

# Elektrische Aandrijvingen

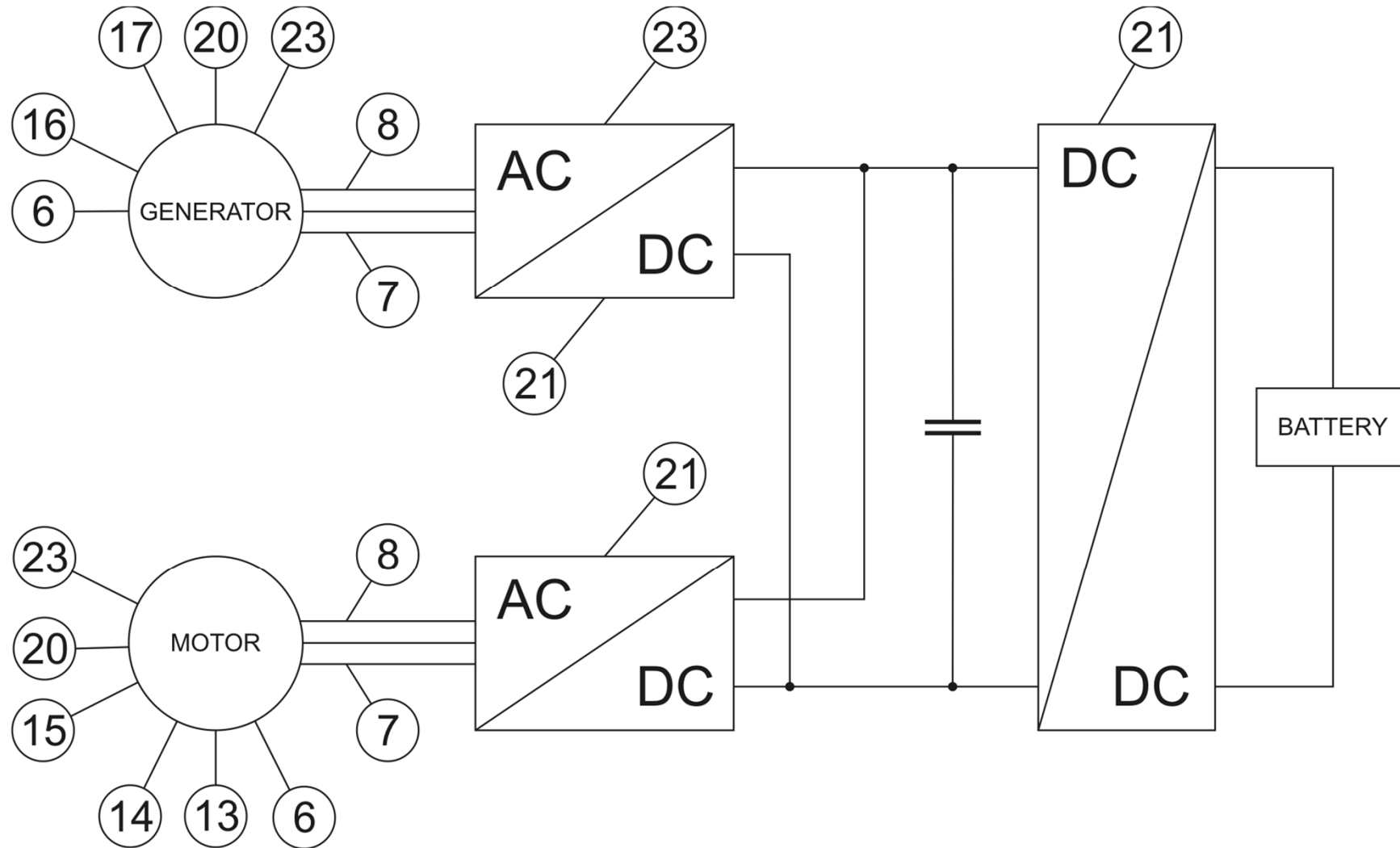
WTB

Lokatie/evenement

P.BAUER

February 22, 2013

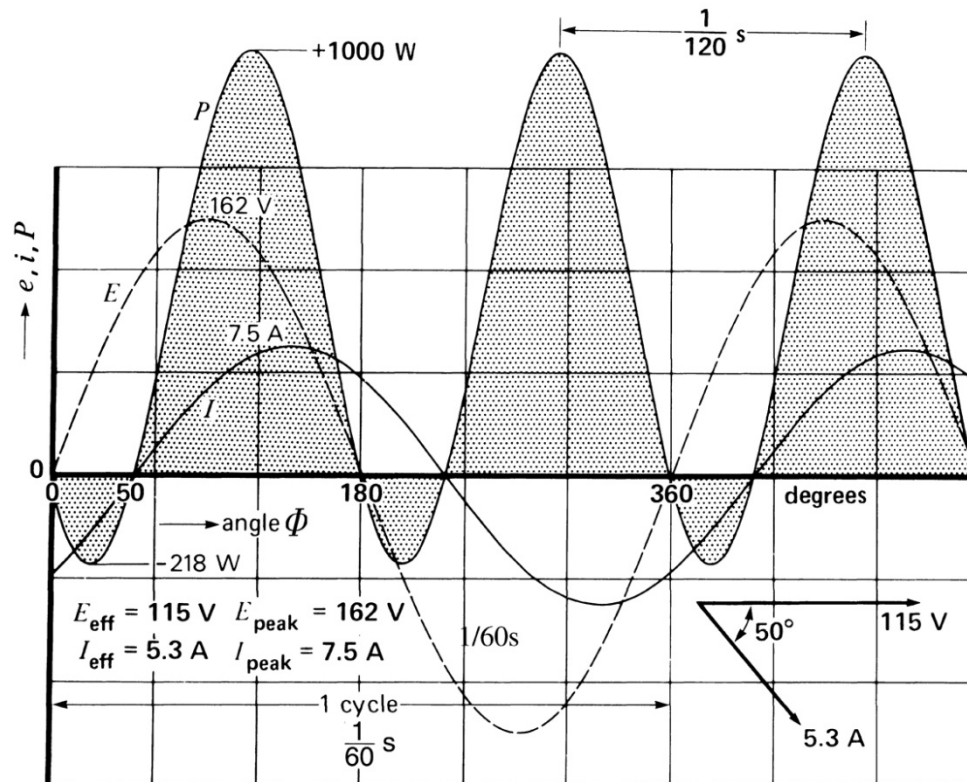
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# Active, Reactive and Apparent Power

Voltage 162 V, 60Hz  
Current 7,5A lags 50

FIGURE 7-1 Instantaneous voltage, current, and power in an ac circuit. (See Example 7-1.)

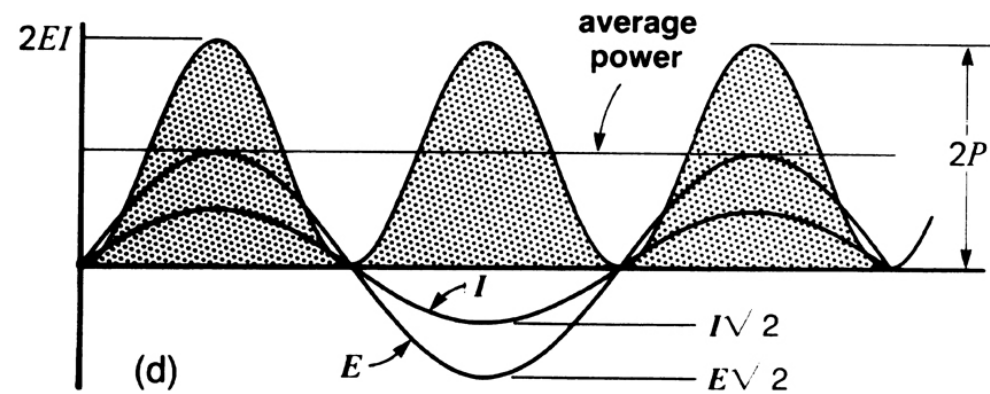
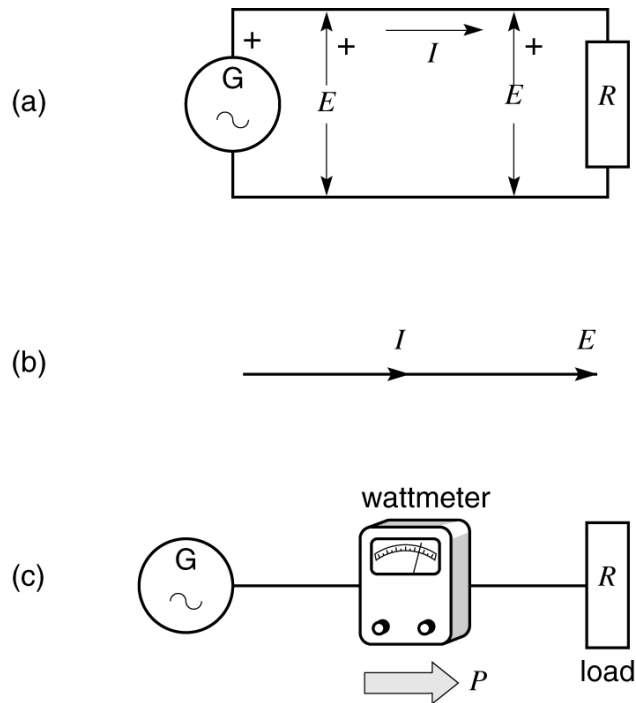


Voltage and current  $\Phi$   
Inst.voltage, current, p  $120^\circ$

- $e = E_m \sin \Phi = 162 \sin \Phi$
- $i = I_m \sin(\Phi - \theta) = 7,5 \sin(\Phi - 50^\circ)$
- $\Phi = 120^\circ$
- $i = 7,05 \text{ A}$
- $p = e \cdot i = 140.3 \times 7,05$

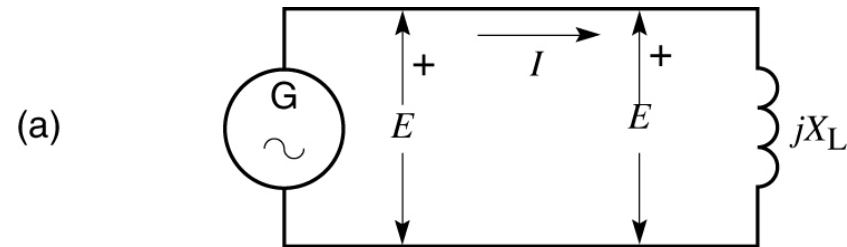
# Active Power

FIGURE 7-2 a. An ac voltage  $E$  produces an ac current  $I$  in this resistive circuit. b. Phasors  $E$  and  $I$  are in phase. c. A wattmeter indicates  $EI$  watts. d. The active power is composed of a series of positive power pulses.

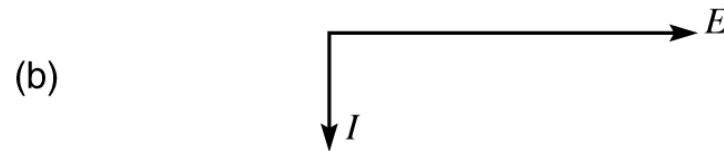


# Reactive Power

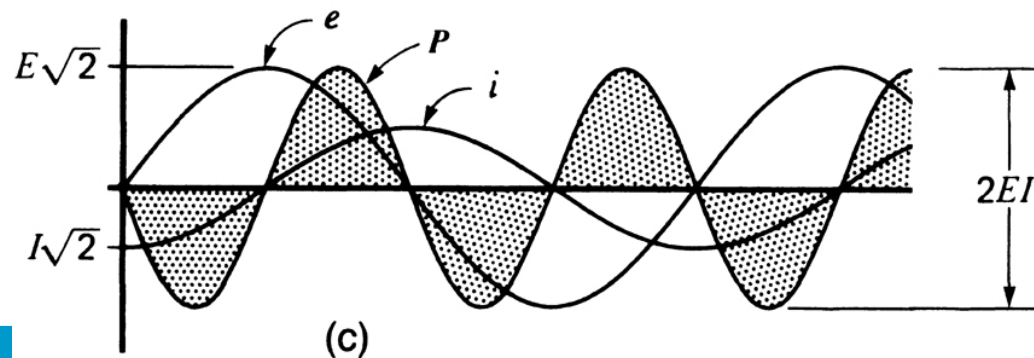
FIGURE 7-4 a. An ac voltage  $E$  produces an ac current  $I$  in this inductive circuit. b. Phasor  $I$  lags  $90^\circ$  behind  $E$ . c. Reactive power consists of a series of positive and negative power pulses.



What is load and what is source of reactive power?

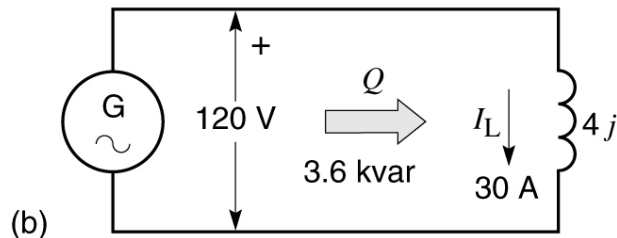
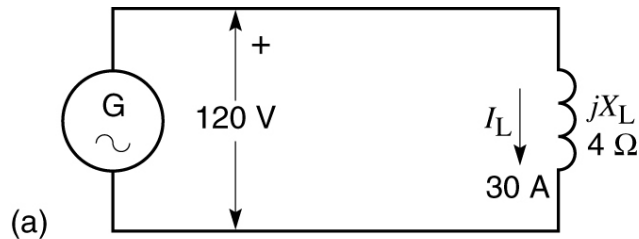


Impossible to say, reactor is considered to be a reactive load



# Reactive Load and Reactive Source

FIGURE 7-6 See Example 7-2.



Reactor having an inductive reactance  $4 \Omega$ , connected to 120 V AC generator

- Calculate the current
- Calculate the reactor power
- Calculate generator power
- Draw the phasor diagram

- $I_L = E/X_L = 120/4 = 30 \text{ A}$
- $Q = EI = 120 \cdot 30 = 3,6 \text{ kVAr}$

# Capacitor and Reactive Power

## Add capacitor

FIGURE 7-6 See Example 7-2.

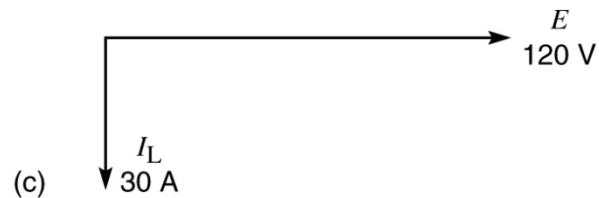
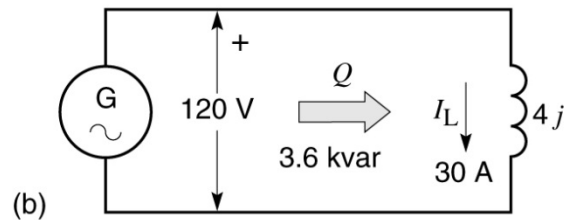
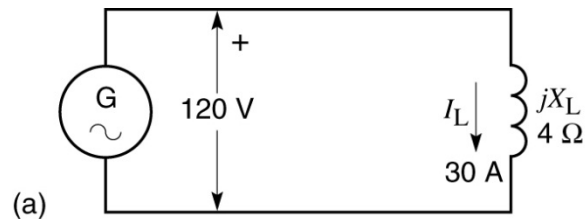
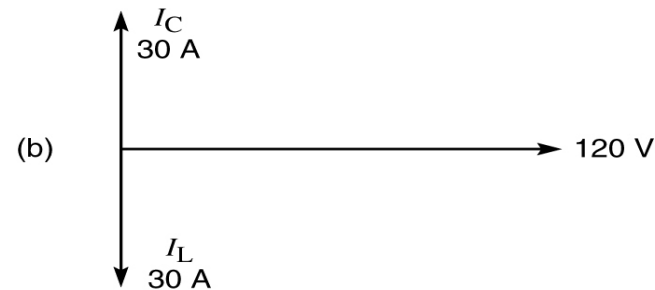
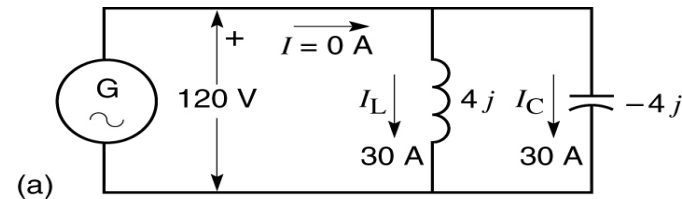


FIGURE 7-7 See Example 7-3.

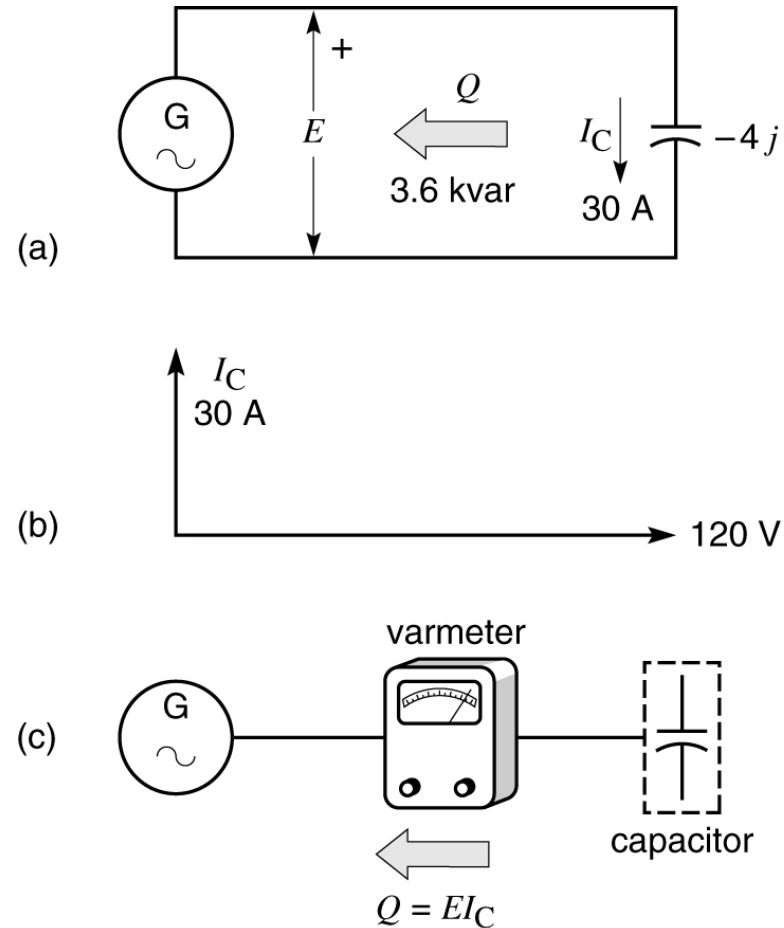


Generator does not supply any power

- Reactive power delivered by capacitor
- $Q = E I_C = 120 \cdot 30 = 3,6 \text{ kVAR}$

# Capacitor and Reactive Power

FIGURE 7-8 a. Capacitor connected to an ac source. b. Phase  $I_C$  leads  $E$  by  $90^\circ$ . c. Reactive power flows from the capacitor to the generator.

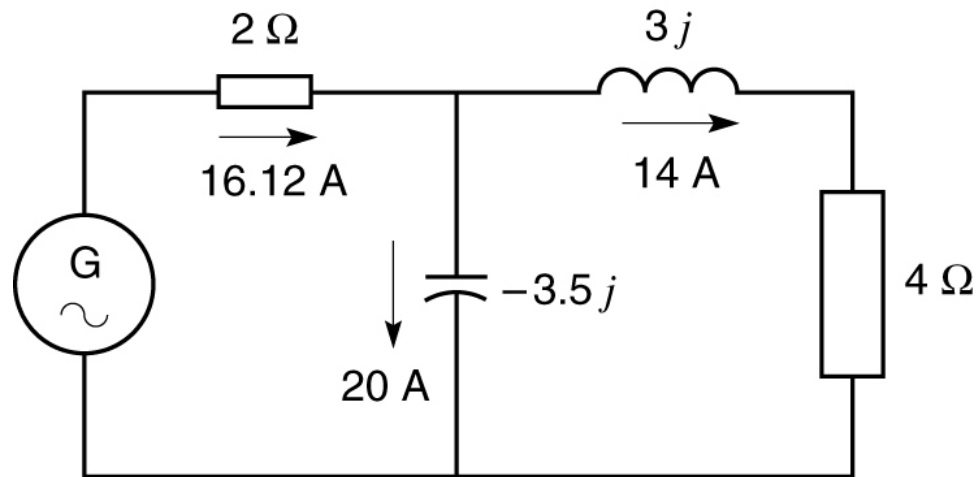


Where does the power go ? Capacitor delivers reactive power to the generator



## Example 7.3

- Calculate the Active and reactive power of G



- $P = R I^2 = 14^2 \cdot 4 + 16,12^2 \cdot 2 = 1304\text{W}$
- $Q_l = X_l I^2 = 14^2 \cdot 3 = 588 \text{ VAr}$
- $Q_c = X_c I^2 = 20^2 \cdot 3,5 = 1400 \text{ VAr}$
- $1400 - 588 = 812 \text{ VAr}$

# Active and Reactive load: Apparent power

FIGURE 7-10 a. Circuit consisting of a source feeding an active and reactive load. b. Phasor diagram of the voltage and current. c. Active and reactive power flow from source to load.

Active and reactive power – cannot be converted

(a)

Function independently

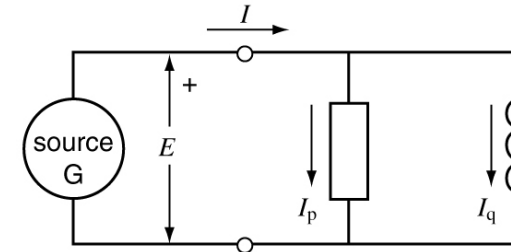
Can be treated separately

Place a burden on line and generator

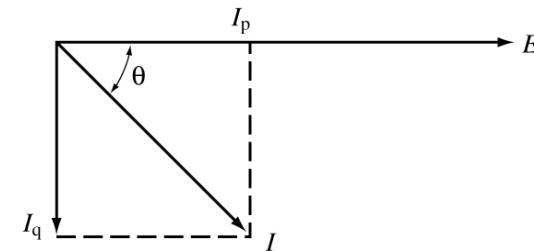
All inductive devices absorb reactive power

Ammeter, power supplied  $P$ ,  $EI$

Apparent power

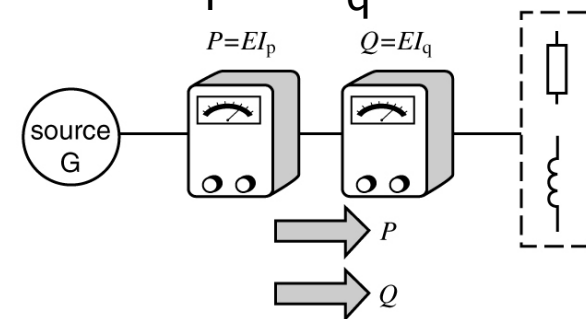


(b)



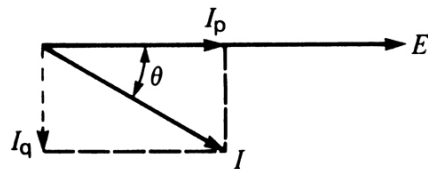
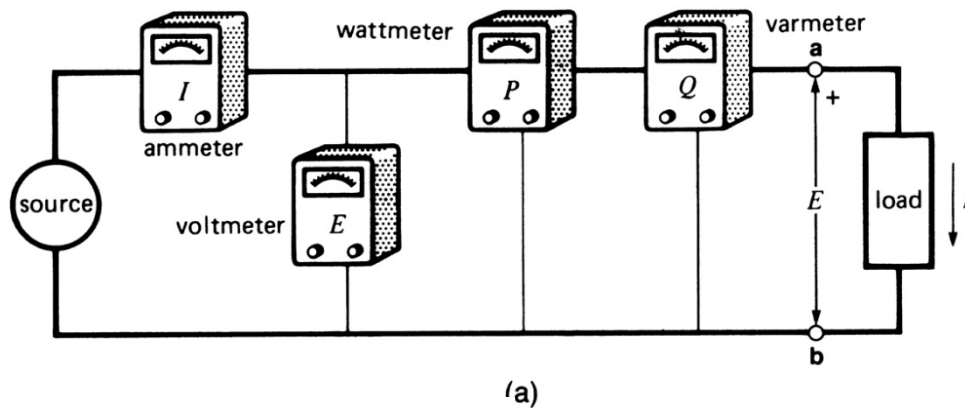
- $I^2 = I_p^2 + I_q^2$

(c)



# P, Q, and S

FIGURE 7-11 a. Instruments used to measure  $E$ ,  $I$ ,  $P$ , and  $Q$  in a circuit.  
b. The phasor diagram can be deduced from the instrument readings.



Generator does not supply any power

- $I_p = P/E$
- $I_q = Q/E$

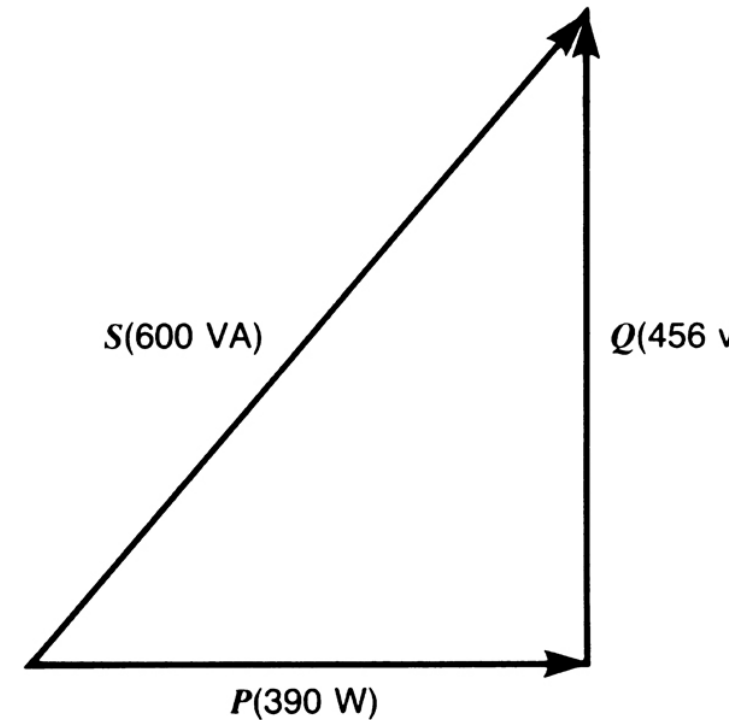
- $S = E I$
- $I = S/E$

- $I^2 = I_p^2 + I_q^2$
- $S^2 = P^2 + Q^2$

- S apparent power [VA]
- P active power [W]
- Q reactive power [VAr]
- Power factor  $pf = P/S$

## Example 7.8

- Motor draws 5 A from 120 V, 60 Hz,  $pf=0,65$
- $S = E I = 120 \cdot 5 = 600 \text{ VA}$
- $P = S \cos \theta = 600 \cdot 0,65 = 390 \text{ W}$
- $Q = \text{SQRT}(S^2 - P^2)$
- $Q = 456 \text{ VAR}$



# Power Factor and Power Triangle

FIGURE 7-12 Power triangle of a motor. See Example 7-8.

- Power Factor =  $P/S$

Active power – horizontally absorbed or delivered

Reactive power – vertically absorbed or delivered

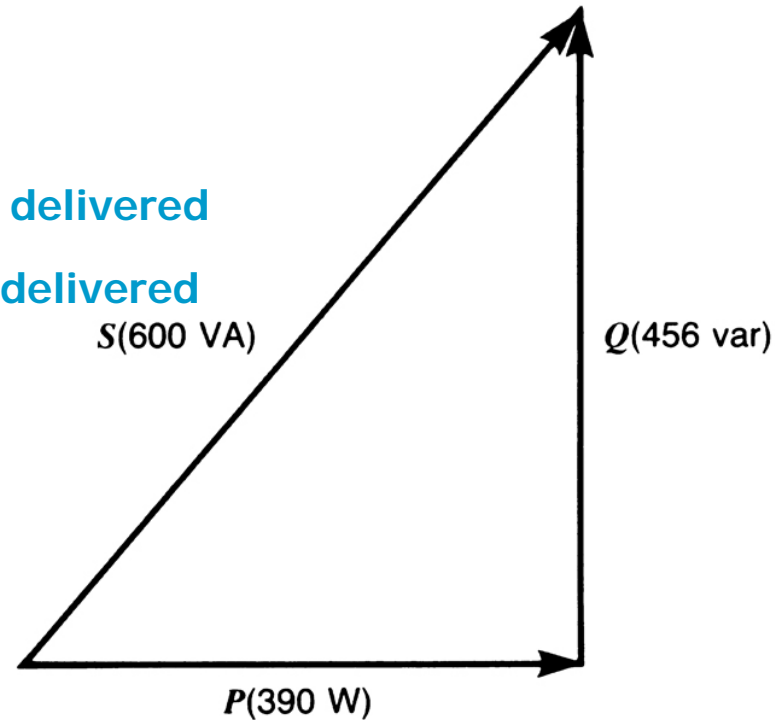
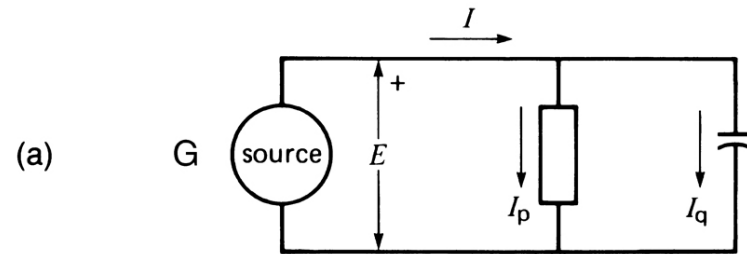
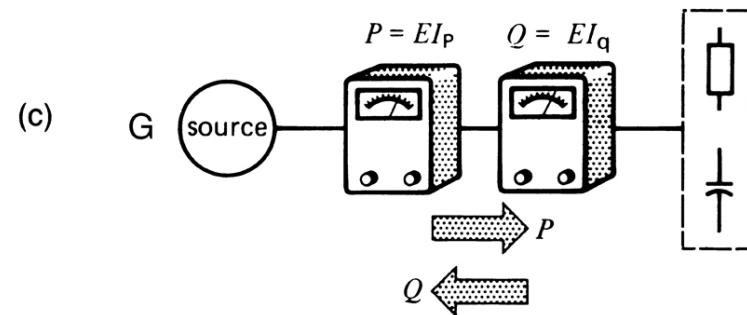
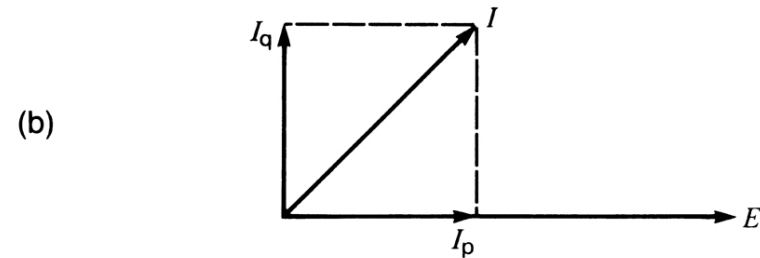


FIGURE 7-13 a. Source feeding an active and reactive (capacitive) load. b. Phasor diagram of the circuit. c. The active and reactive powers flow in opposite directions.



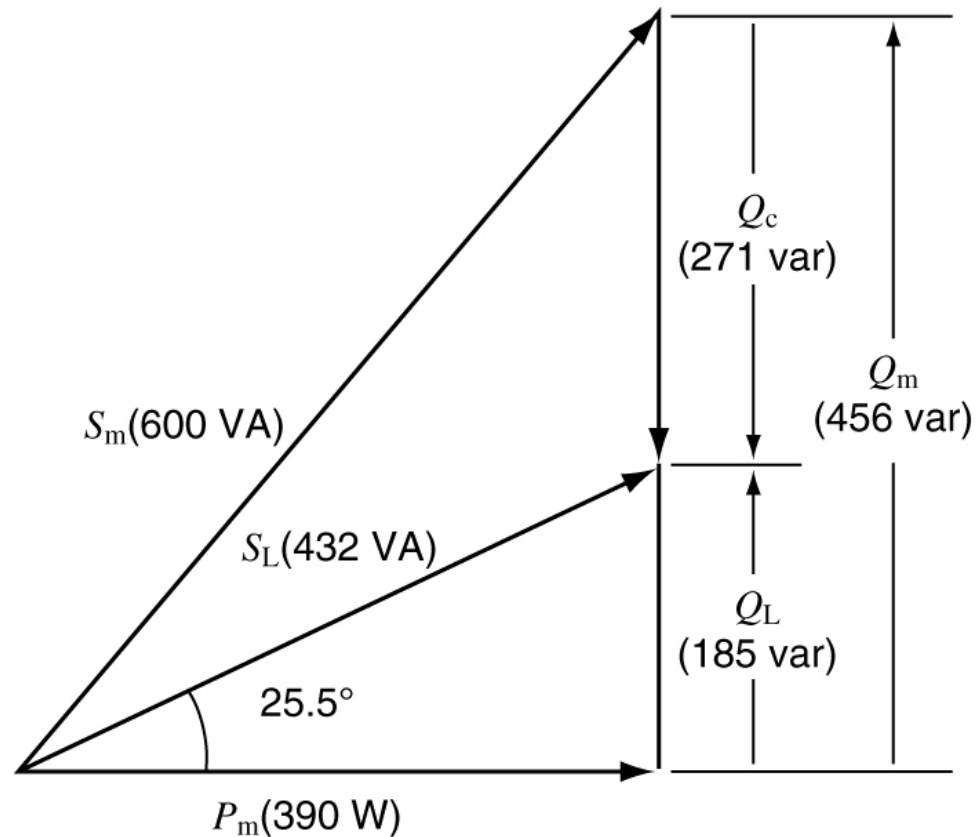
## Two powers in opposite direction



- Motor draws 5 A from 120 V, 60 Hz,  $\text{pf}=0,65$
- ## Example 7-9

FIGURE 7-14 Power triangle of a motor and capacitor connected to an ac line. See Example 7-9.

+ Capacitor 50 $\mu$ F



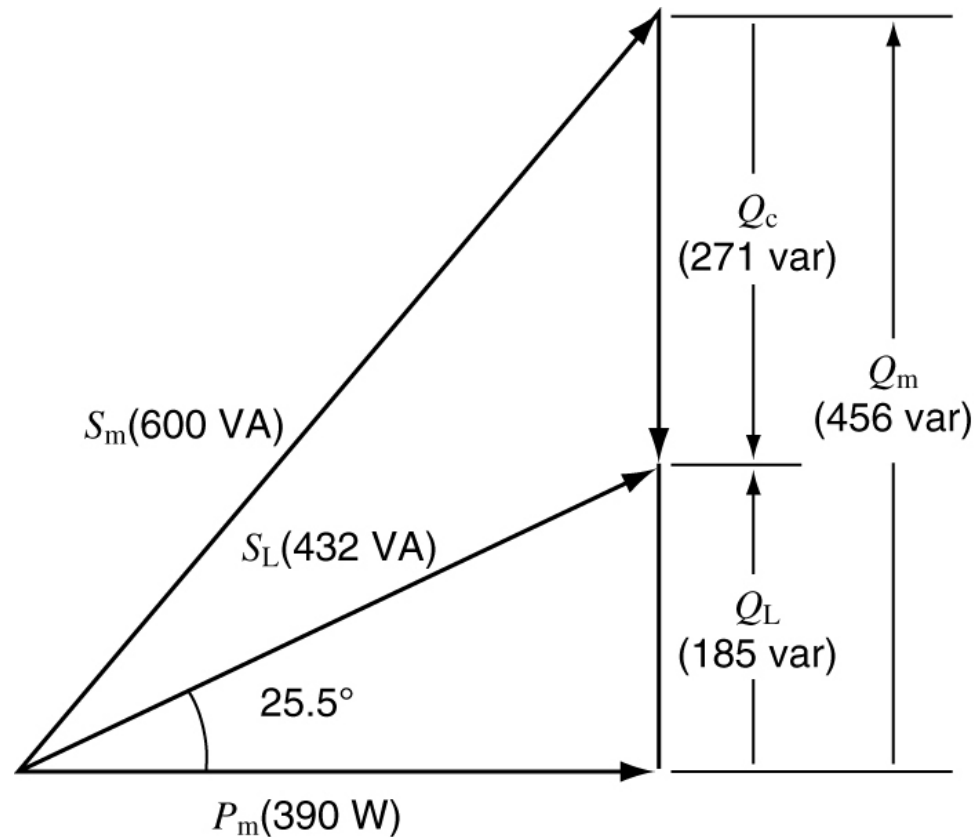
- Motor draws 5 A from 120 V, 60 Hz, pf=0,65

## Example 7-9

FIGURE 7-14 Power triangle of a motor and capacitor connected to an ac line. See Example 7-9.

+ Capacitor 50 $\mu$ F

- $X_C = 1/\omega C = 53 \text{ } \Omega$
- $I = E/X_C = 2,26 \text{ A}$
- $Q_C = E I_q = 271 \text{ VAR}$
- $P_m = 390 \text{ W}$
- $Q_m = 456 \text{ VAR}$
- $Q_L = Q_m - Q_C$
- $S_L = \text{SQR}(P_{L2} + Q_{L2})$
- $I = S_L/E = 3,6 \text{ A}$





# Several Loads

FIGURE 7-15 a. Example of active and reactive loads connected to a 380 V source.  
 b. All loads are assumed to be directly connected to the 380 V receptacle.

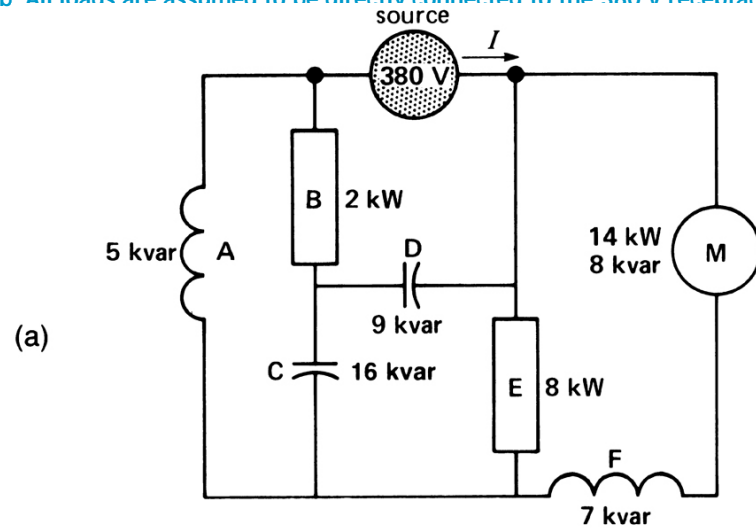
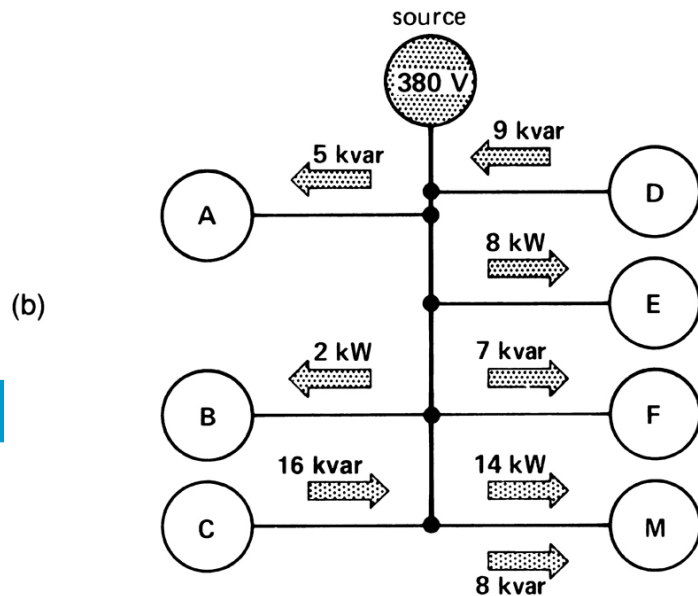


FIGURE 7-15c Power triangle of the system.



# Several Loads

FIGURE 7-15 a. Example of active and reactive loads connected to a 380 V source.  
 b. All loads are assumed to be directly connected to the 380 V receptacle.

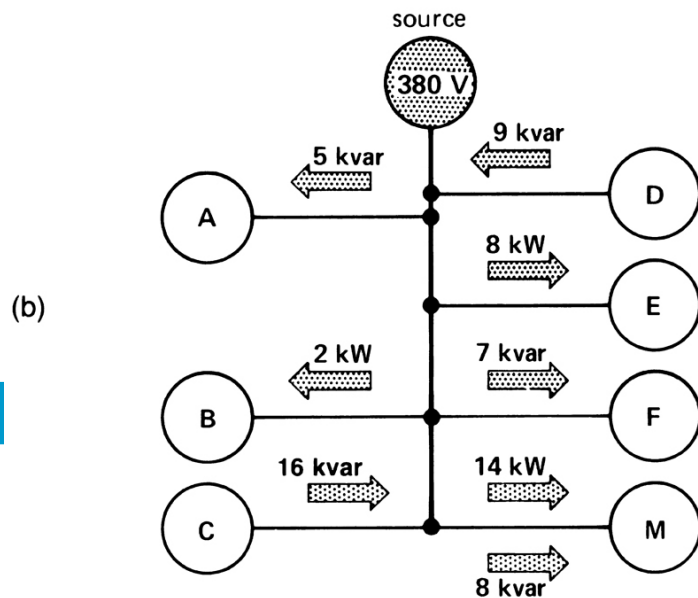
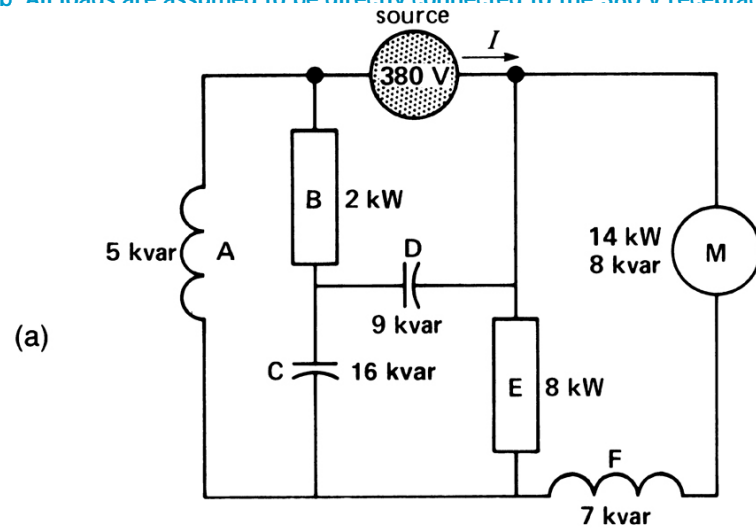


FIGURE 7-15c Power triangle of the system.

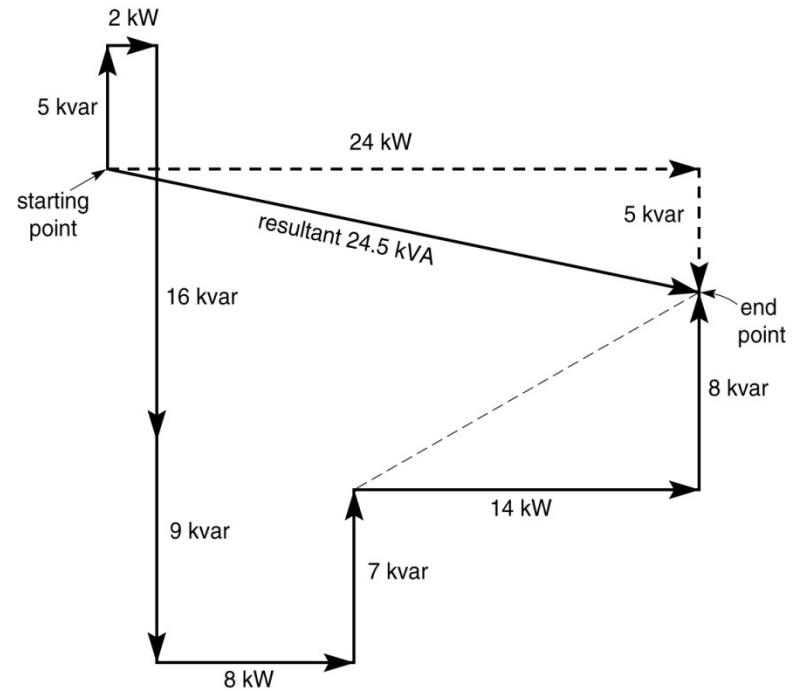


FIGURE 7-16 a. Active and reactive power flow in a switched resistive load. b. The delayed current flow is the cause of the reactive power absorbed by the system.

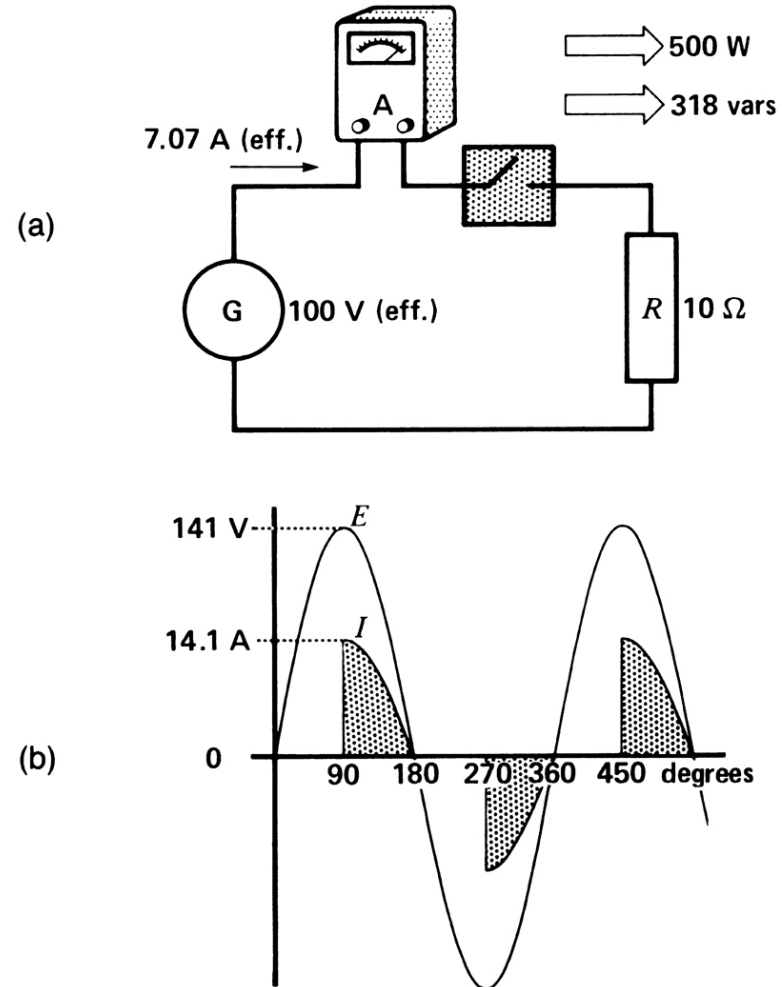
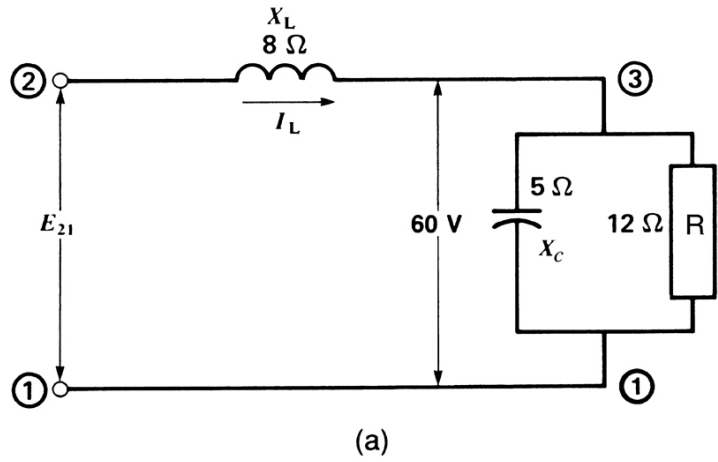
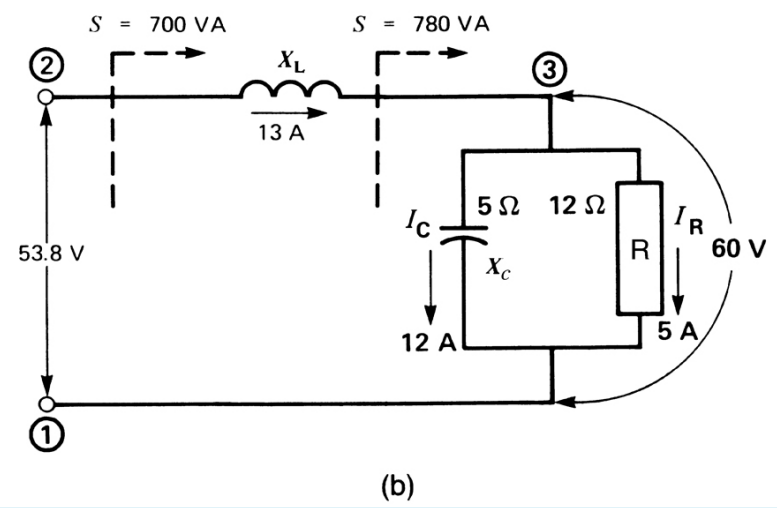


FIGURE 7-17 a. Solving ac circuits by the power triangle method. b. Voltages and currents in the circuit. See Example 7-10.



Current in each element



Voltage between 1 - 2

## AC Voltage 1

1 An inductance and a resistor are in series connected to a power source of 220 V and 50 Hz.  
 $R = 30 \Omega$ ;  $L = 127.3 \text{ mH}$ .

Calculate the rms current in the source [in A]

2 For the same inductance and resistor:

What is the powerfactor?

3 For the same inductance and resistor:

Calculate the rms voltage of the resistor [in V]

4 For the same inductance and resistor:

Calculate the rms voltage of the inductance [in V]

5 For the same inductance and resistor connected to a power source of 220 V and 60 Hz.  
( $R = 30 \Omega$ ;  $L = 127.3 \text{ mH}$ )

Calculate the rms current in the source [in A]

6 A capacitor is connected to a voltage source of 220 V / 50 Hz.  
 $C = 33 \mu\text{F}$ .

Calculate the rms current in the source [in A]

7 A resistor and a inductor in series, are in parallel connected with a capacitor as shown in the schematic.  
 $X_L = 4 \Omega$ ;  $R_L = 3 \Omega$ ;  $X_C = 8 \Omega$

Calculate the total equivalent impedance .

