

Problem 1 (10 points)

$$U=120V$$

$$f=60\text{Hz}$$

$$I=5A$$

$$\text{Pf}=\cos\varphi=0,65$$

a. Calculate the reactive power generated by the capacitor. (2 points)

$$X_c = \frac{1}{2 \cdot \pi \cdot f \cdot C} = \frac{1}{2 \cdot \pi \cdot 60 \cdot 60 \cdot 10^{-6}} = 44,21\Omega \quad I_c = \frac{U}{X_c} = \frac{120}{44,21} = 2,71A$$

$$Q_c = U \cdot I_c = 120 \cdot 2,71 = 325\text{VAR}$$

b. Calculate the active power absorbed by the motor. (2 points)

$$P = U \cdot I \cdot \cos\varphi = 120 \cdot 5 \cdot 0,65 = 390W$$

c. The reactive power absorbed from the line. (2 points)

$$\text{Reactive power absorbed by the motor. } Q_{m_r} = U \cdot I \cdot \sin\varphi = 120 \cdot 5 \cdot \sin 49,46^\circ = 455,96VA,$$

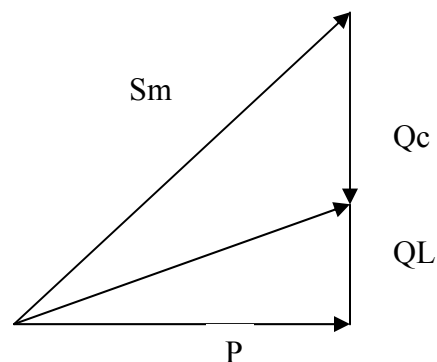
$$\text{Add the reactive powers (} Q_c \text{ negative) } 455,96-325=130,95\text{VAR}$$

d. The line current. (2 points)

$$S = \sqrt{P^2 + Q^2} = \sqrt{390^2 + 130,95^2} = 411,4VA$$

$$I = \frac{S}{U} = \frac{411,4}{120} = 3,43A$$

e. Draw the power triangle of the motor and capacitor connected to the line. (2 points)



Problem 2 (10 points).

A 300 hp, 2300V, 60 Hz, 3 phase squirrel-cage induction motor turns at a full load speed of 590 rpm. The synchronous speed is 600 rpm.

a. Calculate the approximate value of the rotor I^2R losses. (2 points)

$$P_L = 300 \text{ hp} = 300 / 1.34 = 223.9 \text{ kW}$$

$$s = (600 - 590) / 600 = 0.0167$$

$$P_m \approx P_L \text{ so, } P_m = P_r(1 - s) \Rightarrow 223.9 = P_r(1 - 0.0167)$$

$$P_r = 227.7 \text{ kW} \quad P_{jr} = \text{rotor losses} = s \cdot P_r = 0.0167 \cdot 227.7 = 3.8 \text{ kW}$$

If the line voltage then drops to 1944 V, calculate the following:

b. The new speed, knowing that the load torque remains the same. (3 points)

$$s_x = s_n \left(\frac{E_n}{E_x} \right)^2 = 0.0167 \left(\frac{2300}{1944} \right)^2 = 0.0233$$

$$\text{speed} = 600(1 - 0.0233) = 586 \text{ r/min}$$

c. calculate the number of poles.

$$n_s = \frac{60 \cdot f}{p/2} \Rightarrow 600 = \frac{3600}{p/2} \Rightarrow p = 12$$

$$P_L = 300 \text{ hp} = 300 \div 1.34 = 223.9 \text{ kW}$$

$$s = (600 - 590) / 600 = 0.0167$$

Because $P_m \approx P_L$ (Fig. 13-15), we have

$$P_m = P_r(1 - s) \quad (\text{Eq. 13-8})$$

$$223.9 = P_r(1 - 0.0167) \quad \therefore P_r = 227.7 \text{ kW}$$

$$P_{jr} = \text{rotor losses} = sP_r = 0.0167 \times 227.7 = 3.8 \text{ kW}$$

$$\text{a. } s_x = s_n \left(\frac{E_n}{E_x} \right)^2 = 0.0167 \left(\frac{2300}{1944} \right)^2 = 0.0233$$

$$\text{speed} = 600(1 - 0.0233) = 586 \text{ r/min}$$

$$\text{b. } P_L = 300 \times (586/590) = 298 \text{ hp} = 222.4 \text{ kW}$$

Problem 3 (10 points)

$$21-34 \quad \text{a) DC voltage between A and 2} = DE_H = 0.35 \times 600 \\ = 210 \text{ V}$$

$$\text{A is (+) with respect to 2} \quad E_{A2} = + 210 \text{ V}$$

$$\text{b) DC voltage between B and 2} = (1 - D) E_H \\ = (1 - 0.35) \times 600 \\ = 390 \text{ V}$$

$$\text{B is (+) with respect to 2} \quad E_{B2} = + 390 \text{ V}$$

c) From Kirchhoff's voltage law we can write:

$$E_{AB} + E_{B2} + E_{2A} = 0$$

$$\therefore E_{AB} = E_{A2} - E_{B2} = + 210 - 390 = - 180 \text{ V}$$

hence A is negative with respect to B.

- The average voltage between terminals A and 2. (2 points) 210V
- Is terminal A positive with respect to terminal 2? (1 point) (+)
- The average DC voltage between terminals B and 2. (2 points) 390V
- Is terminal B positive with respect to terminal 2? (1 point) (+)
- The average DC voltage between terminals A and B. (2 points) -180V
- What is the polarity of A with respect to B? (2 points) (-)

Questions (10 points)

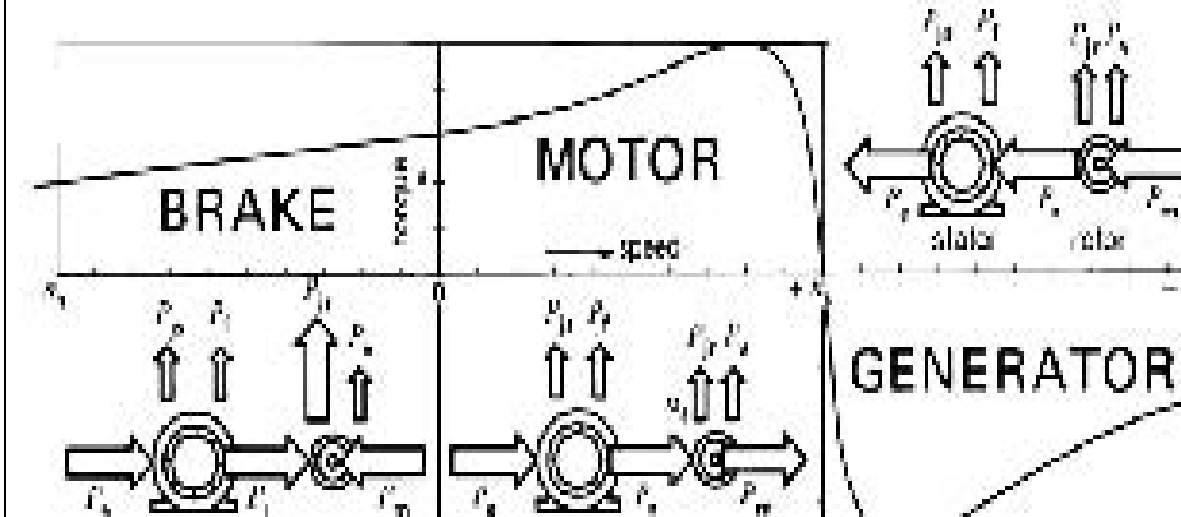
1. (1 point)

State the basic properties of a diode.

A diode conducts only in one direction.

2. (3 points)

Draw the complete torque speed curve of a 3 phase induction machine and mark the brake + motor and generator region.



3. (3 points)

Cycloconverter.

Draw the schematic of a cycloconverter and the typical output of a cycloconverter.

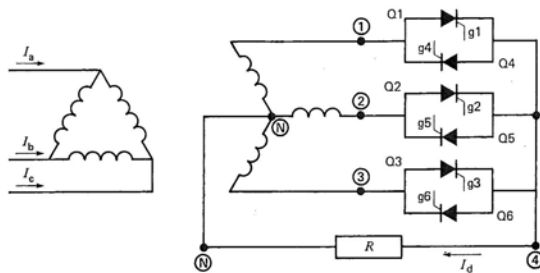
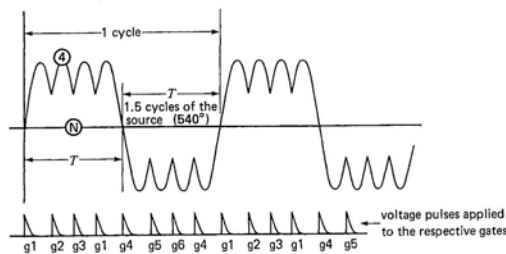
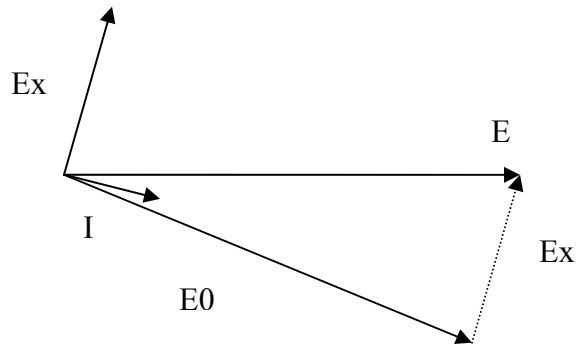


Figure 21.34 Elementary cycloconverter.



4. (2points)

Draw the fasor diagram of a synchronous motor with torque angle 30°



5. (1 point)

What is the definition of “power factor” PF?

The cos of the angle between the current and the voltage.

$$PF = P/S$$