

# Introduction to Aerospace Engineering

Lecture slides

A black and white photograph showing a wing in a flow field. The wing is dark and elongated, with a curved leading edge and a sharp trailing edge. The flow field is characterized by numerous concentric, wavy lines that represent shock waves and vortices, indicating a highly turbulent and complex aerodynamic environment. The background is a light, textured surface.

# Introduction to Aerospace Engineering

## Aerodynamics 9 &10

Prof. H. Bijl    ir. N. Timmer

# 9 & 10

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## *Airfoils and pressure distributions*

*Anderson 5.1- 5.16 (exc. 5.11)*






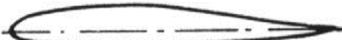

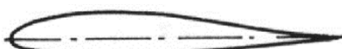

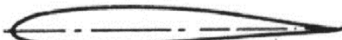

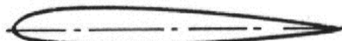

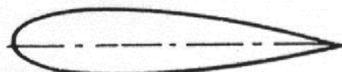
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# Topics

- Airfoils
- Pressure coefficient

# History of wing profiles

Early years: many different airfoil descriptions

<i>Designation</i>	<i>Date</i>	<i>Diagram</i>	<i>Designation</i>	<i>Date</i>	<i>Diagram</i>
Wright	1908		Göttingen 387	1919	
Beriot	1909		Clark Y	1922	
R.A.F. 6	1912		M-6	1926	
R.A.F. 15	1915		R.A.F. 34	1926	
U.S.A. 27	1919		N.A.C.A. 2412	1933	
Joukowski (Göttingen 430)	1912		N.A.C.A. 23012	1935	
Göttingen 398	1919		N.A.C.A. 23021	1935	

# History of wing profiles

National Advisory Committee for Aeronautics (NACA) – 1915  
supported research & development (at Langley)

a.o. aerodynamics (first open windtunnels)

airfoils (large overview in 1933)

specific nomenclature to describe:

2412 means:

**2**% camber at

**0.4** of the chord; and

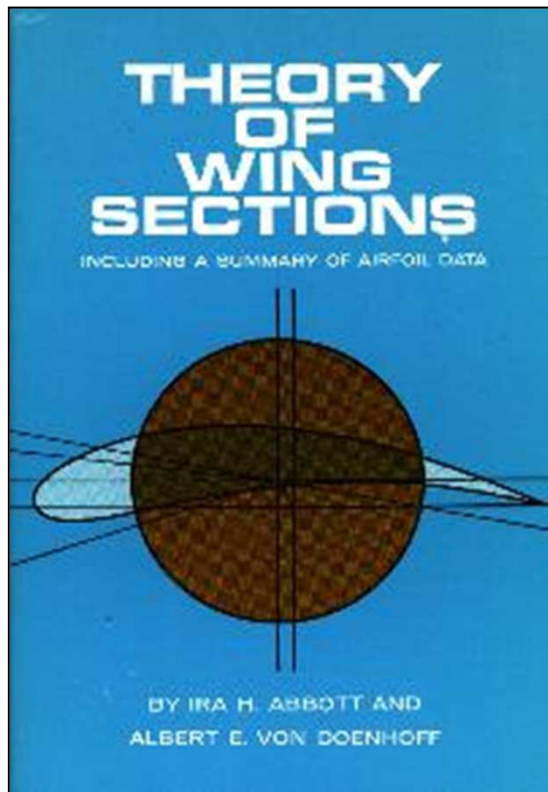
**12**% thickness/chord ratio (or 0.12)

retractable landing gear; engine nacelles, propellers, etc.

# Airfoil Data

A well known source for airfoil data :

**“Theory of Wing Sections”, by Abbott & von Doenhoff**



## Contents

- The significance of wing-section characteristics
- Simple two-dimensional flows
- Theory of wing sections of finite thickness
- Theory of thin wing sections
- The effects of viscosity
- Families of wing sections
- Experimental characteristics of wing sections
- High-lift devices
- Effects of compressibility at subsonic speeds

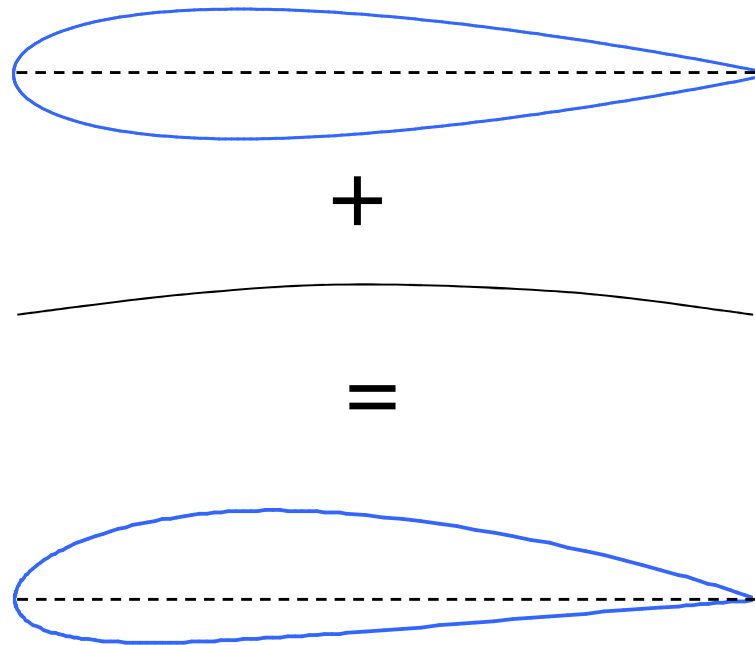
# NACA airfoil development

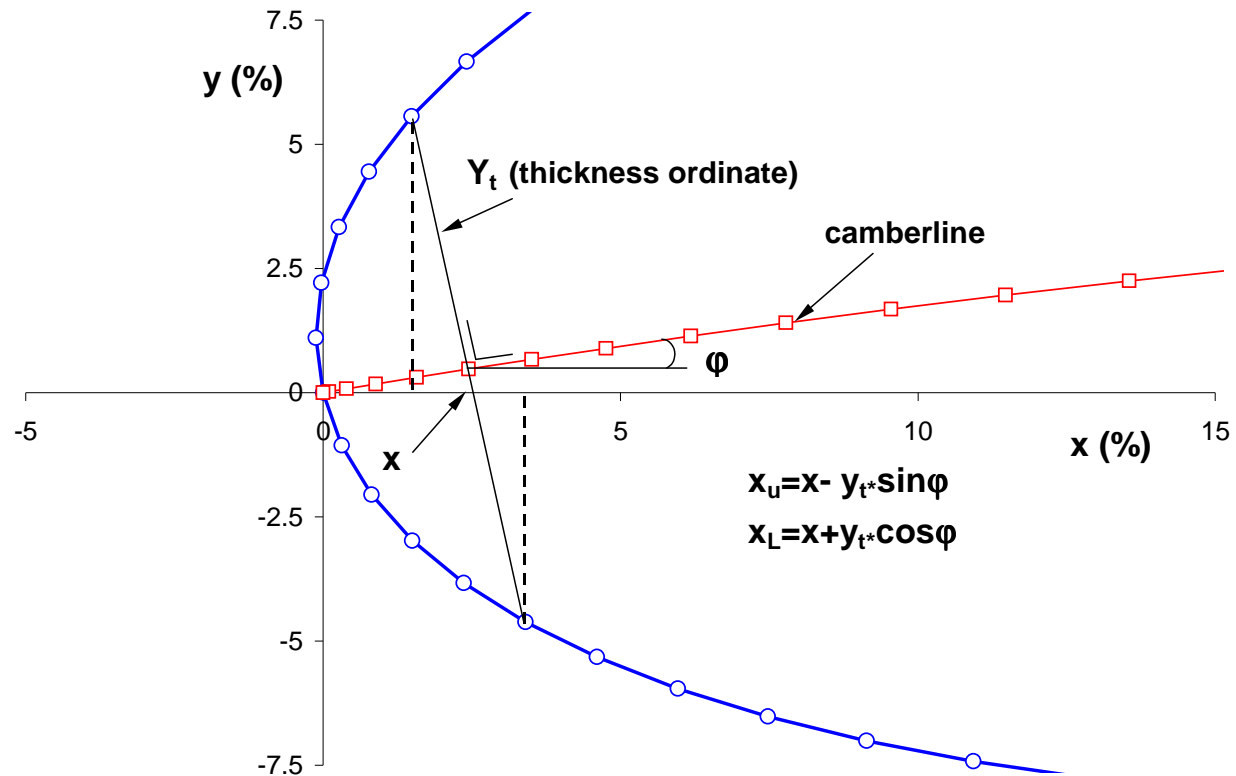
- National advisory committee on aeronautics
- A systematic investigation of the effect of maximum thickness, thickness distribution, camber, camber distribution, Reynolds number, L.E. roughness and flap deflection on the performance of airfoils for aeronautical application
- Most known are NACA 44xx, NACA 230xx, 63 and 64 series



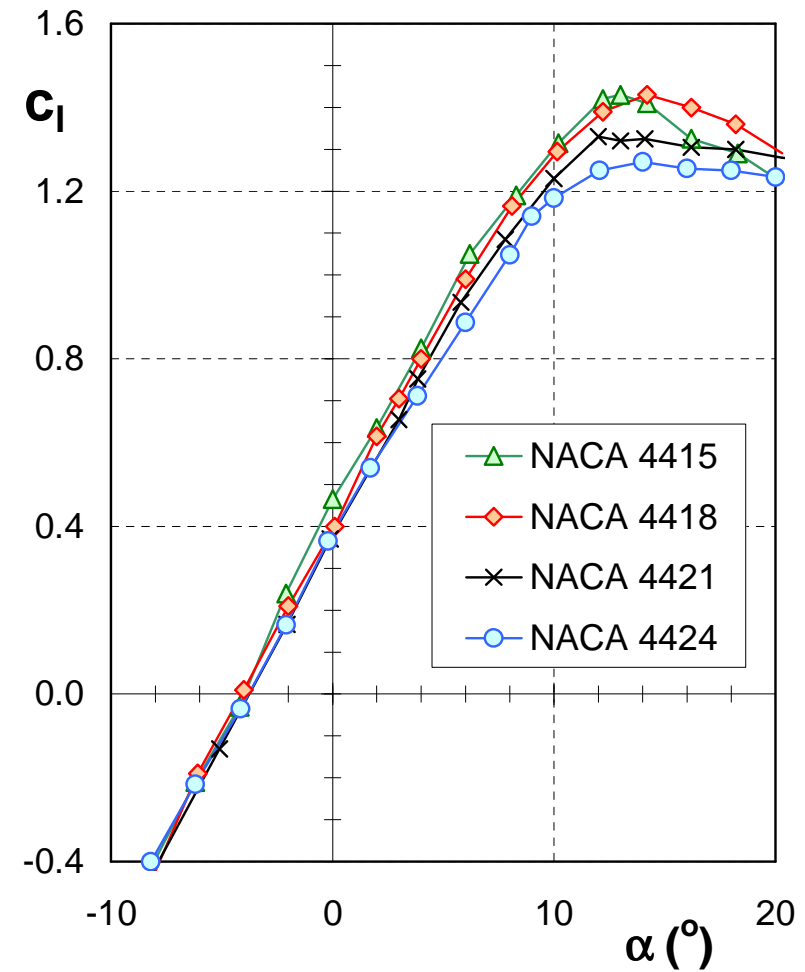
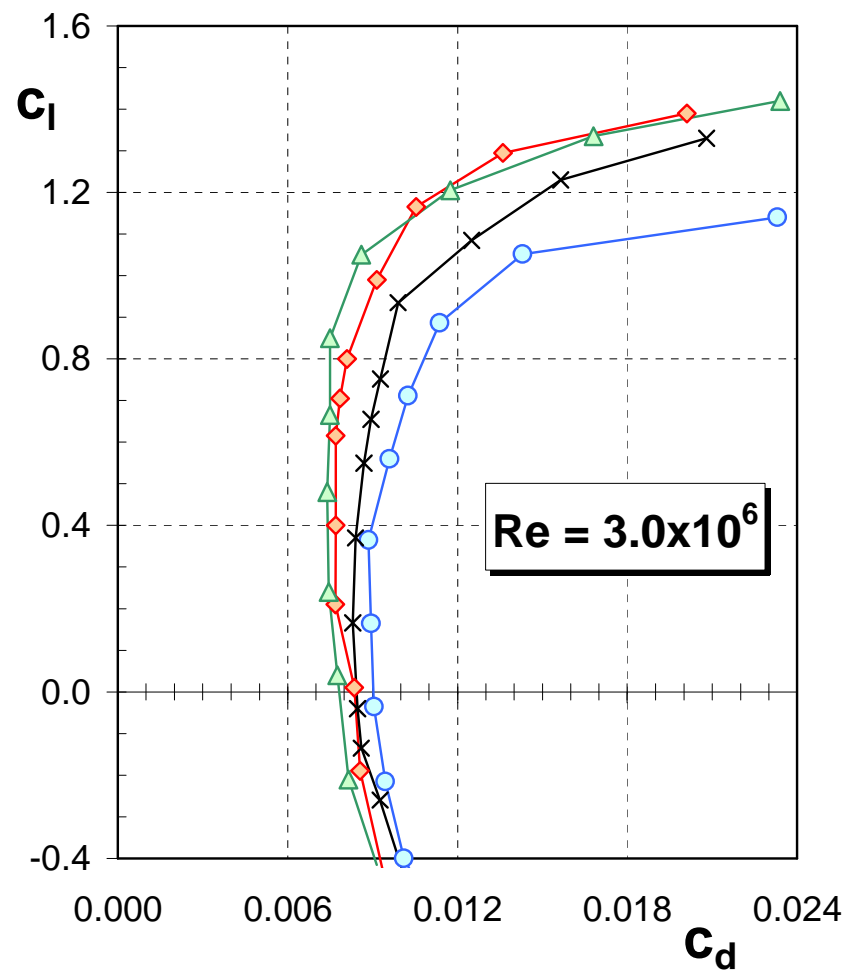
# NACA airfoil development

- Systematic in the sense that different camberlines were combined with different (symmetric) thickness distributions

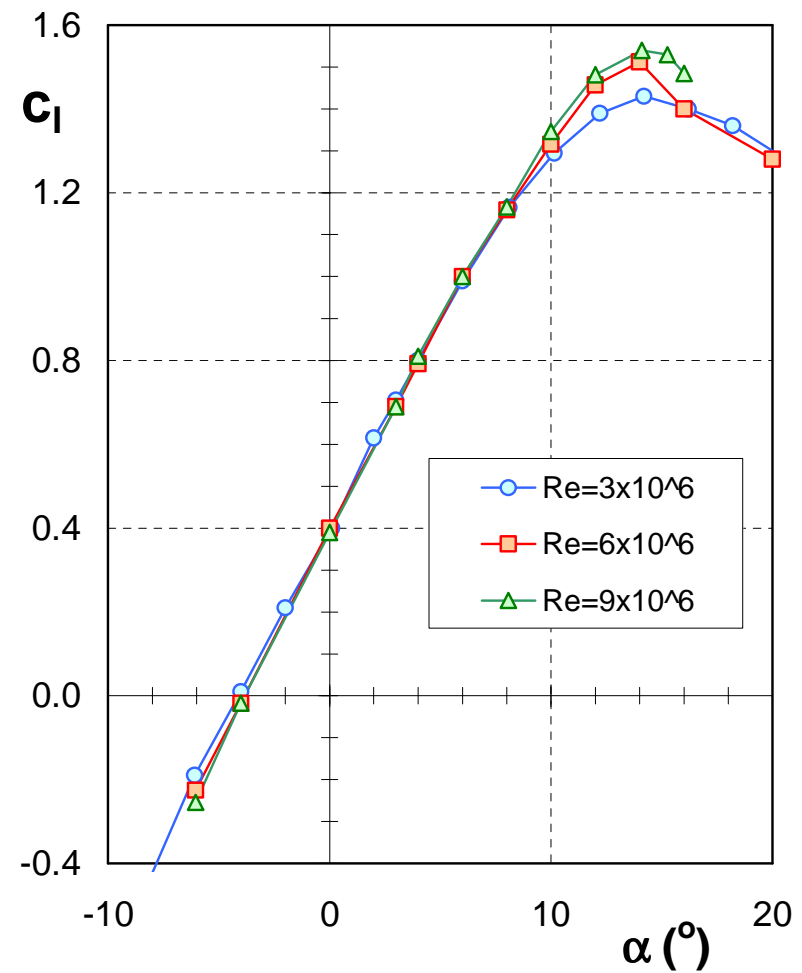
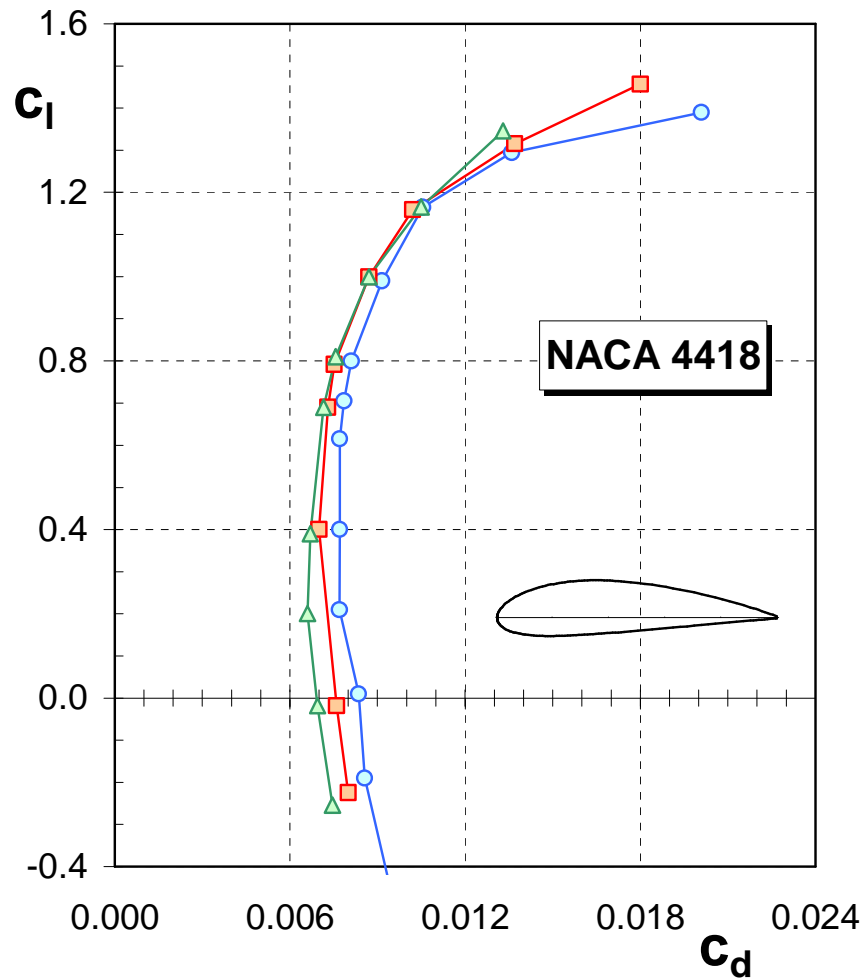


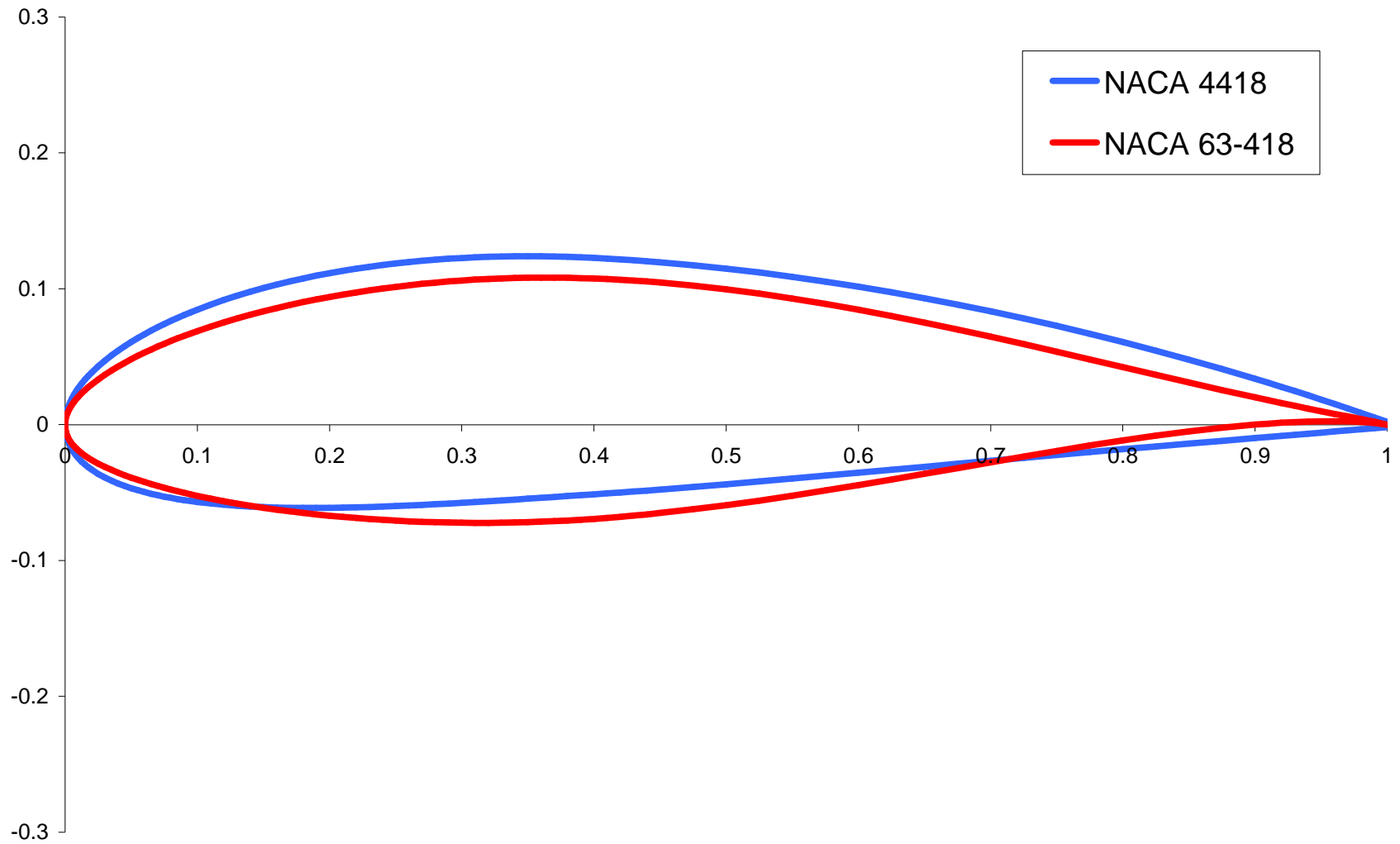


# Effect of airfoil maximum thickness

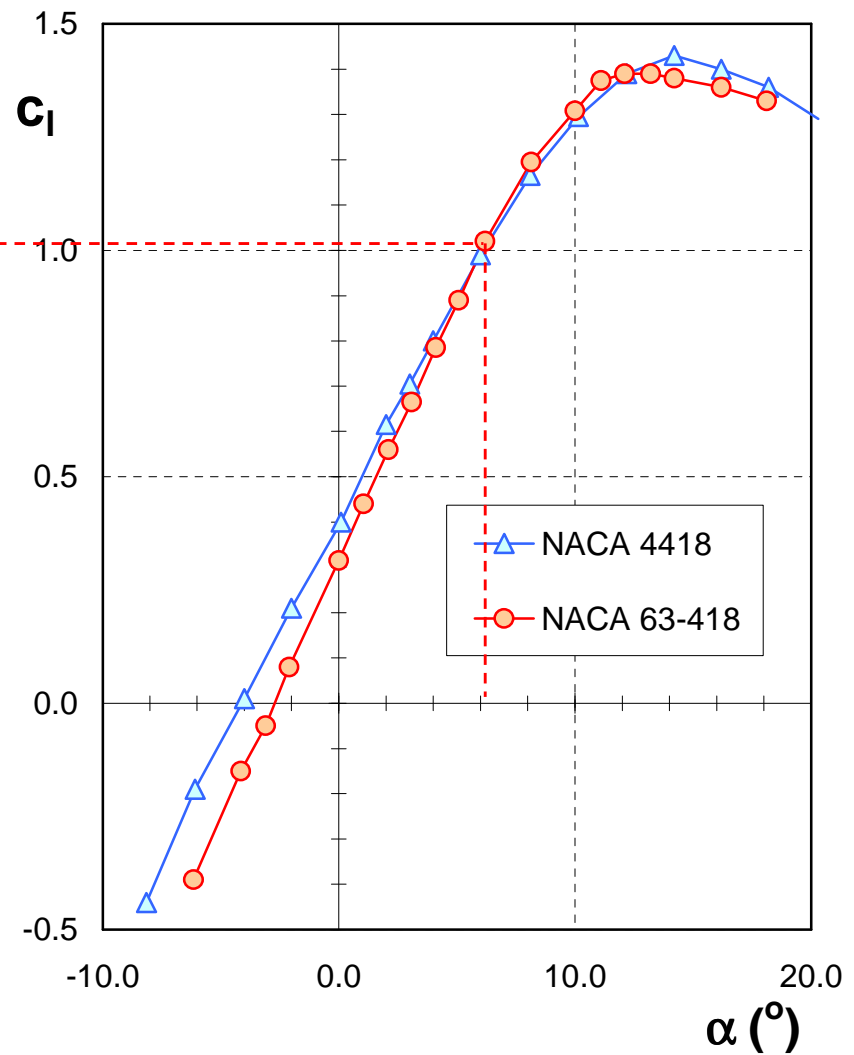
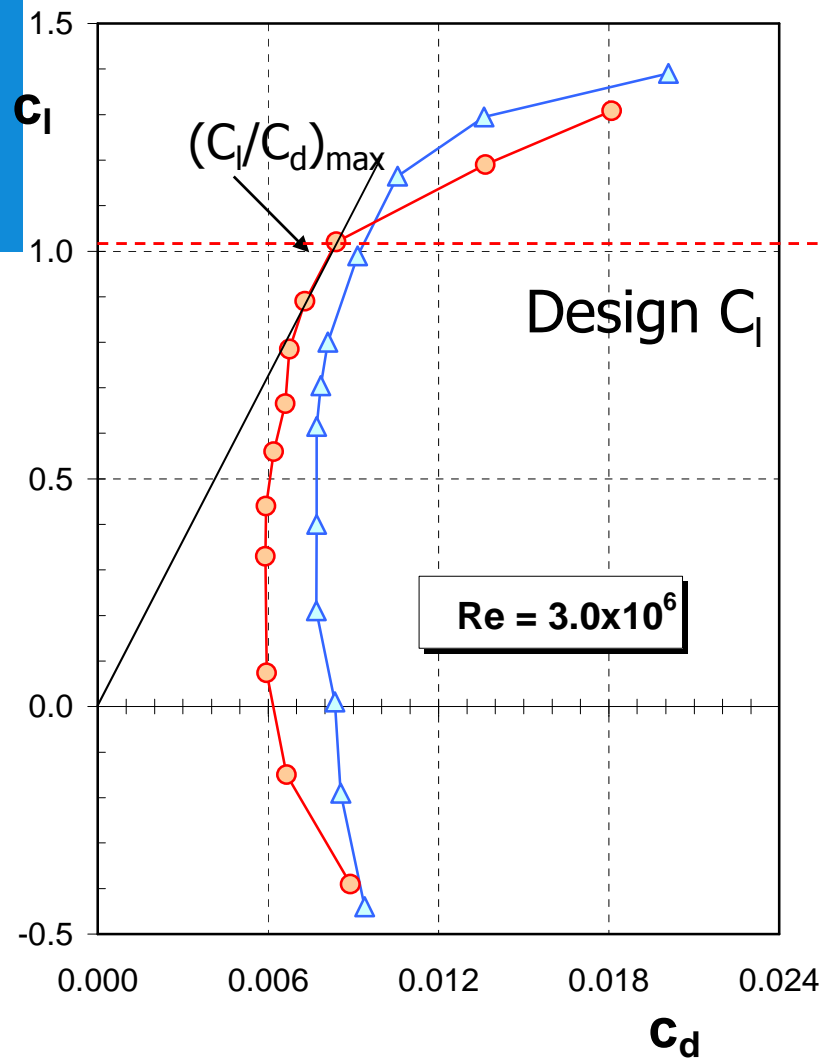


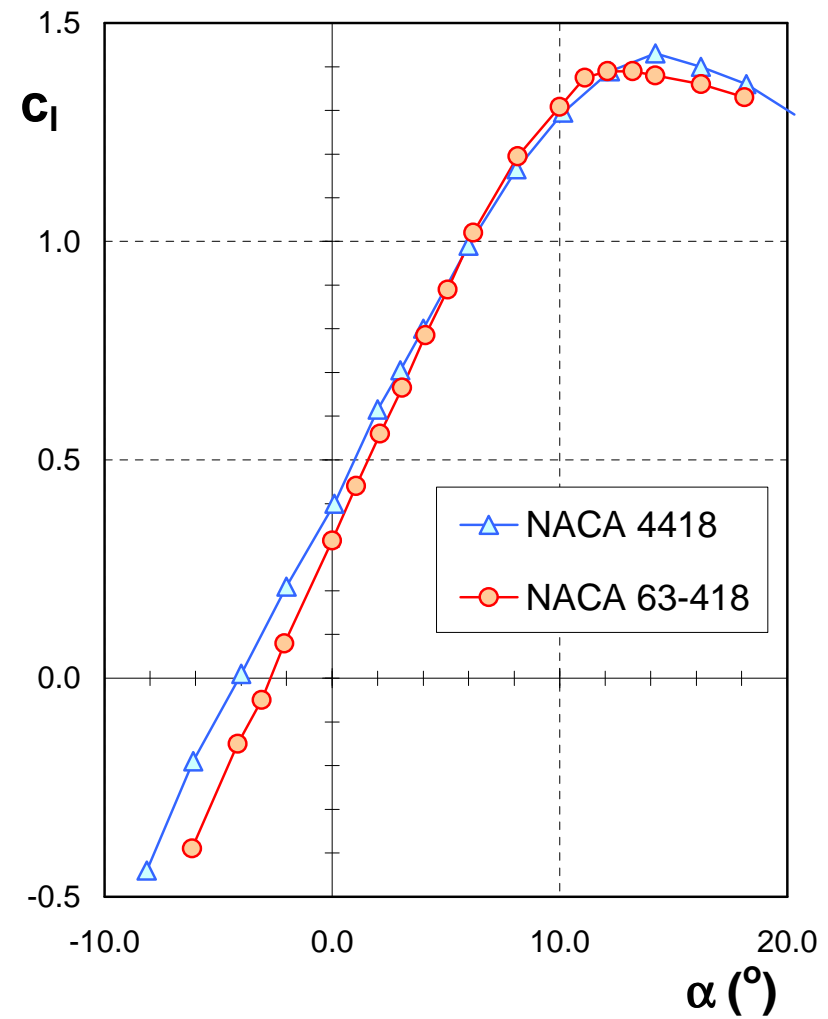
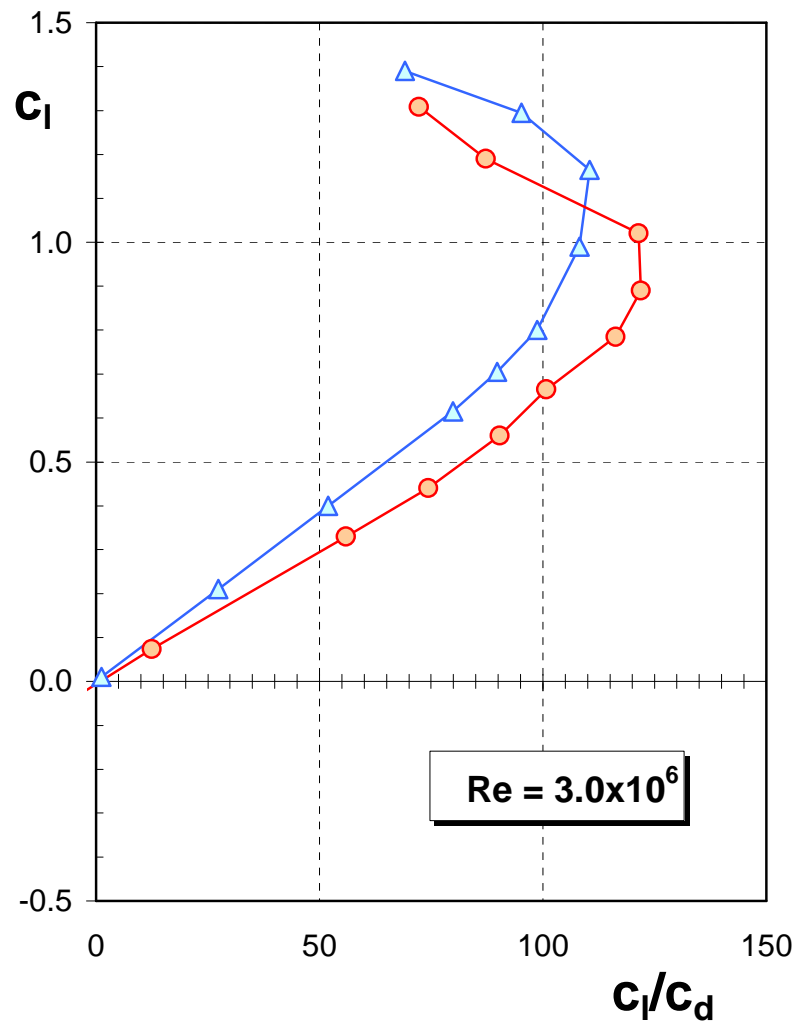
# Effect of Reynolds number



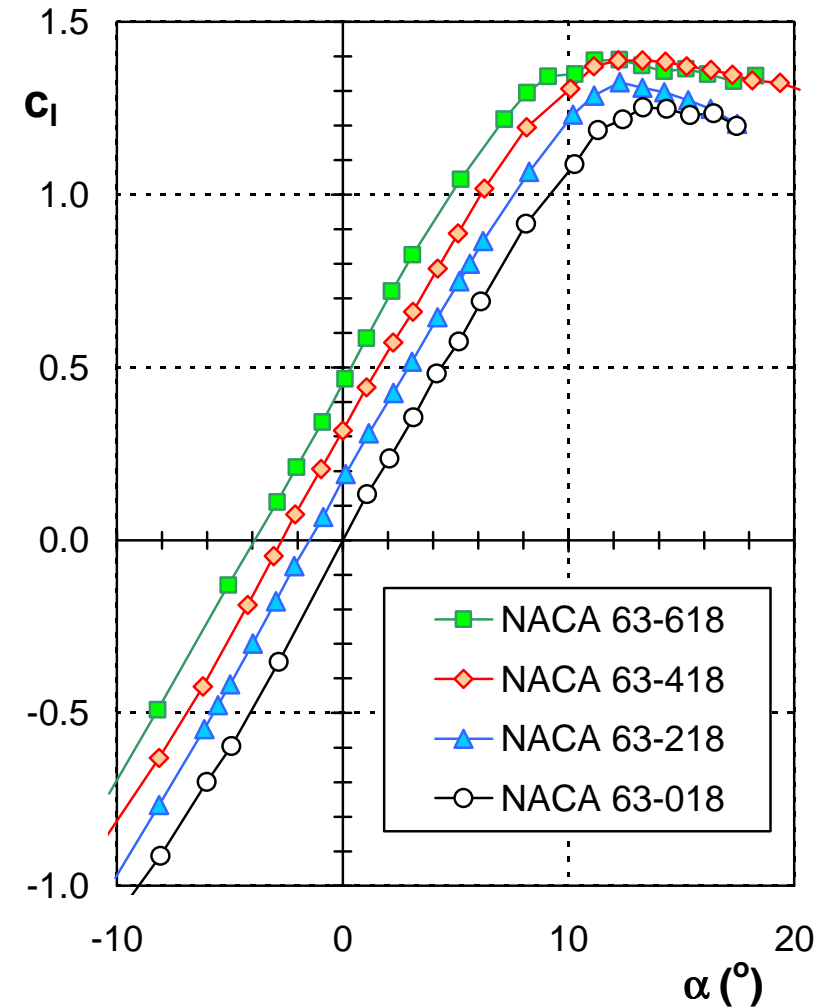
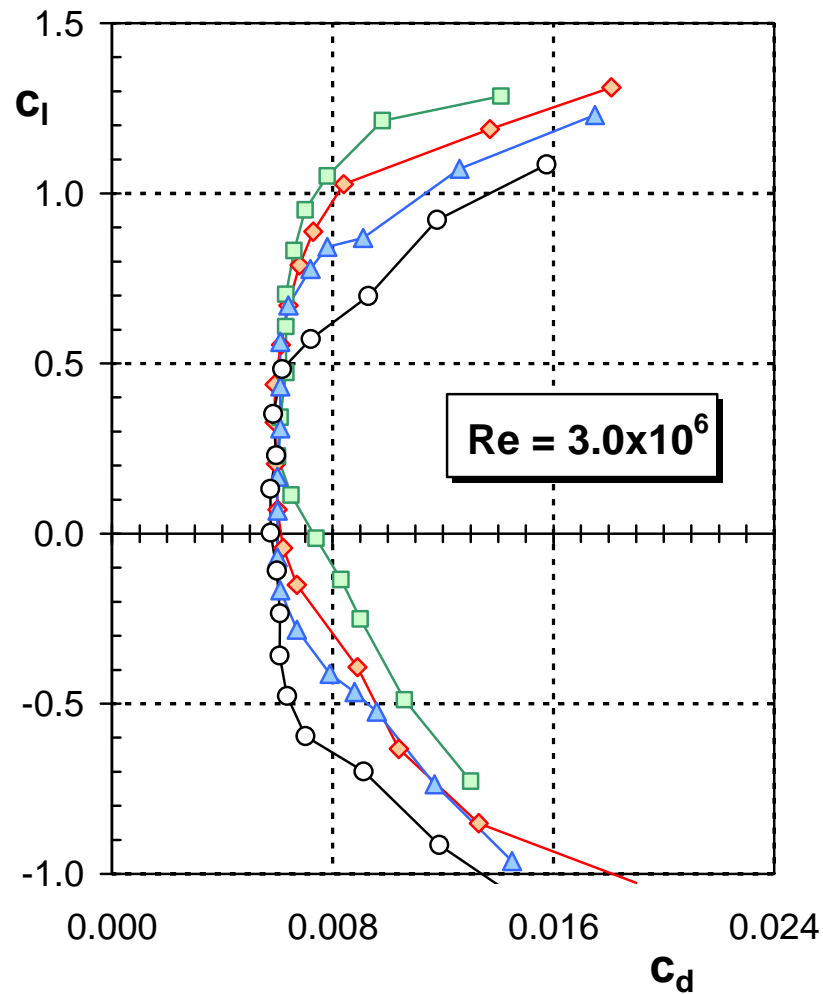


# A turbulent and a laminar airfoil



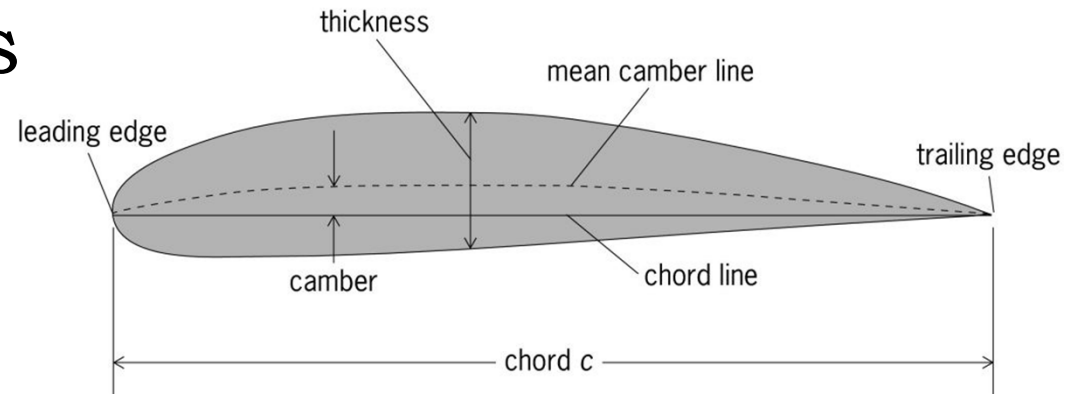


# The effect of camber on the NACA 63-series



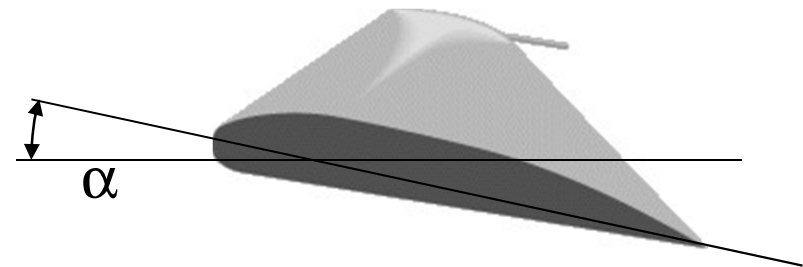


# Lift-parameters



$C_l$  (Lift coefficient) depends on (a.o.)

- airfoil or wing profile
- angle of attack ( $\alpha$ )



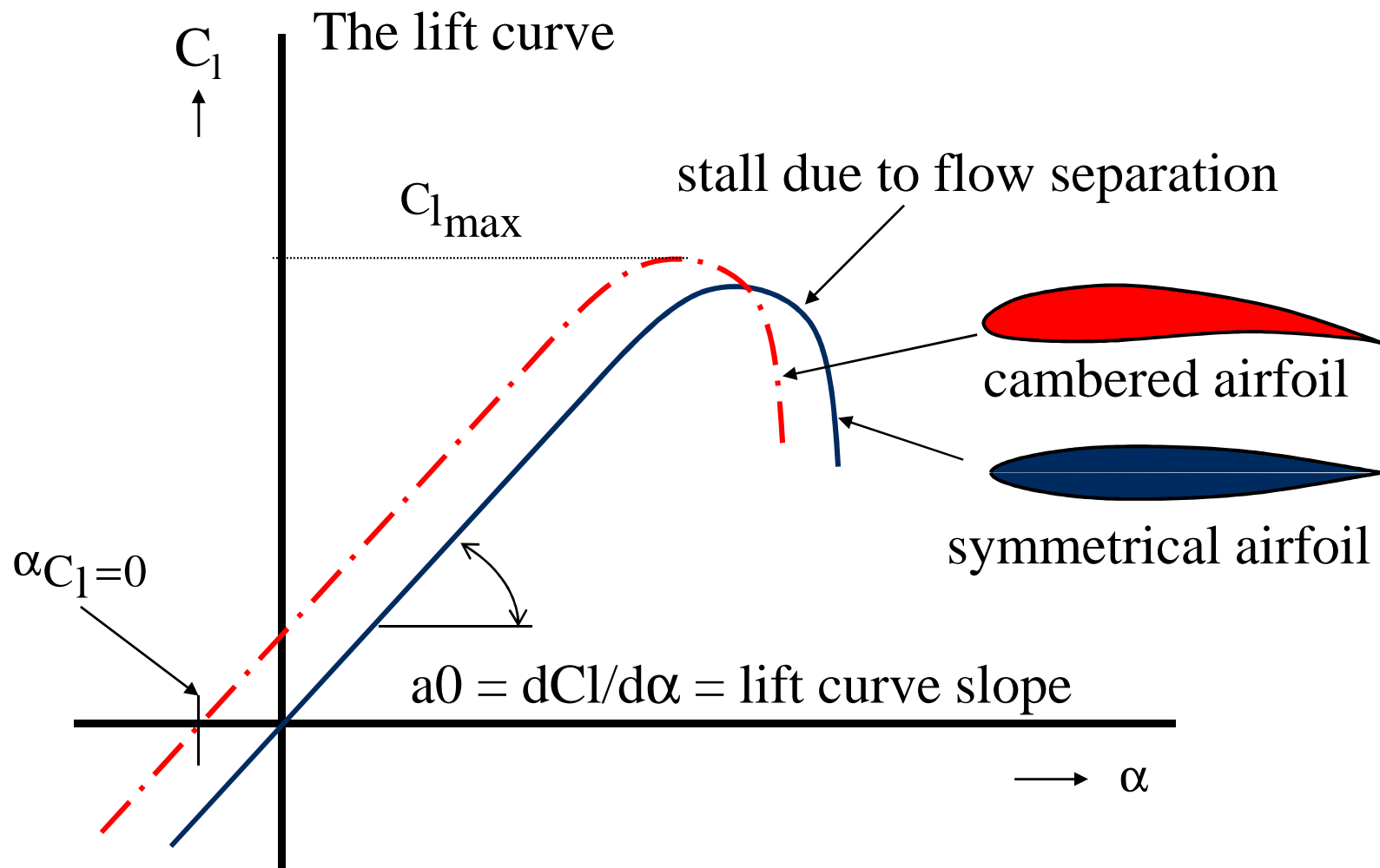
$\rho$  (air density) depends on:

- altitude & temperature (atmosphere)

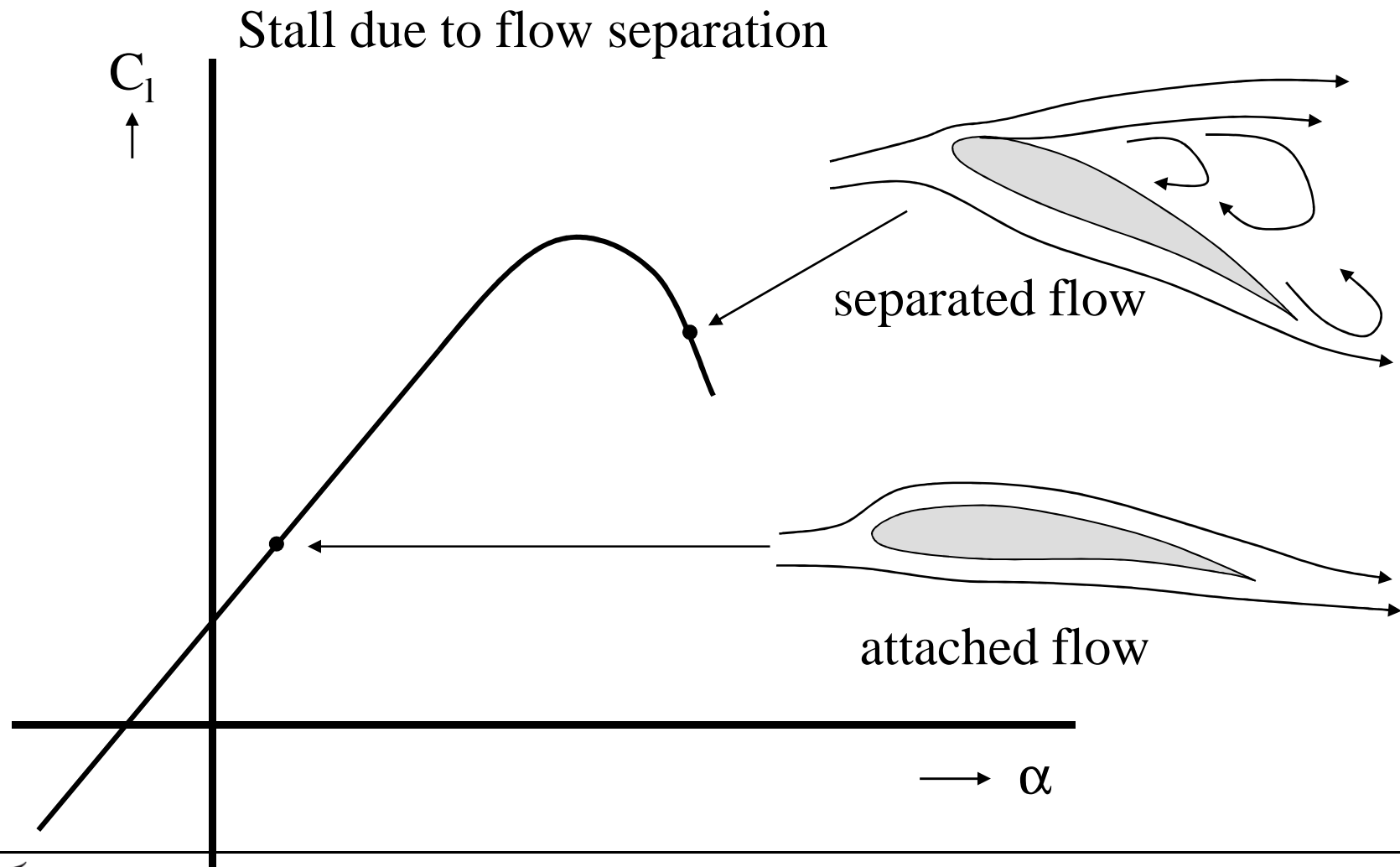
$V$  (air speed) and  $S$  (wing area) are design parameters

Lift due to **pressure differences** over the airfoil - Bernoulli

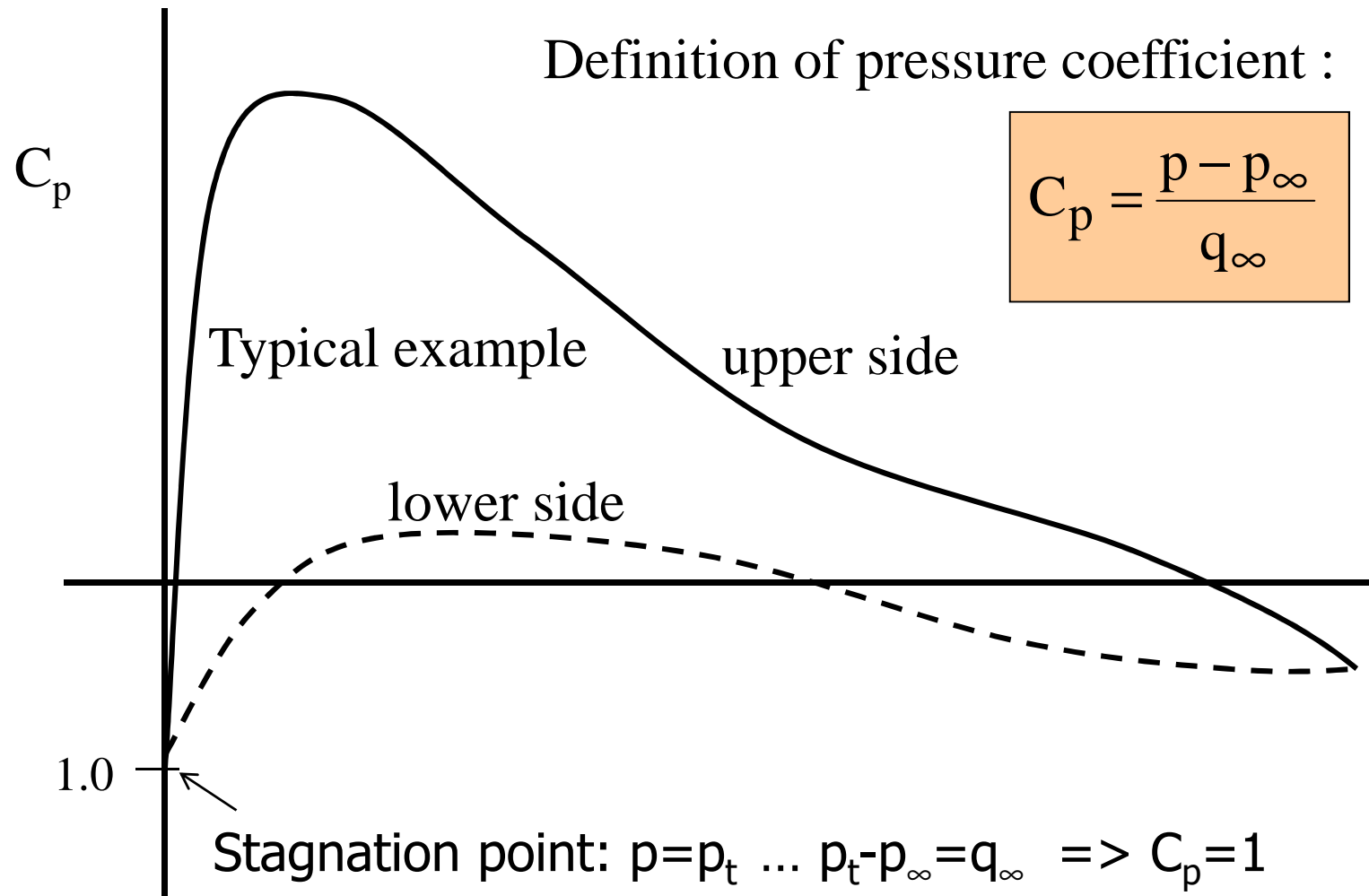
# Airfoil data



# Airfoils



# Pressure coefficient (negative is up)



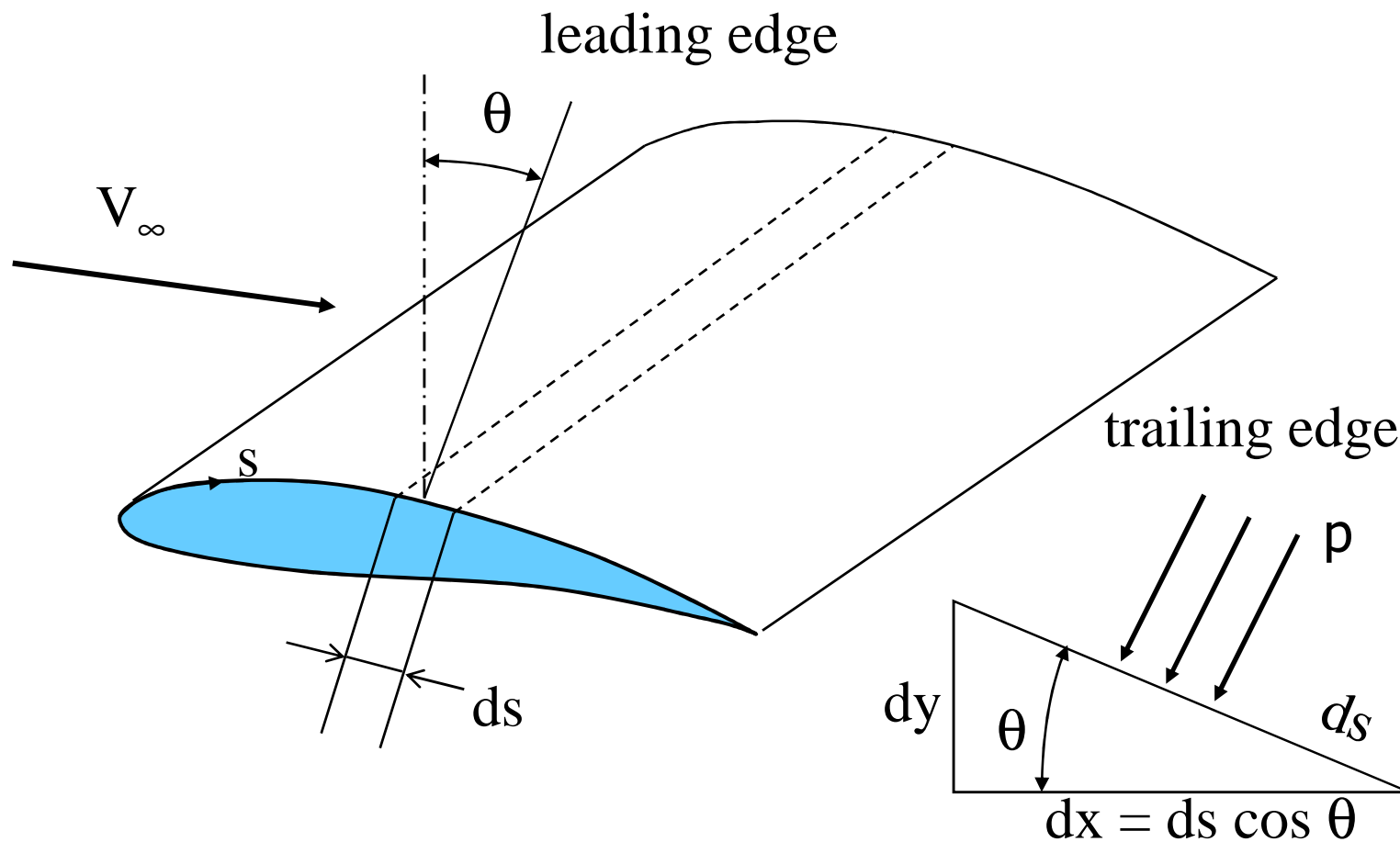
## Example 5.6

- The pressure on a point on the wing of an airplane is  $7.58 \times 10^4$  N/m<sup>2</sup>. The airplane is flying with a velocity of 70 m/s at conditions associated with standard altitude of 2000m. Calculate the pressure coefficient at this point on the wing

$$2000 \text{ m:} \quad p_{\infty} = 7.95 \cdot 10^4 \text{ N/m}^2 \quad \rho_{\infty} = 1.0066 \text{ kg/m}^3$$

$$C_p = \frac{p - p_{\infty}}{q_{\infty}} \quad \Rightarrow \quad C_p = -1.50$$

# Obtaining lift from pressure distribution



# Obtaining lift from pressure distribution

Normal force per meter span:  $N = \int_{LE}^{TE} p_l \cos \theta ds - \int_{LE}^{TE} p_u \cos \theta ds$

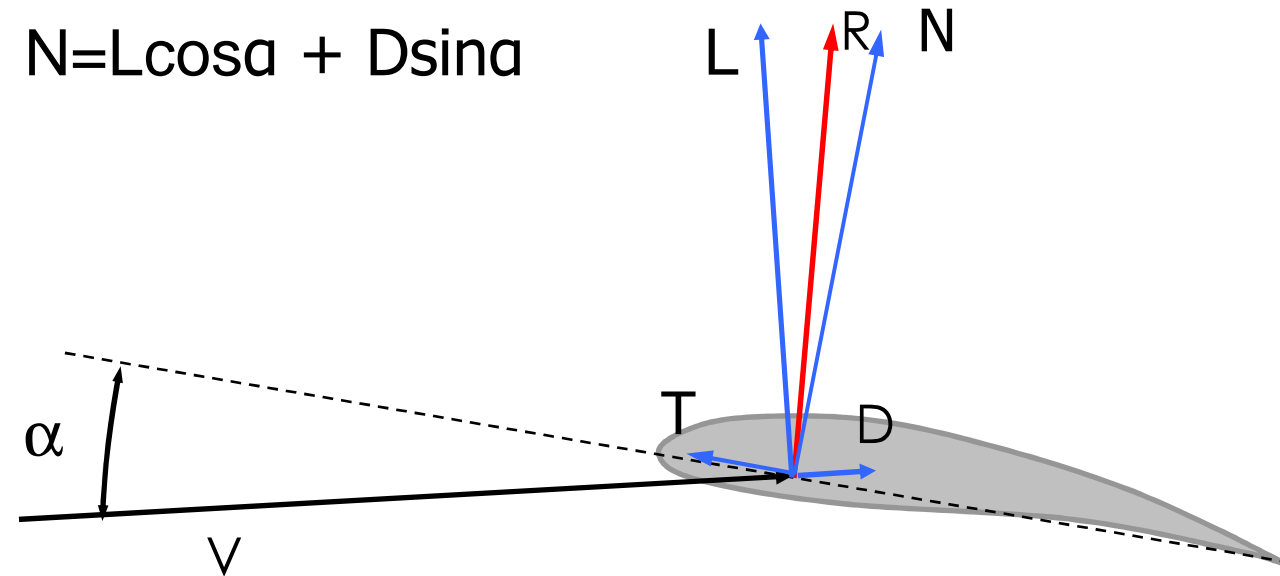
with  $ds \cos \theta = dx$   $N = \int_0^c p_l dx - \int_0^c p_u dx$

Write dimensionless force coefficient:  $C_n = \frac{N}{\frac{1}{2} \rho V_\infty^2 c} = \frac{N}{q_\infty c}$

$$C_n = \int_0^1 \frac{p_l - p_\infty}{q_\infty} d\left(\frac{x}{c}\right) - \int_0^1 \frac{p_u - p_\infty}{q_\infty} d\left(\frac{x}{c}\right)$$

$$C_n = \int_0^1 (C_{p_l} - C_{p_u}) d\left(\frac{x}{c}\right)$$

$$T = L \sin \alpha - D \cos \alpha$$
$$N = L \cos \alpha + D \sin \alpha$$



$\alpha$  = angle of attack



# Obtaining lift from normal force coefficient

$$L = N \cos \alpha - T \sin \alpha$$

$$c_l = c_n \cos \alpha - c_t \sin \alpha$$

$$\frac{L}{q_\infty c} = \frac{N}{q_\infty c} \cos \alpha - \frac{T}{q_\infty c} \sin \alpha$$

For small angle of attack  $\alpha \leq 5^\circ$  :  $\cos \alpha \approx 1$ ,  $\sin \alpha \approx 0$

$$C_l \approx \frac{1}{c} \int_0^1 (C_{p_l} - C_{p_u}) d(x)$$

## Example 5.11

Consider an airfoil with chord length  $c$  and the running distance  $x$  measured along the chord. The leading edge is located at  $x/c=0$  and the trailing edge at  $x/c=1$ . The pressure coefficient variations over the upper and lower surfaces are given as

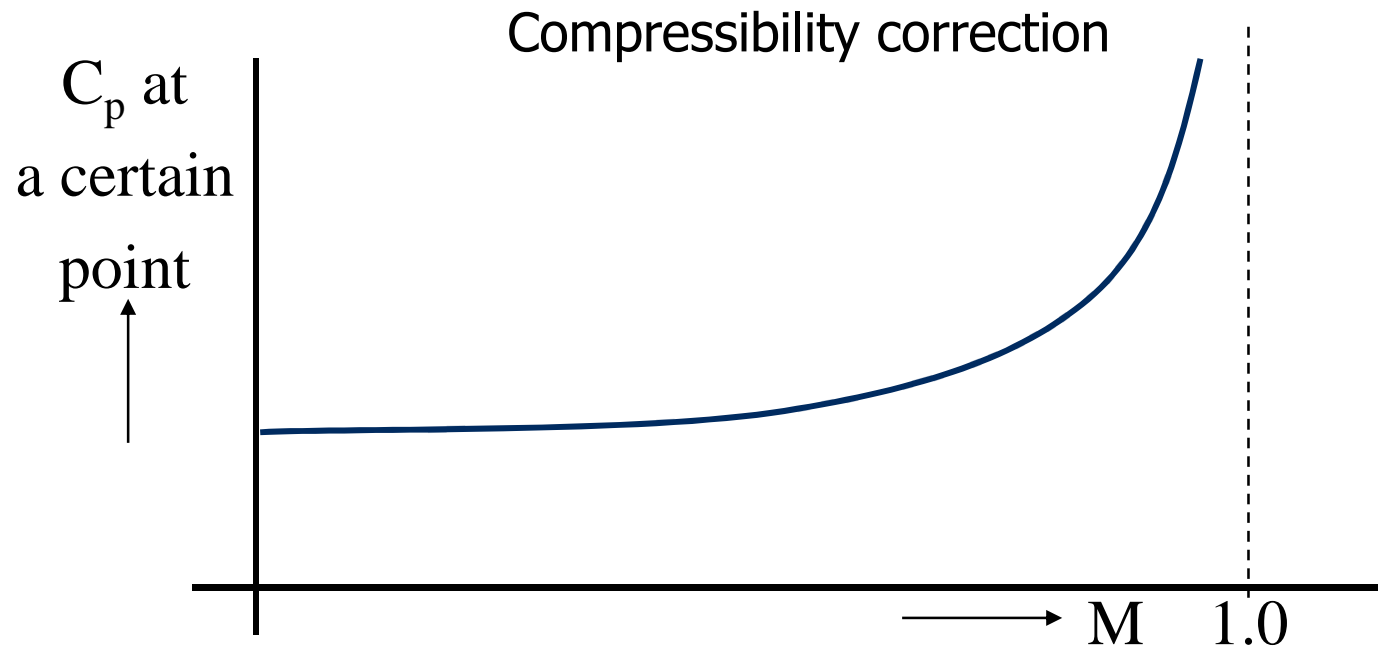
$$C_{p,u} = 1 - 300 \left( \frac{x}{c} \right)^2 \quad \text{for } 0 \leq \left( \frac{x}{c} \right) \leq 0.1$$

$$C_{p,u} = -2.2777 + 2.2777 \left( \frac{x}{c} \right) \quad \text{for } 0.1 \leq \left( \frac{x}{c} \right) \leq 1.0$$

$$C_{p,l} = 1 - 0.95 \left( \frac{x}{c} \right) \quad \text{for } 0 \leq \left( \frac{x}{c} \right) \leq 1.0$$

Calculate the normal force coefficient.

# Compressibility correction of the pressure coefficient



Approximate theoretical correction (valid for  $0 < M < 0.7$ ) :

$$C_p = \frac{C_{p,0}}{\sqrt{1 - M_\infty^2}}$$

Prandtl-Glauert Rule

# Compressibility correction for lift coefficient

$$C_l \approx \frac{1}{c} \int_0^c \frac{(C_{p_l} - C_{p_u})_o d(x)}{\sqrt{1 - M_\infty^2}} =$$

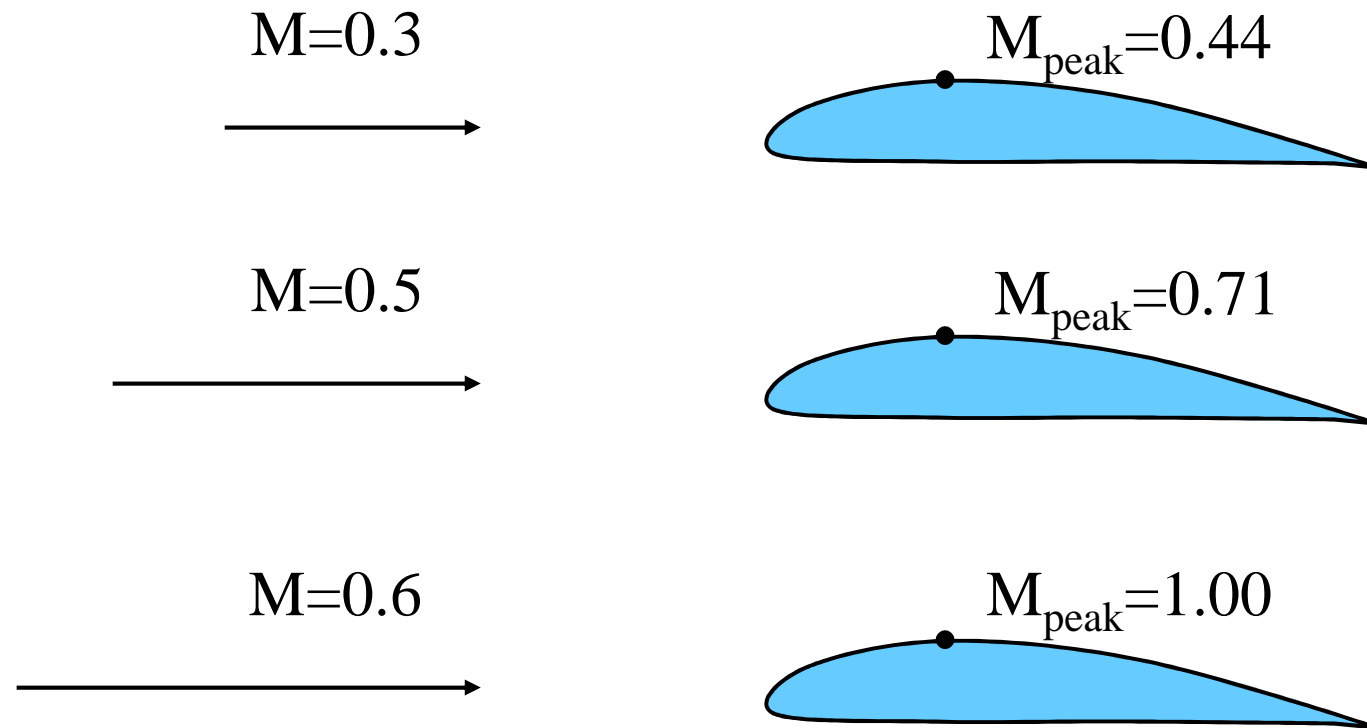
$$C_{l,0} \equiv \frac{1}{c} \int_0^c (C_{p_l} - C_{p_u})_o d(x)$$

$$C_l = \frac{C_{l,0}}{\sqrt{1 - M_\infty^2}}$$

## Example 5.12

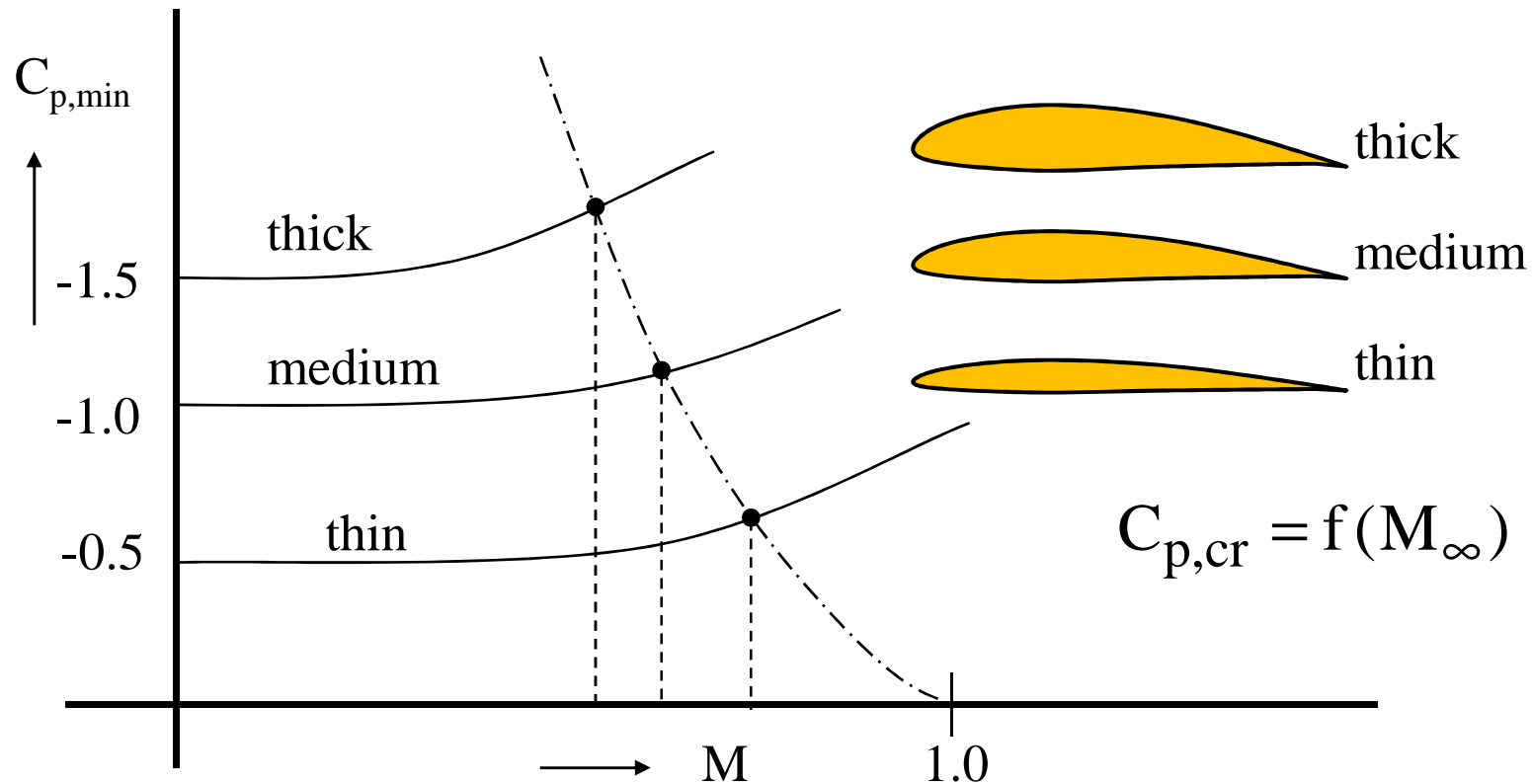
- Consider an NACA 4412 airfoil at an angle of attack of  $4^\circ$ . If the free-stream Mach number is 0.7, what is the lift coefficient?
- - From App. D for angle of attack of  $4^\circ$ ,  $c_l = 0.83$ . However, these data were obtained at low speeds. Use the Prandtl-Glauert correction to calculate the lift coefficient at  $M=0.7$

# Critical Mach number and critical pressure coefficient



Critical Mach number for the airfoil

# Critical pressure coefficient



Thicker airfoil reaches critical pressure coefficient  
at a lower value of  $M_\infty$