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Space above not to be filled in by the student

Delft Applied Mechanics Course Statics

AE1-914 part I – 27 October 2008 09.00h - 12.00h

Answer sheets

Last name and initials: *Model Answer*

Study no.:

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Only hand in the answer sheets!
Other sheets will not be accepted

Write your name and study number on every page
Sheets without name or study number will not be accepted.

Write relevant calculations on the answer sheet
Use the blank sides of the answer sheets if necessary.
Answers without calculations or motivation will not be taken into account.

Use possible checks to avoid calculation errors
The order of answering the questions is free
NOTE: this exam consists of 5 problems.

The **neatness of the presentation** of the answers
will be considered in the marking.

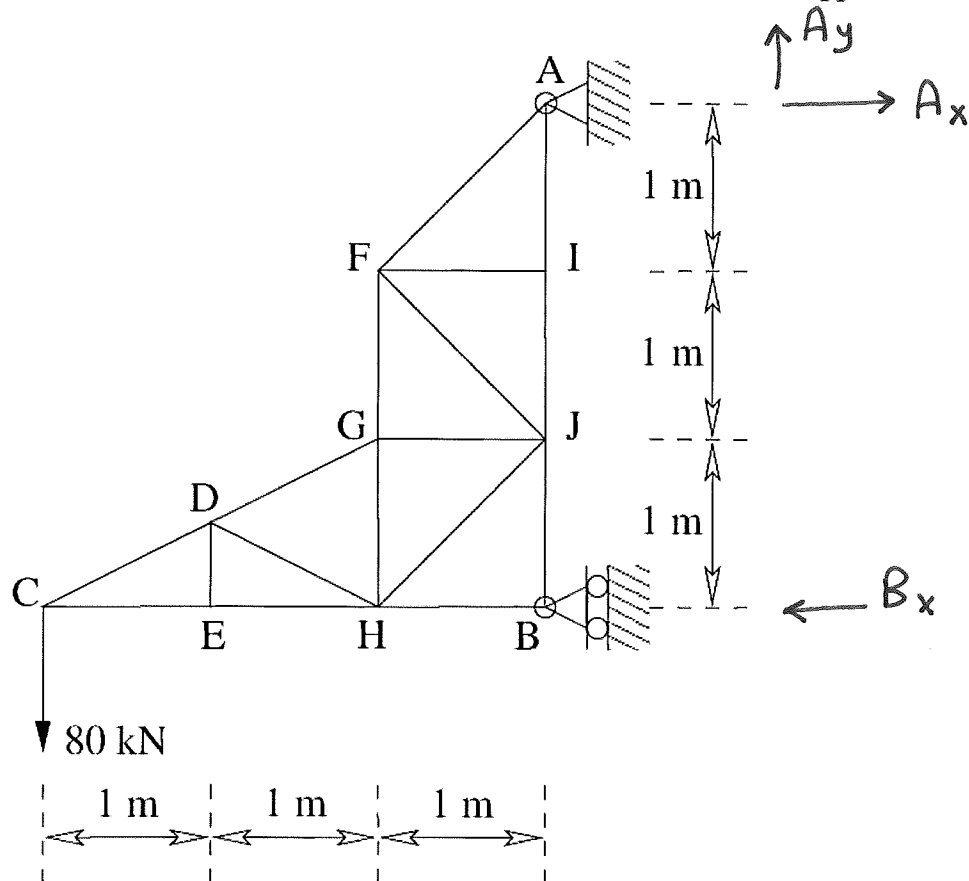
All answers must be given mentioning the correct SI units.

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Problem 1 (Weight 2.5 - approx. 40 minutes)

The truss structure given in the figure is loaded by a force of 80 kN in node C.

Gegeven onderstaand vakwerk onder een verticale belasting van 80 kN in knooppunt C.



- a) Calculate the reaction forces in the supports A and B.

Bereken de reactiekrachten in de steunpunten A en B.

Answer:

$$\checkmark \sum M_A = 0 = 80(3) - B_x(3) \rightarrow B_x = 80 \text{ kN}$$

$$\sum F_x = 0 = -B_x + A_x \rightarrow A_x = 80 \text{ kN}$$

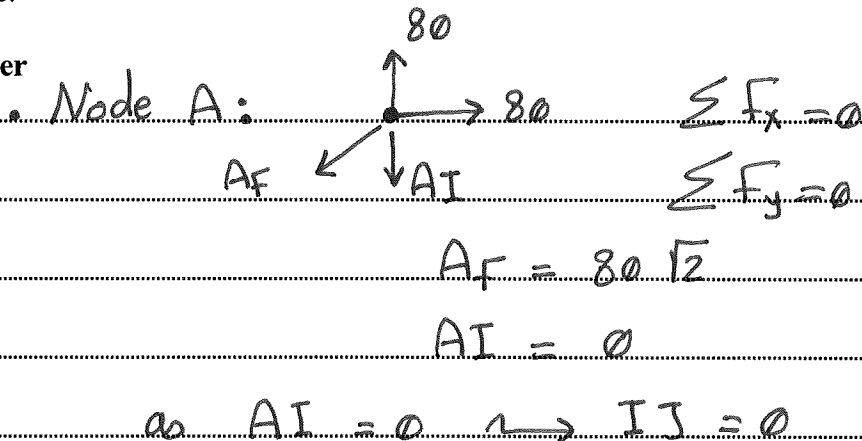
$$\sum F_y = 0 = -80 + A_y \rightarrow A_y = 80 \text{ kN}$$

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- b) Somebody claims that bar IJ is a zero-force member. Is this correct? Motivate your answer.

Iemand beweert dat staaf IJ een nulstaaf is. Is dat correct? Licht uw antwoord toe.

Answer



- c) Indicate which bars are zero-force members.

Geef alle nulstaven in het vakwerk aan.

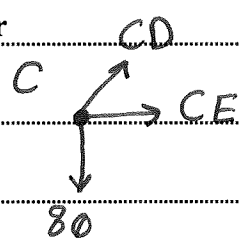
Answer

AI, IJ, FI; BJ, DE, DH

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- d) Calculate the forces in all bars with the correct sign for tension and compression. Collect your results in the table provided on the answer form.
*Bereken alle staafkrachten met het juiste teken voor trek- en drukkrachten.
 Zet uw resultaten in de tabel op dit antwoordformulier.*

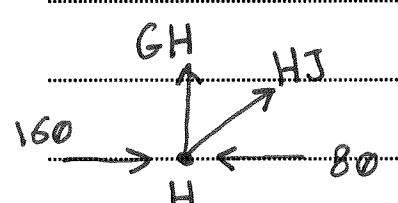
Answer



$$\left. \begin{aligned} \frac{2}{5} CD + CE &= 0 \\ \frac{1}{5} CD - 80 &= 0 \end{aligned} \right\} \begin{aligned} CD &= 80\sqrt{5} \\ CE &= -160 \text{ kN} \end{aligned}$$

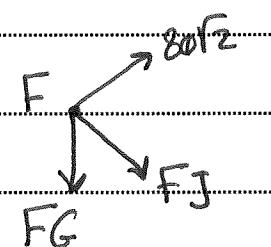
$\Rightarrow EH = CE$
 $DG = CD$

$$HB = -B = -80 \text{ kN}$$

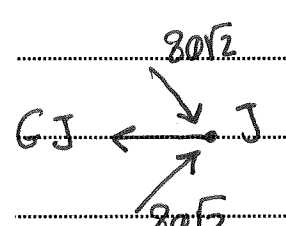


$$\left. \begin{aligned} \sum F_x &= 0 \\ \sum F_y &= 0 \end{aligned} \right\} \begin{aligned} HJ &= -80\sqrt{2} \text{ kN} \\ GH &= 80 \text{ kN} \end{aligned}$$

$$AF = \sqrt{A_x^2 + A_y^2} = 80\sqrt{2} \text{ kN}$$



$$\left. \begin{aligned} -FG - FJ \cdot \frac{\sqrt{2}}{2} + 80 &= 0 \\ 80 + \frac{\sqrt{2}}{2} FJ &= 0 \end{aligned} \right\} \begin{aligned} FJ &= -80\sqrt{2} \text{ kN} \\ FG &= 160 \text{ kN} \end{aligned}$$



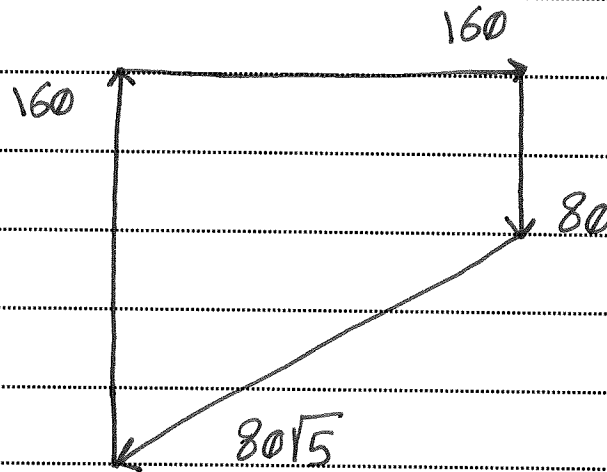
$$\Rightarrow GJ = 160 \text{ kN}$$

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- e) Draw the force polygon for node G.

Teken de krachtenveelhoek voor knooppunt G.

Answer

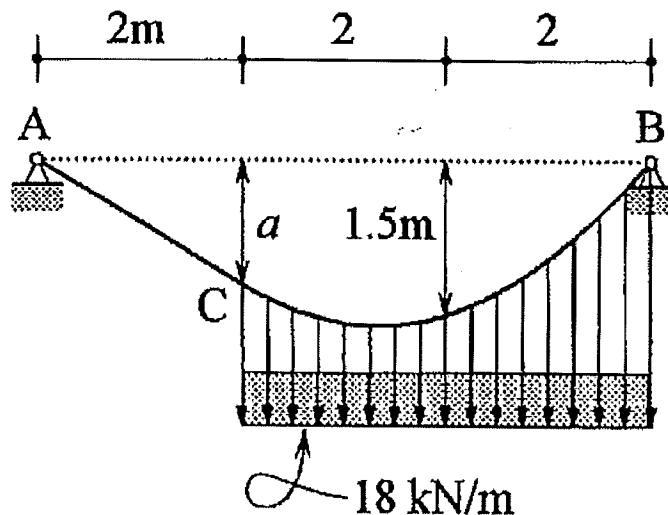


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Problem 2 (Weight 2 - approx. 30 minutes)

Due to the uniformly distributed load of 18 kN/m on CB, cable AB assumes the shape shown.

Onder invloed van de uniform verdeelde belasting van 18 kN/m op kabeldeel CB krijgt kabel AB de vorm zoals aangegeven in onderstaande figuur.



- a) Determine the horizontal component of the cable force.
Bepaal de horizontale component van de kracht in de kabel.

0.5

Answer

$H Z_k = M$

$$+\downarrow \sum F_z = 0 \rightarrow R_A + R_B = (18)(4) = 72 \quad (I)$$

$$+\downarrow \sum M_y|_B = 0 \rightarrow -R_A(6) + (18 \times 4)(2) = 0$$

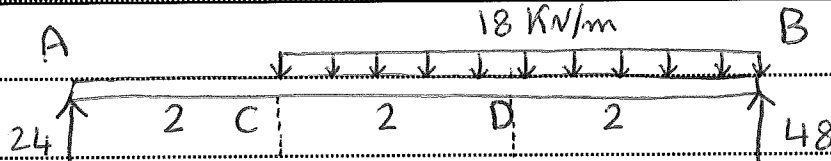
$$\therefore R_A = 24 \uparrow \text{ kN} \quad (II)$$

$$\therefore R_B = 72 - 24 = 48$$

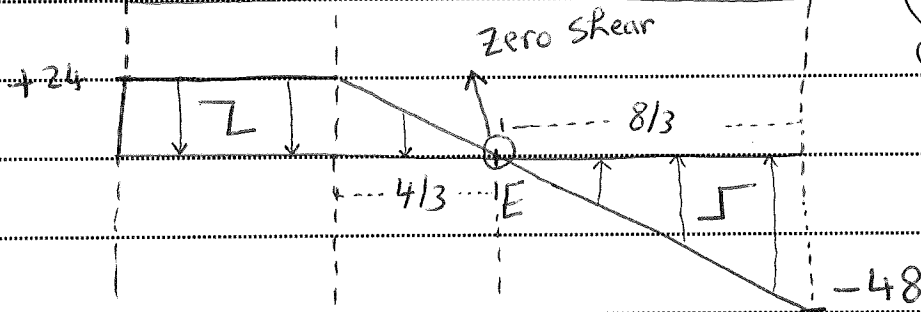
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Exam Ae1-914 part I

Name:



$$\frac{dM}{dx} = V$$



$$24 = 18 \times \frac{4}{3}$$

$$\therefore x = \frac{24}{18} = \frac{4}{3}$$

$$4 - \frac{4}{3} = \frac{12-4}{3} = \frac{8}{3}$$

$$(24)(2) = 48$$

$$\frac{1}{2} \times 24 \times \frac{2}{3} = 16$$

$$\therefore 48 + 16 = 64$$

+48

+64

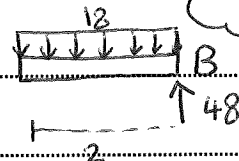
max.

Moment

To Calculate Horizontal Force; They have to calculate Moment @ D; because the Height of the Cable is given at point D = 1.5 m $\rightarrow H \cdot z_D = M_D$

$$\sum M_D = 0 = -M_D + 48(2) - (18 \times 2)(1)$$

$$\therefore M_D = 60 \text{ kN}\cdot\text{m}$$



$$1.5 \times H = 60$$

$$\therefore H = 40 \text{ kN}$$

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Exam Ae1-914 part I

Name:

- b) Determine the maximum cable force.
Bepaal de maximum kabelkracht.

0.5

Answer

Max. Cable force (N) is at where the slope of cable is Max. $\rightarrow$ at 'B'

$$\therefore N_{\max} = \sqrt{H^2 + V_B^2} = \sqrt{(40)^2 + (48)^2}$$

$$N_{\max} = 62.48 \text{ kN}$$

- c) Determine the support reactions at A and B.
Bepaal de steunpuntreacties in A en B.

0.25

Answer

From solution of part (a)

$$R_A = 24 ; R_B = 48$$

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Exam Ae1-914 part I

Name: _____

d) Determine the sag at C.

Bepaal de doorhang van de kabel in punt C.

0.5

Answer

To Determine Sag at 'C' simply apply the same Eqn $\Rightarrow H_C \times Z_C = M_C$

as $H = \text{constant along all cable} = 40$

$\therefore 40 \times Z_C = 48 \rightarrow$ From moment diagram at part (a)

$\therefore Z_C = 1.2$

e) Determine the maximum sag of the cable.

Bepaal de maximale doorhang van de kabel.

0.25

Answer

Max Sag is at the point where moment is maximum [check moment Diagram]

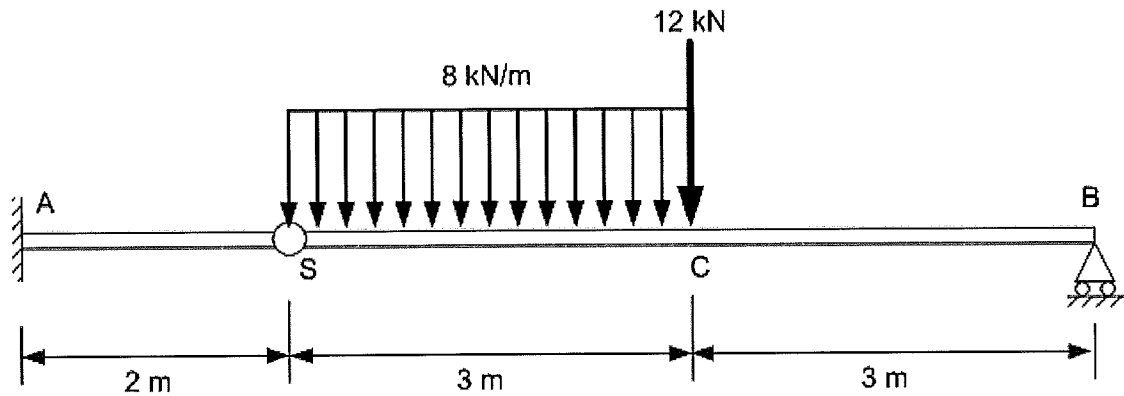
$M_{\max} = 64 \checkmark$ and we know $H = \text{const} = 40$

$\therefore 40 \times Z_{\max} = 64$

$\therefore Z_{\max} = 1.6$

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Problem 3 (Weight 1 - approx. 30 minutes)



- a) Determine the support reactions at A and B.
Bepaal de steunpuntreacties in A en B.

0.3

Answer

∴ We have '4' Reactions and only '3' Equilibrium Eqns.

∴ We have Extra Reaction (Statically Indeterminate) but we have joint at 'S' which gives us an Extra Eqn. that Moment = Zero @ S for the left part and the Right part.

∴ $\sum M_S = 0 = R_B(5) - 12(3) - (8 \times 3)(1.5)$

∴ $R_B = 12$

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Exam Ae1-914 part I

Name:

[Right part]: $\sum F_x = 0 \rightarrow S_x = 0$; $+\uparrow \sum F_y = 0 \rightarrow S_y = 24 + 12 - 12 = 24$

[Left part]: $\sum F_x = 0 \rightarrow H_A = 0$; $\sum F_y = 0 \rightarrow V_A = -24$

$+\circlearrowleft \sum M_A = 0 \rightarrow M_A - 24(2) = 0 \Rightarrow M_A = 48$

$\therefore H_A = 0$; $V_A = -24$; $M_A = 48$; $R_B = 12$

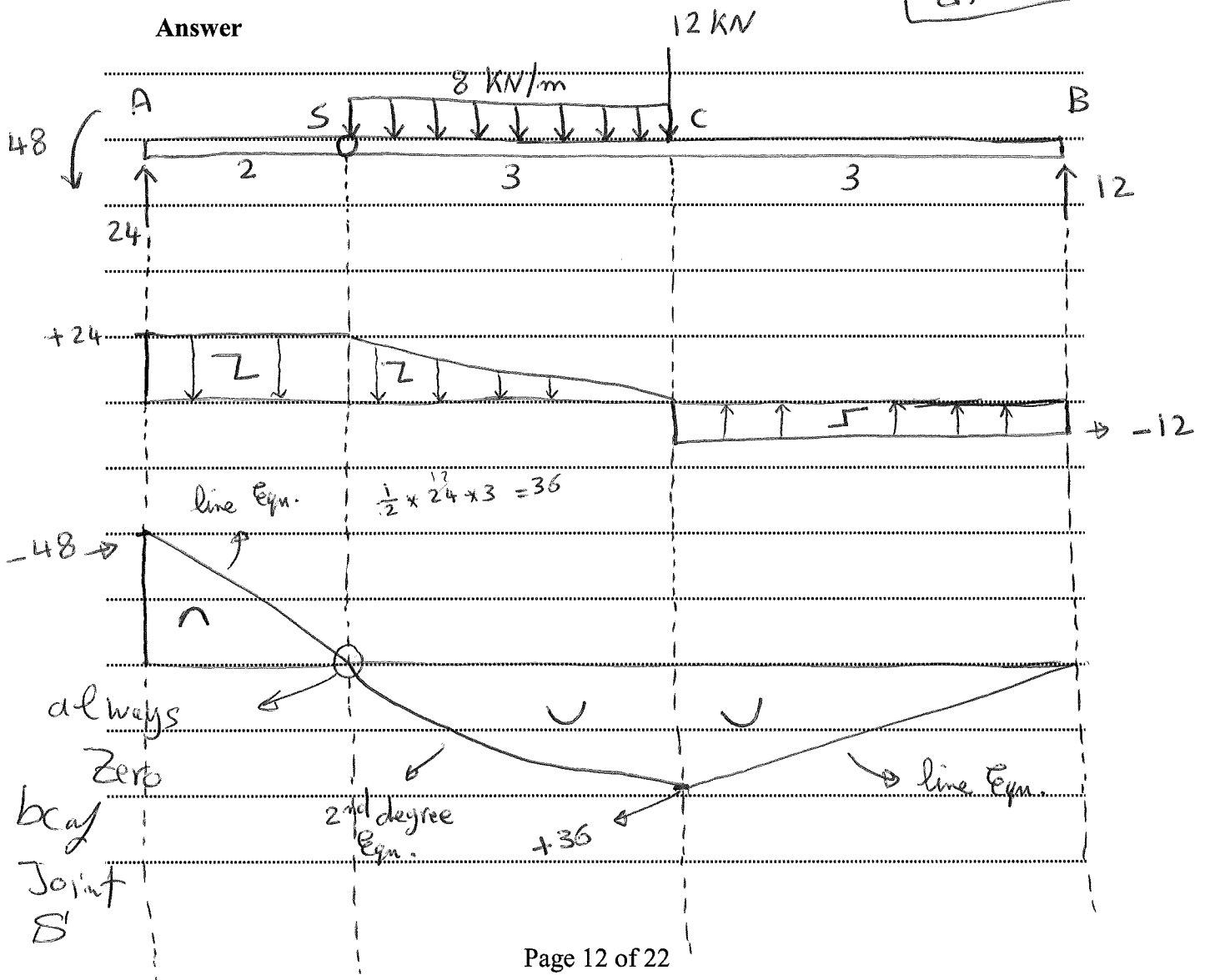
b) Draw the V and M diagrams for the entire structure.

Tekenen de V- en M-lijnen voor de gehele constructie.

0.5

$$\frac{dM}{dx} = V$$

Answer



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Exam Ae1-914 part I

Name:

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- c) Determine the location and magnitude of the maximum bending moment.
Bepaal de positie en de grootte van het maximale buigend moment.

0.2

Answer

.....

x at A $\rightarrow M_{max} = 48$

If They got Reaction $M_A = 48$ Correct ✓

and They wrote $M_{max} = 36$ ^{at C}, then

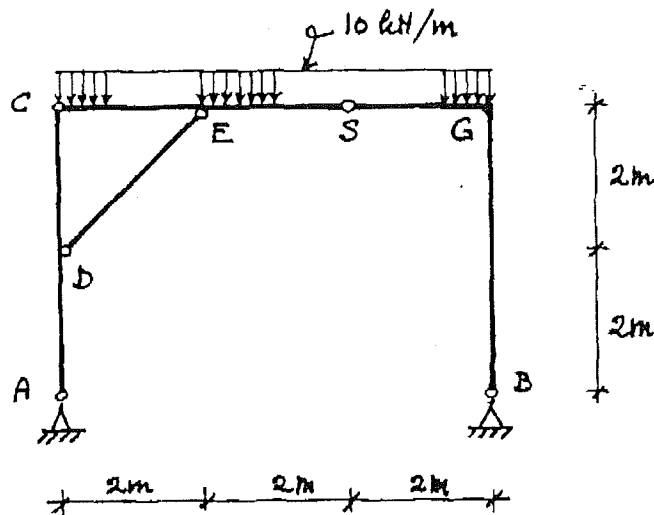
Give them 0.1 mark

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Problem 4 (Weight 2.5 - approx. 45 minutes)

A shored three-hinged frame with a uniformly distributed full load of 10 kN/m on the girder CEG is given.

Een geschoord (ondersteund) driescharnierenspant wordt belast met een uniform verdeelde belasting van 10 kN/m op de ligger CEG.



- a) Determine the support reactions at A and B.
Bepaal de steunpuntreacties in A en B.

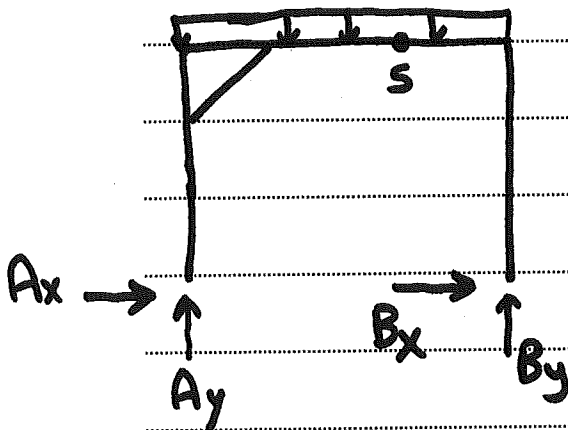
Answer

$$\sum T_z|_B = 0 = -A_y \cdot 6 + 60 \cdot 3$$

$$\rightarrow A_y = 30 \text{ kN}$$

$$\sum T_z|_A = 0 = B_y \cdot 6 - 60 \cdot 3$$

$$\rightarrow B_y = 30 \text{ kN}$$

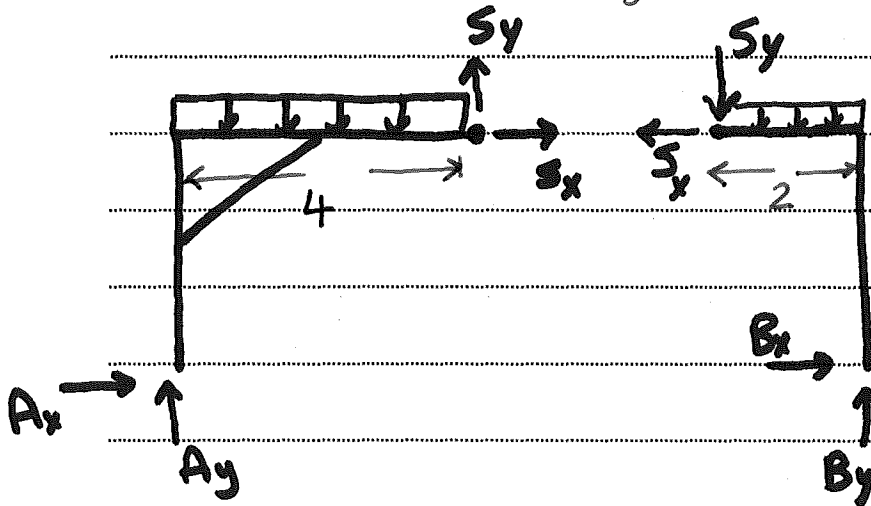


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Exam Ae1-914 part I

Name:

make a section through joint 'S':



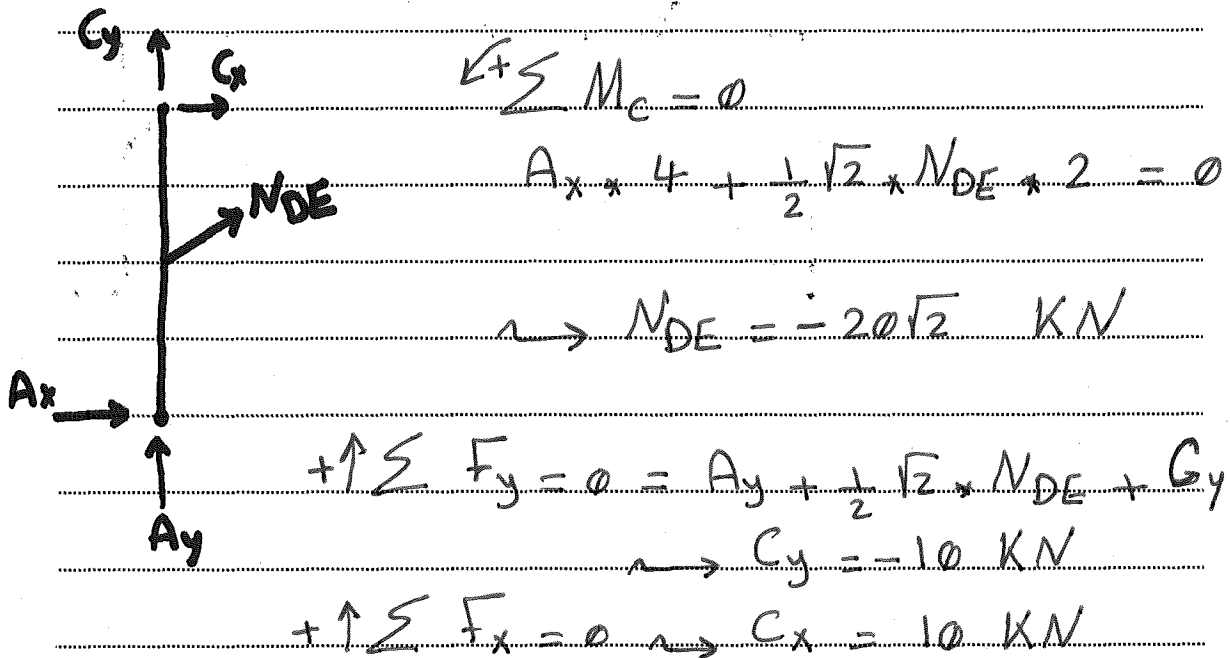
(Left part) $\sum \overset{+}{\curvearrowright} T_2|_S = 0 = (40) \times 2 - A_y \times 4 + A_x \times 4$
 $\rightarrow A_x = 10 \text{ kN}$

(Right part) $\sum \overset{+}{\curvearrowright} T_2|_S = 0 = -20 \times 1 + B_y \times 2 + B_x \times 4$
 $\rightarrow B_x = -10 \text{ kN}$

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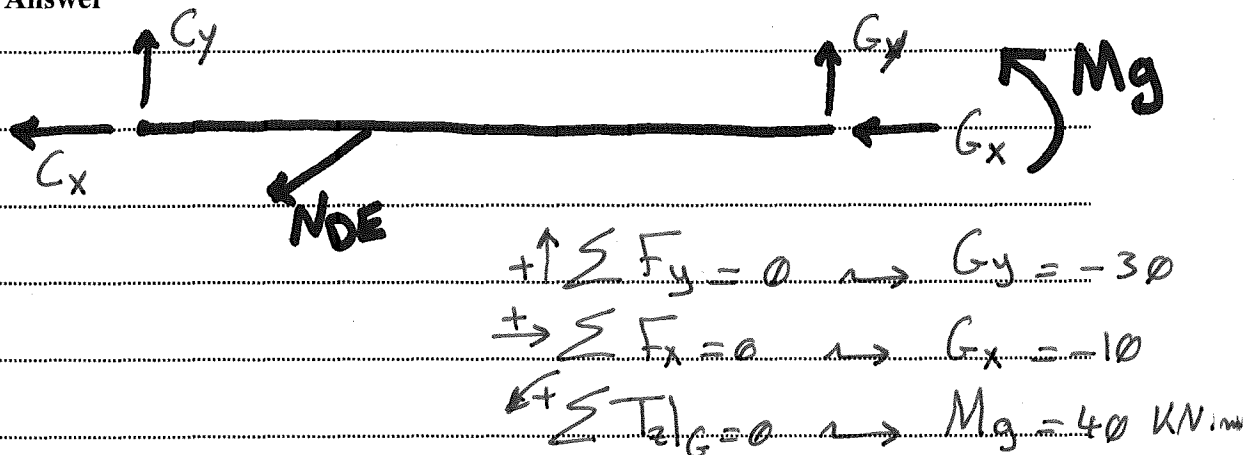
- b) Determine the force in shore DE, with the correct sign.
Bepaal de kracht in staaf DE, met het juiste teken.

Answer



- c) Draw N, V, and M diagrams for CESG.
Teken de N-, V- en M-lijnen voor ligter CESG.

Answer

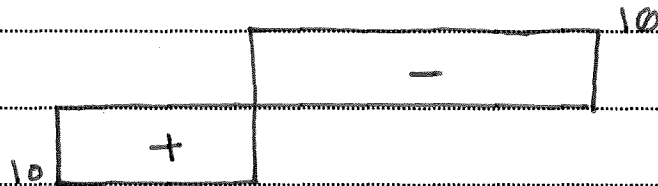


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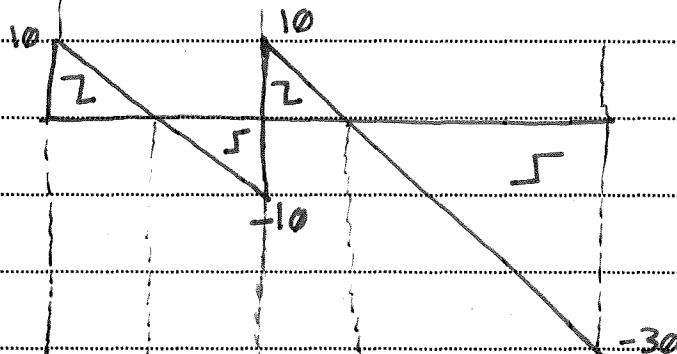
Exam Ae1-914 part I

Name:

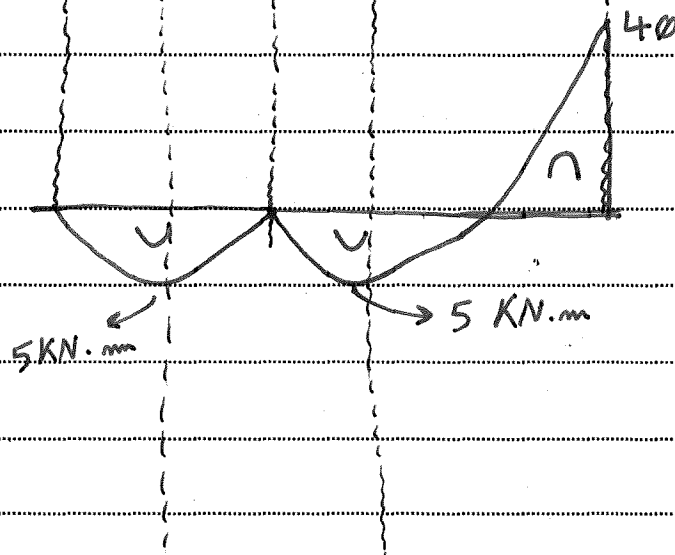
* N-diagram:



* V-diagram:



* M-diagram:



Answer sheets

Student no:

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Exam Ae1-914 part I

Name: _____

- d) Determine the location and magnitude of the extreme moments in CESG.
Bepaal de positie en de grootte van de extreme momenten in CESG.

Answer

Extreme at point G = 40 kNm

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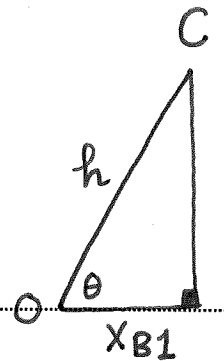
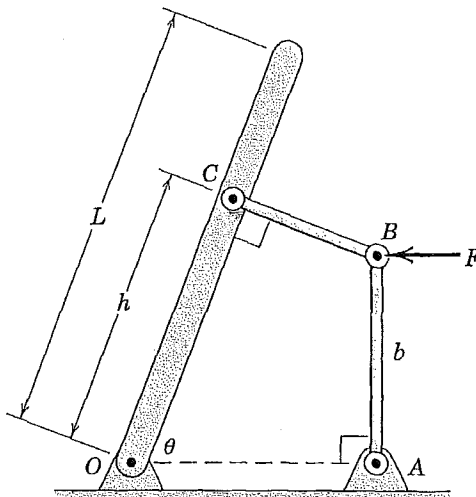
Exam Ae1-914 part I

Name: _____

Problem 5 (Weight 2 - approx. 35 minutes)

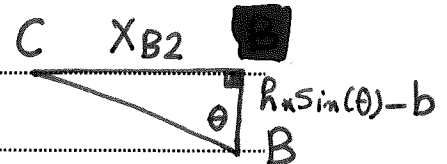
- a) The uniform bar of mass m is held in the inclined position θ by the horizontal force F applied to the links AB and BC whose masses are negligible. For the position shown AB is perpendicular to AO and BC is perpendicular to the bar, determine F . Use the principle of virtual work.

Onder invloed van een horizontale kracht F wordt de uniforme balk met massa m in een positie θ gehouden. Een horizontale kracht F grijpt aan in punt B, waar de massaloze staven CB en AB scharnierend met elkaar zijn verbonden. Voor de getekende positie staat staaf AB loodrecht op AO en staat staaf CB loodrecht op de uniforme balk. Bereken, met het principe van virtuele arbeid, de kracht F die nodig is om de balk in de getekende positie te houden.



$$X_B = X_{B1} + X_{B2}$$

$$X_{B1} = h \times \cos(\theta)$$



$$X_{B2} = [h \sin(\theta) - b] \times \tan(\theta)$$

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Exam Ae1-914 part I

Name:

$$\circ \delta x_B = -h \cdot \sin(\theta) \cdot \delta \theta$$

$$\circ \delta A = F \cdot \delta x_B + mg \left[-\frac{L}{2} \cdot \cos(\theta) \right] = 0$$

$$\circ F = \frac{-1}{2} \cdot \frac{mgL}{h} \cdot \frac{\cos(\theta)}{\sin(\theta)}$$

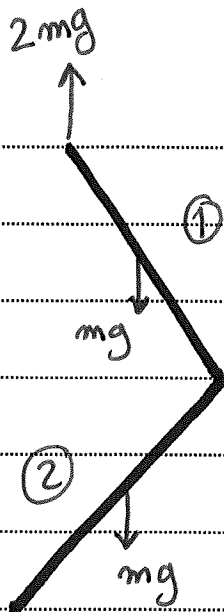
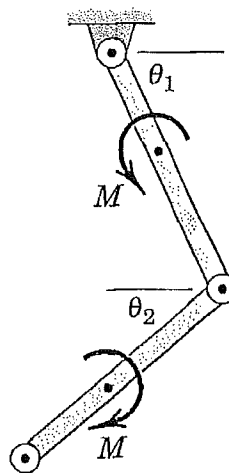
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Exam Ae1-914 part I

Name:

- b) Each of the uniform identical links has a length l and mass m and is subjected to a couple M , one clockwise and the other counterclockwise, applied as shown. Determine the angle which each link makes with the horizontal when the system is in its equilibrium configuration. Use the principle of virtual work.

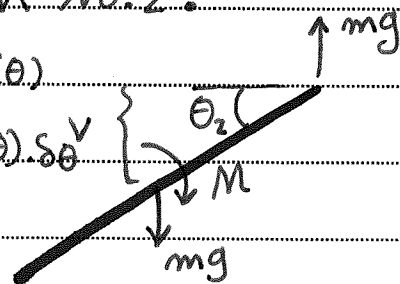
Elk van de uniforme balken heeft lengte l en massa m . Beide balken worden belast met een moment M , zoals in onderstaande figuur. Bepaal de hoek die elke balk maakt met de horizontaal voor de getekende evenwichtpositie. Gebruik het principe van virtuele arbeid.



Study link No. 2:

$$V = \frac{L}{2} \sin(\theta)$$

$$\delta V = \frac{1}{2} \cos(\theta) \cdot \delta \theta$$



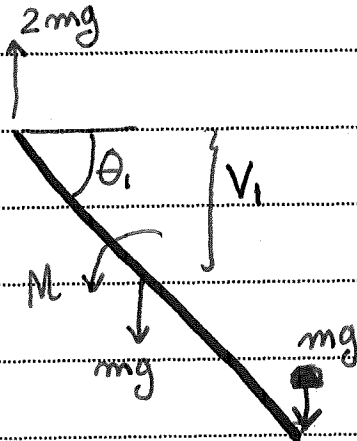
$$\delta A = 0 = -M \delta \theta + \frac{1}{2} L \cos(\theta) \delta \theta + mg \cos(\theta_2)$$

$$\Rightarrow \theta_2 = \cos^{-1} \left(\frac{2M}{mgL} \right)$$

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Exam Ae1-914 part I

Name:



$$V_1 = \frac{L}{2} \sin \theta_1$$

$$V_2 = L \sin \theta_1$$

$$\therefore \delta V_1 = \frac{L}{2} \cos(\theta_1) \delta \theta_1$$

$$\delta V_2 = L \cos(\theta_1) \delta \theta_1$$

$$\delta A = 0 = -M \delta \theta + mg \cdot \frac{L}{2} \cos(\theta_1) \delta \theta +$$

$$mg \cdot L \cos(\theta_1) \delta \theta$$

$$\therefore \rightarrow \theta_1 = \cos^{-1} \left(\frac{2M}{3mgL} \right)$$