

**Final Examination**  
**Electronic Instrumentation (ET8017)**

**Monday, November 5, 2012, 14:00-17:00**

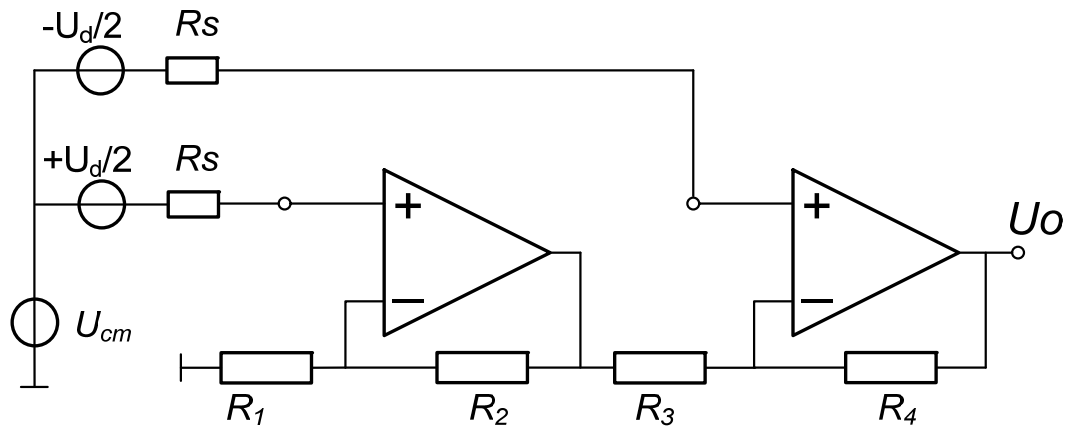
There are 5 questions in the exam  
**all** of which should be attempted.

Please support your answers with the appropriate  
explanations, drawings and circuit diagrams

**Only the book and the slides**  
can be taken into the exam

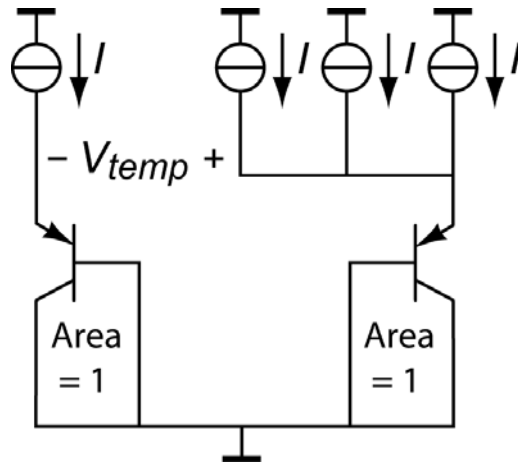
— Good luck! —

1. Figure below shows an instrumentation amplifier (INA), built from two identical opamps, which is connected to a sensor with a source impedance  $R_s = 10 \text{ k}\Omega$ .



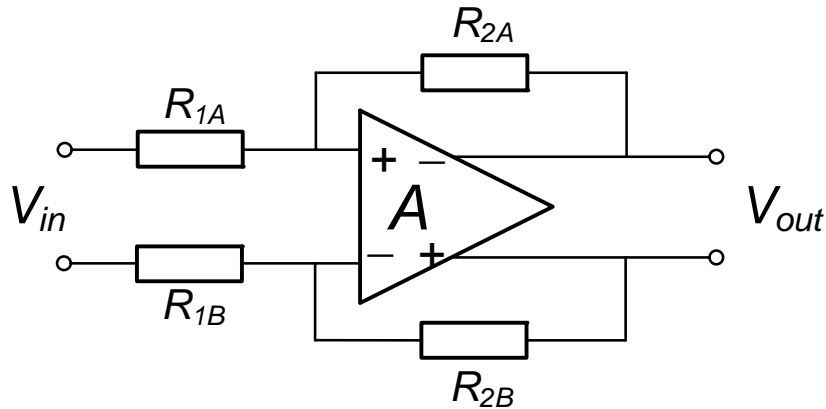
- A) If the INA has a gain of 100 and  $R_2 = R_3 = 10 \text{ k}\Omega$ , what must the values of the other resistors  $R_1$  and  $R_4$  be?
- B) Calculate the detection limit due to offset and input bias current if each opamp has the following specifications:
- |                       |                           |
|-----------------------|---------------------------|
| Input offset voltage: | $V_{os} = 1 \text{ mV}$   |
| Input offset current: | $I_{os} = 100 \text{ nA}$ |
| Input bias current:   | $I_b = 50 \text{ nA}$     |
- C) If the amplifier's output  $U_o$  can swing from 0 to 5V and  $U_{cm} = 2.5 \text{ V}$ , calculate the maximum value of the differential input signal  $U_d$  for a distortion-free output.
- D) If the various resistor ratios suffer from up to 1% mismatch, calculate the worst-case value of the INA's  $CMRR$ .

- 2.** The following circuit employs two BJTs and four current sources to generate a voltage  $V_{temp}$  that is proportional to absolute temperature.

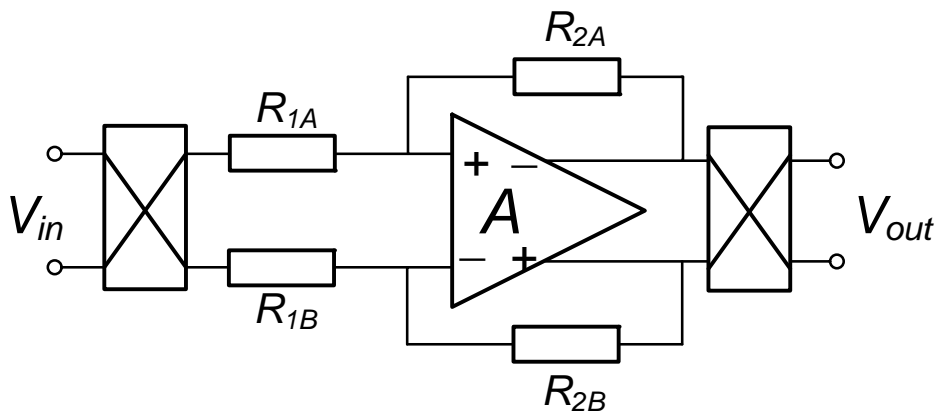


- A)** Derive an expression for  $V_{temp}$  in terms of the Boltzmann constant  $k$  and the electron charge  $q$ .
- B)** Assuming that one of the current sources suffers from 1% mismatch at room temperature ( $21^\circ\text{C}$ ), calculate the worst-case equivalent temperature error in  $V_{temp}$ .
- C)** Using a circuit diagram, describe how dynamic-element matching (DEM) can be used to mitigate the effects of the current source mismatch on the accuracy of  $V_{temp}$ . How many switches are required for your scheme?
- D)** After the application of this DEM scheme, compute the equivalent temperature error in the average value of  $V_{temp}$ .

3. Figure below shows a fully differential amplifier based on a differential opamp with an input referred noise of  $30 \text{ nV}/\sqrt{\text{Hz}}$  and  $10\text{mV}$  offset.

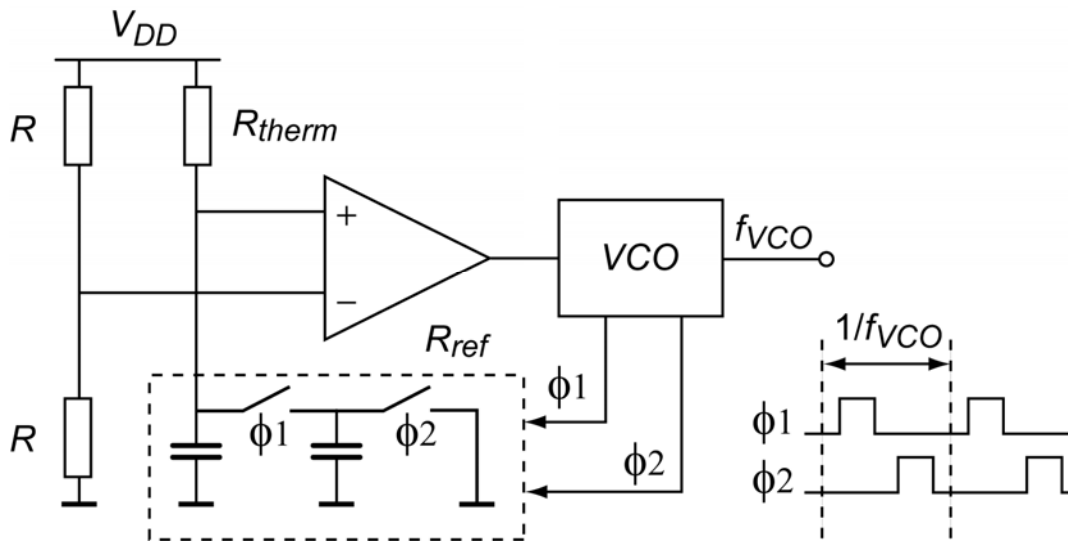


- A) If the amplifier is to have a closed-loop gain of 100 and an input resistance of  $100\text{k}\Omega$ , calculate the corresponding values of  $R_{2A} = R_{2B}$  and  $R_{1A} = R_{1B}$ .
- B) If the amplifier is to have a closed-loop gain of 100 and an input-referred noise is less than  $50\text{nV}/\sqrt{\text{Hz}}$ , find the maximum (or minimum) value for the input resistors ( $R_{1A}$  and  $R_{1B}$ ). Note:  $4\text{kT} = 1.62 \times 10^{-20} \text{ (W/Hz)}$ .
- C) To reduce the effect of the opamp's offset, the entire amplifier is chopped as shown below. Make a sketch of the output waveform assuming that the input signal has a common-mode voltage of  $0\text{V}$  and a differential voltage of  $10\text{mV}$ . What is the input-referred amplitude of the ripple?



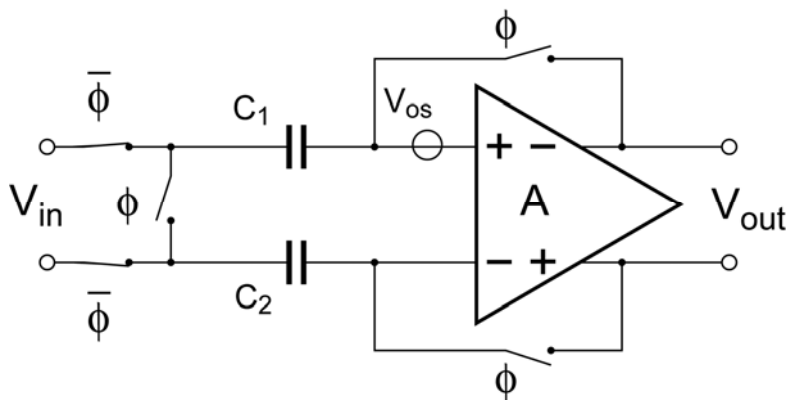
- D) To reduce the amplitude of the output ripple, the chopped amplifier is followed by a 1<sup>st</sup> order low-pass filter. Given that the amplifier's input-referred noise is  $50 \text{ nV}/\sqrt{\text{Hz}}$  and the chopping frequency is  $10\text{kHz}$ , calculate the maximum cut-off frequency of the low-pass filter such that the input-referred amplitude of the ripple is less than the input-referred rms noise.

4. Consider the circuit below in which a thermistor  $R_{therm}$  is incorporated in a bridge circuit, which further consists of two fixed resistors and a variable reference resistance  $R_{ref}$ . This is implemented as a switched-capacitor network that periodically dumps charge to ground and whose effective resistance depends on the frequency  $f_{VCO}$  output by a voltage-controlled oscillator (VCO). Capacitor  $C_1$  is much larger (100x) than  $C_2$  and serves as a charge reservoir that reduces the ripple across  $R_{therm}$  to negligible levels. The bridge is embedded in a feedback loop, which adjusts  $f_{VCO}$  in such a way that the bridge is always balanced.



- A) Derive an expression for  $R_{ref}$  in terms of  $f_{VCO}$ . Given that  $C_2 = 4\text{pF}$  and that  $R_{therm} = 6.6\text{ k}\Omega$  at room temperature, what is the corresponding value of  $f_{VCO}$ ?
- B) Assuming that  $R_{therm}$  has a tempco of  $0.3\%/K$ , what change in  $f_{VCO}$  corresponds to a  $1\text{mK}$  temperature change and how many bits of resolution are required to digitize this frequency change such that the resulting error is less than  $\frac{1}{2}$  an LSB.
- C) If  $V_{DD} = 1.8\text{V}$ , what amount of opamp offset corresponds to an error of  $0.1^\circ\text{C}$
- D) DISCUSS the effect of the following non-idealities on the circuit: a non-linear VCO transfer function, VCO jitter, the charge injection associated with the two switches in the  $R_{ref}$  circuit..

5. Consider the auto-zeroed amplifier shown below:



- A) If the amplifier's offset  $V_{os} = 10\text{mV}$ , determine the gain  $A$  of the basic amplifier such that the input-referred offset after auto-zeroing is less than  $1\mu\text{V}$ .
- B) If both the auto-zeroing and the amplification phases last  $10\mu\text{s}$ , and given that all the switches have an on-resistance of  $2\text{k}\Omega$ , determine the worst-case value of  $C_1$  ( $= C_2$ ) such that settling errors are below  $1\mu\text{V}$  (input-referred). Note: the opamp may be assumed to be ideal.
- C) If both the auto-zeroing and the amplification phases last  $10\mu\text{s}$ , determine the unity-gain bandwidth of the opamp such that all settling errors are below  $1\mu\text{V}$  (input-referred). Note: the switches may be assumed to be ideal.
- D) If the amplifier is assumed to be noise-free, what value of  $C_1$  ( $= C_2$ ) ensures that the residual input-referred noise after auto-zeroing is less than  $1\mu\text{V}$  (rms).  
 Note:  $4kT = 1.62 \times 10^{-20}$  (W/Hz)