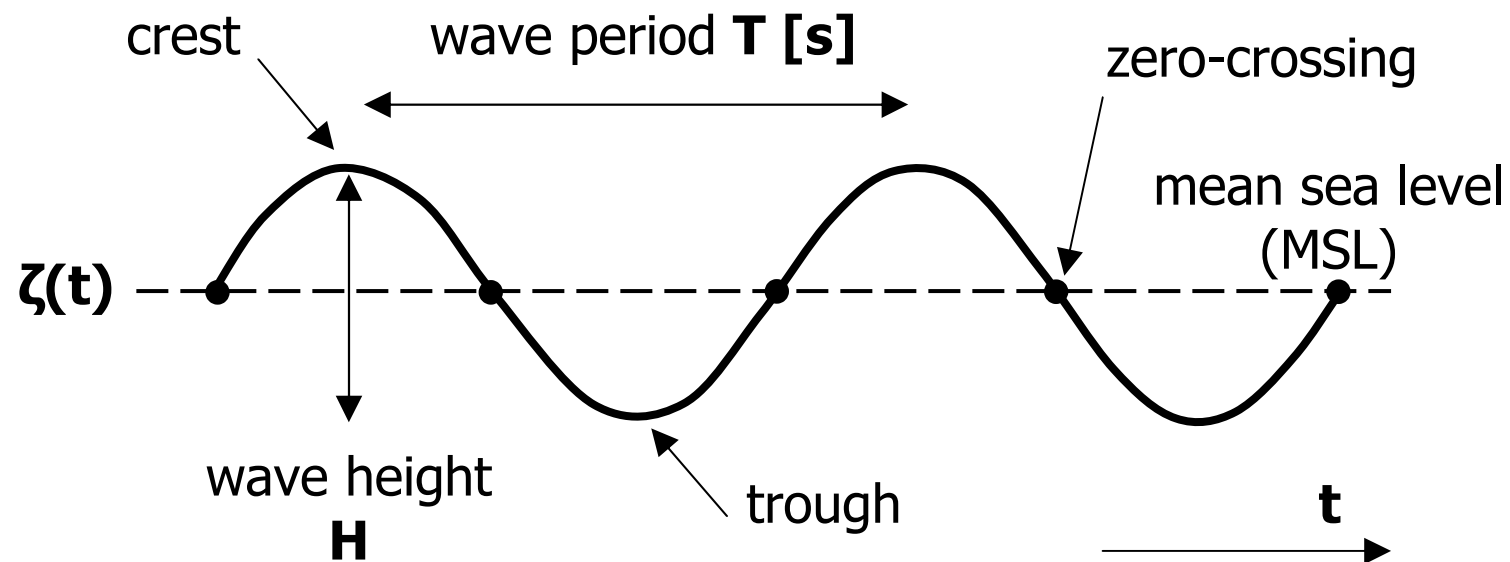


Regular Waves



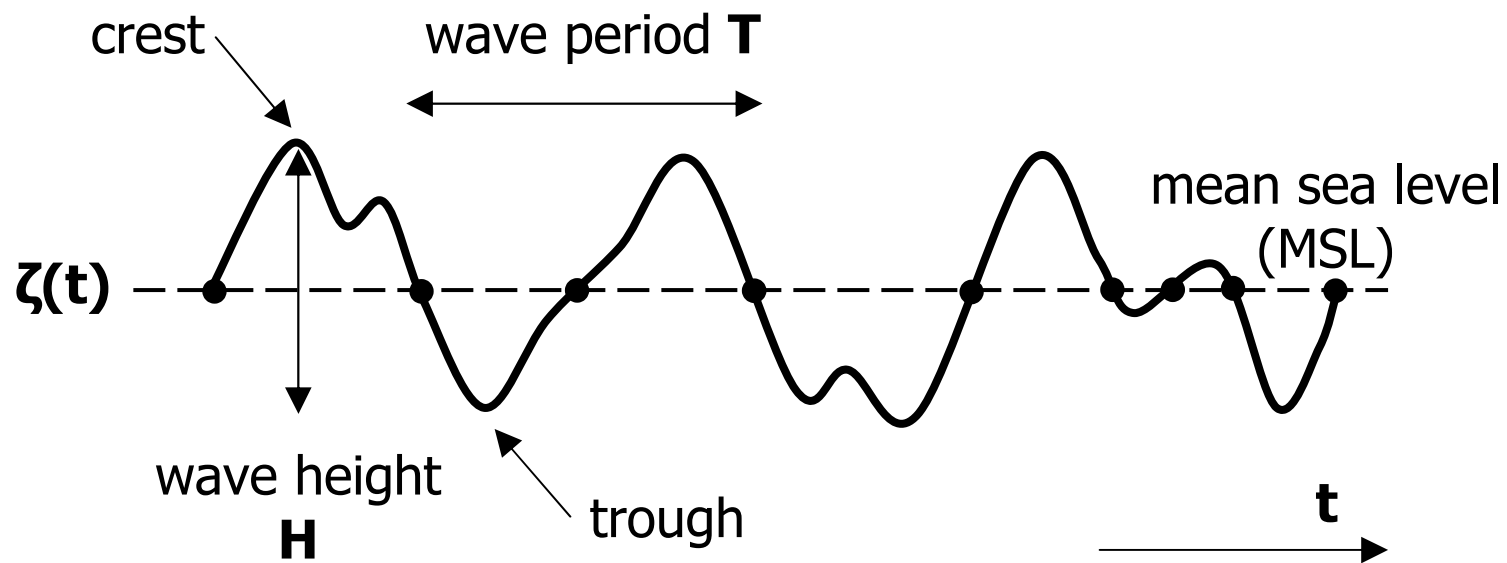
snap shot: $t = \text{fixed}$

Regular Waves



time history: $x=\text{fixed}$

Irregular Waves



time history: $x=\text{fixed}$

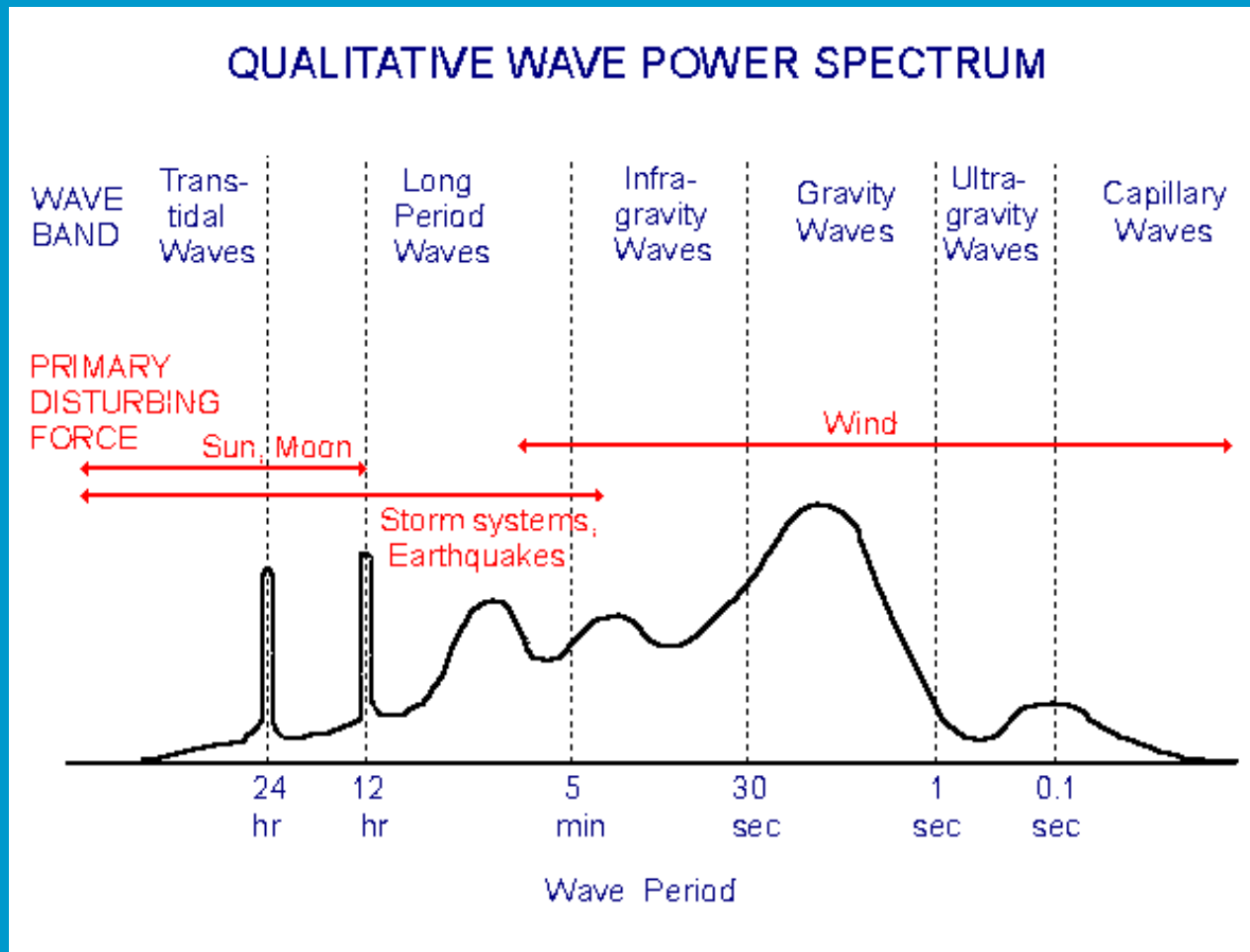
Irregular Waves

T_z = Mean zero (up/down)-crossing period [s]

H_s = Significant wave height [m]

"Average of highest 1/3 of the waves in the record."

Wind Waves

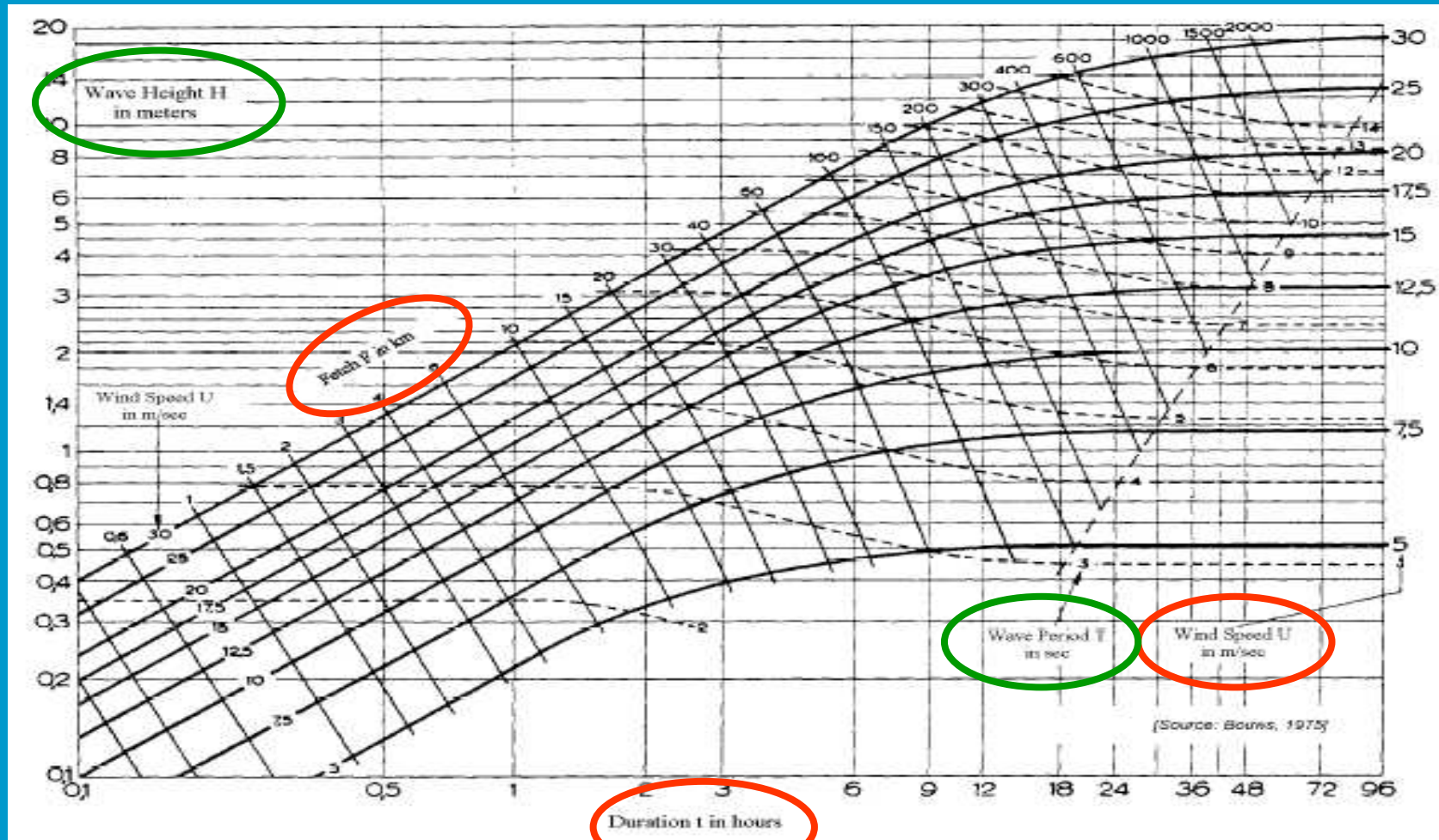


Wind Waves

Wave generation influenced by:

- Wind speed
- Fetch: distance over which the waves have travelled under that wind field
- Duration of the wind speed

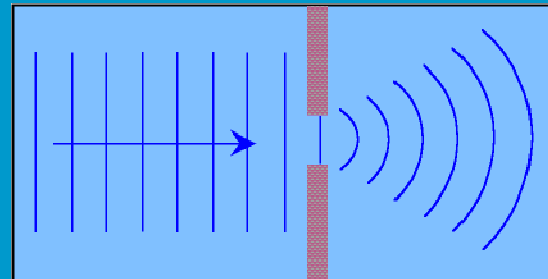
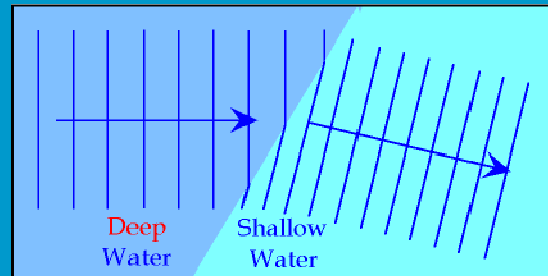
Wind Waves



Wind Waves

Wave characteristics influenced by:

- Refraction
- Diffraction
- Breaking Waves



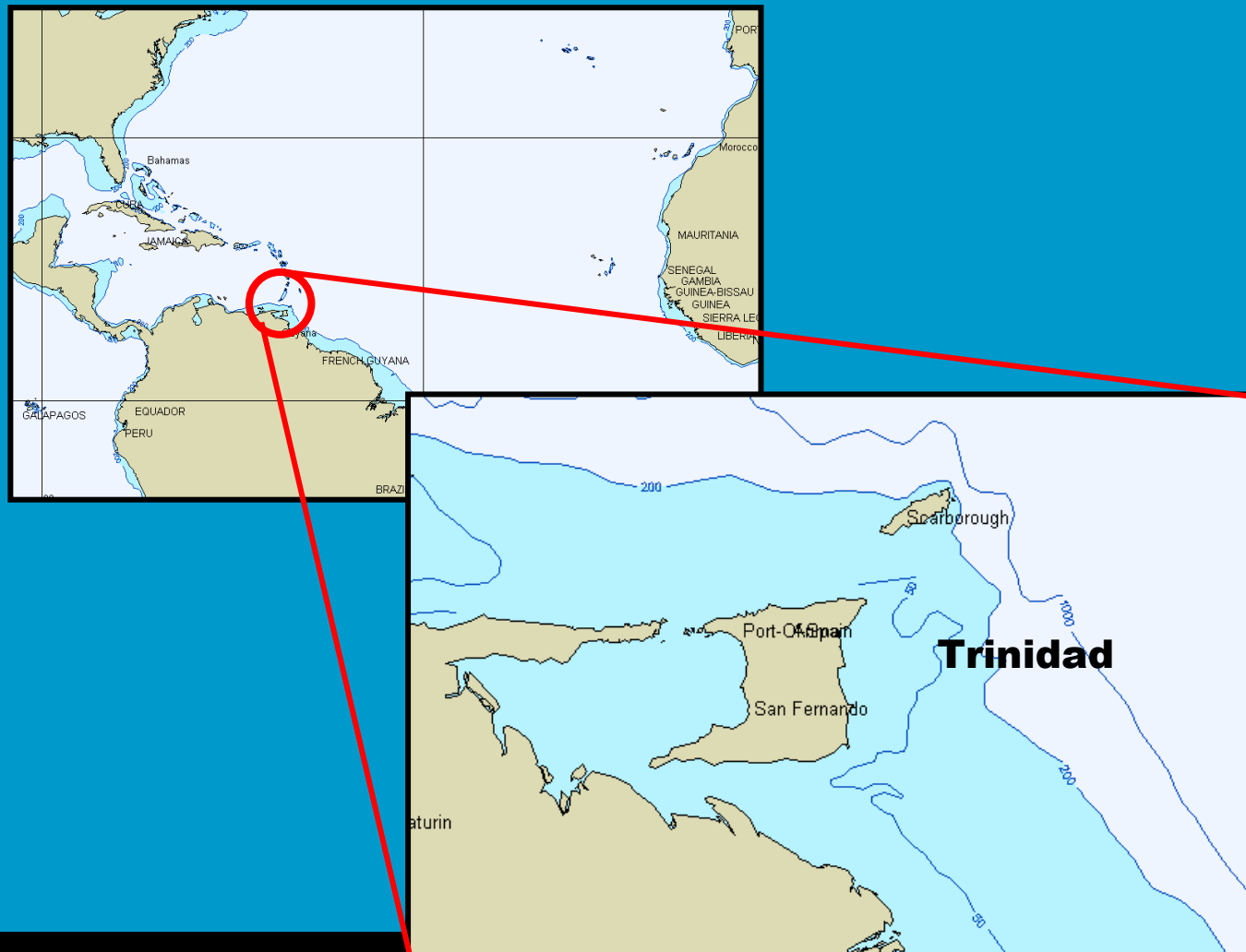
$$H \leq 0.78 * d$$

Wind Waves

SO:

Look at the map and use common sense!

Wind Waves



Wind Waves Resuming

The development of wind waves requires:

- Wind speed
- Fetch
- Time
- Water Depth

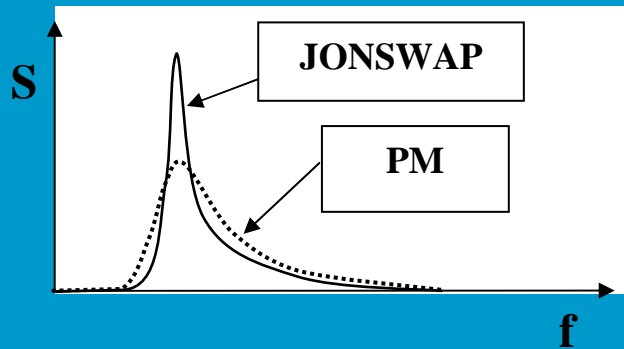
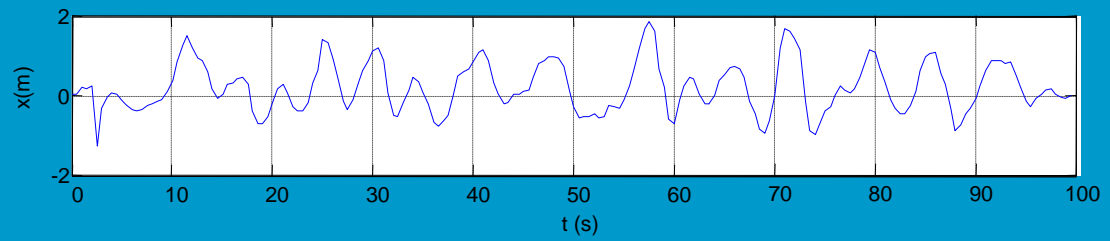
Wave Statistics

Required for Simulations & Calculations

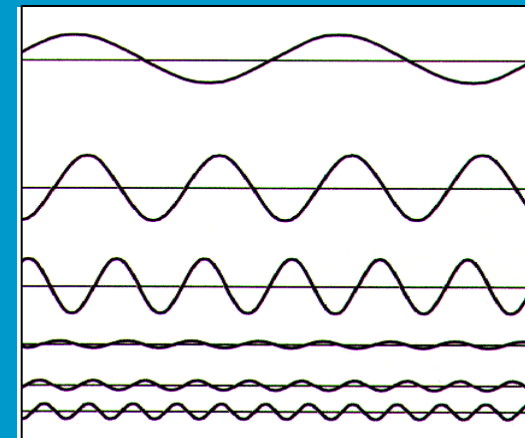
- Short term 3 hours
- Long term year(s)

Short term statistics

Wave Time Series:
Irregular!



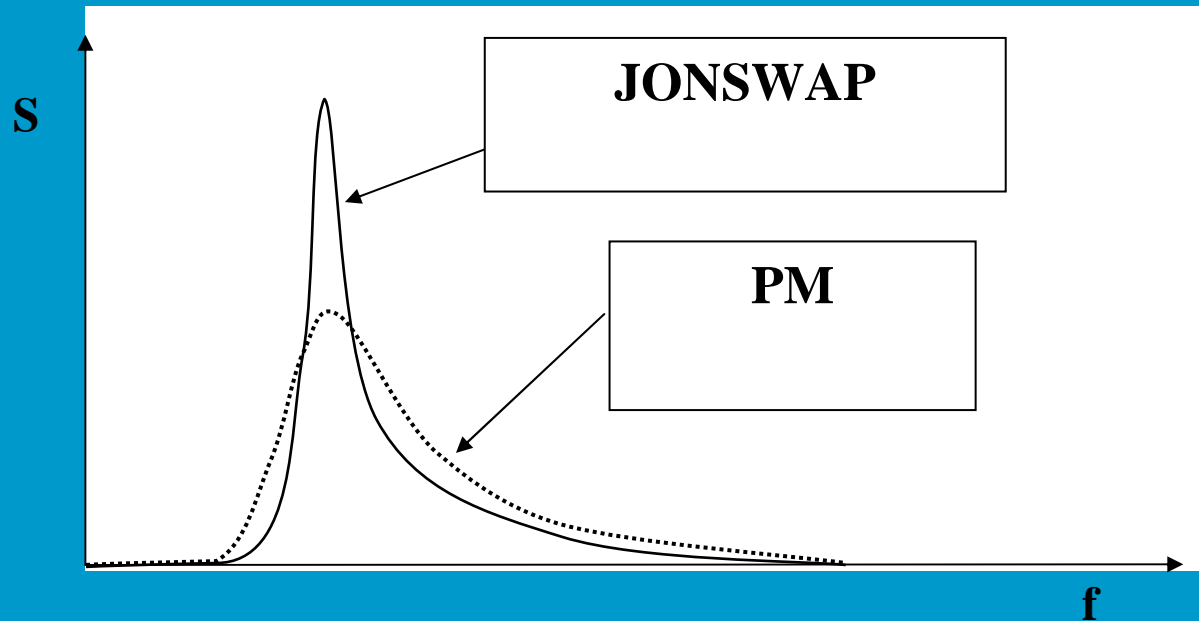
Wave Spectrum:
Statistical representation of
3-hour sea state



Series of regular waves

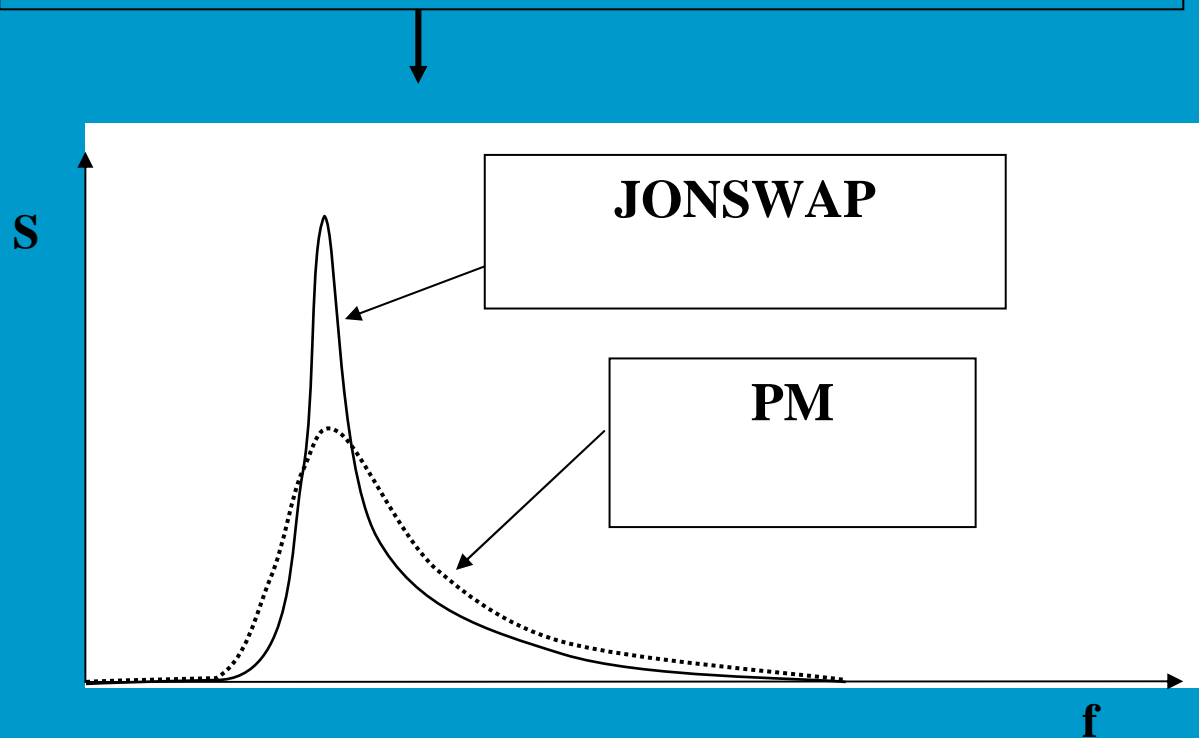
Short term statistics

JONSWAP: Fetch limited
Pierson-Moskowitz: Fully developed sea

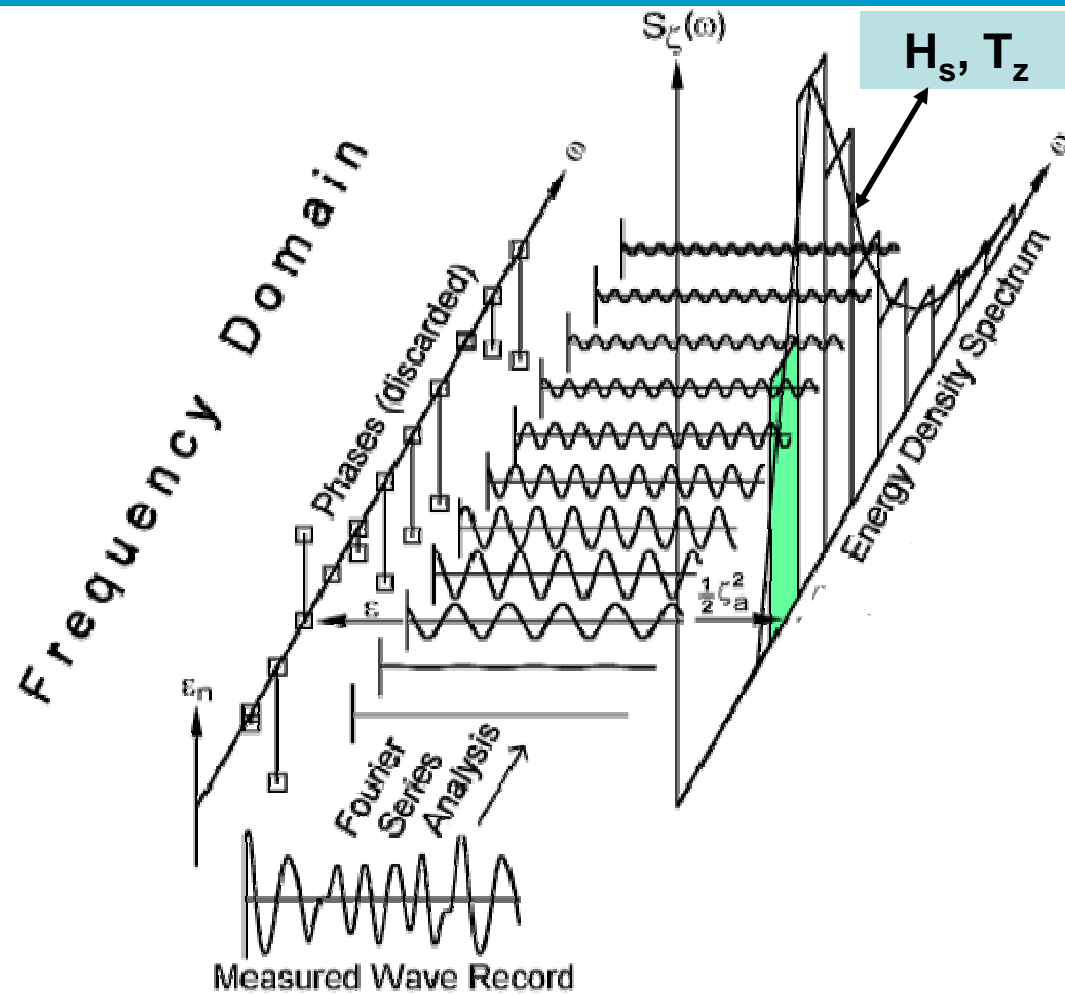


Short term statistics

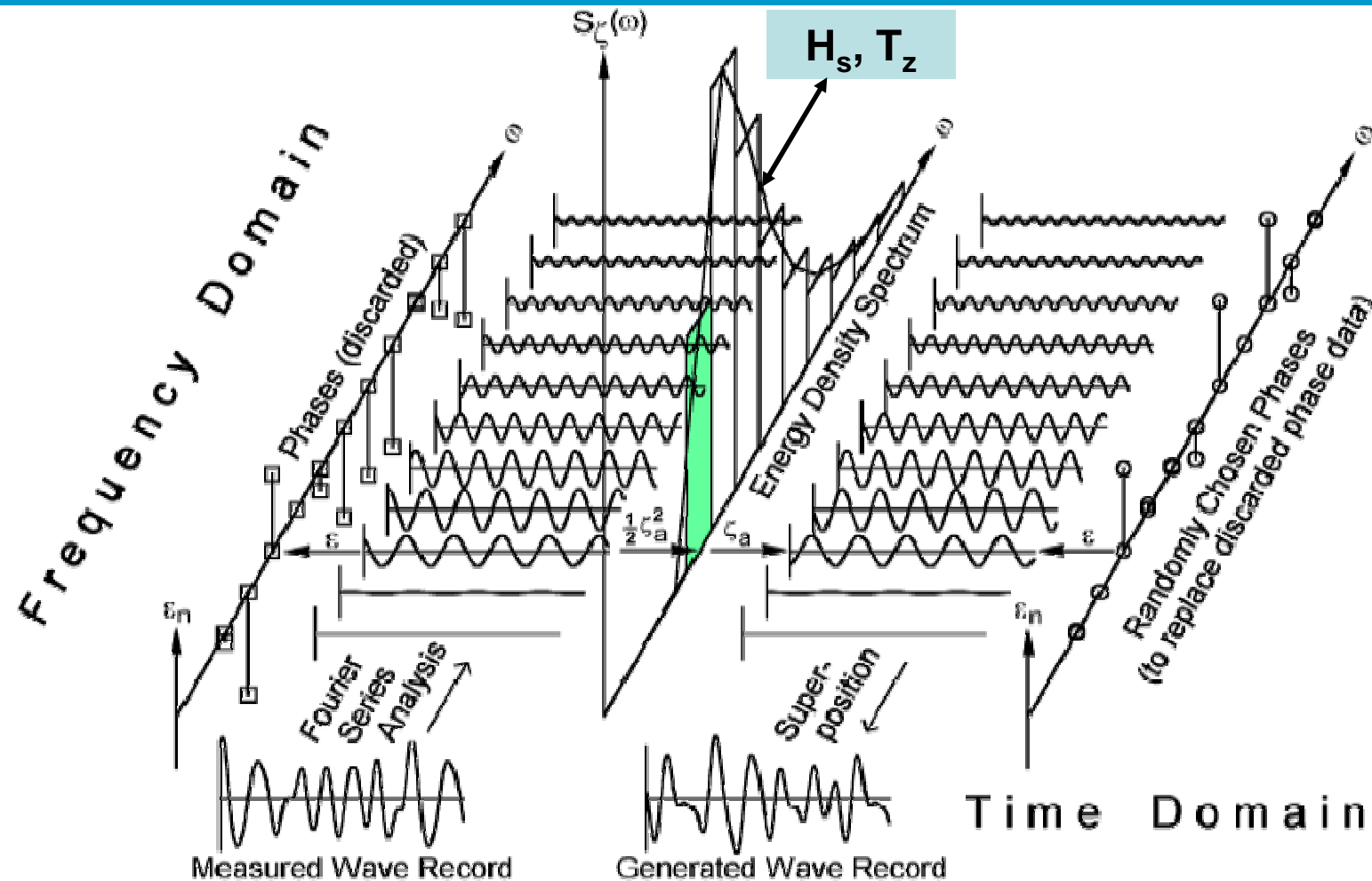
H_s = Significant Wave Height [m]
 T_z = Mean Zero Crossing Period [s]



Short term statistics



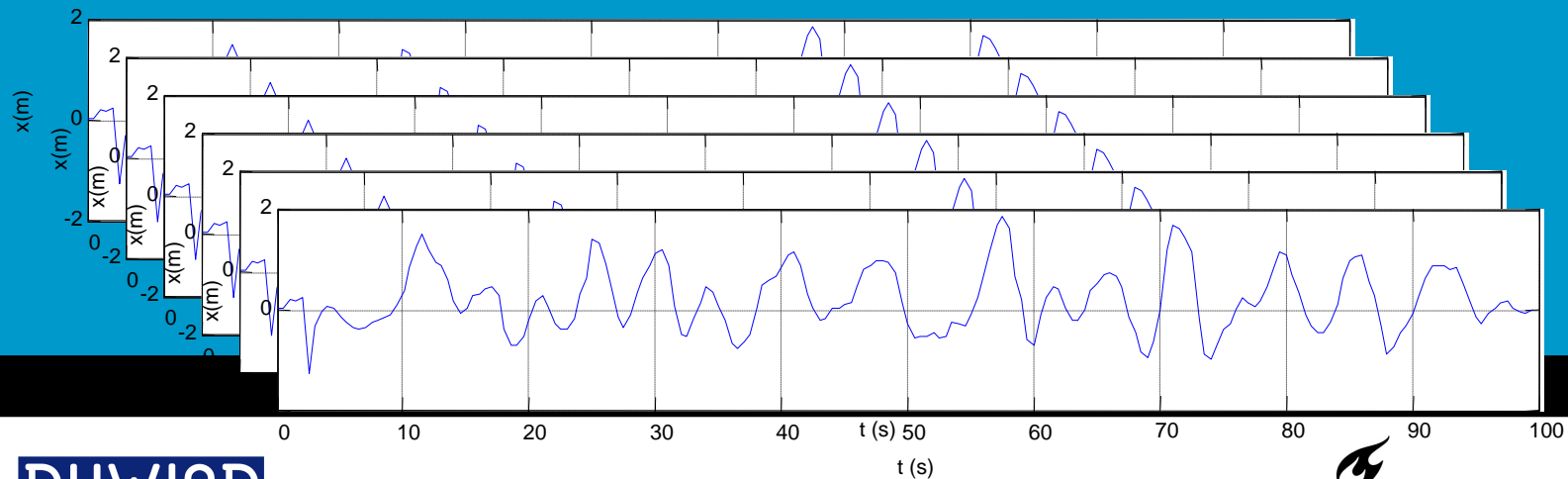
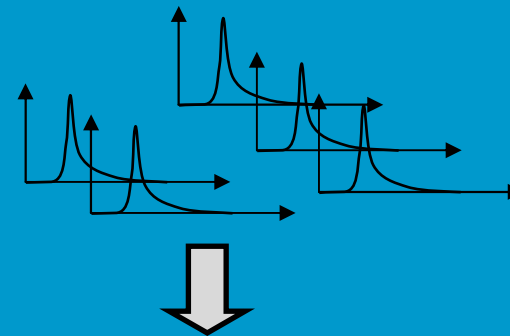
Short term statistics



Long term statistics

So: Wave scatter diagram is the long-term statistical representation of sea states

H_s [m]	T_z [s]	0 - 1	1 - 2	2 - 3	3 - 4	4 - 5	5 - 6	6 - 7	7 - 8	Sum:
6.5 - 7.0										0
6.0 - 6.5								0.1	0.1	0.1
5.5 - 6.0							0.1	0.1	0.1	0.2
5.0 - 5.5							0.1	0.1	0.1	0.2
4.5 - 5.0							1			1
4.0 - 4.5							4			4
3.5 - 4.0							4	5		9
3.0 - 3.5							19	0.1		19.1
2.5 - 3.0						0.1	38			38.1
2.0 - 2.5						27	43			70
1.5 - 2.0				0.1	115	5				120.1
1.0 - 1.5				6	220	1				227
0.5 - 1.0				236	145	1				382
0.0 - 0.5	1		1	113	14	0.1	0.1			129.2
sum:		1	0	1	355.1	521.1	111.1	10.4	0.3	1000



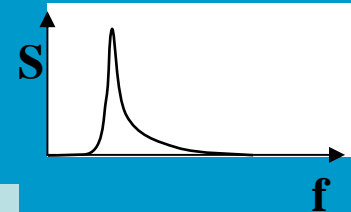
Environmental Data

Scatter diagram gives the wave data:

- Over a certain period
- For a certain location

Long term statistics

Wave scatter diagram



H_s [m]	T_z [s]	0 - 1	1 - 2	2 - 3	3 - 4	4 - 5	5 - 6	6 - 7	7 - 8	Sum:
6.5 - 7.0										0
6.0 - 6.5									0.1	0.1
5.5 - 6.0								0.1	0.1	0.2
5.0 - 5.5								0.1	0.1	0.2
4.5 - 5.0								1		1
4.0 - 4.5								4		4
3.5 - 4.0							4	5		9
3.0 - 3.5							19	0.1		19.1
2.5 - 3.0						0.1	38			38.1
2.0 - 2.5						27	43			70
1.5 - 2.0					0.1	115	5			120.1
1.0 - 1.5					6	220	1			227
0.5 - 1.0					236	145	1			382
0.0 - 0.5		1		1	113	14	0.1	0.1		129.2
sum:		1	0	1	355.1	521.1	111.1	10.4	0.3	1000

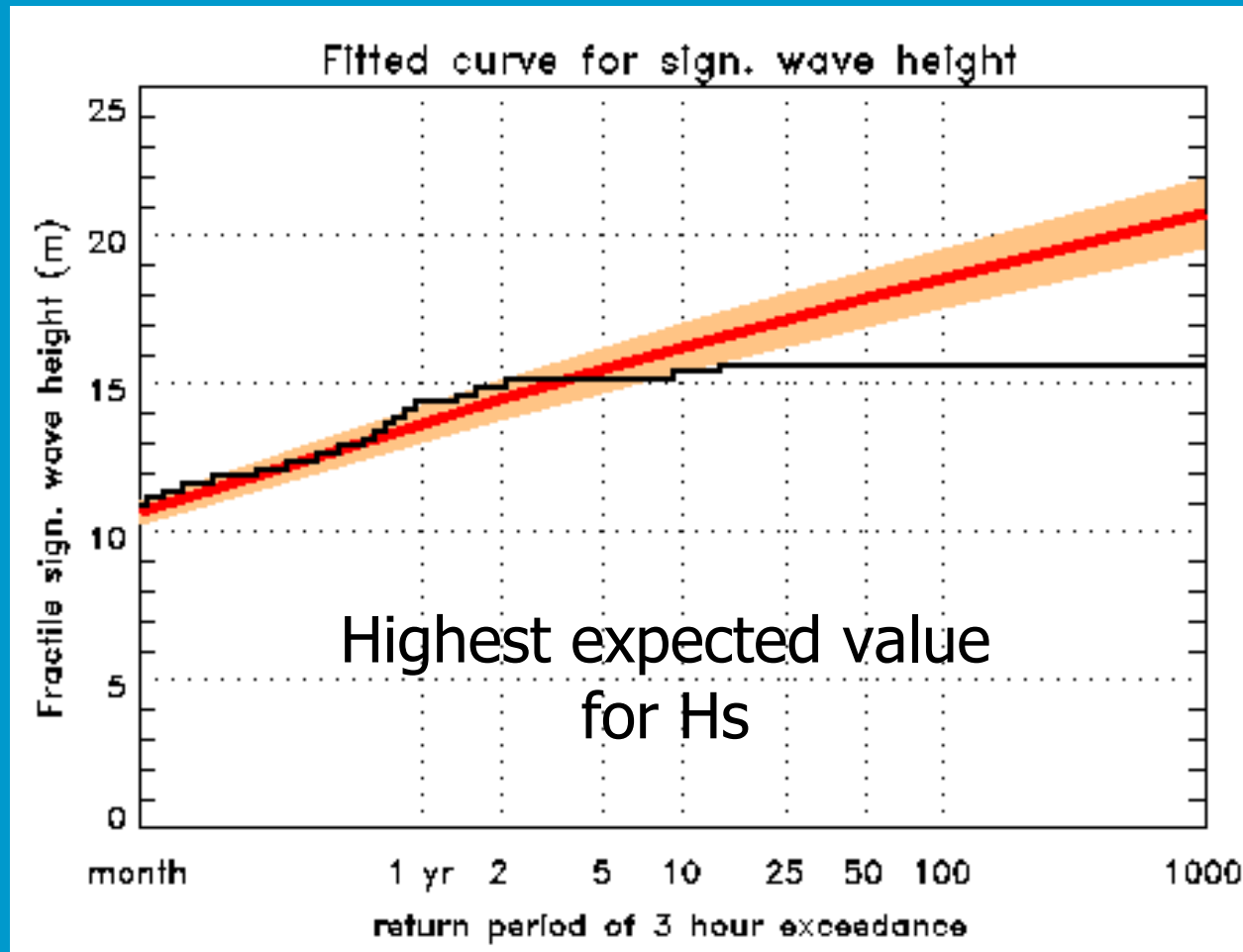
Extreme wave height

Wave scatter diagram

H _s [m]	T _z [s]	0 - 1	1 - 2	2 - 3	3 - 4	4 - 5	5 - 6	6 - 7	7 - 8	Sum:
6.5 - 7.0										0
6.0 - 6.5									0.1	0.1
5.5 - 6.0								0.1	0.1	0.2
5.0 - 5.5								0.1	0.1	0.2
4.5 - 5.0								1		1
4.0 - 4.5								4		4
3.5 - 4.0							4	5		9
3.0 - 3.5							19	0.1		19.1
2.5 - 3.0						0.1	38			38.1
2.0 - 2.5						27	43			70
1.5 - 2.0					0.1	115	5			120.1
1.0 - 1.5					6	220	1			227
0.5 - 1.0					236	145	1			382
0.0 - 0.5		1		1	113	14	0.1	0.1		129.2
sum:		1	0	1	355.1	521.1	111.1	10.4	0.3	1000

Chance of occurrence

Extreme wave height



Extreme wave height

Largest wave during lifetime:

From Rayleigh probability density function

or

$$H_{max} \approx 1.86 * H_s$$

or

$$H_{max} = 0.78 * d$$

Extreme wave height

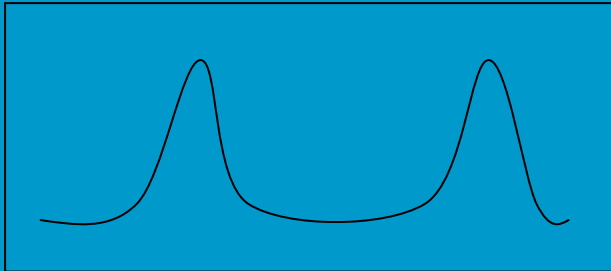
Extreme wave height known
add period to wave height:

$$T_{\min} = 2.46 \sqrt{H_{\max}} \quad \text{steepness} \quad (1:9.5)$$

$$T_{\max} = 3.70 \sqrt{H_{\max}} \quad (1:21)$$

Extreme wave height

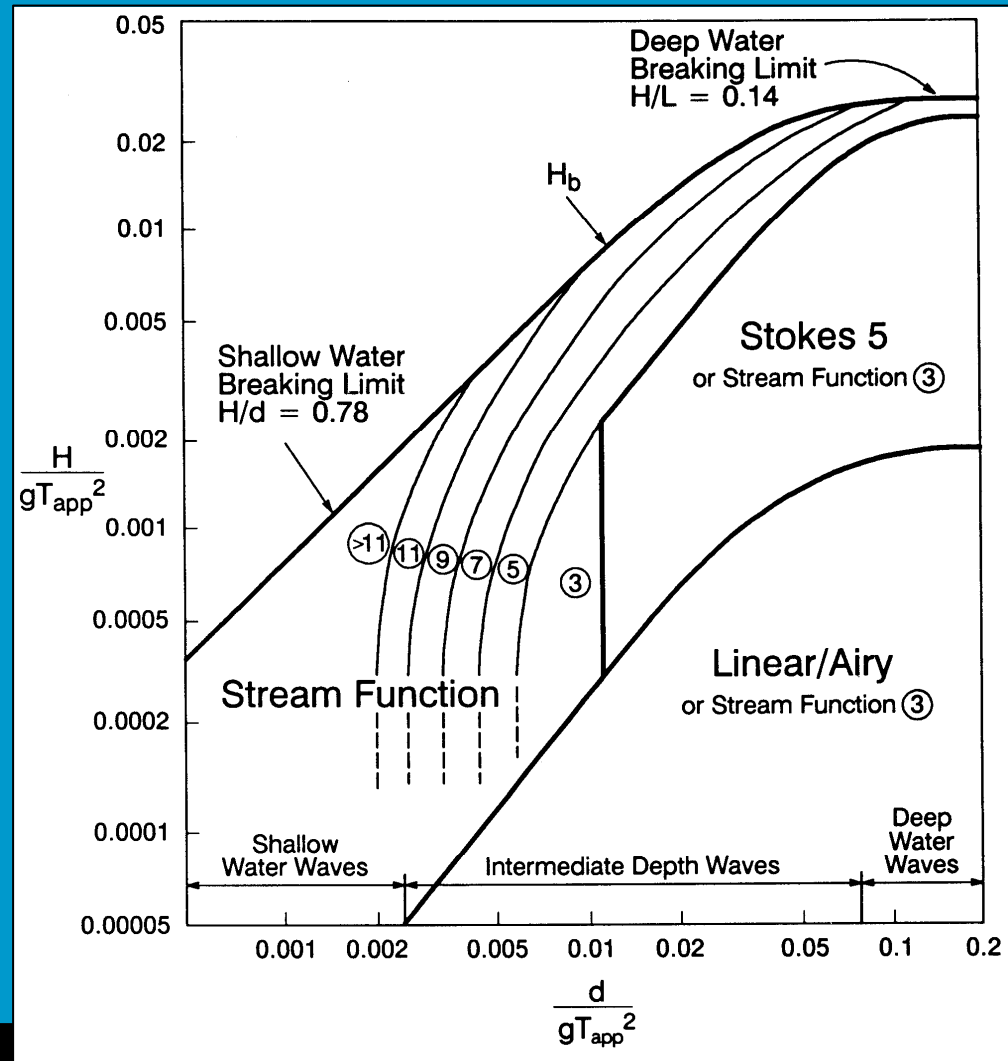
Wave form:



Wave theory



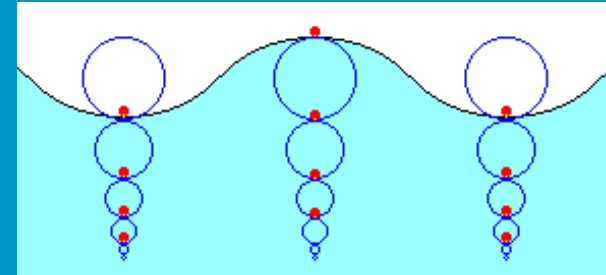
Water particle
velocities and
accelerations



Extreme wave height

For Example:

Linear/Airy Wave theory:



$$u_n(z,t) = \zeta_{a,n} \cdot \omega_n \cdot \frac{\cosh k_n(z+d)}{\sinh k_n d} \cdot \sin(\omega_n t + \varepsilon_n)$$

$$\dot{u}_n(z,t) = \zeta_{a,n} \cdot \omega_n^2 \cdot \frac{\cosh k_n(z+d)}{\sinh k_n d} \cdot \cos(\omega_n t + \varepsilon_n)$$

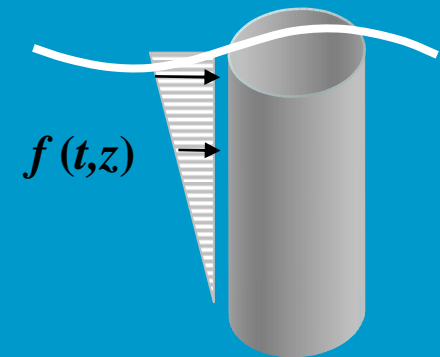
Extreme wave height

Finally determine loads:
the Morison Equation

$$f(t, z) = C_m \cdot \frac{1}{4} \rho \pi D^2 \cdot \dot{u} + C_d \cdot \frac{1}{2} \rho D \cdot |u| u$$

acceleration \nearrow velocity \nearrow

- Unit: [N/m]
- Vertically distributed load along pile



Resuming

- Extreme Wave Load
- From Extreme Maximum Wave Height H_{\max}
- From Extreme Significant Wave Height H_s
- From Scatter Diagram

Fatigue

Scatter diagrams: waves and wind



Environmental conditions during entire lifetime



All loads during entire lifetime



All stress variations during entire lifetime

Fatigue

$H_S - V_W$

$H_S - T_Z$

	lower	00	04	05	06	07	08	09	10	11	12	0	0	0	0	0
lower	upper	04	05	06	07	08	09	10	11	12	13	0	0	0	0	0
00	01	0	0.2	0	0.5	0	0	0	0	13	14	0	0	0	0	0
01	02	0	2.0	6.0	6.4	1.8	0.7	0	0	14	15	0	0	0	0	0
02	03	0	0	9.1	9.1	3.6	3.1	0	0	15	16	0	0	0	0	0
03	04	0	0	0.5	12.2	8.6	1.8	1.1	0	16		0	0	0	0	0
04	05	0	0	0	1.1	6.6	2.0	0	0	total		1.8	4.1	10.2	16.1	19.8
05	06	0	0	0	0	4.2	3.1	1.3	0.4	0	0.2	0	0	0	0	9.2
06	07	0	0	0	0	0.2	3.5	2.2	0	0	0	0	0	0	0	5.9
07	08	0	0	0	0	0	1.8	1.3	0.2	0	0	0	0	0	0	3.3
08	09	0	0	0	0	0	0	1.6	0	0	0	0	0	0	0	1.6
09	10	0	0	0	0	0	0	0.2	0.2	0	0	0	0	0	0	0.4
10	11	0	0	0	0	0	0	0	0	0.4	0	0	0	0	0	0.4
11	12	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0
12	13	0	0	0	0	0	0	0	0	0	0.2	0	0	0	0	0.2
13		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0
total		0.0	2.2	15.6	29.3	25.0	16.0	9.3	1.4	0.8	0.2	0.0	0.2	0.0	0.0	

	lower	00	02	04	06	08	10	12	14	16	18	20	22	24	
lower	upper	02	04	06	08	10	12	14	16	18	20	22	24		total
00	01	0.1	0.1	0.3	0.1	0.0	0	0	0	0	0	0	0	0	0.6
01	02	1.0	2.0	4.6	4.5	2.0	0.3	0.0	0	0	0	0	0	0	14.4
02	03	0.6	1.5	3.7	7.1	8.7	4.7	1.3	0.1	0.0	0.0	0	0	0	27.7
03	04	0.1	0.4	1.2	3.2	5.1	6.2	4.1	1.0	0.3	0.0	0	0	0	21.6
04	05	0.0	0.1	0.4	1.0	2.9	3.7	4.1	2.3	0.7	0.1	0.0	0.0	0	15.3
05	06	0	0.0	0.0	0.2	0.9	1.6	2.5	2.7	1.4	0.2	0.0	0	0	9.5
06	07	0	0	0.0	0.0	0.2	0.4	0.8	1.3	1.2	0.4	0.0	0	0	4.3
07	08	0	0	0	0.0	0.0	0.2	0.3	0.6	1.1	0.6	0.1	0	0	2.9
08	09	0	0	0	0	0.0	0.0	0.1	0.2	0.8	0.6	0.1	0	0	1.8
09	10	0	0	0	0	0	0.0	0.0	0.1	0.3	0.3	0.1	0	0	0.8
10	11	0	0	0	0	0	0	0.0	0.0	0.1	0.1	0.0	0	0	0.2
11	12	0	0	0	0	0	0	0.0	0.0	0.0	0.1	0.1	0.0	0	0.2
12	13	0	0	0	0	0	0	0.0	0.0	0.0	0.1	0.0	0.0	0	0.1
13	14	0	0	0	0	0	0	0	0	0	0.0	0.0	0.0	0	0.0
14	15	0	0	0	0	0	0	0	0	0	0.0	0.0	0	0	0.0
15	16	0	0	0	0	0	0	0	0	0	0	0.0	0	0	0.0
16		0	0	0	0	0	0	0	0	0	0	0	0	0	0.0
total		1.8	4.1	10.2	16.1	19.8	17.1	13.2	8.3	5.9	2.5	0.4	0.0	0.0	

Fatigue

$$H_s - T_z - V_w$$

93 states

Hs	Tz		< 3.0	3.0 - 4.0	4.0 - 5.0	5.0 - 6.0	6.0 - 7.0	7.0 - 8.0	8.0 - 9.0	9.0 - 10.0	10.0-11.0	
>4.0	17.5						0.2	0.7		0.4		1.3
	15						0.3	0.6				0.9
	12.5						0.4	0.4				0.8
3.5 - 4.0	17.5						0.7	0.4				1.1
	15						0.9					0.9
	12.5						1.0					1.0
3.0 - 3.5	17.5					0.2	1.4					1.6
	15					0.3	1.2					1.5
	12.5					0.4	0.9					1.3
2.5 - 3.0	17.5					1.1		0.9				2.0
	15					2.0	0.2					2.2
	12.5					3.0						3.0
	10					0.3						0.3
2.0 - 2.5	17.5					2.5	0.5					3.0
	15					3.0	0.4					3.4
	12.5					4.0	0.2					4.2
	10					1.1						1.1
	7.5					0.2						0.2
	2.5					0.2						0.2
1.5 - 2.0	17.5							0.1	0.3	0.4	0.5	1.3
	15				1.4	1.4	0.2	0.4	0.3	0.3	0.2	4.2
	12.5				3.0	2.8	0.2	0.1				6.1
	10				3.9	0.6						4.5
	7.5				1.6							1.6
	5				0.5							0.5
	2.5				0.4							0.4
1.0 - 1.5	15					0.1	0.1	0.3	0.2	0.4	0.5	1.6
	12.5					0.6	0.2	0.7	0.4	0.2	0.1	2.2
	10				4.4	1.8	0.5					6.7
	7.5											4.5
	5											1.9
0.5 - 1.0	12.5										0.2	0.4
	10					3.0	0.2					3.0
	7.5					2.4	3.0					7.1
0.0 - 0.5	5					2.8	2.0					4.9
	2.5					4.3						4.3
	10							0.2			0.1	0.3
	7.5					2.2	0.3					2.5
	5					1.6	0.1					4.6
	2.5					0.2						6.0
			0.8	14.2	31.2	34.4	10.3	4.6	1.2	1.7	1.6	100.0

Fatigue

$H_s - T_z - V_w$

Reduce to
16 states

	Hs	Tz	Vw	%
1	0.25	3.82	3.30	8.7
2	0.25	5.63	6.47	4.6
3	0.75	3.84	5.19	14.5
4	0.75	5.54	9.15	5.0
5	0.58	10.5	11.67	0.3
6	1.25	4.44	6.00	7.8
7	1.25	4.86	10.29	6.9
8	1.25	8.28	13.19	3.6
9	1.75	4.59	8.64	7.0
10	1.75	4.99	13.31	8.6
11	1.75	8.73	15.83	3.0
12	2.25	5.59	13.97	12.1
13	2.75	5.77	14.47	7.5
14	3.25	6.3	15.17	4.4
15	3.75	6.63	15.08	3.0
16	4.25	7.47	15.42	3.0
				100.0

Fatigue

Now lifetime loads can be simulated:

- Aerodynamic loads: BEM
- Hydrodynamic loads: Morison

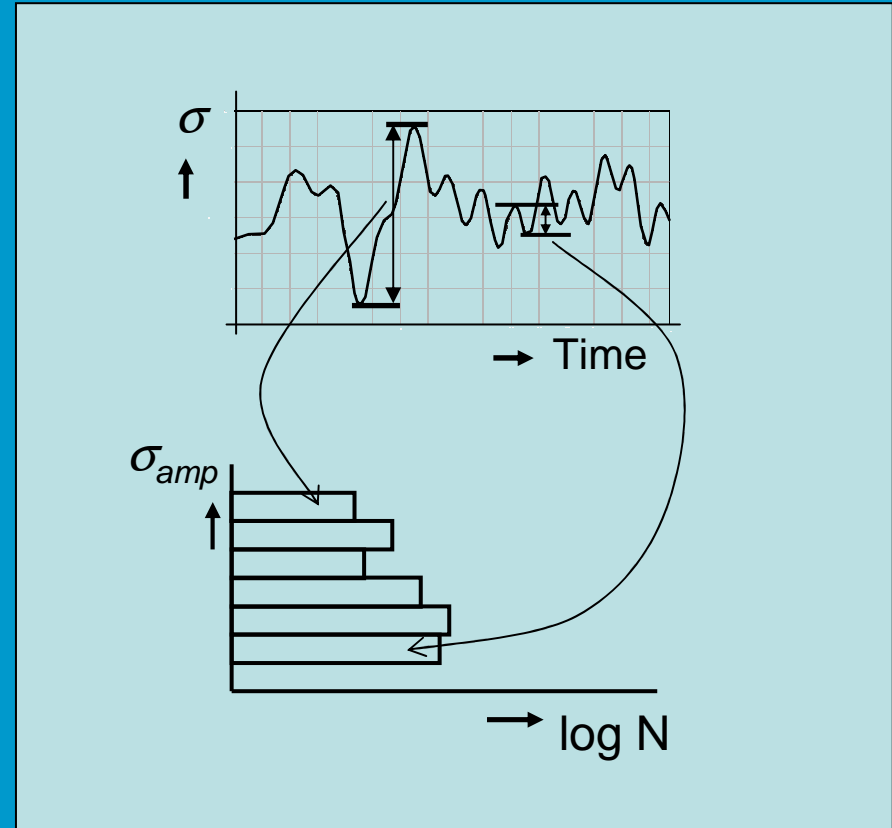
Then stresses can be determined along structure

Fatigue

Stress Time Series



Stress Histogram

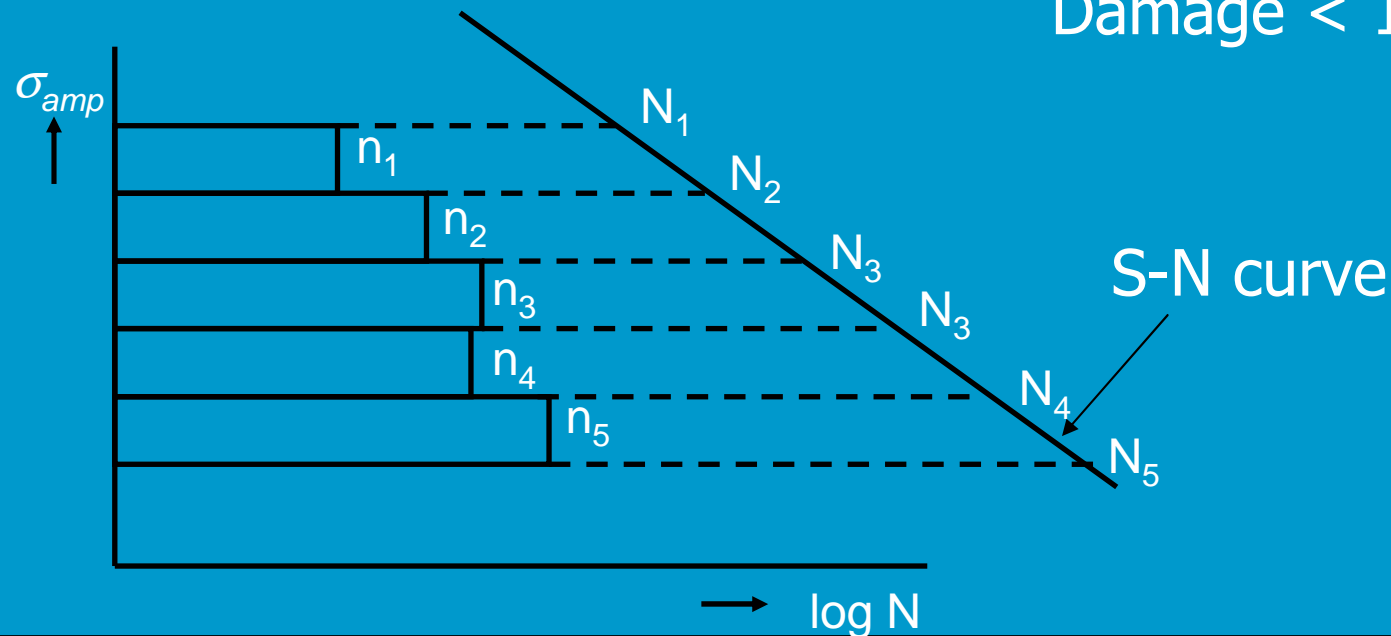


Fatigue

Miner's Damage Rule:

$$\sum \frac{n_i}{N_i} = \frac{n_1}{N_1} + \frac{n_2}{N_2} + \frac{n_3}{N_3} + \frac{n_4}{N_4} + \frac{n_5}{N_5}$$

Damage < 1.0



Installation & Maintenance

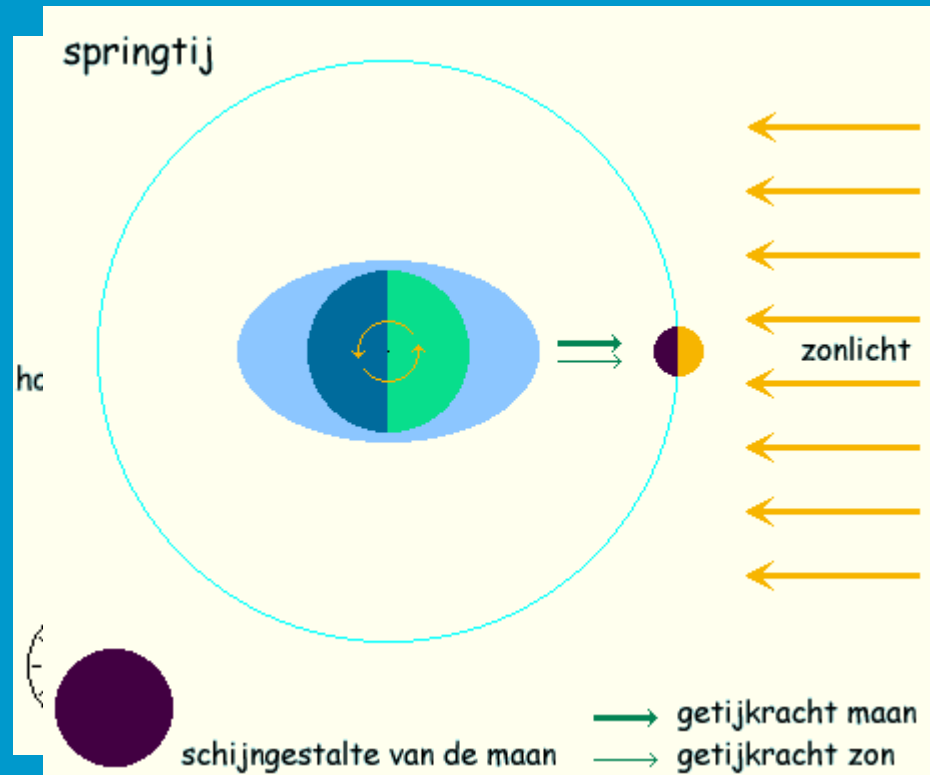
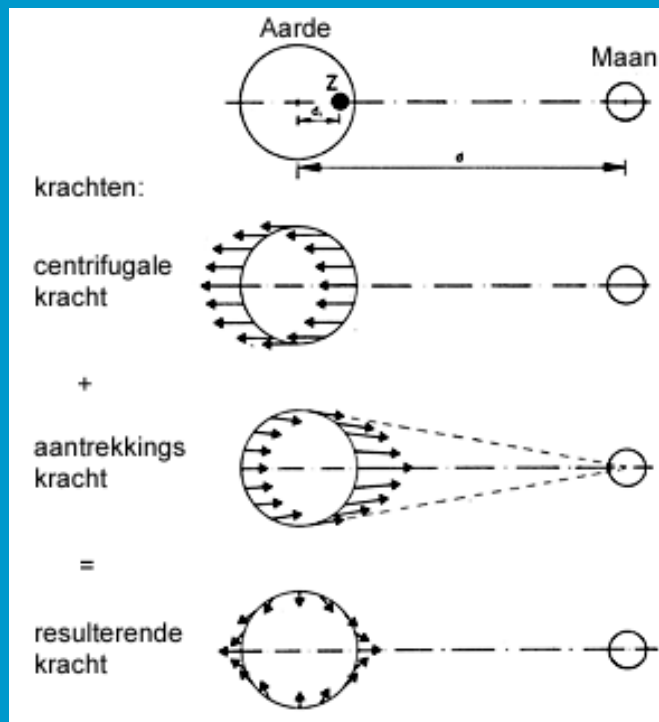
Workability:

Different activities have different workability limits

Sailing	$H_s = 4\text{m}$
Transfer	$H_s = 2\text{m}$
Jacking up	$H_s = 1\text{m}$
Jack-up working	$H_s = 3\text{m}$

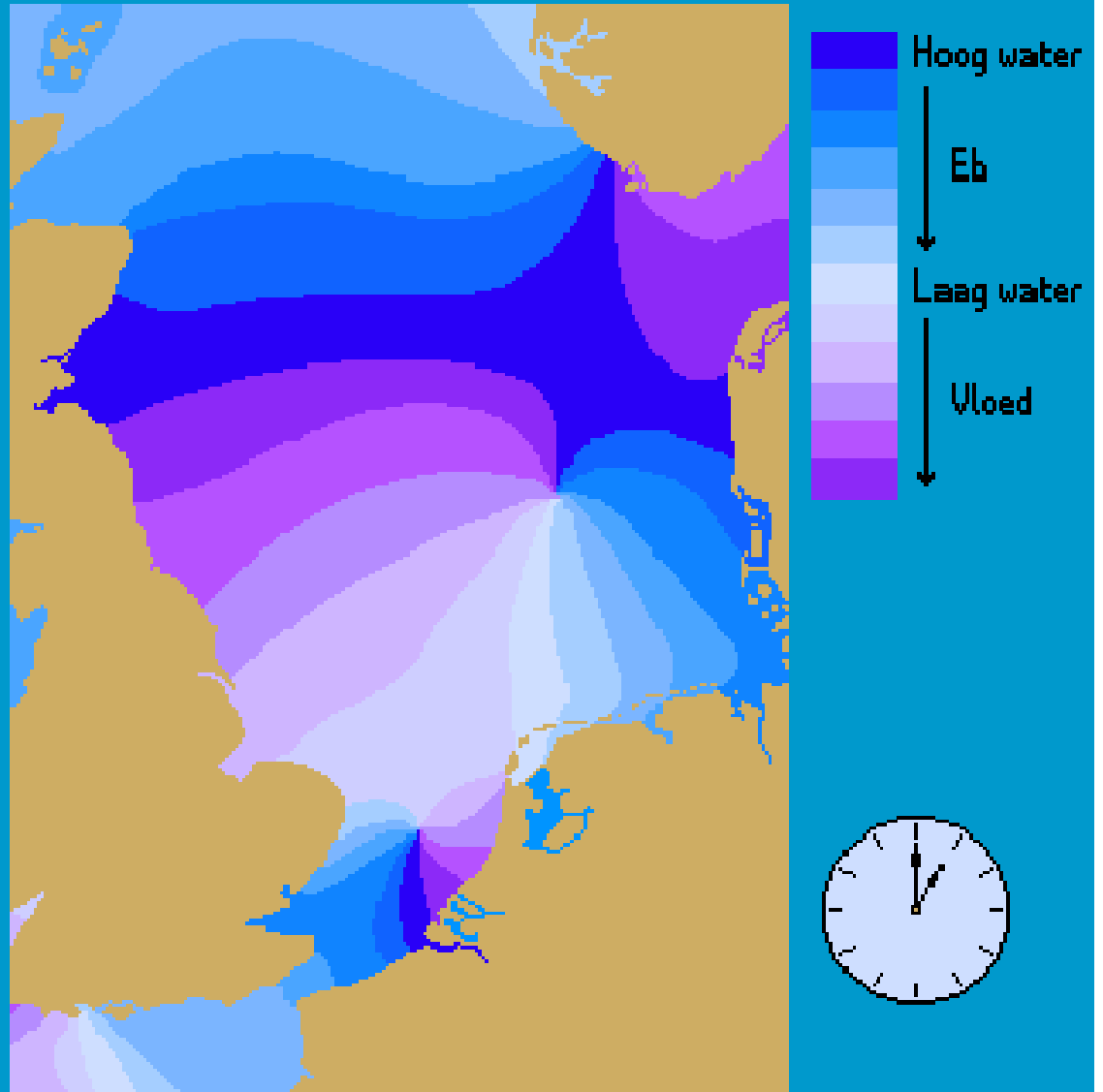
Current

Horizontal movement of water, due to tidal waves



Current

Flow pattern North Sea



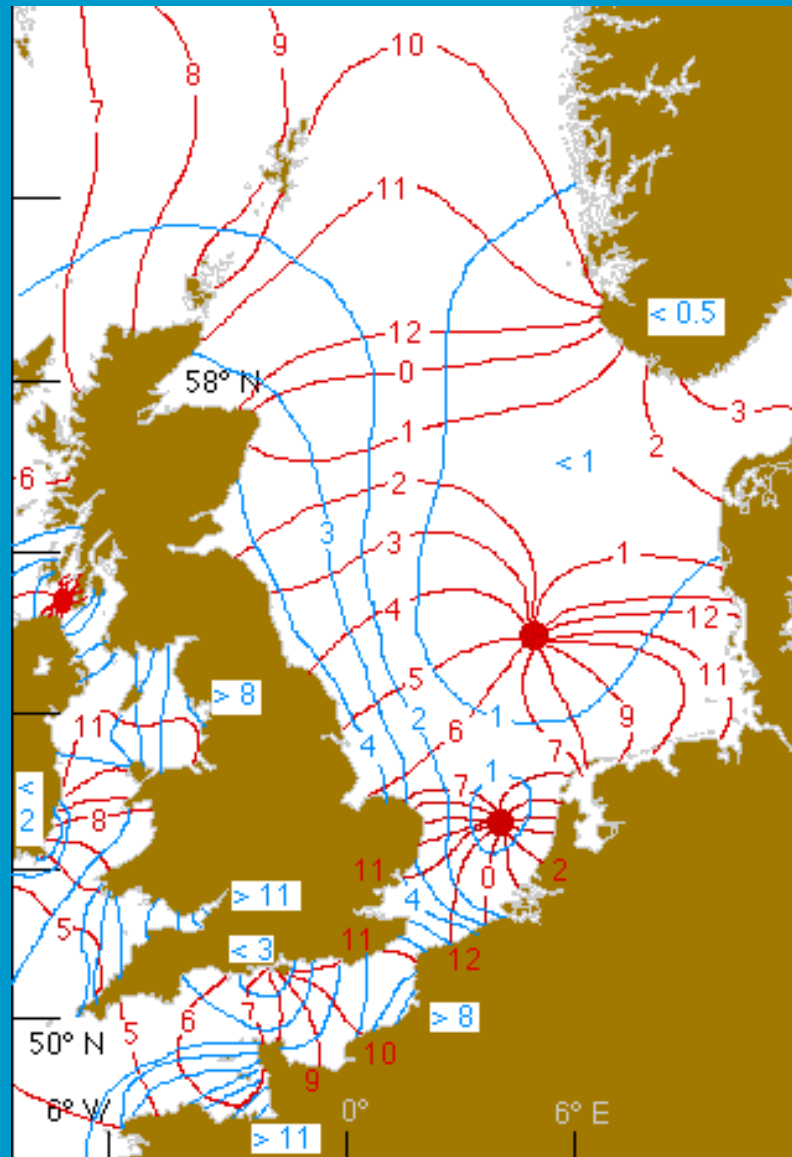
Current

Determine flow patterns
and tidal differences

BIG DIFFERENCE

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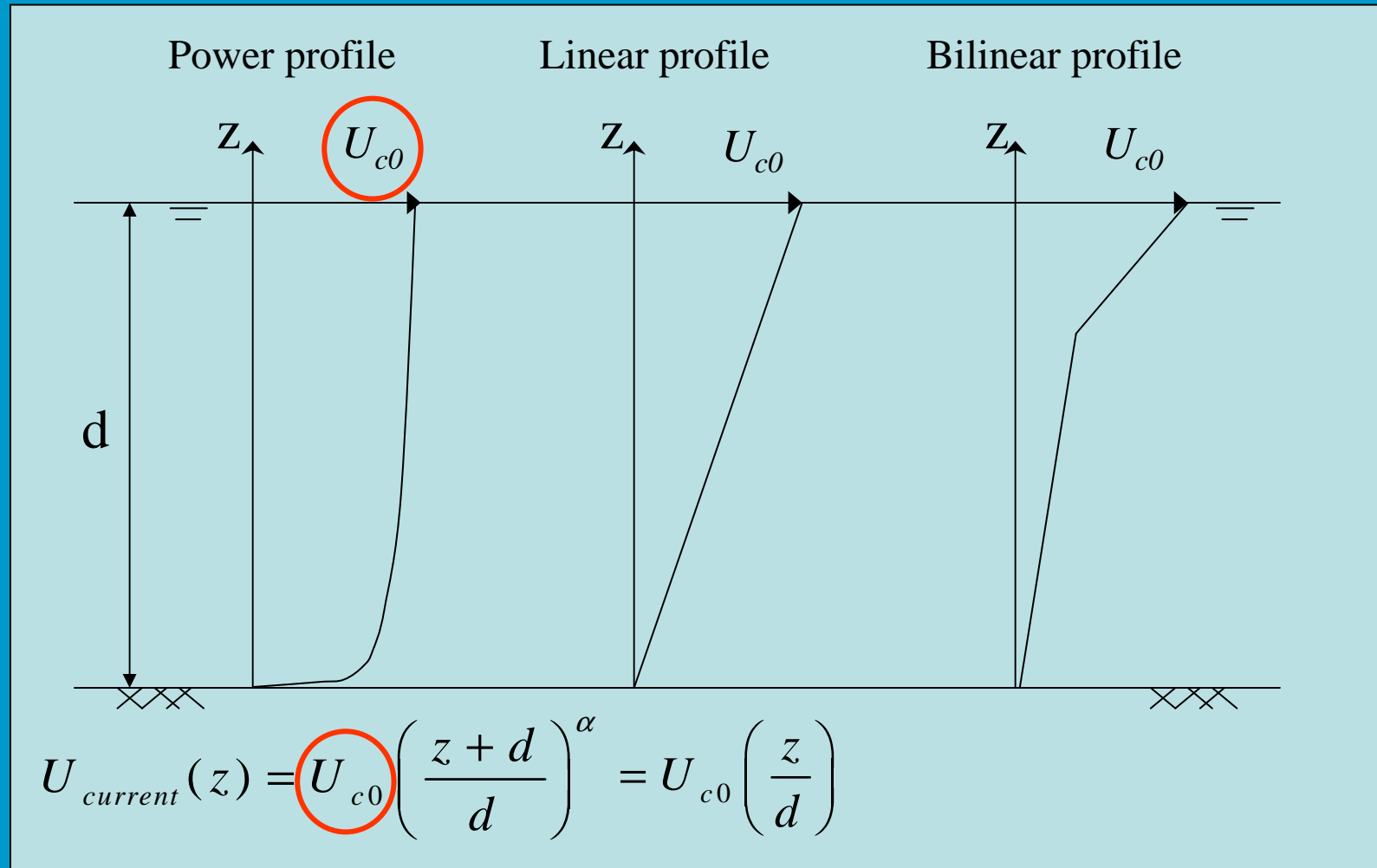
BIG CURRENT



Current

- Length and time scale of tidal waves much larger than of wind waves
- Currents considered as flow of constant velocity
- Vertical variation: Current profile over depth

Current profiles



Current effects

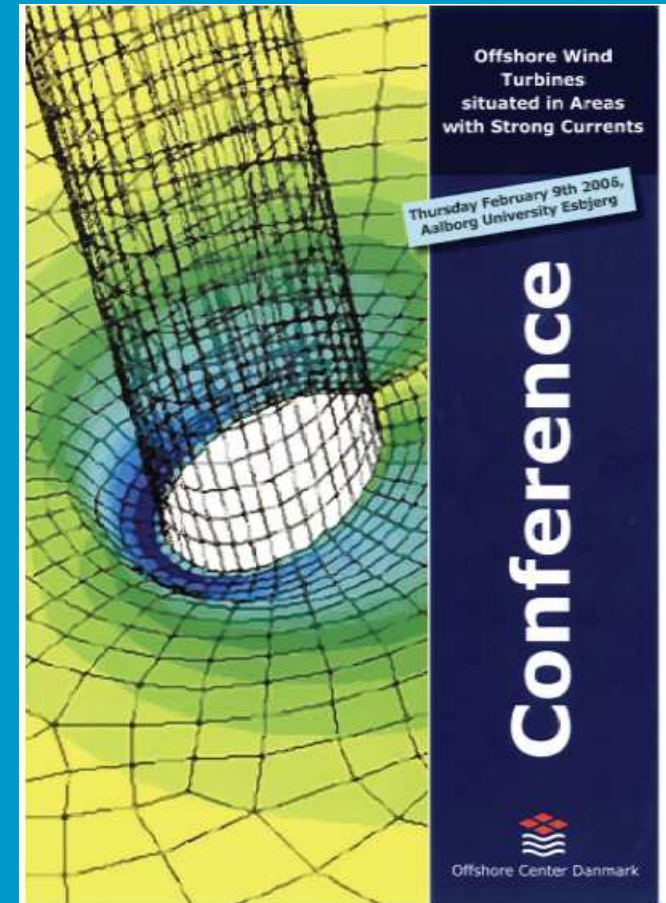
- Hydrodynamic loads on monopile

Morison Equation:

$$f(t) = C_m \cdot \frac{1}{4} \rho \pi D^2 \cdot \dot{u} + C_d \cdot \frac{1}{2} \rho D \cdot \underbrace{u u}_{\text{velocity}}$$

Current effects

- Hydrodynamic loads on monopile
- Scour
 - Caused by current
 - Between $1.3 \cdot D$ and $2.5 \cdot D$
 - Consider when designing



Current effects

- Hydrodynamic loads on monopile
- Scour
- Installation & Maintenance: vessel manoeuvring

So.... Resuming:

- Long term: scatter diagrams
- Short term: wave spectra
- H_s and T_z
- Current velocity & profile
- Extremes
- Fatigue
- Installation & Maintenance
- Scour