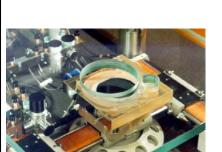




### Mechatronic system design

Mechatronic system design wb2414-2013/2014 Course part 6





#### Power electronics

Prof.ir. R.H.Munnig Schmidt Mechatronic System Design



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#### Contents

- Power electronics, what's so special about it?
- Passive (power) electronic filters
  - · Why so many inductors?
- Current or voltage source amplifier output
  - Actuator determined spec.
- Linear, dissipative power amplifiers
- Dynamic impact of power amplifiers
  - Stability and frequency dependent characteristics
- Switched mode power conversion
  - 4 quadrant power delivery
  - PWM Amplifiers
  - 3-phase amplifiers

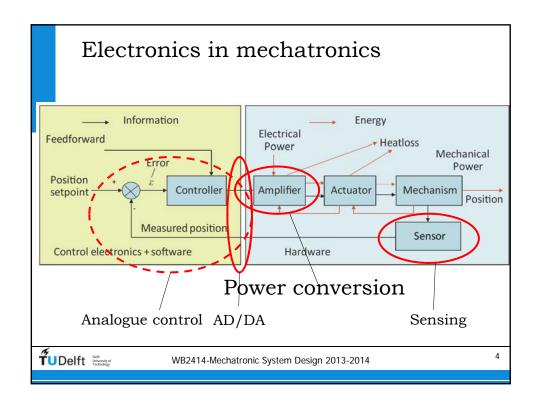


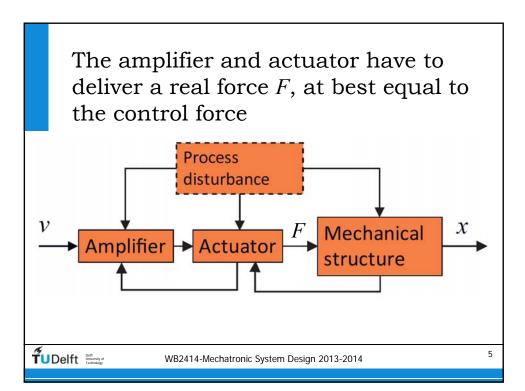
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# The task of the power amplifier is that of a controller!

- Controlling the characteristics of an electromagnetic actuator/motor by controlling the actuator-input signal: the voltage and current.
- Distinguishing items:
  - Power capability (Voltage × Current)
  - Dynamic properties like stability and control bandwidth
  - Low or high output impedance (voltage or current source output)
  - · Efficiency (Power dissipation)
  - Linearity, full range proportional output value (freedom of distortion)



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### Power Capability is directly visible

- High voltage and current levels limit small size (solidstate) integration
  - Discrete Components
  - Switching relays
  - Thermal Control
- Risk of interference by strong magnetic and electric fields (EMC)



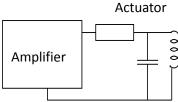


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### Dynamic Properties in two directions

- Amplifiers are part of the position feedback loop
  - Delay for instance from latency in a digitally controlled amplifier, will reduce stability .
  - Also the bandwidth, how quickly can the current follow a setpoint change (HF behaviour), is related to a negative impact on the phase.
- The dynamic load from the actuator(L,R,C) will impact stability of the amplifier



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# Low or high output impedance of an Amplifier

- Low impedance (voltage source output):
  - When damping is necessary
    - Loudspeakers
    - Feedforward (no feedback)



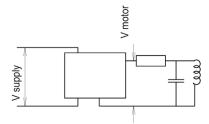
- When the current/force has to be independent of the movement (Lorentz actuators).
- When the current/force has to be independent of the self inductance (servo systems)



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#### Efficiency

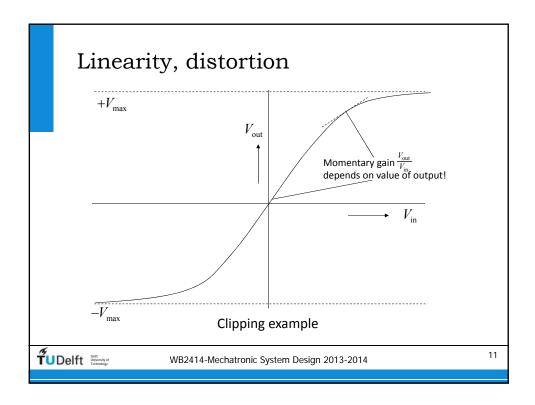


Actuator

- An amplifier converts a supply voltage/ current into a motor voltage/current.
- A difference of voltage means power loss unless....
- A difference in current requires energy buffering in capacitors or batteries.
- Switched mode/PWM amplifiers reduce dissipation but have other special properties that have to be known.



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# First a few definitions while keeping "real" electronics to the bare minimum

- Voltage and current source
- Ohm's law
- Resistors
- Capacitors
- Inductors



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### Ideal voltage and current sources

An ideal voltage source is a circuit element where the voltage across it is
independent of the load (current). It has a zero source impedance.
It can be replaced by a short circuit when the influence of another electric source
in the circuit is to be determined.



An ideal current source is a circuit element where the current through it is
independent of the load (voltage). It has an infinite source impedance.
It can be replaced by an open circuit when the influence of another electric source
in the circuit is to be determined.

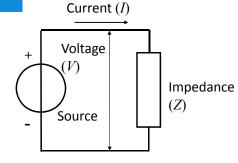


 Both do not exist in reality but only in physical models of circuits. In reality one can only approximate its behaviour.



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# Ohm's law, the definition of impedance



$$V = IR$$
  $I = \frac{V}{R}$ 

Power in Watt (W):

$$P = IV = I^2R = \frac{V^2}{R}$$

Dynamic impedance Z(f)

$$V(f) = I(f)Z(f)$$
  $I(f) = \frac{V(f)}{Z(f)}$ 

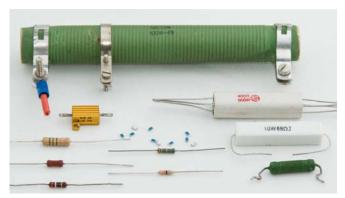


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#### Practical resistors

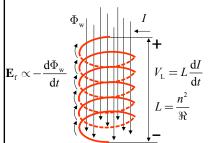
- Resistor size is determined by the power dissipation
- (Wirewound) resistors have parasitic self inductance and capacitance
- Range from  $m\Omega$  to  $G\Omega$



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# First dynamic impedance, the coil or Inductor (symbol L from Lenz).



Self-inductance of windings is related to induced magnetic field

$$L = \frac{\Phi_{w,t}}{I} = n \cdot \frac{\Phi_w}{I} = n \frac{nI}{I\Re} = \frac{n^2}{\Re}$$

Induced voltage by a changing magnetic field (Faraday)

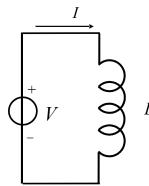
Inductor 
$$L$$
 with  $n$  windings 
$$V_{\rm L} = \mathcal{F}_{\rm e} = n \frac{{\rm d}\Phi_{\rm w}}{{\rm d}t} = \frac{{\rm d}\Phi_{\rm w,t}}{{\rm d}t} = L \frac{{\rm d}I}{{\rm d}t}$$



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# First dynamic impedance, the coil or Inductor (symbol L from Lenz).



 For AC the voltage leads the current with 90°

Fourier transform:

$$\mathcal{F}\left\{\frac{\mathrm{d}}{\mathrm{d}t}\right\} = j\omega$$

$$V(t) = n \frac{d\Phi_{\rm w}}{dt} = L \frac{dI}{dt}$$

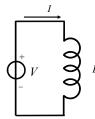
$$\mathcal{F}\left\{V(t)\right\} = V(\omega) = j\omega LI$$

$$Z_c(\omega) = \frac{V}{I}(\omega) = j\omega L$$

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### Power and energy in an inductor.



• The current as function of the voltage equals:

$$\begin{split} V(\omega) &= j\omega L I(\omega) \quad \Rightarrow \quad I(\omega) = \frac{V(\omega)}{j\omega L} \\ V(\omega) &= V_{\rm p} \cos \omega t \quad \Rightarrow \quad I(\omega) = \frac{V(\omega)}{j\omega L} = I_{\rm p} \sin \omega t \quad \left(I_{\rm p} = \frac{V_{\rm p}}{\omega L}\right) \end{split}$$

• The power equals:

$$P = I_p \sin \omega t \cdot V_p \cos \omega t = 0.5 I_p V_p \sin(2\omega t) = \text{ average } 0$$

• And the momentary energy equals

$$E_{L} = \int_{t_{0}}^{t_{1}} P_{L}(t) dt = \int_{t_{0}}^{t_{1}} I(t) L \frac{dI}{dt} dt = L \int_{0}^{t_{1}} I(t) dI = \frac{1}{2} L I_{1}^{2}$$
(compare:  $E_{\text{spring}} = 0.5 k F^{2}$ )



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#### **Practical Inductors**

- Inductor size is determined by the selfinductance and the current
- Inductors have parasitic capacitance, resistance and eddy current losses
- Range from μH to several mH



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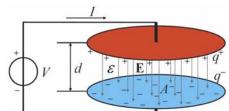
# Second dynamic impedance, the Capacitor

A capacitor is storing electrical energy in charge on two separated plates with distance D and surface A

- The capacitance is:  $C \approx \frac{\varepsilon A}{d}$
- In vacuum the permittivity  $\varepsilon_0$  is:

$$\varepsilon_0 = \frac{1}{c^2 \mu_0} \approx 8.85 \cdot 10^{-12}$$

- The charge is: q = CV
- With AC the current leads the voltage



$$I(t) = \frac{dQ}{dt} = C\frac{dV}{dt} \ ; \qquad \mathcal{F}\left\{I(t)\right\} = I(\omega) = j\omega CV \ ; \quad Z(\omega) = \frac{V}{I} = \frac{1}{j\omega C} \ ; \label{eq:energy}$$

$$P = V_{\rm p} \sin \omega t \cdot I_{\rm p} \cos \omega t = 0.5 V_{\rm p} I_{\rm p} \sin(2\omega t) = \text{ average 0}; \quad E = 0.5 CV^2 \quad \text{(compare: } E_{\rm kin} = 0.5 mv^2\text{)}$$



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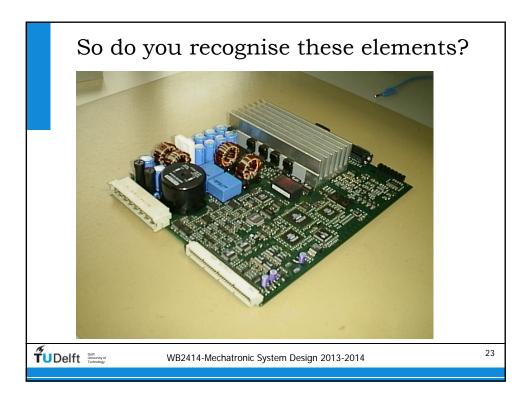
#### **Practical Capacitors**

- Capacitor size is determined by the Capacitance and current.
- Capacitors have parasitic self inductance and resistance
- Range from 1pF (ceramic) to ~ > 1 F (electrolytic super caps)



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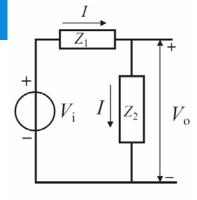
These parts are used to make filters for the output of switching-mode amplifiers

- Voltage dividers or attenuators
- 1st order low-pass filters
- 2<sup>nd</sup> order low-pass filters



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### A voltage divider



$$I = \frac{V_i}{Z_1 + Z_2}$$

$$V_o$$

$$V_o = I \cdot Z_2 = \frac{V_i Z_2}{Z_1 + Z_2}$$

a: Voltage divider

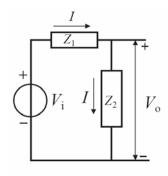


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#### Discussion:

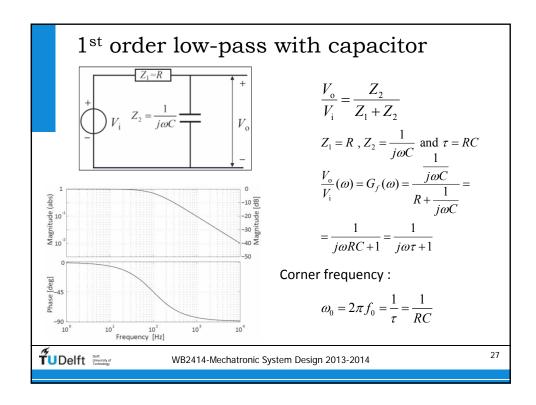
- Design a first-order low pass filter for 1000Hz
  - Use voltage divider
  - Choose best suitable components
  - Determine frequency response
  - Determine component values

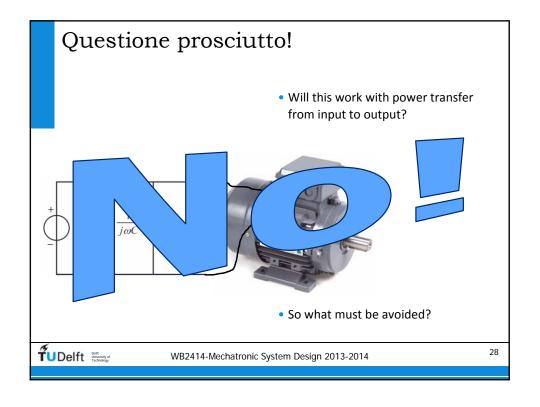


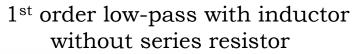
a: Voltage divider

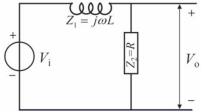


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$$Z_2$$
 represents the power in the load.

$$\frac{V_{\rm o}}{V_{\rm i}} = \frac{Z_2}{Z_1 + Z_2}$$

$$Z_1 = j\omega L$$
,  $Z_2 = R$  and  $\tau = \frac{L}{R}$ 

$$\frac{V_o}{V_i} = \frac{Z_2}{Z_1 + Z_2}$$

$$V_o \qquad Z_1 = j\omega L , Z_2 = R \text{ and } \tau = \frac{L}{R}$$

$$\frac{V_o}{V_i}(\omega) = G_f(\omega) = \frac{R}{R + j\omega L} = \frac{1}{L}$$

$$= \frac{1}{L} = \frac{1}{L}$$

$$=\frac{1}{j\omega\frac{L}{R}+1}=\frac{1}{j\omega\tau+1}$$

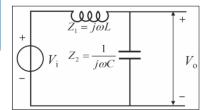
Corner frequency:

$$\omega_0 = 2\pi f_0 = \frac{1}{\tau} = \frac{R}{L}$$

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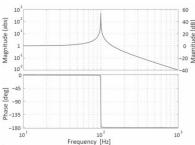
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#### A second order passive low pass filter without series resistor



$$\frac{V_{\rm o}}{V_{\rm i}} = \frac{Z_2}{Z_1 + Z_2}$$

$$Z_1 = j\omega L$$
,  $Z_2 = \frac{1}{j\omega C}$ ,  $\omega_0 = \frac{1}{\sqrt{LC}}$ 



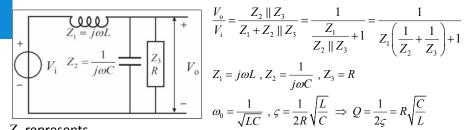
$$\frac{V_{o}}{V_{i}}(\omega) = G_{f}(\omega) = \frac{\frac{1}{j\omega C}}{j\omega L + \frac{1}{j\omega C}} =$$

$$= \frac{1}{(j\omega)^2 LC + 1} = \frac{1}{-\frac{\omega^2}{\omega_0^2} + 1}$$

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### A second order low pass filter with parallel damping



$$\frac{V_{o}}{V_{i}} = \frac{Z_{2} \parallel Z_{3}}{Z_{1} + Z_{2} \parallel Z_{3}} = \frac{1}{\frac{Z_{1}}{Z_{2} \parallel Z_{3}} + 1} = \frac{1}{Z_{1} \left(\frac{1}{Z_{2}} + \frac{1}{Z_{3}}\right) + 1}$$

$$Z_1 = j\omega L$$
,  $Z_2 = \frac{1}{i\omega C}$ ,  $Z_3 = R$ 

$$\omega_0 = \frac{1}{\sqrt{LC}}$$
,  $\varsigma = \frac{1}{2R}\sqrt{\frac{L}{C}} \implies Q = \frac{1}{2\varsigma} = R\sqrt{\frac{C}{L}}$ 

 $Z_3$  represents

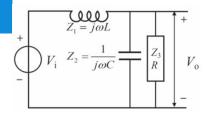
the power in the load.

$$\begin{split} &\frac{V_{o}}{V_{i}}(\omega) = G_{f}(\omega) = \frac{1}{j\omega L \left(j\omega C + \frac{1}{R}\right) + 1} = \\ &= \frac{1}{(j\omega)^{2}LC + j\omega \frac{L}{R} + 1} = \frac{1}{-\frac{\omega^{2}}{\omega_{0}^{2}} + \frac{2\varsigma j\omega}{\omega_{0}} + 1} = \frac{1}{-\frac{\omega^{2}}{\omega_{0}^{2}} + \frac{j\omega}{\omega_{0}Q} + 1} \end{split}$$

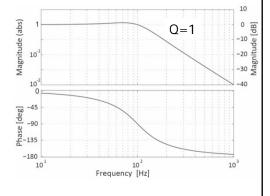


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### A second order low pass filter with parallel damping



$$G_f(\omega) = \frac{1}{-\frac{\omega^2}{\omega_0^2} + \frac{j\omega}{\omega_0 Q} + 1}$$



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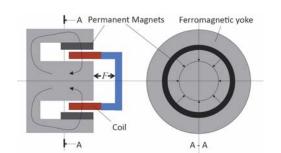


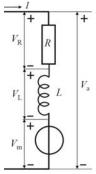
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### Group discussion

 Discuss difference of voltage and current control to drive an actuator in mechatronic systems





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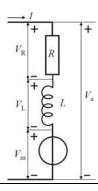
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# A current source output will cancel effects of the self inductance and motion EMF

With a voltage source the current is:

$$I = \frac{V_{R}}{R} = \frac{V_{a} - V_{m} - V_{L}}{R} = \frac{V_{a} - V_{m} - L \frac{dI}{dt}}{R}$$

With a Lorentz actuator a current source will create a direct conversion from the setpoint (control force) to actuator force.



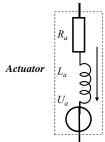


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# Low or high output impedance of an Amplifier

- Low impedance (voltage source output):
  - When damping is necessary
    - Loudspeakers
    - · Feedforward (no feedback)



- High impedance (current source output)
  - When the current/force has to be independent of the movement (Lorentz actuators).
  - When the current/force has to be independent of the self inductance (servo systems)



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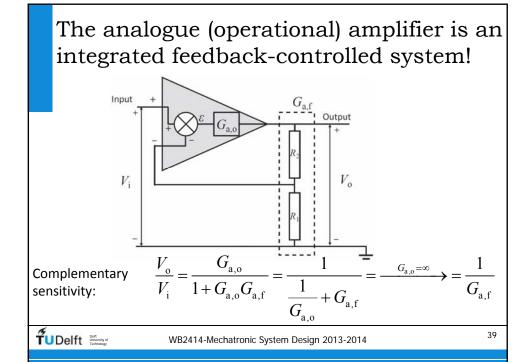
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### Linear power amplifiers

- A linear power amplifier is nothing else than a powerful version of a small signal amplifier.
- It is often designed like an operational amplifier with high-power output stage
- So it starts with the basic Op-amp.

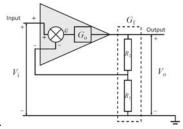
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### Main guidelines of determining the behaviour of an ideal Op-Amp circuit

- 1. Input currents in the Op-amp are zero
- 2. With negative feedback the output will do whatever it can to keep the negative input voltage equal to the positive input voltage.



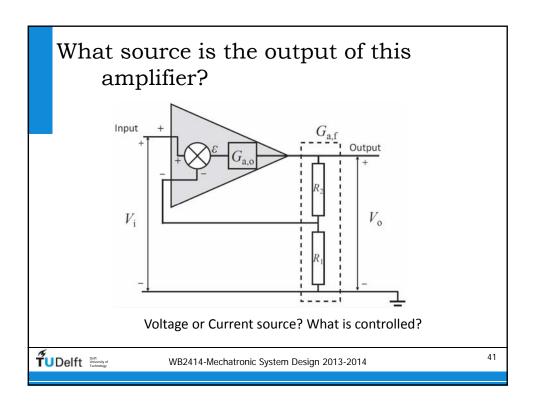
#### Modelling:

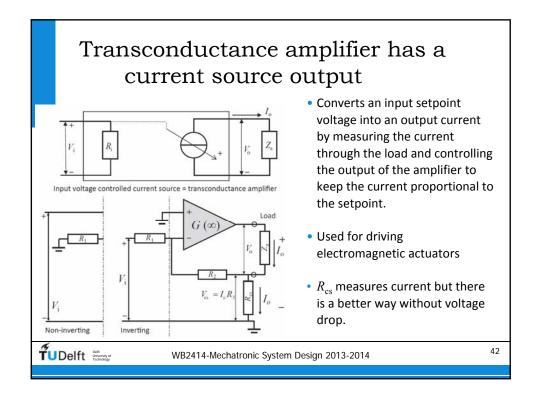
- 1. Verify that there is Negative Feedback
- 2. Calculate the voltage on the positive input.
- Calculate the voltage at the output by applying rule 1 and 2, which means that it generates the same voltage over the feedback path at the negative input as was calculated in step 2.

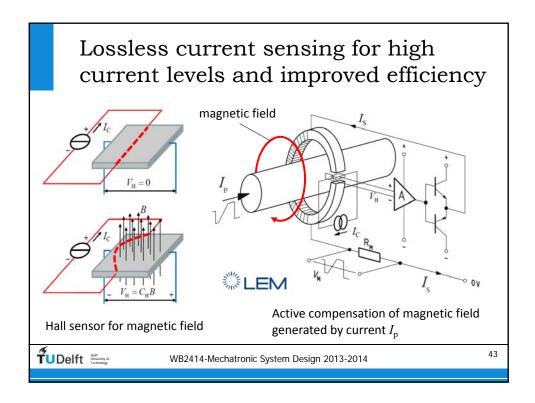


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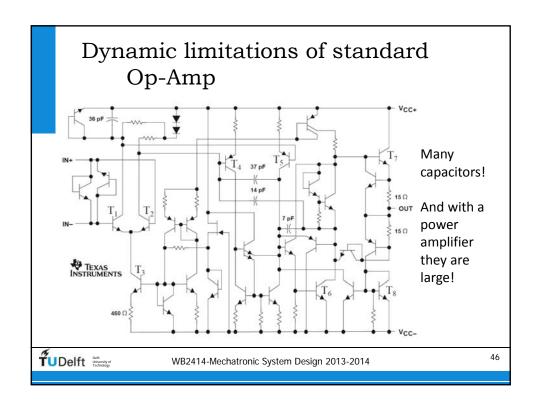
# Ideal and real properties of regular (non-power) operational amplifiers

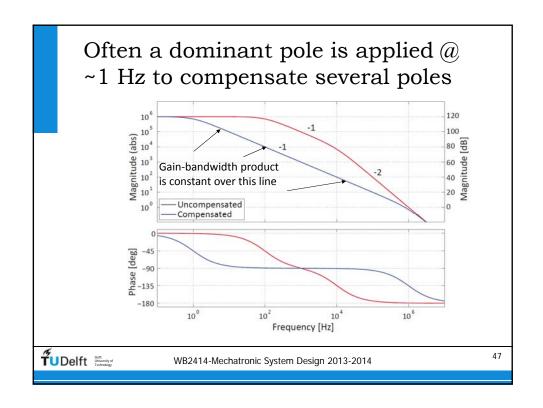
Parameter	Ideal Op Amp	OPA27	Unit
DC Open loop Gain $(G_0)$	× ×	120 (=106)	dB
Input impedance (Z <sub>in</sub> )	$\infty$	6.106	Ω
Output impedance (Z <sub>out</sub> )	0	70	Ω
Input offset voltage ( $V_{os}$ )	0	< 25	μV
Temp. coëff of $V_{os}(\gamma)$	0	0,6	μV/°C
Input bias current $(I_b)$	0	40	nA
Input offset current $(I_{os})$	0	10	nA
Gain bandwidth product	$\infty$	5.106	Hz.
Common mode rejection ratio (CMRR)	œ	120 (=106)	dB

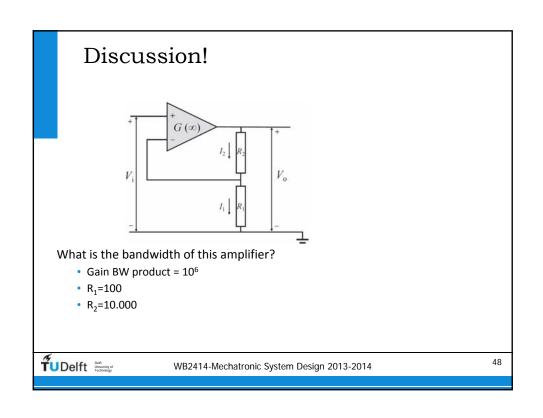


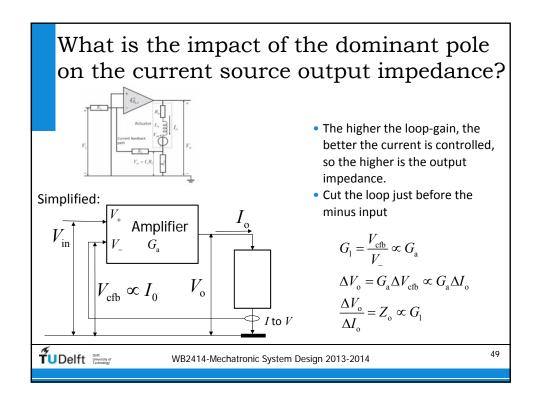
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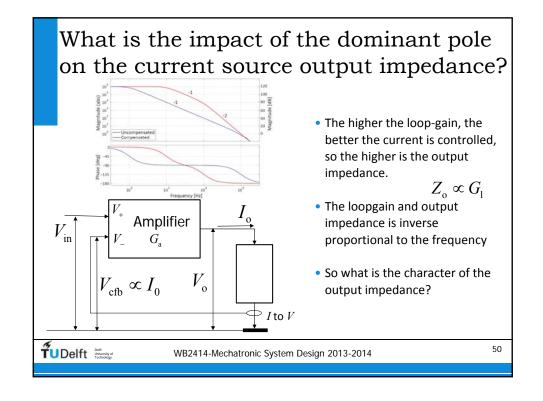
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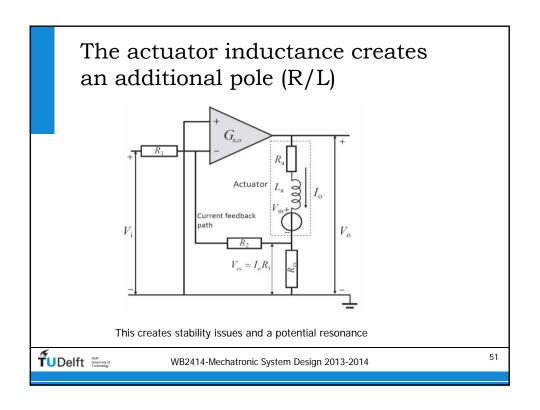


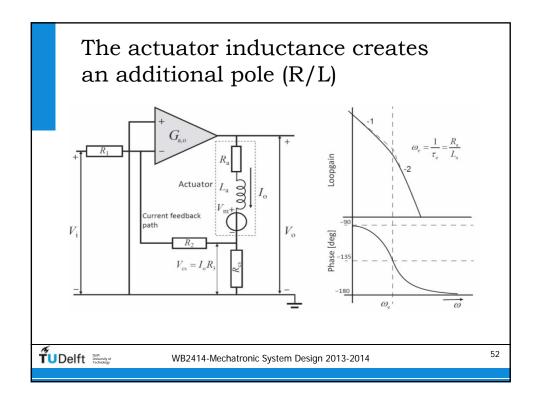


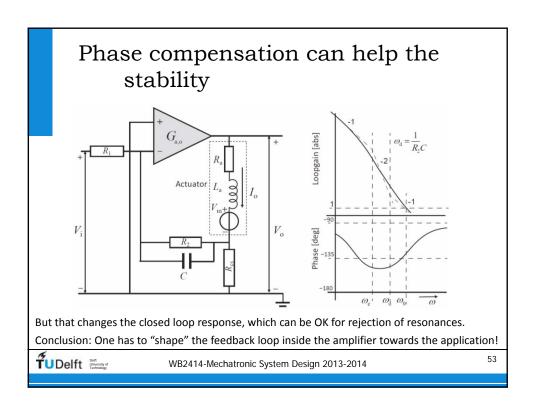


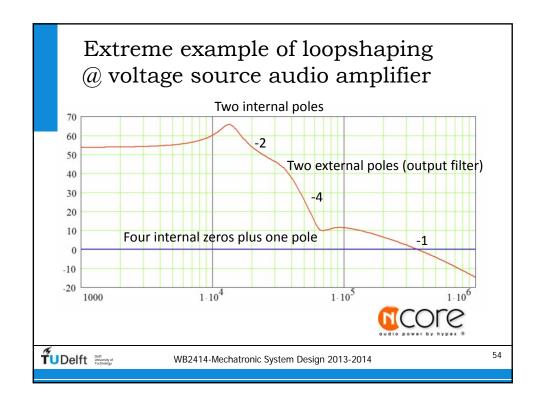












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- Linear, dissipative power amplifiers
- Dynamic impact of power amplifiers
  - Stability and frequency dependent characteristics
- Switched mode power conversion
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  - 3-phase amplifiers



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### Main drawback of a linear non-switching power output stage is dissipation of energy

Issue 1: High supply voltage is needed with an inductive load:

$$V_{\rm a} = V_{\rm R} + V_{\rm m} + V_{\rm L} = IR + V_{\rm m} + L \frac{\mathrm{d}I}{\mathrm{d}t}$$

$$Jerk = \frac{d^3x}{dt^3} \propto \frac{dI}{dt}$$

$$V_{\rm m} + L \frac{\mathrm{d}I}{\mathrm{d}I}$$
  $V \propto$ 

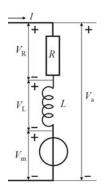
$$Jerk = \frac{d^{3}x}{dt^{3}} \propto \frac{dI}{dt}$$

$$I \propto \ddot{x}$$

$$V_{max} = IR + V_{m} + L\frac{dI}{dt_{max}}$$

$$V \propto \ddot{x} = "Jerk"$$

$$\ddot{x} = "Snap"$$

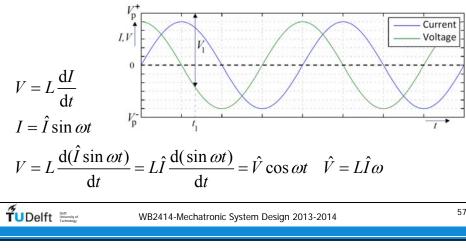




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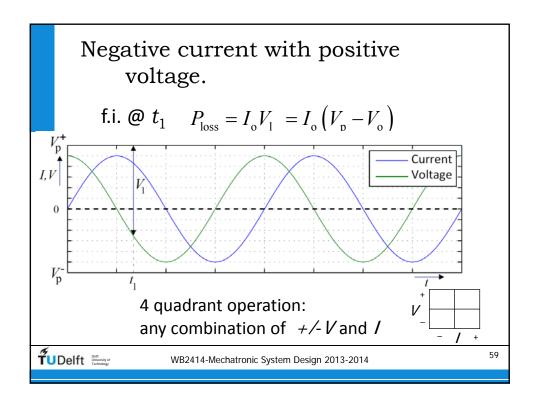
### Issue 2: Current and voltage are not in phase.

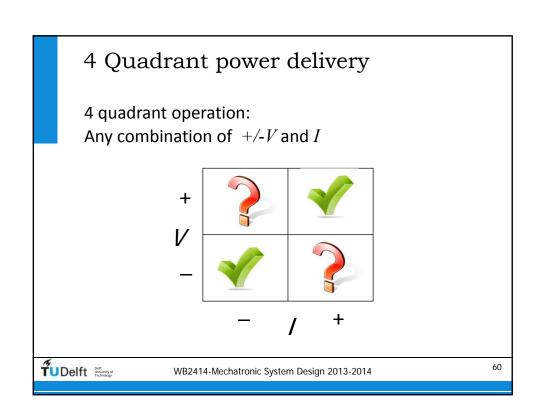
In case of pure inductor:



$$V = L \frac{d(\hat{I}\sin\omega t)}{dt} = L\hat{I} \frac{d(\sin\omega t)}{dt} = \hat{V}\cos\omega t \quad \hat{V} = L\hat{I}\omega$$

# Discussion: What happens at $t_1$ Current I, VVoltage TUDelft Dein University of Technology WB2414-Mechatronic System Design 2013-2014





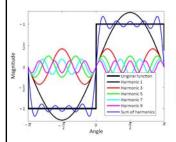
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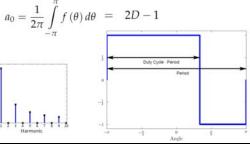
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### PWM or switched mode power conversion

- A switch does not dissipate energy
- Switches can only create squarewave signals (on/off) when switching fast.
- Low pass filtering gives the average value (Fourier) depending on duty cycle.





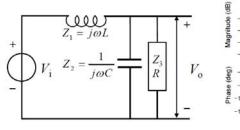


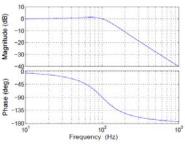
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# PWM or switched mode power conversion

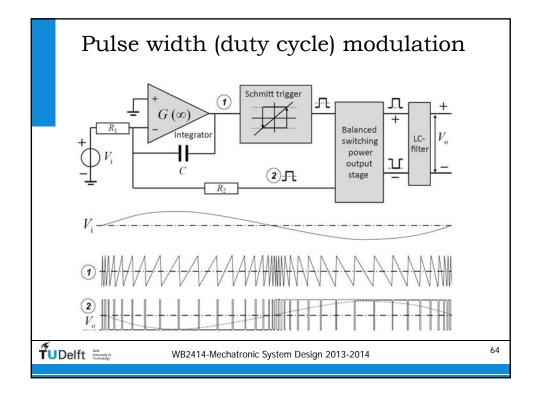
- A switch does not dissipate energy
- Switches can only create squarewave signals (on/off) when switching fast.
- Low pass filtering gives the average value (Fourier).
- L-C filtering is non-dissipative

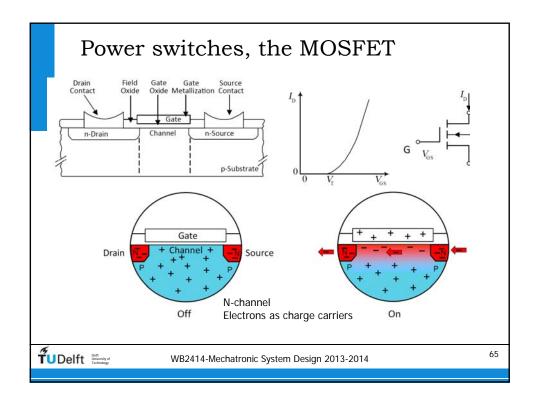


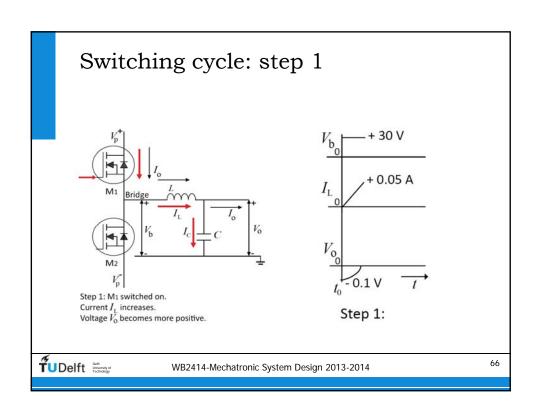


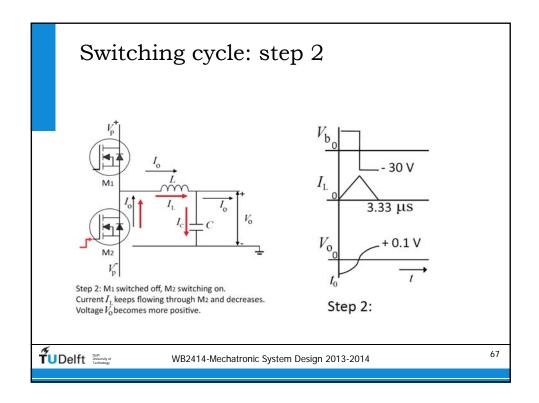
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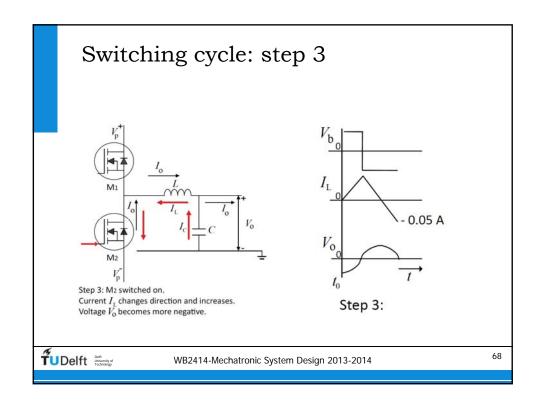
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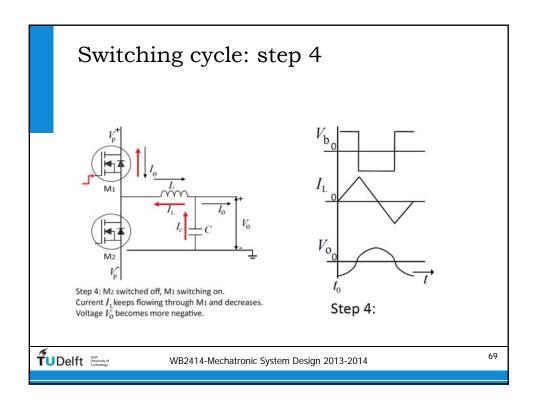


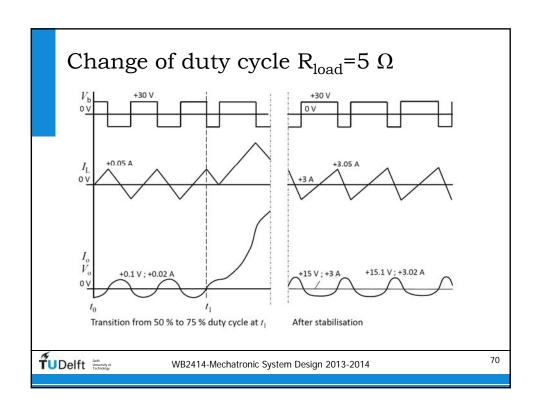


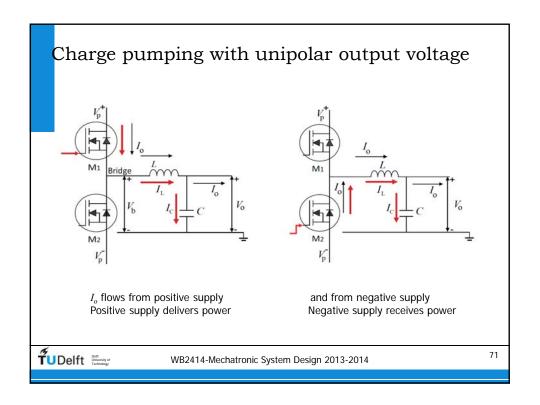


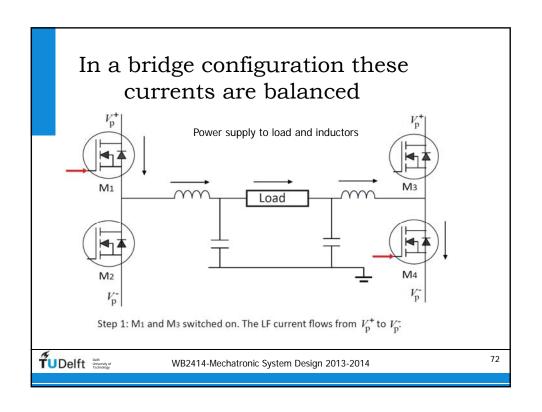


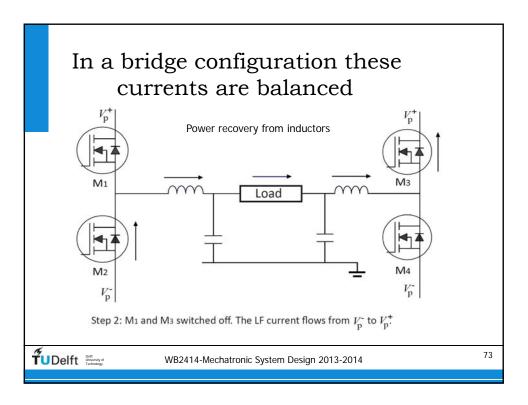








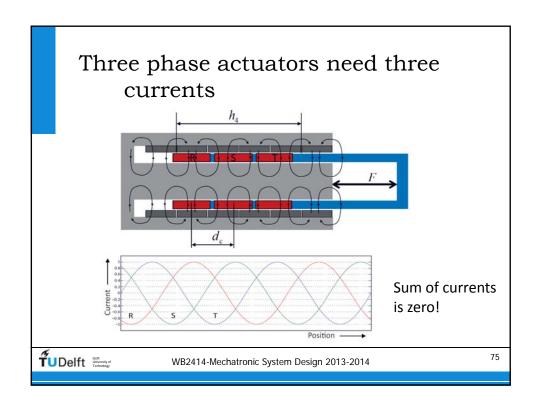


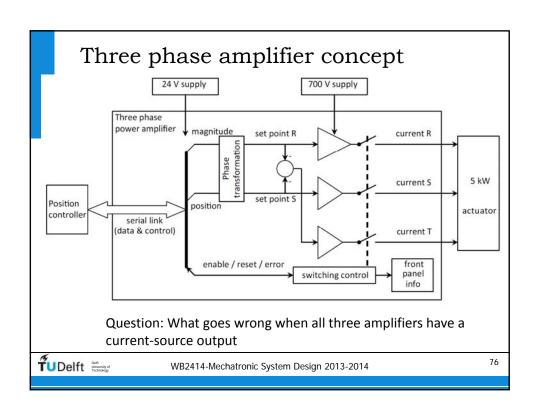


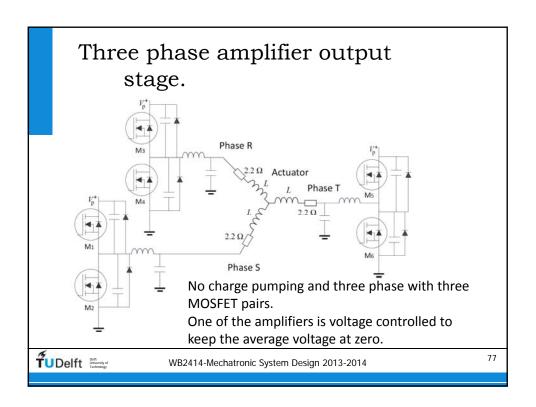
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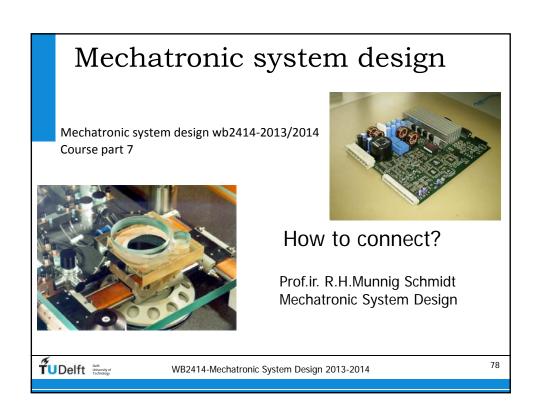


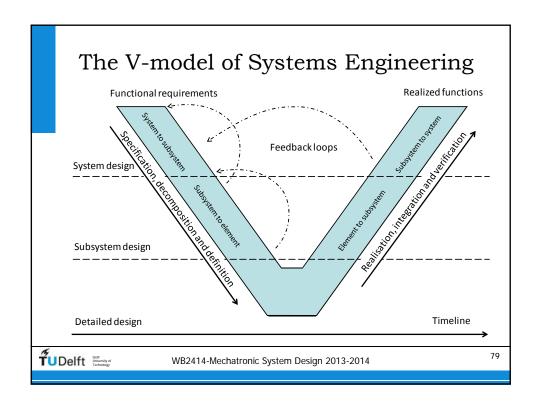
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#### Main items to keep in mind

- "Nesting":
  - Lower parts are nested inside higher parts in the V model
  - Many nested control systems (amplifier, current, motion)
  - All influence eachother in two directions
- Mechanical dynamics determine the final performance
  - Bandwidth limited by eigenmodes
- Power Amplifier and actuator are one
  - · Control force to real force
  - · Optimal tuning in dynamics and electrical properties
- Motion Control is both the connecting lead as the polishing layer
  - Model based feedforward to almost perfection
  - All physical systems (plant=AD/DA, amplifier, actuator, mechanics, sensor) to be included in model
  - Feedback for robustness (to be minimised by feedforward)

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