

Elektrische Aandrijvingen

WTB

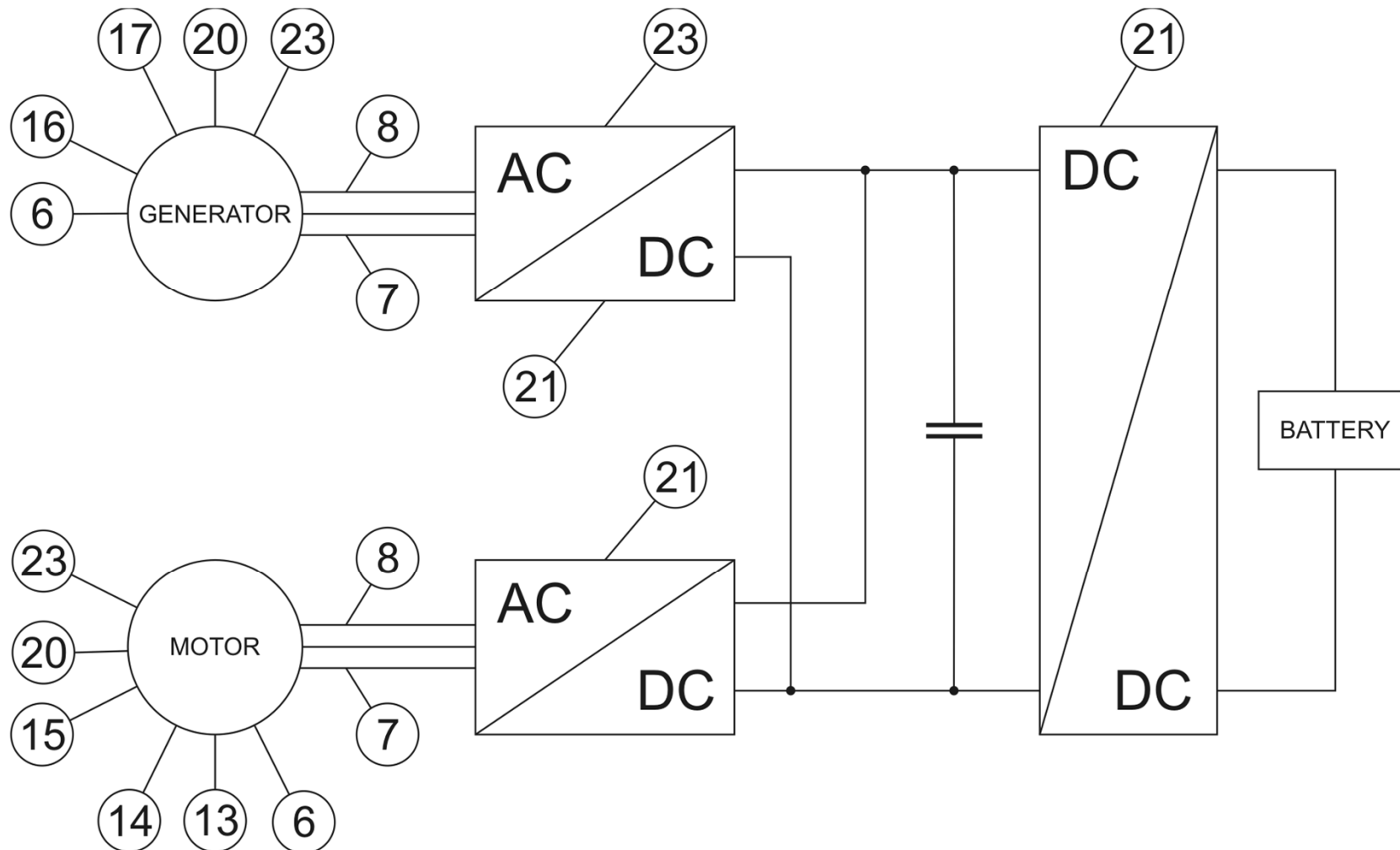
Lokatie/evenement

P.BAUER

February 22, 2013

1

Three phase circuits



Single phase generator

FIGURE 8-1 A single-phase generator with a multiturn coil embedded in two slots. At this instant E_{a1} is maximum (+).

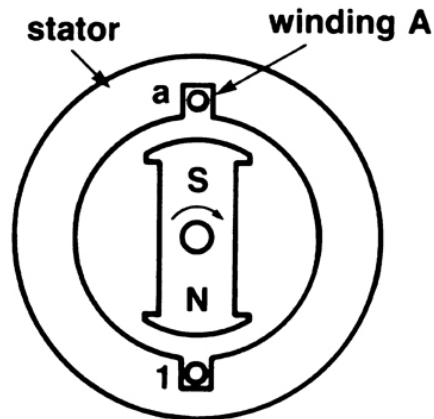
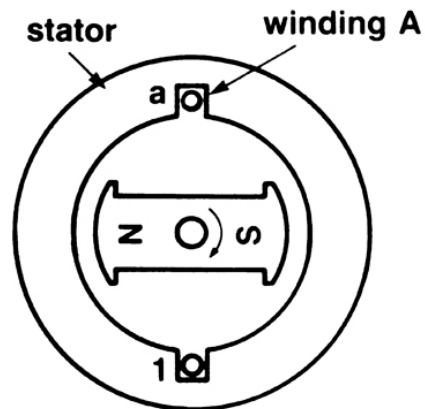
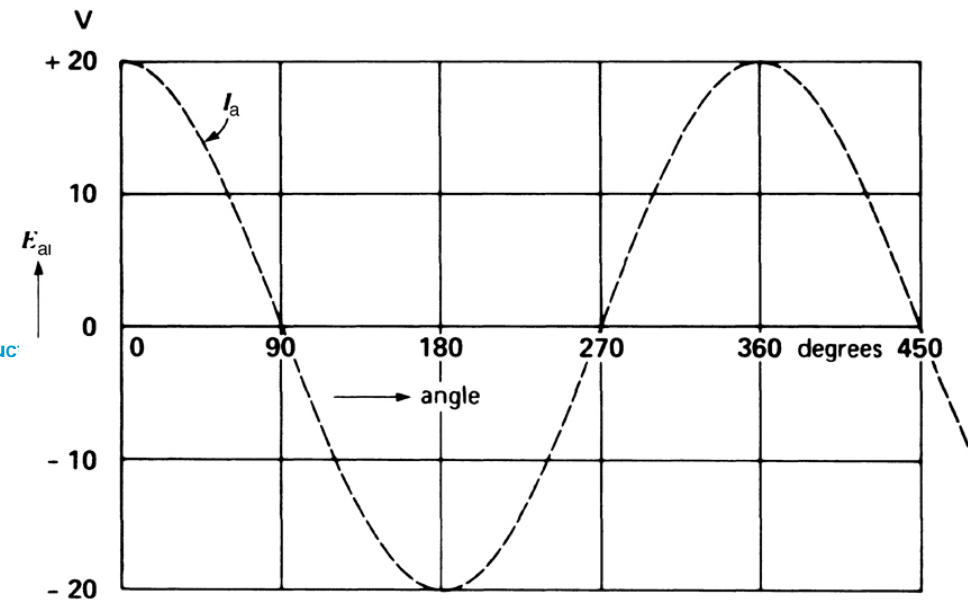


FIGURE 8-2 At this instant $E_{a1} = 0$ because the flux does not cut the conductors.



$$E = B l v$$

FIGURE 8-3 Voltage induced in winding A.



Single Phase Generator

FIGURE 8-4 Single-phase generator delivering power to a resistor.

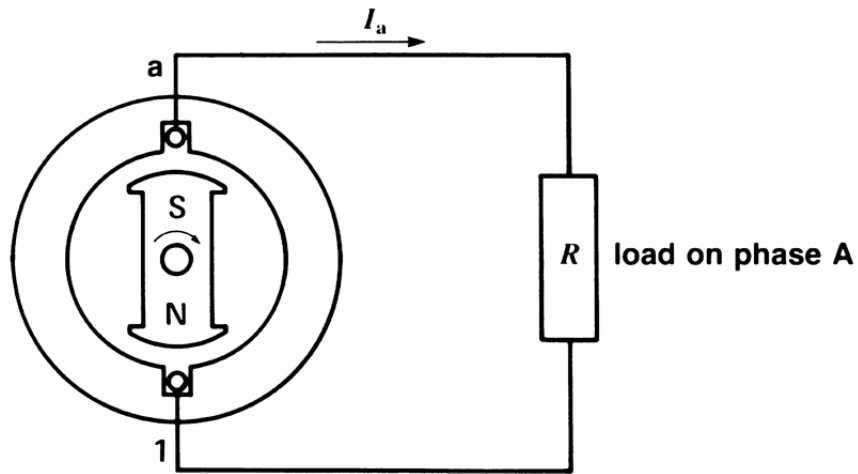
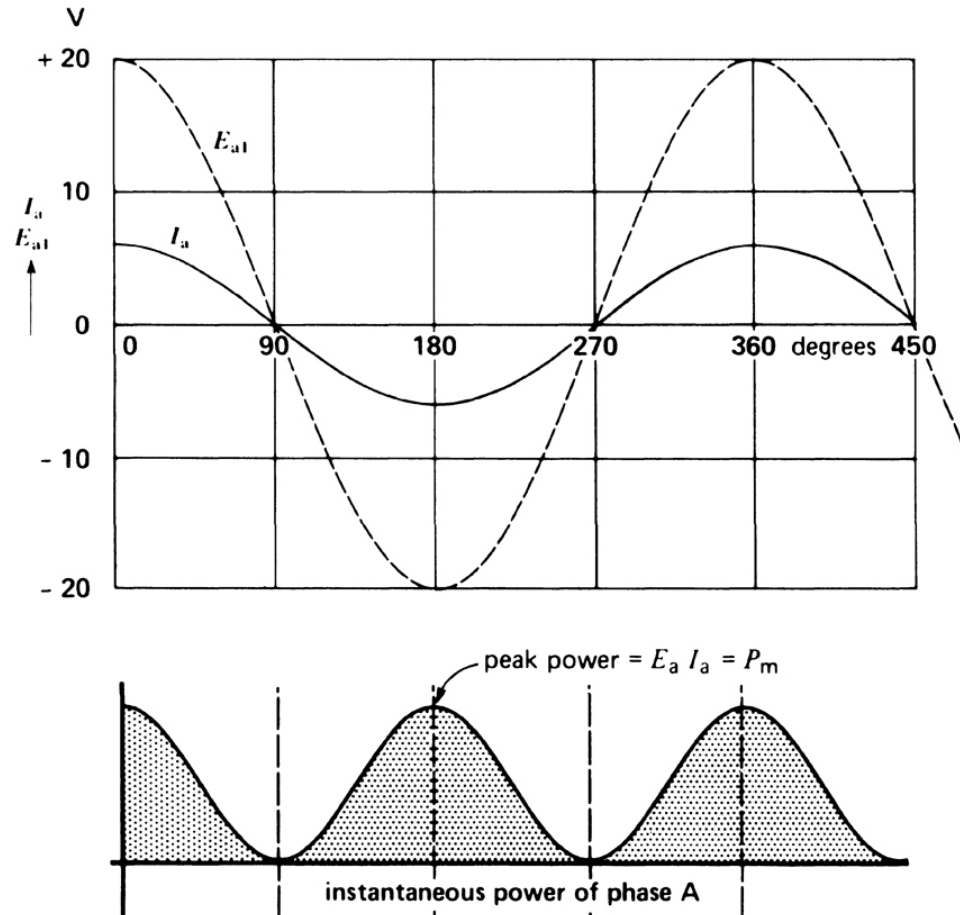


FIGURE 8-5 Graph of the voltage, current, and power when the generator is under load.



Two Phase Generator

FIGURE 8-6 a. Schematic diagram of a 2-phase generator. b. Voltages induced in a 2-phase generator. c. Phasor diagram of the induced voltages.

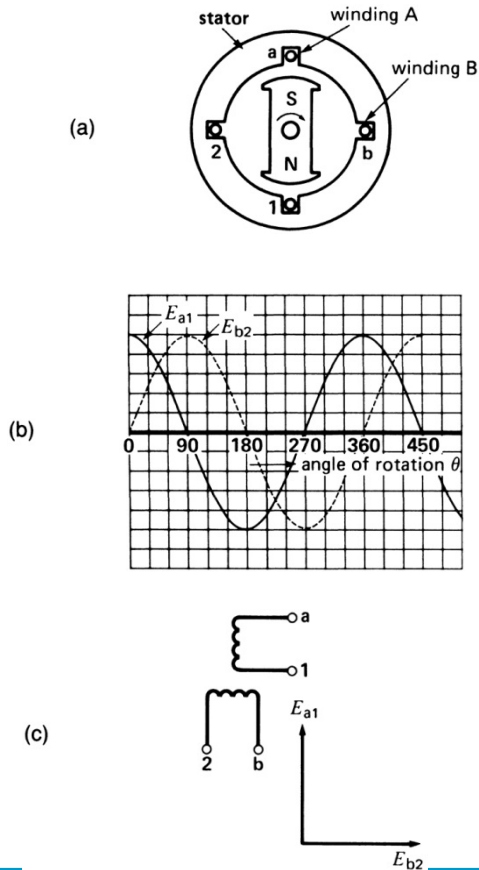
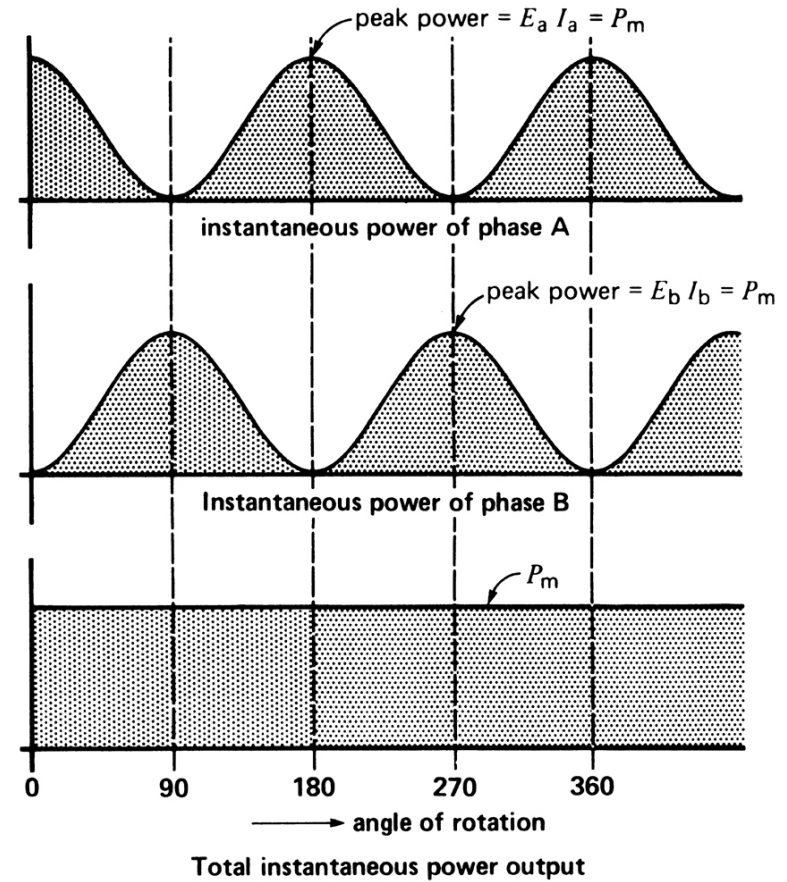


FIGURE 8-8 Power produced by a 2-phase generator.



Power Output of Two Phase Generator

FIGURE 8-7 a. Two-phase generator under load.
b. Phasor diagram of the voltages and currents.

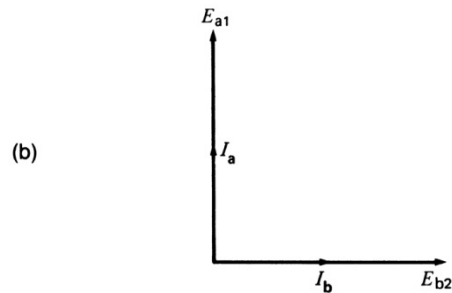
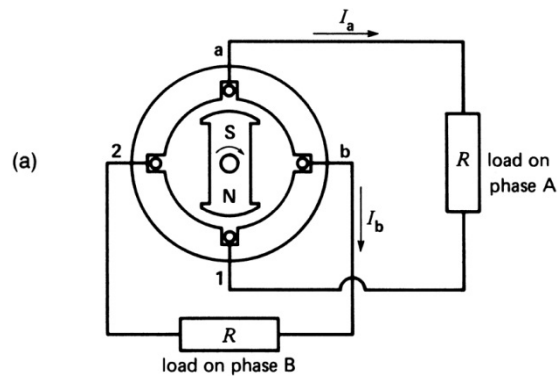
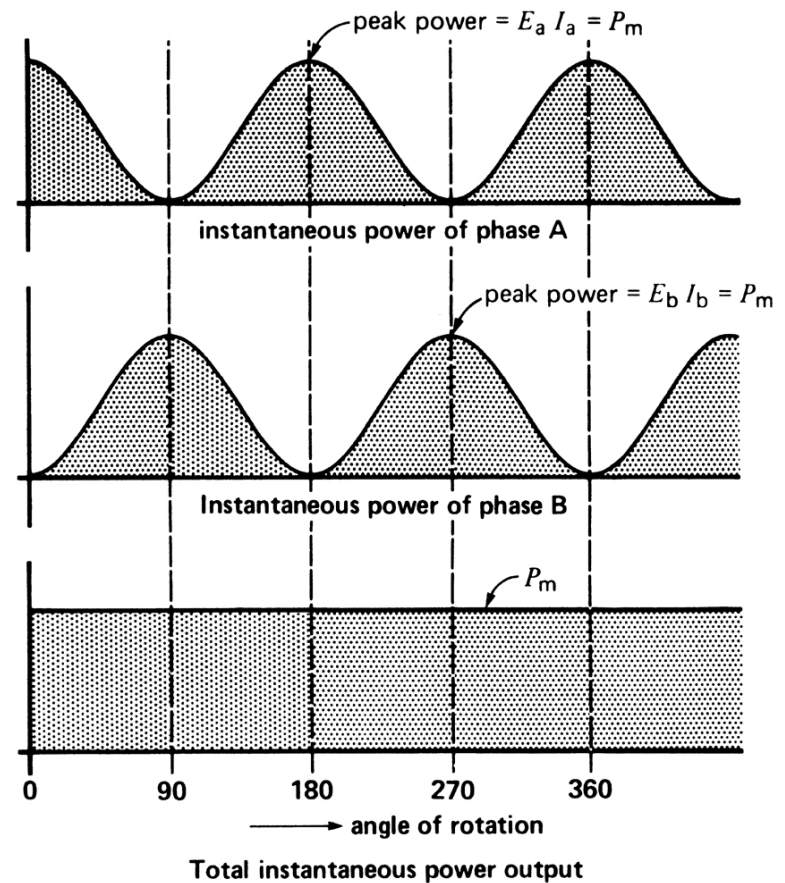


FIGURE 8-8 Power produced by a 2-phase generator.



Three Phase Generator

FIGURE 8-9 a. Three-phase generator.
 b. Voltages induced in a 3-phase generator.
 c. Phasor diagram of the induced voltages.

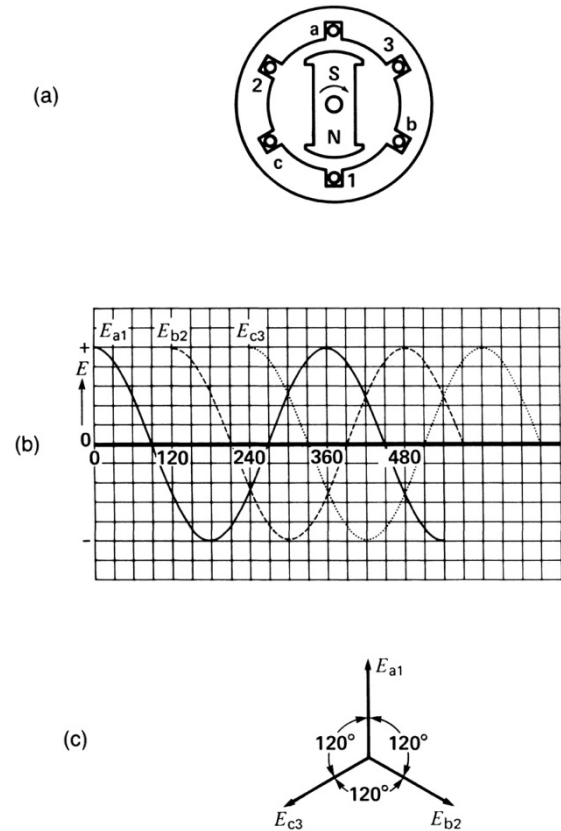
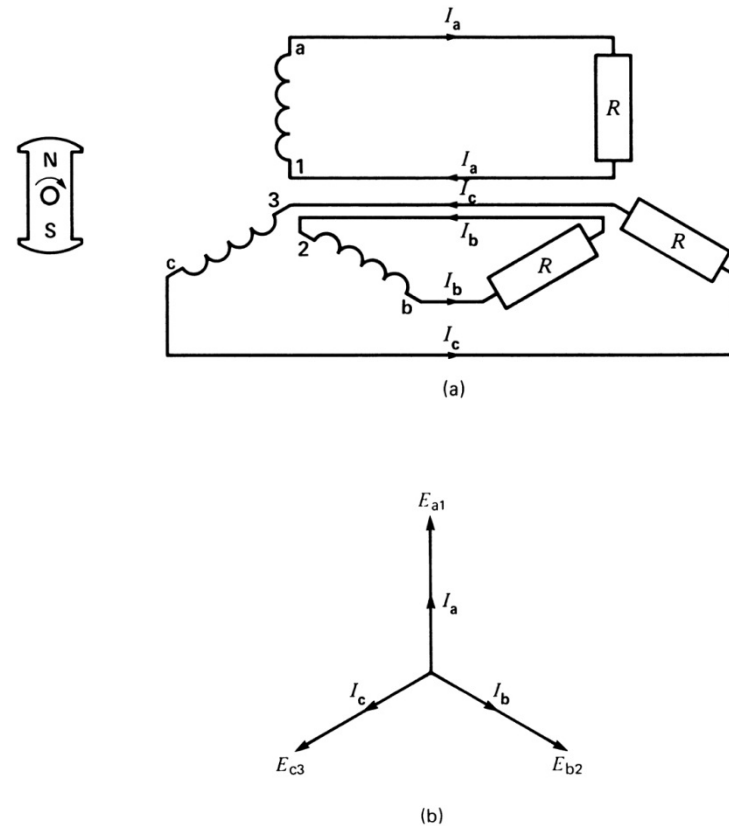


FIGURE 8-10 a. Three-phase, 6-wire system.
 b. Corresponding phasor diagram.

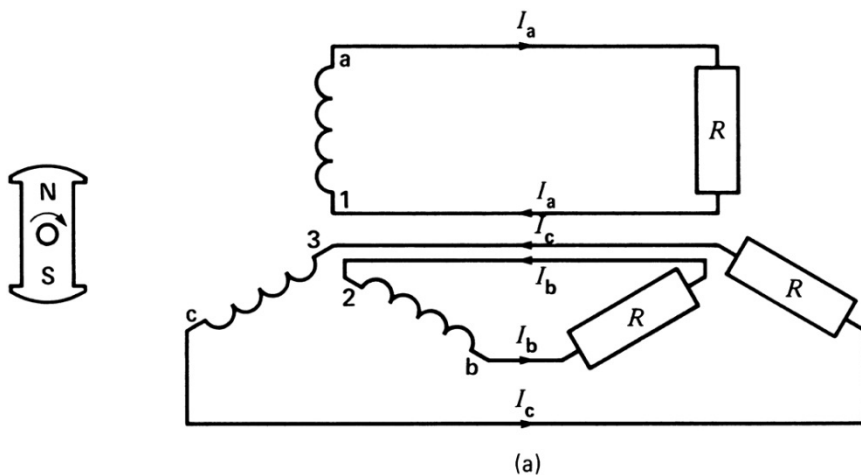


Example 8.2

Three phase generator, 20 ohm load,
Effective voltage induced 120 V

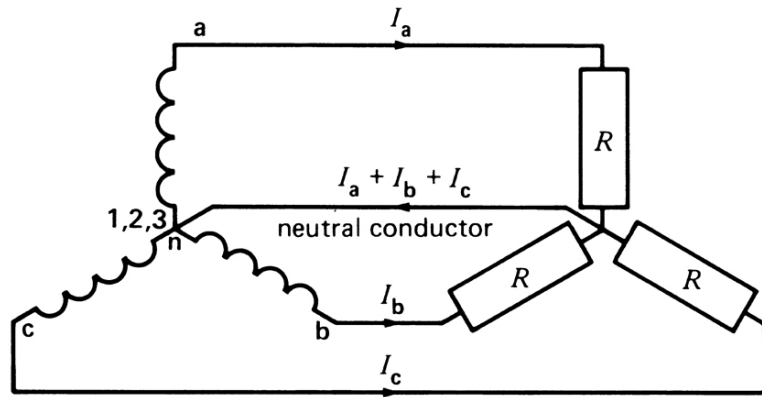
Calculate

- the power dissipated in R
- the power in 3 phase load
- the peak power P_m
- the total 3 phase power comp. P_m

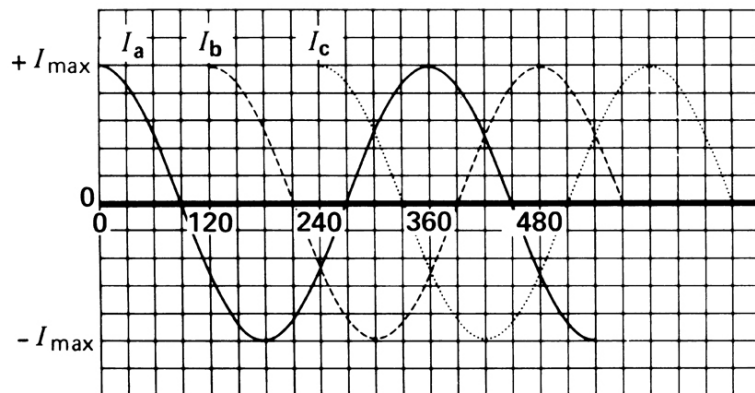


- $P = U^2/R = 120^2/20 = 720 \text{ W}$
- $P_T = 3P = 2160 \text{ W}$
- $E_m = \sqrt{2} E = 169,7$
- $I_m = E_m/R = 8,485 \text{ A}$
- $P_m = E_m I_m$

FIGURE 8-11 a. Three-phase, 4-wire system. b. Line currents in a 3-phase, 4-wire system.

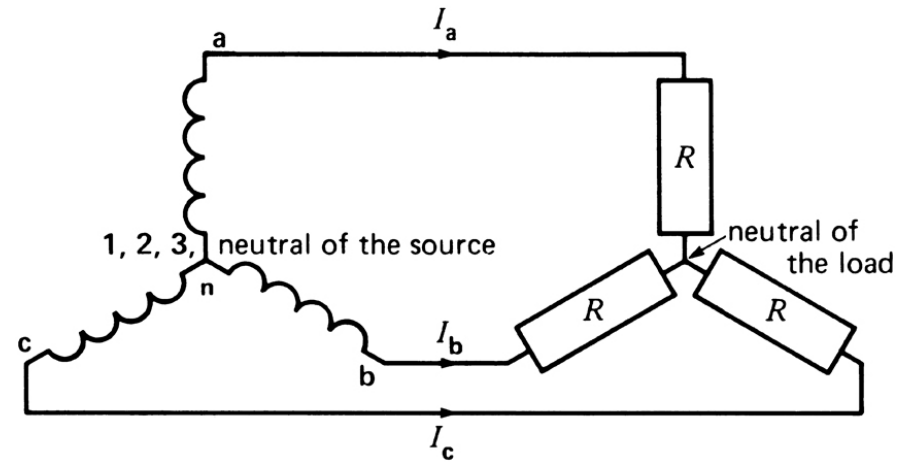


(a)



(b)

FIGURE 8-12 Three-phase, 3-wire system showing source and load.



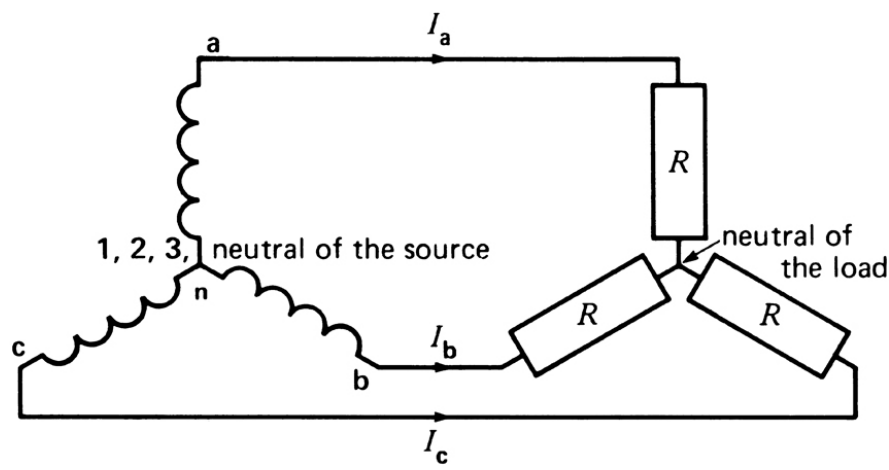
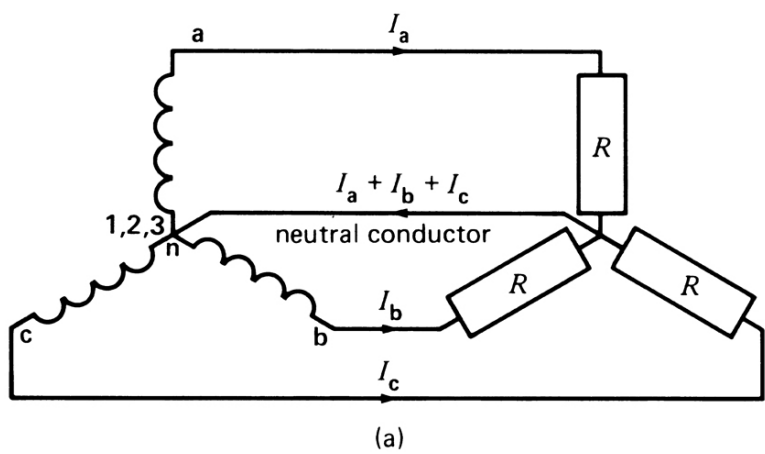
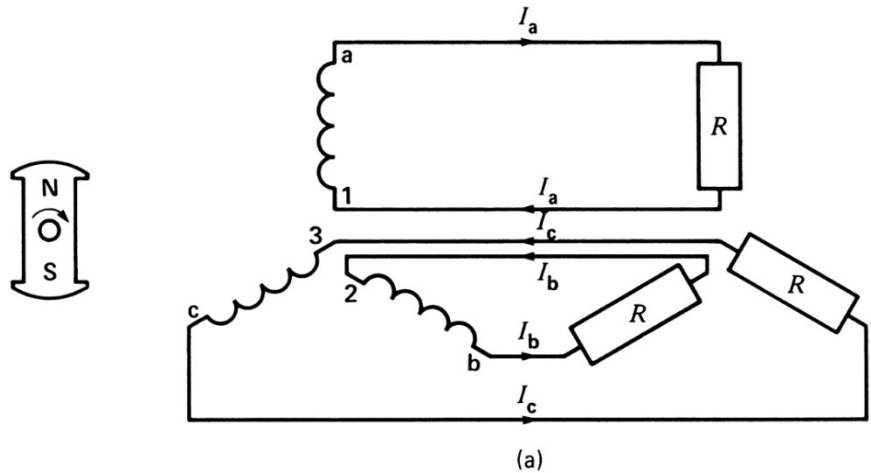
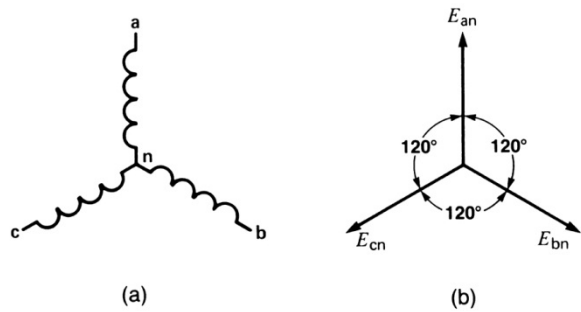


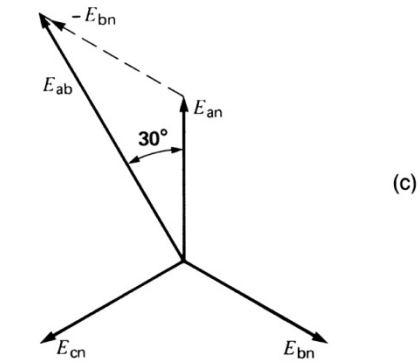
FIGURE 8-13 a. Wye-connected stator windings of a 3-phase generator.
 b. Line-to-neutral voltages of the generator.
 c. Method to determine line voltage E_{ab} .
 d. Line voltages E_{ab} , E_{bc} , and E_{ca} are equal and displaced at 120°.



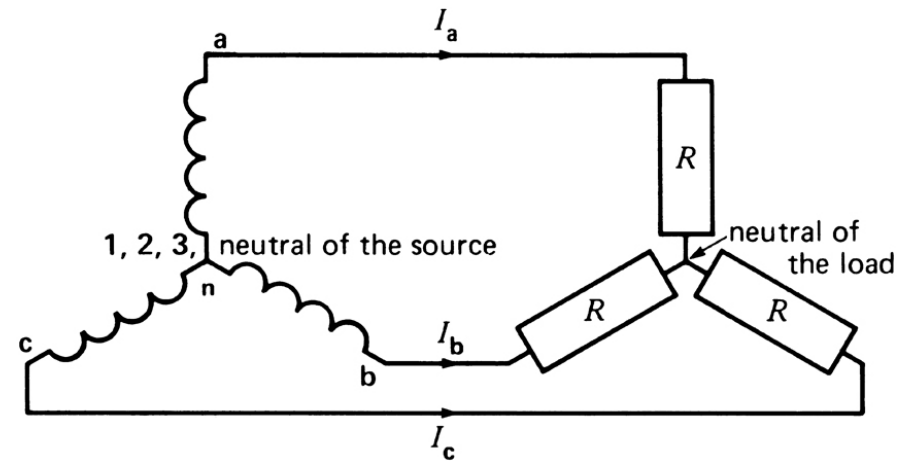
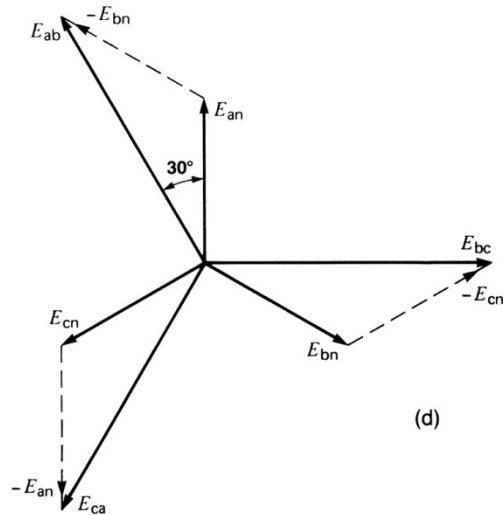
$$E_{AB} = E_{AN} - E_{BN}$$

$$E_{BC} = E_{BN} - E_{CN}$$

$$E_{CA} = E_{CN} - E_{AN}$$



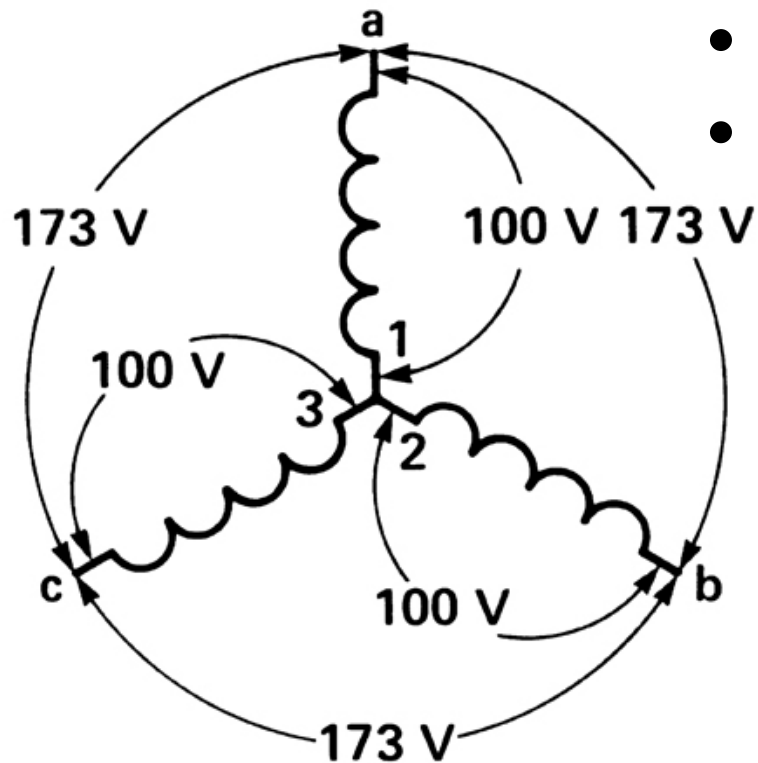
$$E_{AB} = 2 E_{LN} \cos 30 = \text{sqrt}(3) E_{LN}$$



Example 8.3

3 Phase 60 Hz generator 23,9 kV

- Line to neutral voltage
- Time interval between the peak
- Peak value



$$E_{LN} = E_L / \text{SQRT}(3)$$

- $T = 120 / (360 \cdot 60) = 5,55 \text{ ms}$
- $E_m = \text{SQRT}(2) E_L$

Delta Connection

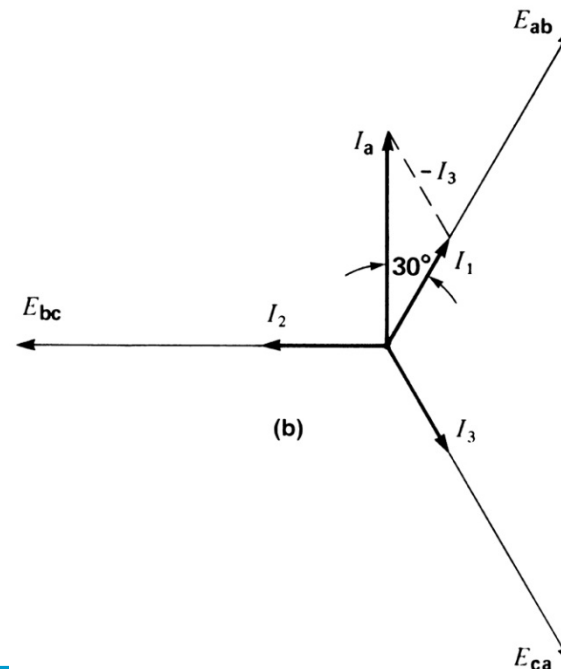
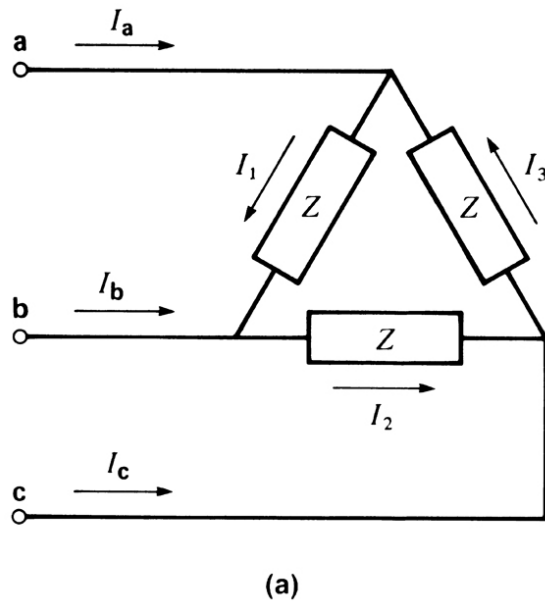
$$I_a = I_1 - I_3$$

$$I_b = I_2 - I_1$$

$$I_c = I_3 - I_2$$

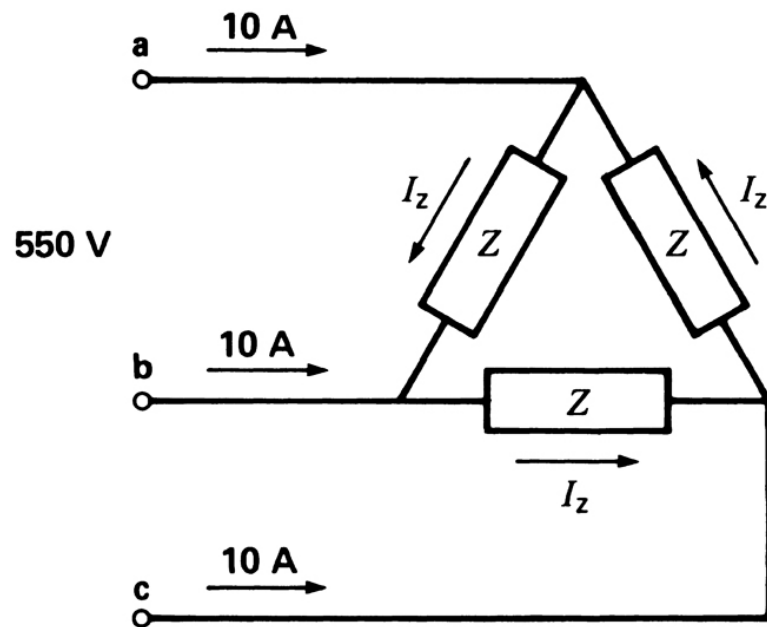
FIGURE 8-15 a. Impedances connected in delta. b. Phasor relationships with a resistive load.

$$I_L = 2 I_Z \cos 30 = \text{sqrt}(3) I_Z$$



Example 8.5

FIGURE 8-15c See Example 8-5.



$$I_z = 10 / \sqrt{3} = 5,77 \text{ A}$$

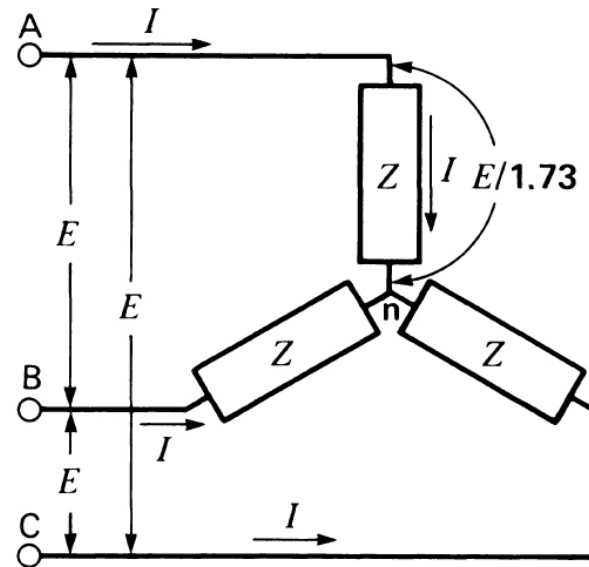
$$Z = E / I_z = 550 / 5,77 = 95$$

Power transmitted by a 3 phase line

Single phase vs three phase

FIGURE 8-16a Impedances connected in wye.

Wye connection



Single phase: EI

Three phase

Each branch

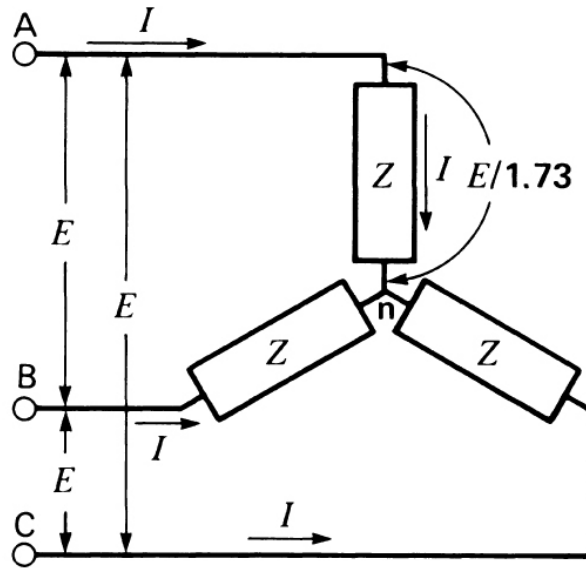
$$S_Z = E I / \text{SQRT}(3)$$

3 phase

$$S = 3 E I / \text{SQRT}(3) = \text{SQRT}(3) EI$$

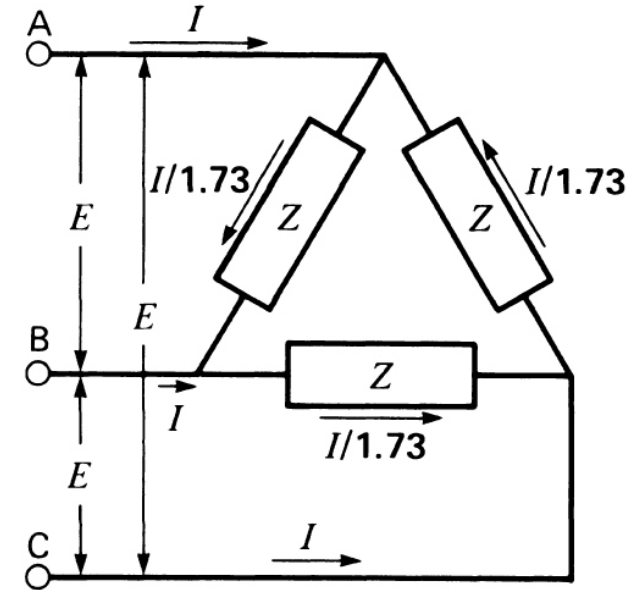
Wye versus Delta

Wye connection



I in each element = I_L
 Voltage across $E/\text{SQRT}(3)$
 V, I elements 120°

Delta connection

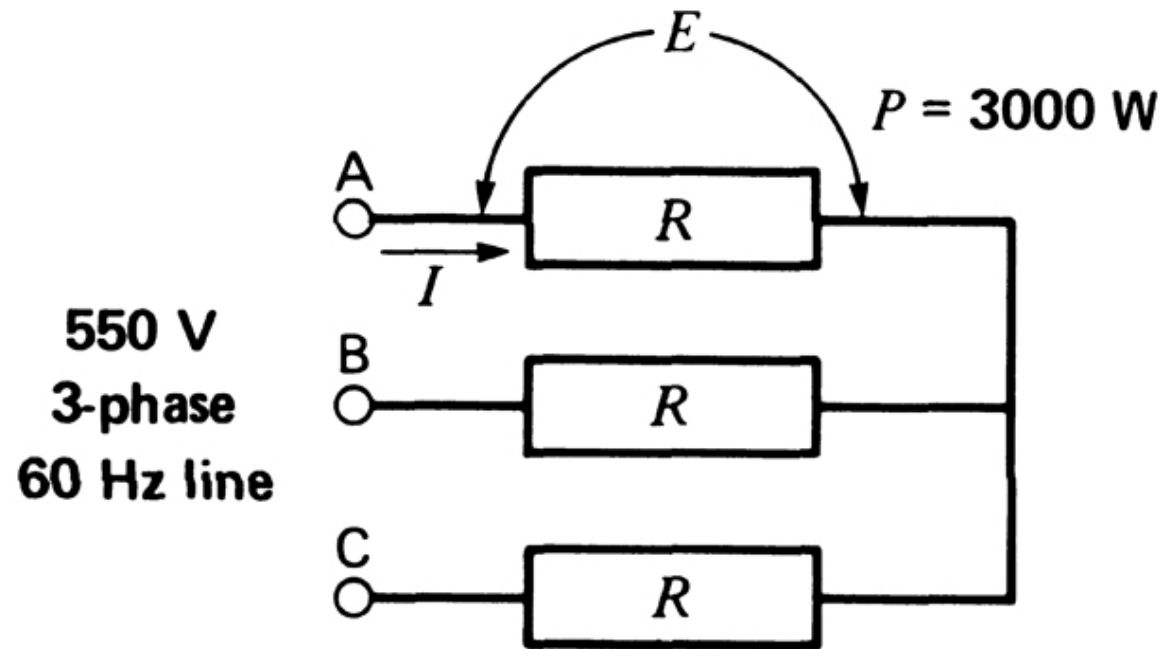


$I_L/\text{SQRT}(3)$
 E
 V, I elements 120°

Active reactive and apparent power

- $S = \text{Sqrt}(P^2 + Q^2)$
- $\cos \Phi = P/S$
- S total 3 phase [VA]
- P..
- Q...

Example 8.7



Three identical R , total P 3000 W, 550 V lineC

$$P = 3000\text{W}/3$$

$$E = 550\text{V}/\text{SQRT}(3)$$

$$I = P/E$$

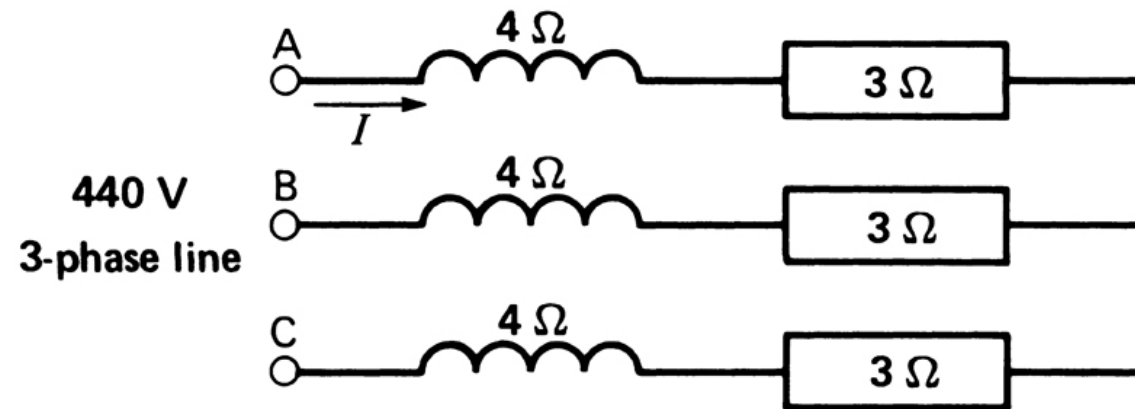
$$R = E/I$$

Example 8.8

The current in each line

The voltage across the inductor terminals

FIGURE 8-18 See Example 8-8.

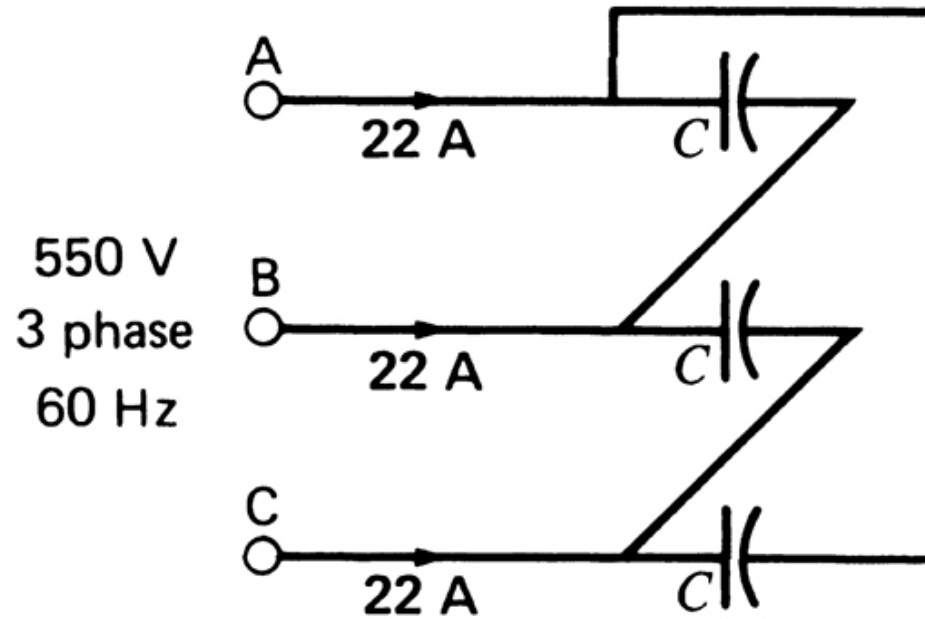


Current in each line, voltage across inductor

$$Z = \dots \quad E_{LN} = \dots \quad I = \dots \quad E = \dots$$

Example 8.9

FIGURE 8-19 See Example 8-9.

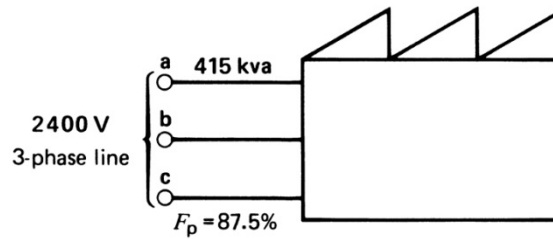


Calculate capacitance

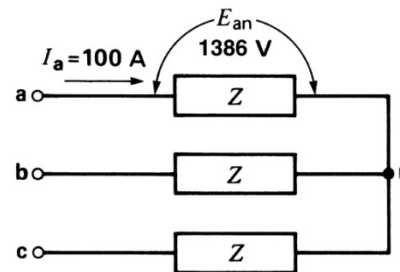
FIGURE 8-20 a. Power input to a factory. See Example 8-10. b. Equivalent wye connection of the factory load. c. Phasor diagram of the voltages and currents.

Example 8.10

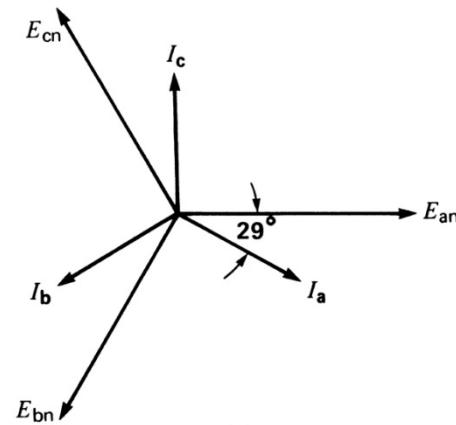
415 kVA,
2400V, pf



(a)



(b)



(c)

FIGURE 8-21 Industrial motor and capacitor. See Example 8-11.

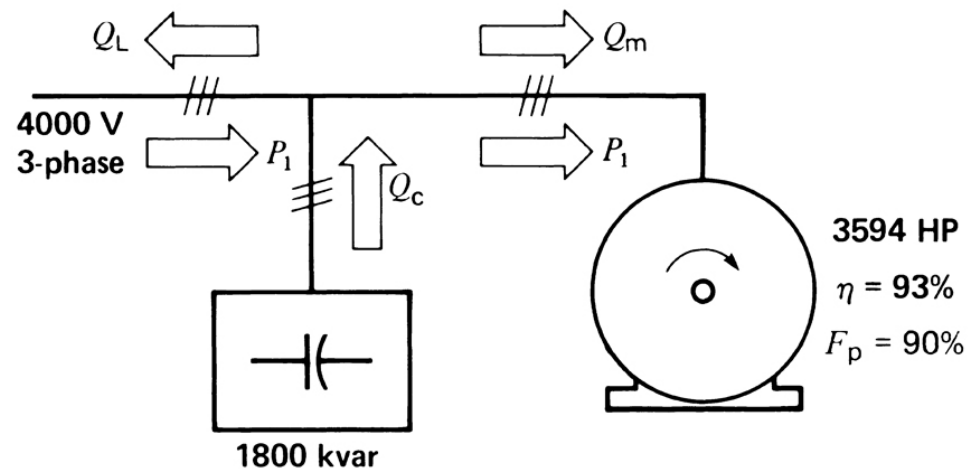


FIGURE 8-22 a. Phasor relationships for one phase. See Example 8-11. b. Line currents. Note that the motor currents exceed the currents of the source.

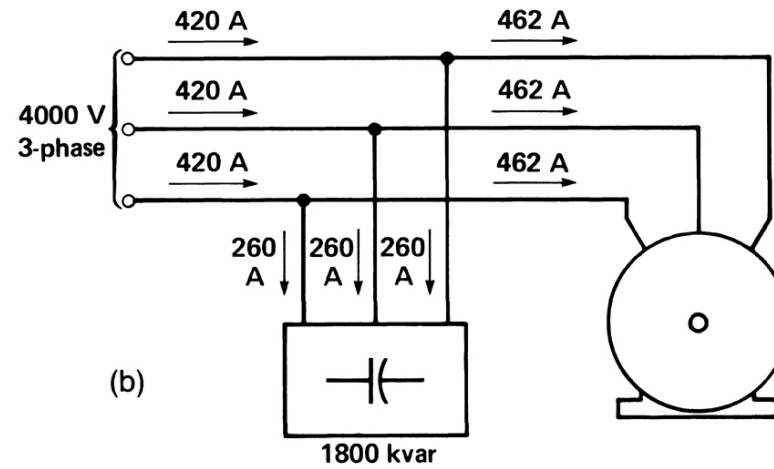
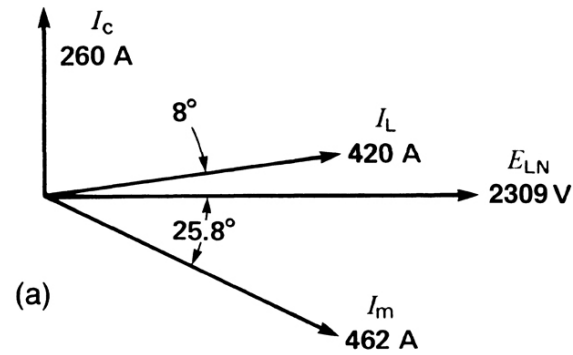


FIGURE 8-23 The letters are observed in the sequence a-b-c.

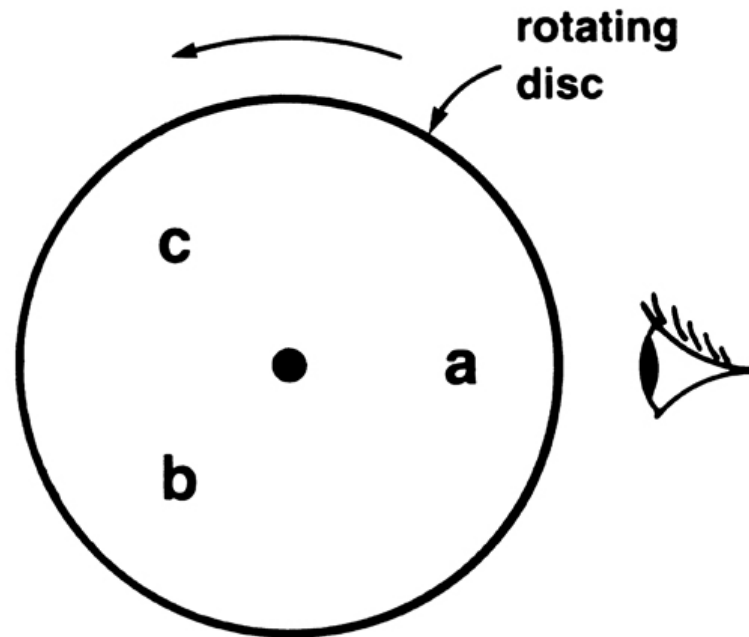


FIGURE 8-24 The letters are observed in the sequence a-c-b.

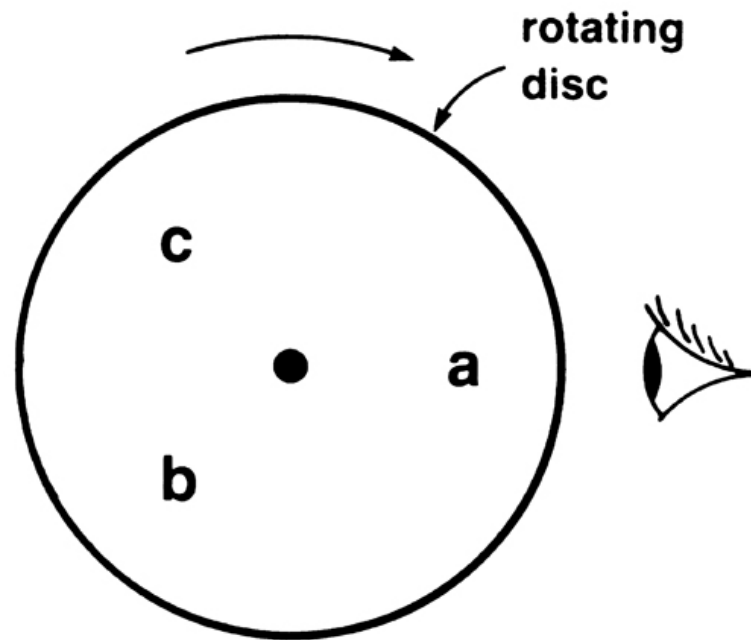


FIGURE 8-25 The letters are observed in the sequence a-c-b.

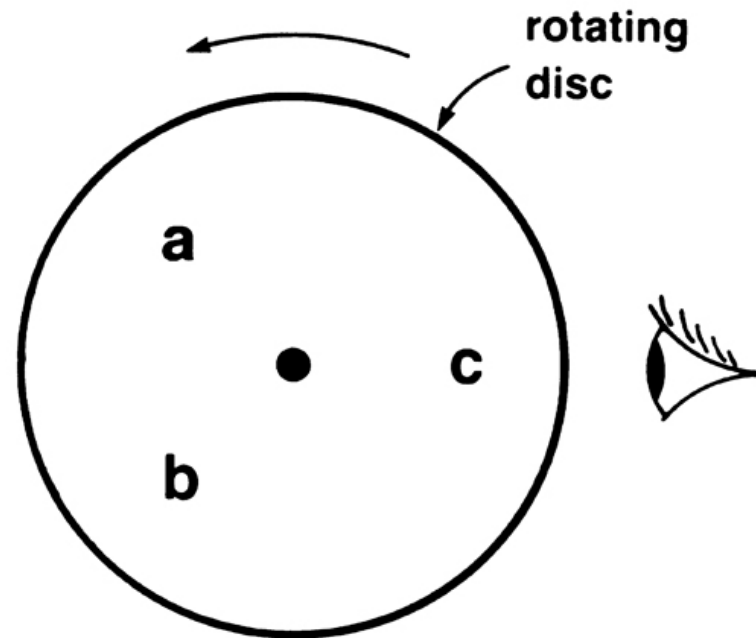
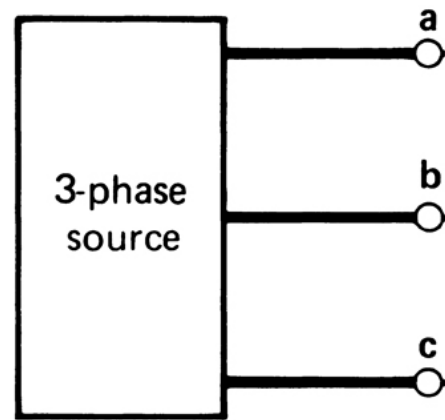
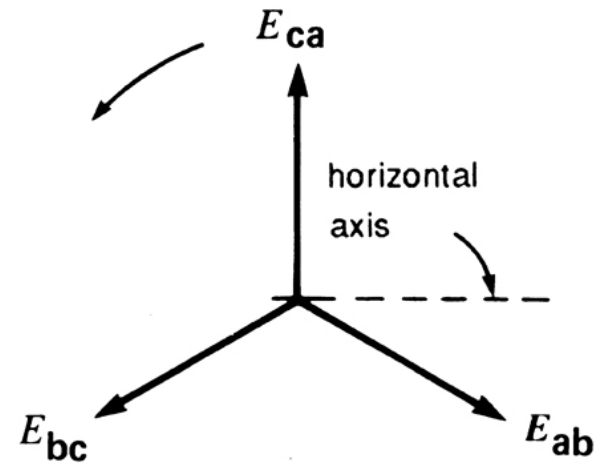


FIGURE 8-26 a. Determining the phase sequence of a 3-phase source. b. Phase sequence depends upon the order in which the line voltages reach their positive peaks.



(a)



(b)

FIGURE 8-27 See Problem 8-12.

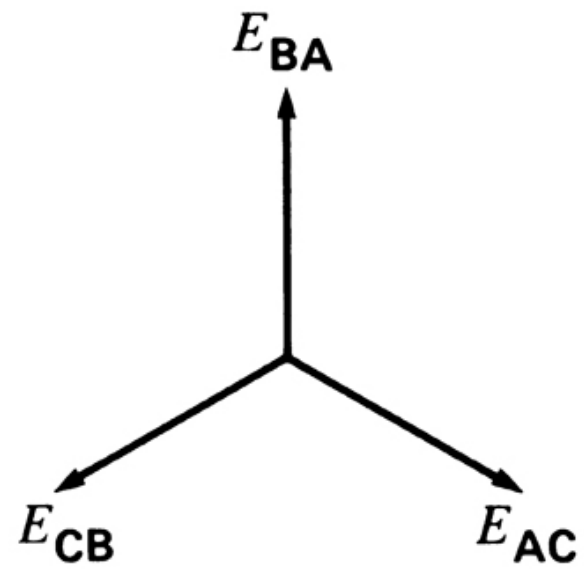


FIGURE 8-28 a. Determining phase sequence using two lamps and a capacitor. b. Resulting phasor diagram.

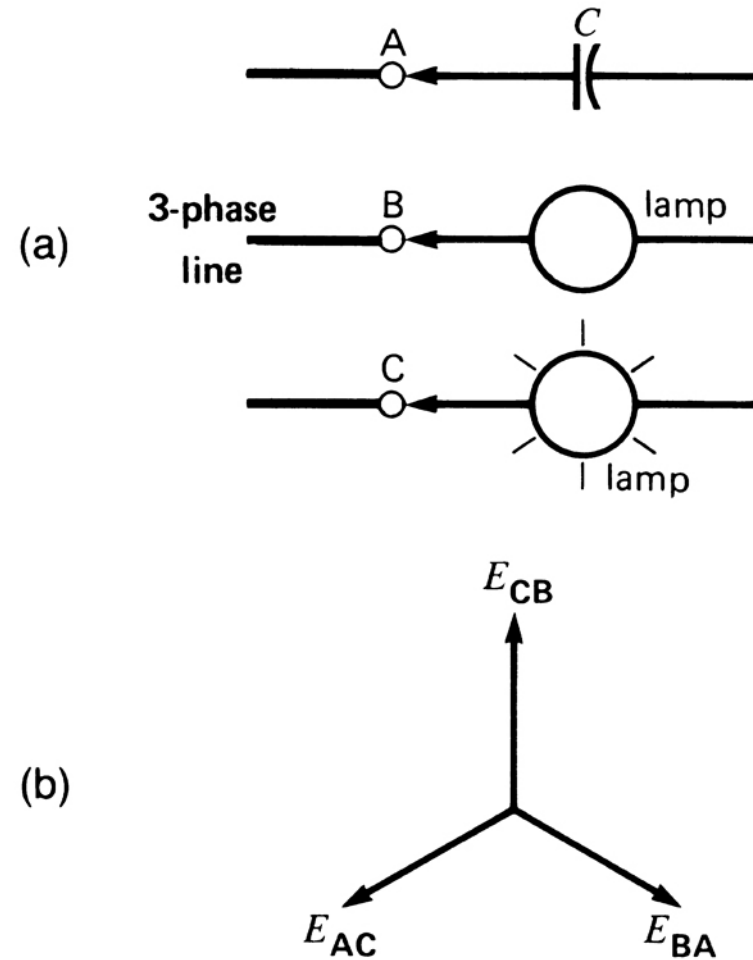


FIGURE 8-33 A single-phase resistive load can be transformed into a balanced 3-phase load.

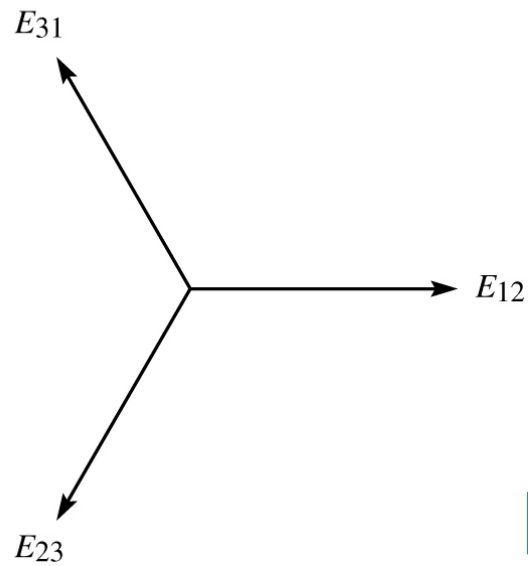
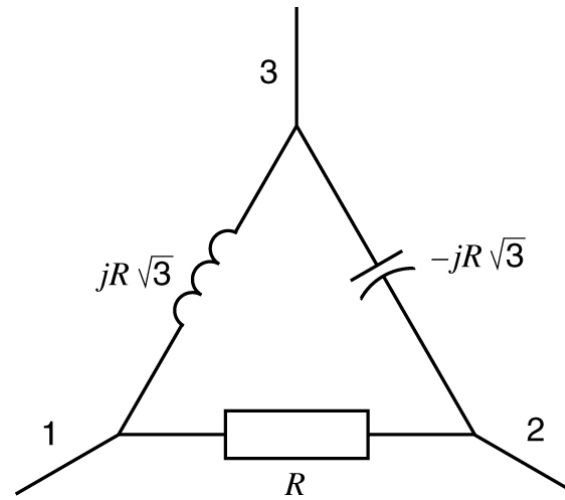


FIGURE 8-34 See Problem 8-14.

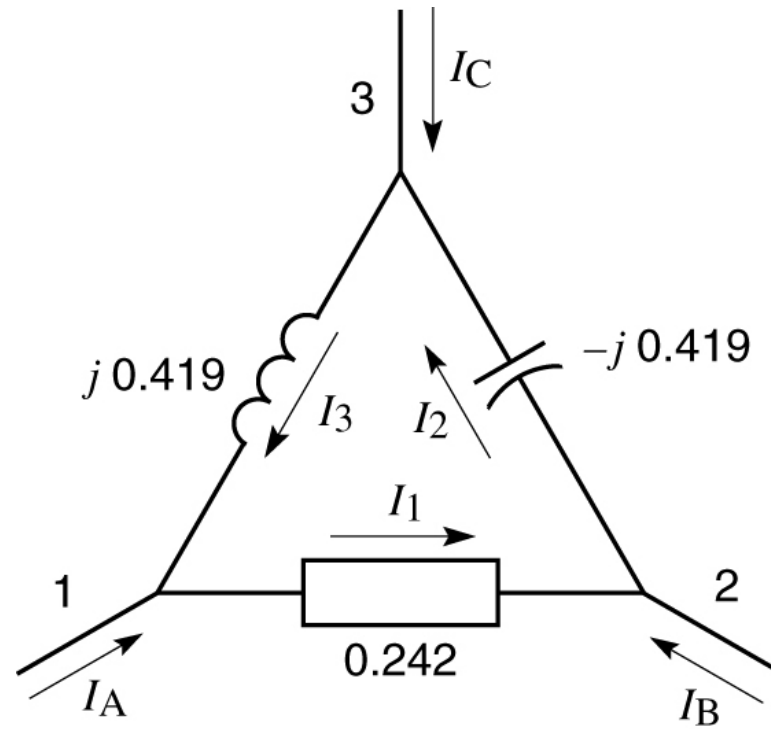


FIGURE 8-35 See Problem 8-14.

