

# **Ships: Loads, stability and erosion**

## **Chapter 9**

**ct4310 Bed, bank and shoreline protection**

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**June 3, 2012**

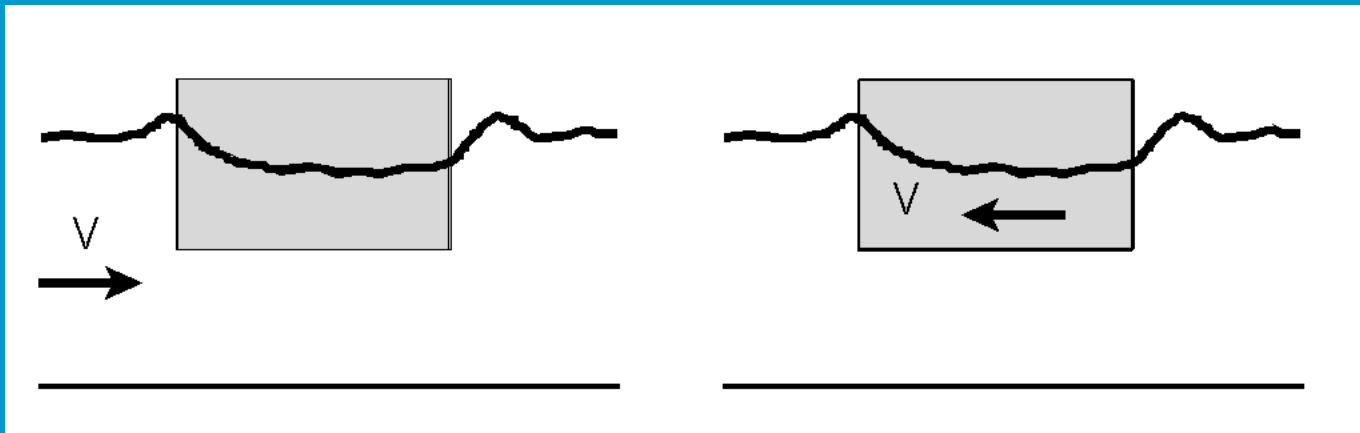
**Faculty of Civil Engineering and Geosciences  
Section Hydraulic Engineering**

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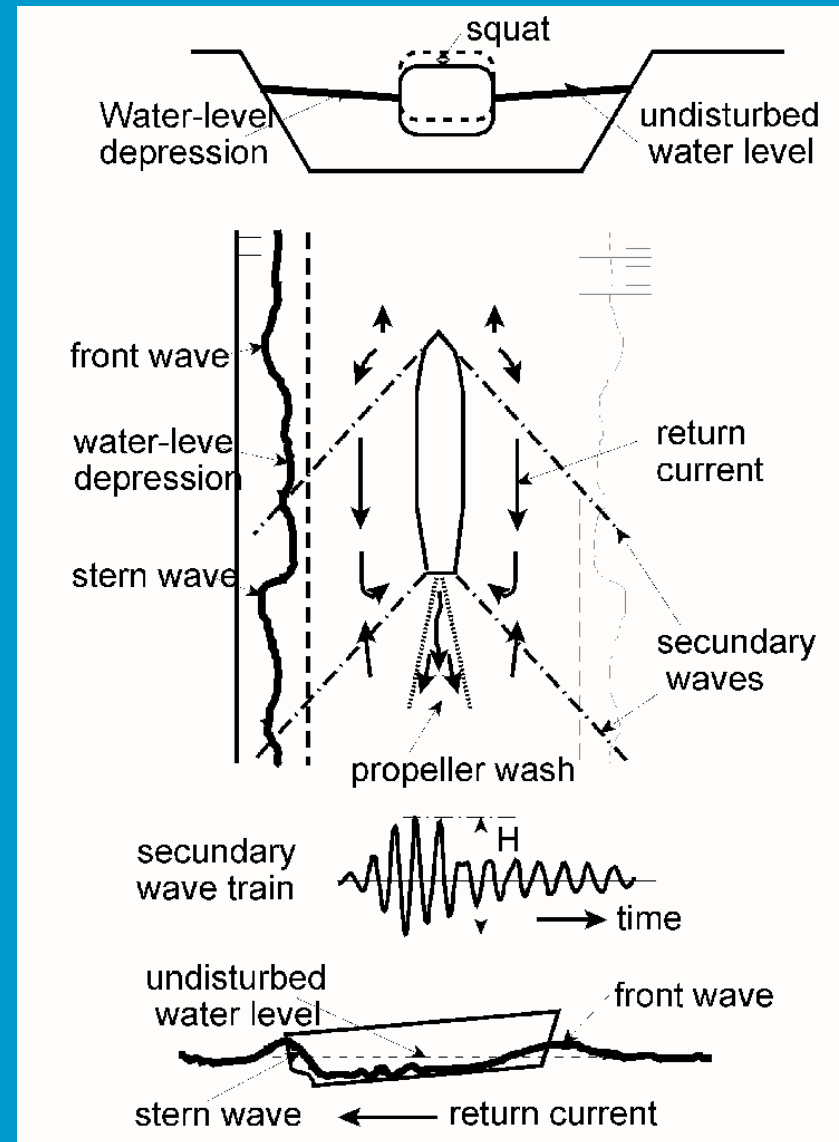
# Introduction

- In inland waterways ships may cause waves
  - primary wave
  - secondary waves
  - propeller wash

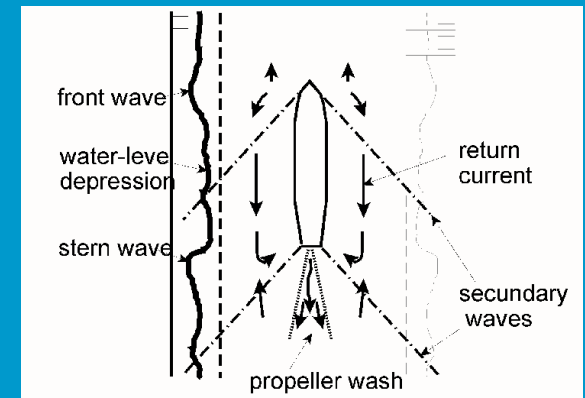
# flow around fixed object & moving object in stagnant water



# Phenomena around a moving ship in a waterway



# Return current and primary wave



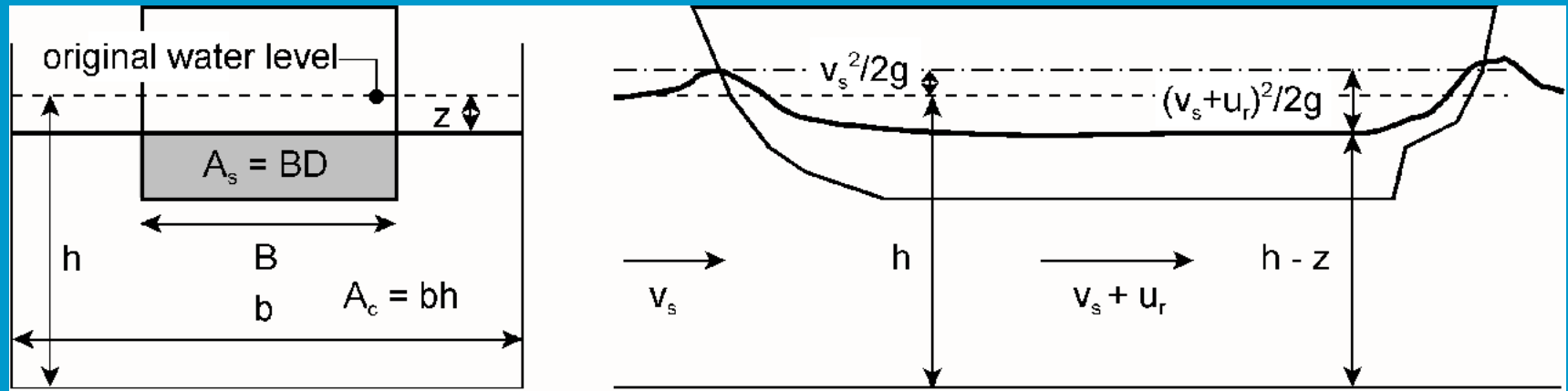
Ship in Elbe river, courtesy prof. Erik Pasche, TU Hamburg

# propeller wash

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# Definition in 1-d approach



$$\left. \begin{aligned} c &= \frac{gT}{2\pi} \tanh \frac{2\pi h}{L} \\ L &= cT \end{aligned} \right\} V_l = c = \sqrt{\frac{gL}{2\pi} \tanh \frac{2\pi h}{L}}$$

# limit speed

$$\text{Bernoulli :} \quad h + \frac{v_s^2}{2g} = h - z + \frac{(v_s + u_r)^2}{2g}$$

$$\text{continuity:} \quad b h v_s = (b h - B D - b z)(v_s + u_r) = Q$$

Maximum speed is reached when return flow becomes critical, i.e. when derivative of return flow to waterlevel becomes zero

$$\frac{dQ}{dz} = \frac{d(v_s + u)(A_c - A_s - bz)}{dz} = 0$$

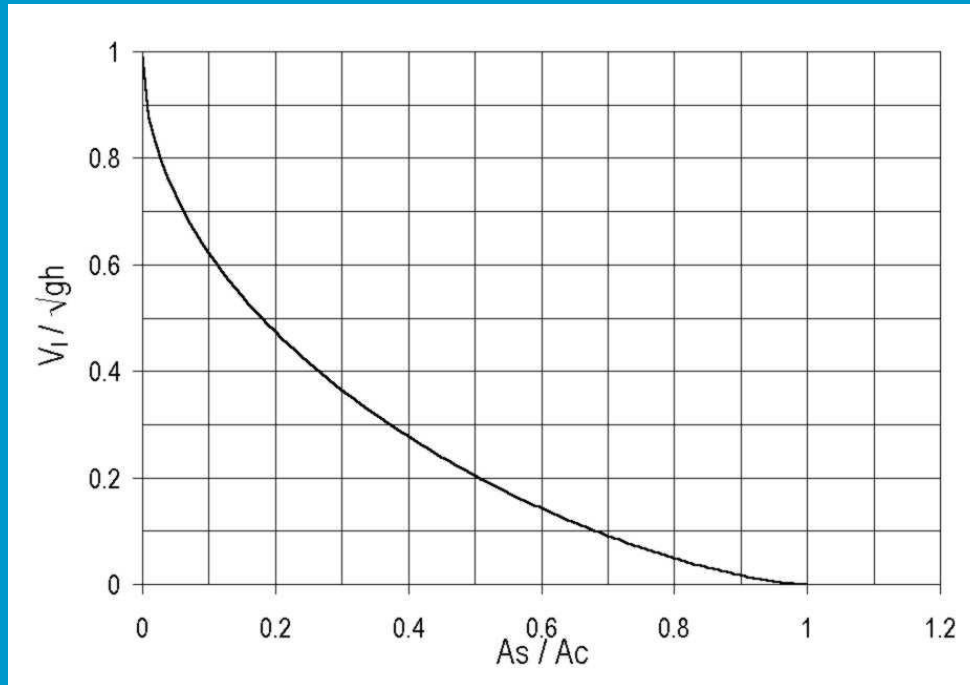
Combine this with Bernoulli:

$$\frac{A_s}{A_c} - \frac{V_l^2}{2gh} + \frac{3}{2} \frac{V_l^{2/3}}{(gh)^{1/3}} = 1$$



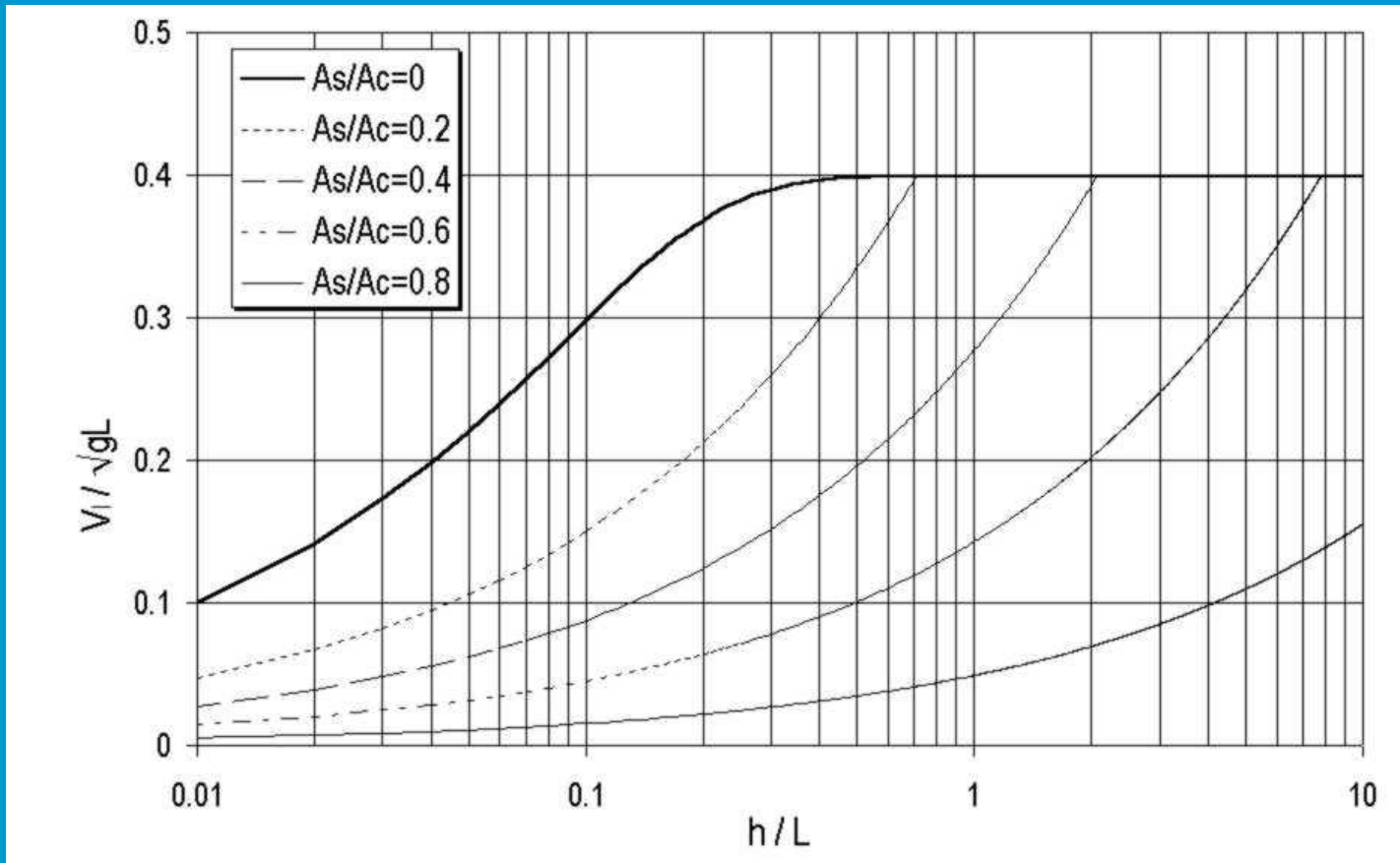
# limit speed a a function of blockage

$A_s/A_c$



$$\frac{A_s}{A_c} - \frac{V_l^2}{2gh} + \frac{3}{2} \frac{V_l^{2/3}}{(gh)^{1/3}} = 1$$

# limit speed as a function of waterdepth and blockage

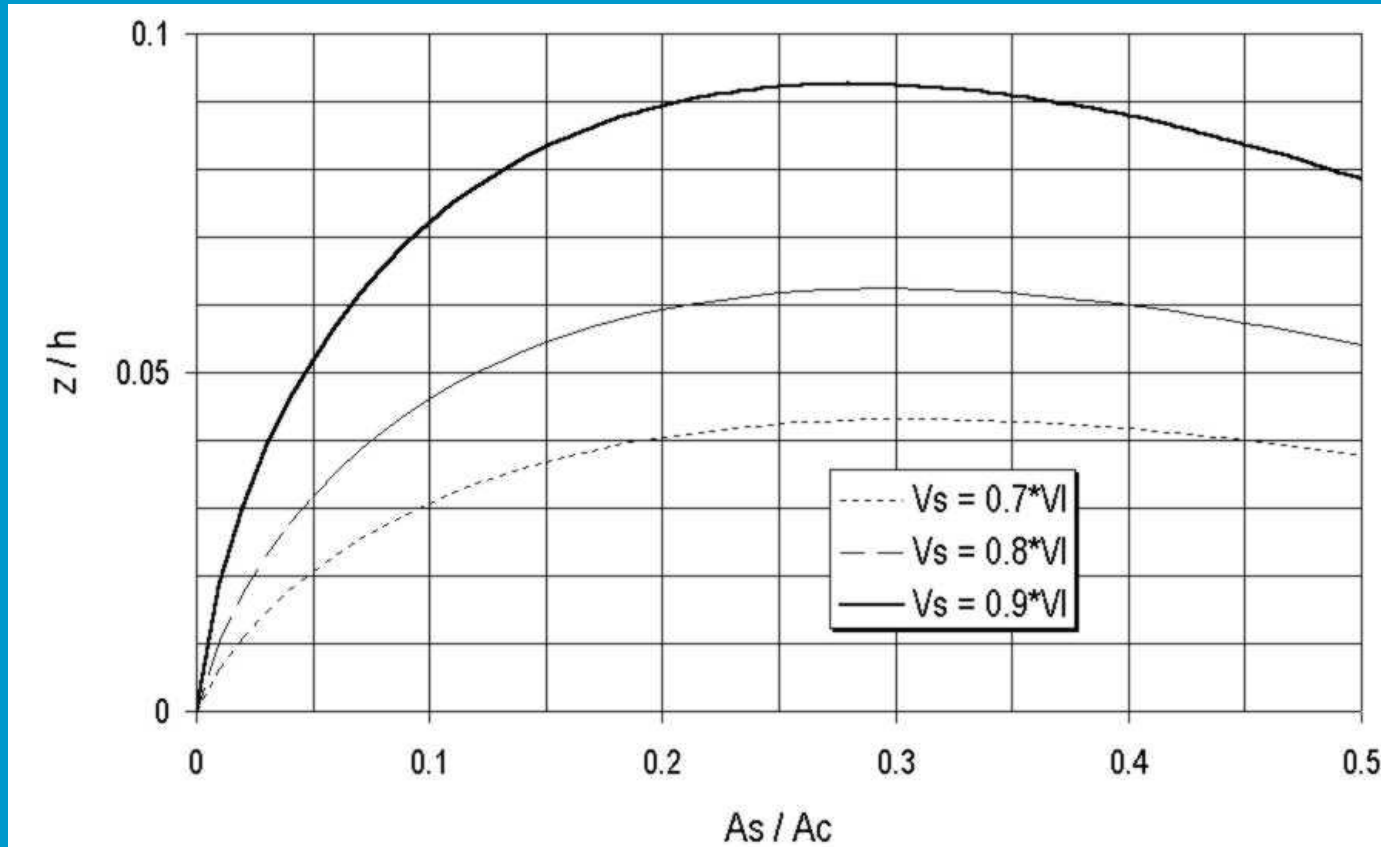


# primary waves

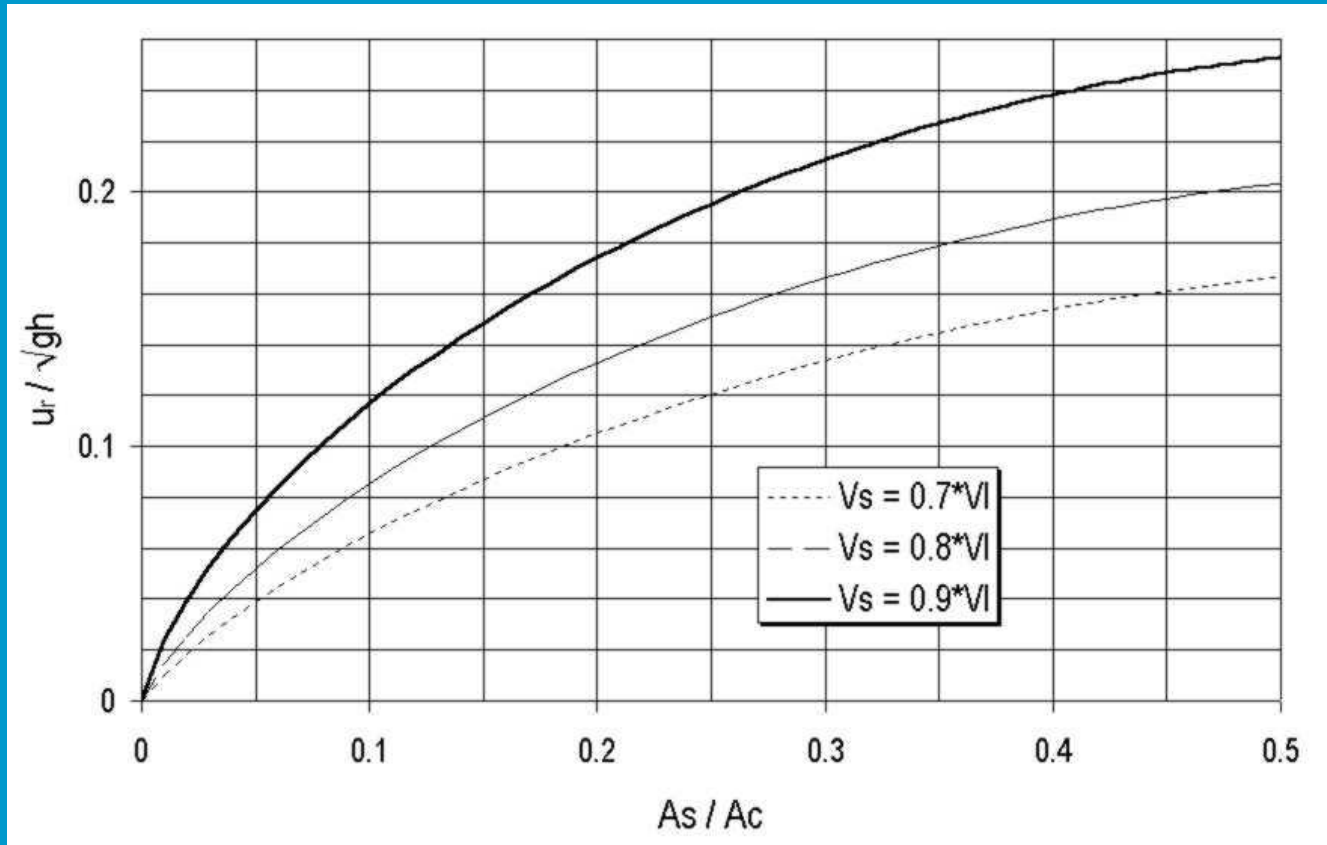
$$\frac{v_s^2}{gh} = \frac{2z/h}{(1 - A_s/A_c - z/h)^{-2} - 1}$$

$$\frac{u_r}{\sqrt{gh}} = \left[ \frac{1}{1 - A_s/A_c - z/h} - 1 \right] \frac{v_s}{\sqrt{gh}}$$

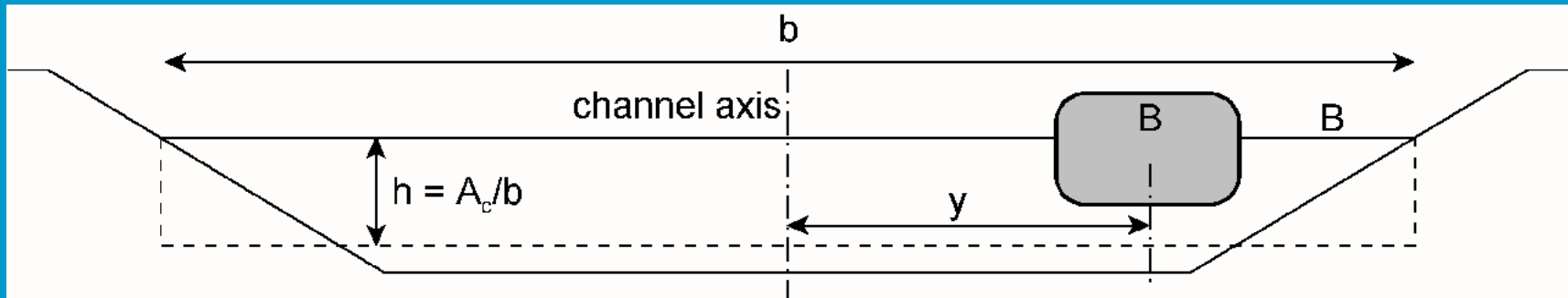
# waterlevel depression as a function of blockage



# return flow velocity as function of blockage



# deviation from the 1-d case

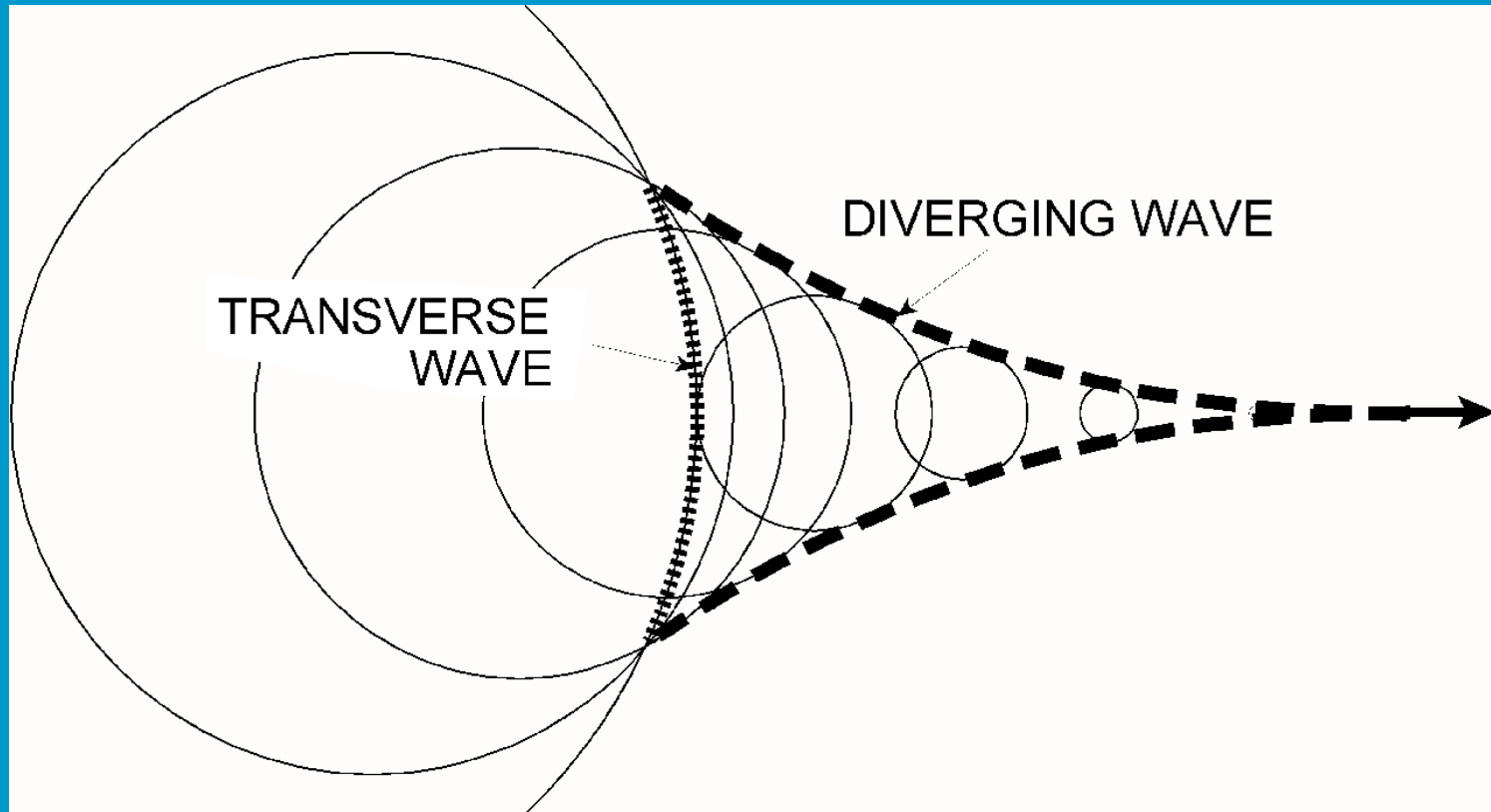


$$z_{ecc} = \left(1 + \frac{2y}{b}\right) z$$

$$u_{r-ecc} = \left(1 + \frac{y}{b}\right) u_r$$

$$z_{\max} = 1.5 z_{ecc}$$

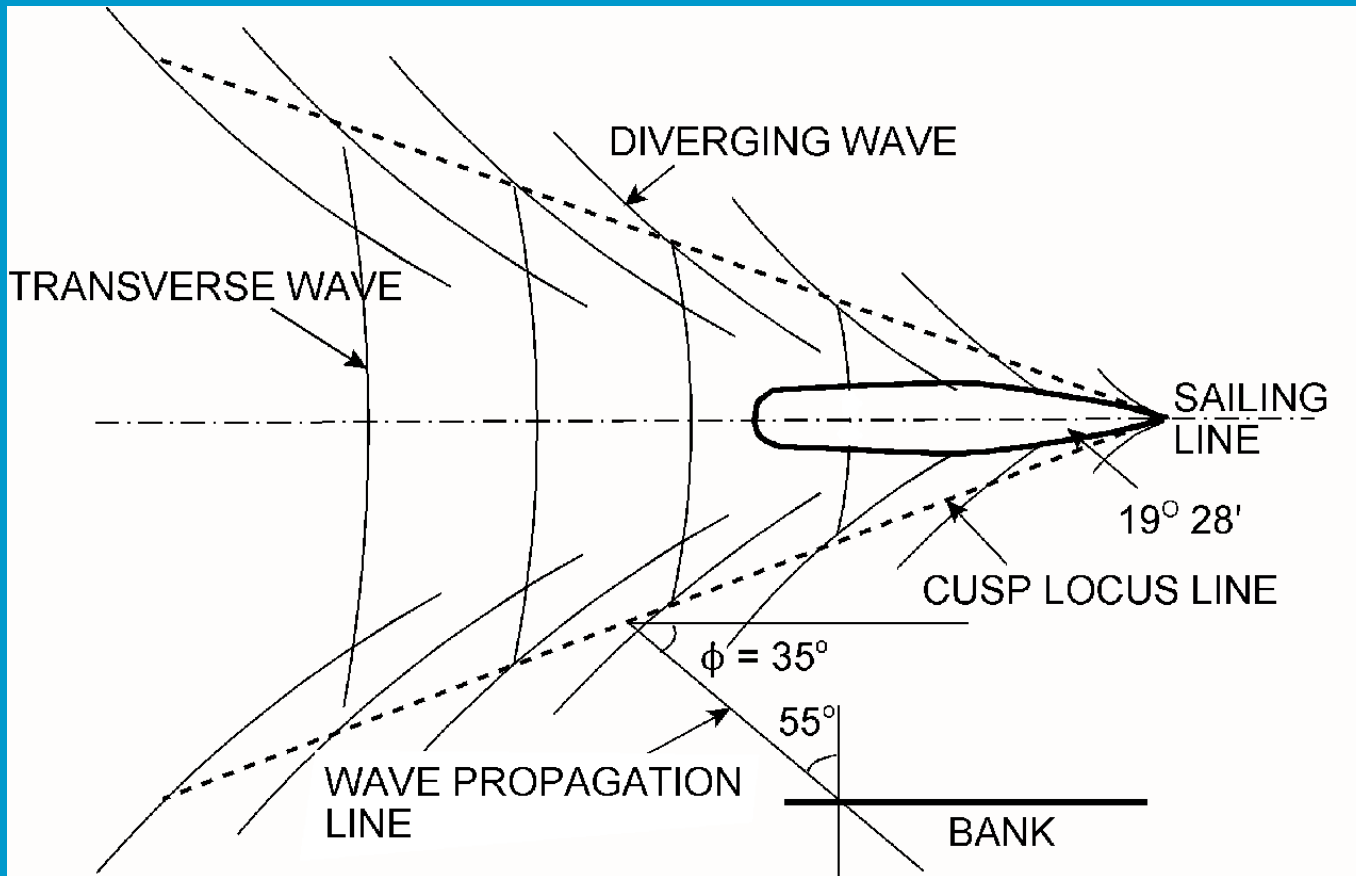
# origin of diverging and transverse waves



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# secondary wave pattern





# Kelvin wave



Christian Eskelund US Navy

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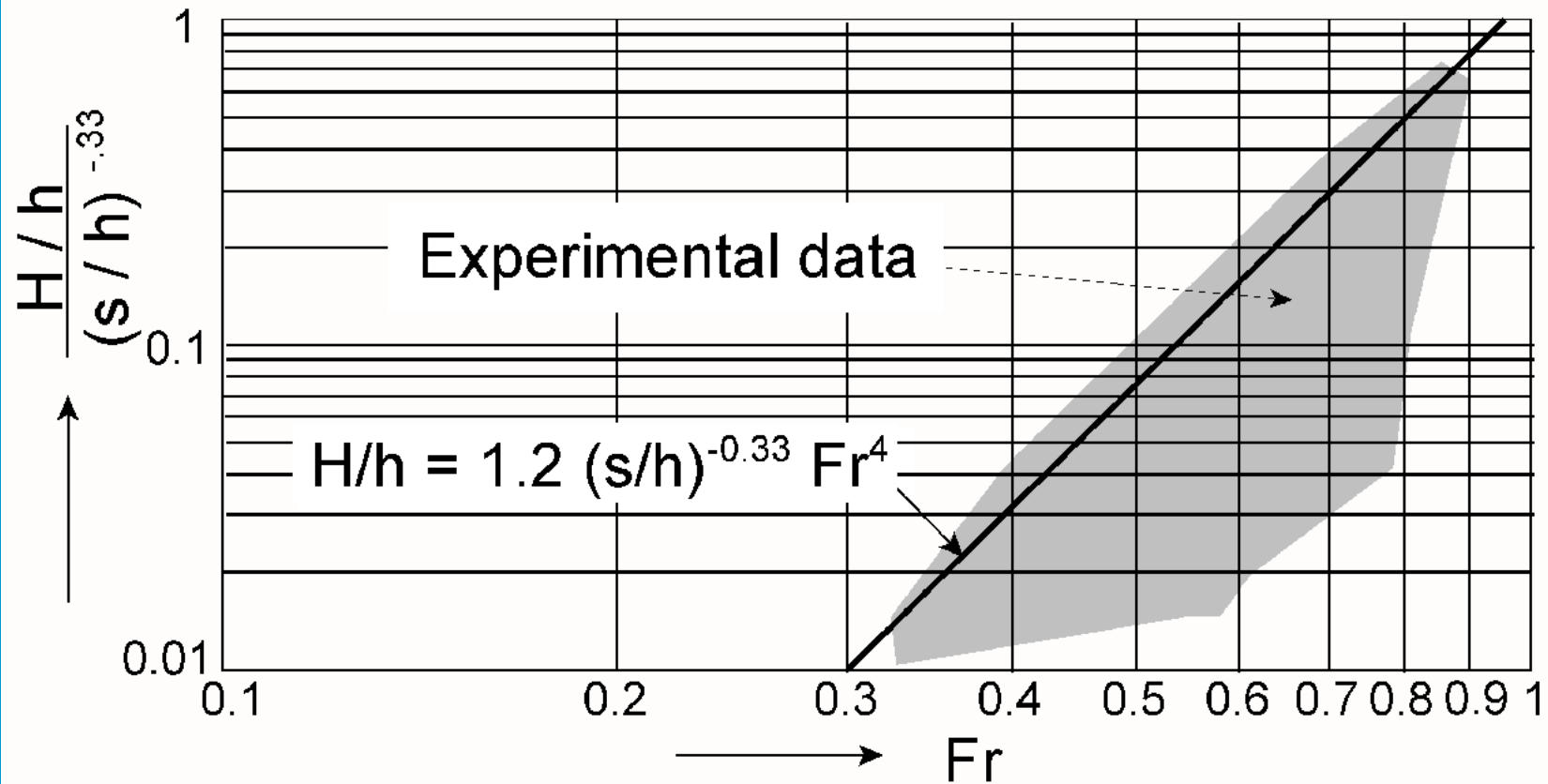
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# Kelvin Duck wave

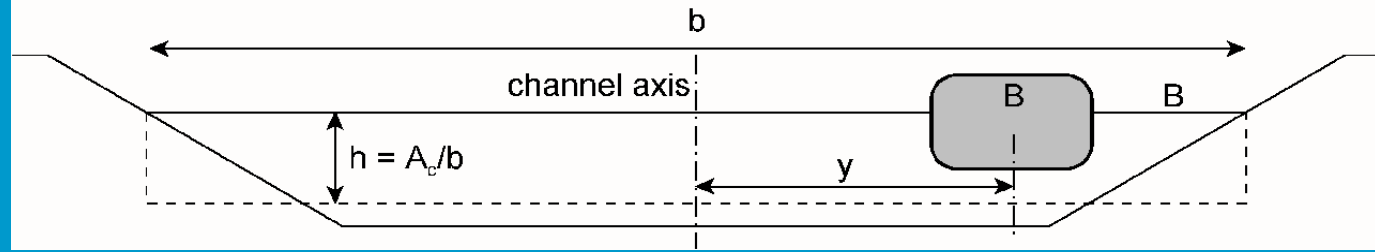


M.S.Cramer, Virginia Tech Duck Pond

# secondary wave height measurements



# example



Given: ship 10 m wide, draught 3 m  
 canal 40 m wide, 5 m deep

Limit speed:  $A_s/A_c = (10 \cdot 3) / (40 \cdot 5) = 0.15$       fig 9.4

$V_f/\sqrt{gh} = 0.55 \rightarrow V_f = 3.8 \text{ m/s}$       design speed  $0.9 \cdot 3.8 = 3.4 \text{ m/s}$

Use fig. 9.6       $z/h = 0.083 \rightarrow z = 0.42 \text{ m}$

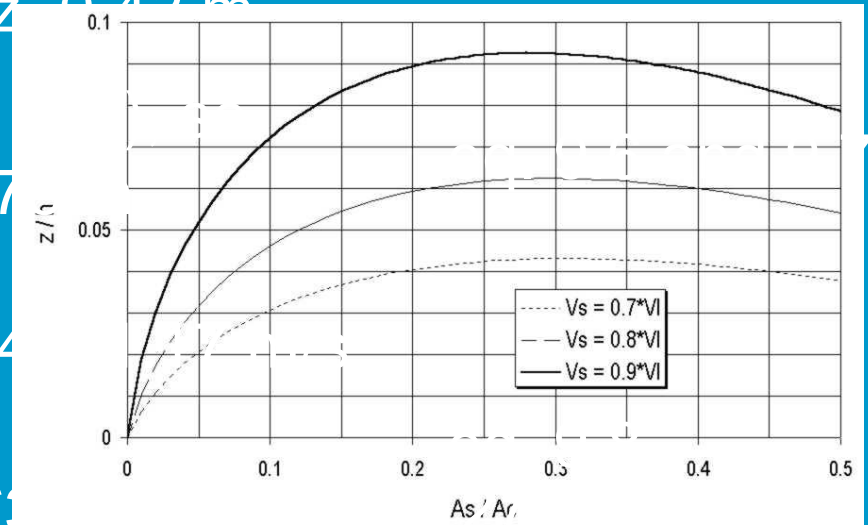
Ship sails 10 m from bank ( $y = 10 \text{ m}$ )

$z_{\max} = 1.5 \cdot ((1 + 2 \cdot 5/40) \cdot 0.42) = 0.7 \text{ m}$

$u_r = 0.15 \cdot \sqrt{gh} = 1.04 \text{ m/s}$

incl. excentricity:  $(1 + 5/40) \cdot 1.04 = 1.12 \text{ m/s}$

$H = 1.2 \cdot h \cdot (s/h)^{-0.33} \cdot v^4 / (gh)^2 =$   
 $1.2 \cdot 5 \cdot (10/5)^{-0.33} \cdot 3.4^4 / (9.81 \cdot 5)^2 = 0.42 \text{ m}$



# standard values in the Netherlands

	Wave heights (m)		Currents (m/s)	
	Wind waves	Ship waves	Natural current	Return current
Lakes	0.25 – 1.00	0.10 – 0.50	0.1 – 0.5	0.1 – 0.25
Canals	0.10 – 0.25	0.25 – 0.75	0.5 – 1.0	0.5 – 1.0
Rivers	0.25 – 1.00	0.25 – 0.75	1.0 – 2.0	0.5 – 1.0
Small waters	0.10 – 0.20	n.a.	0.2 – 1.0	n.a.

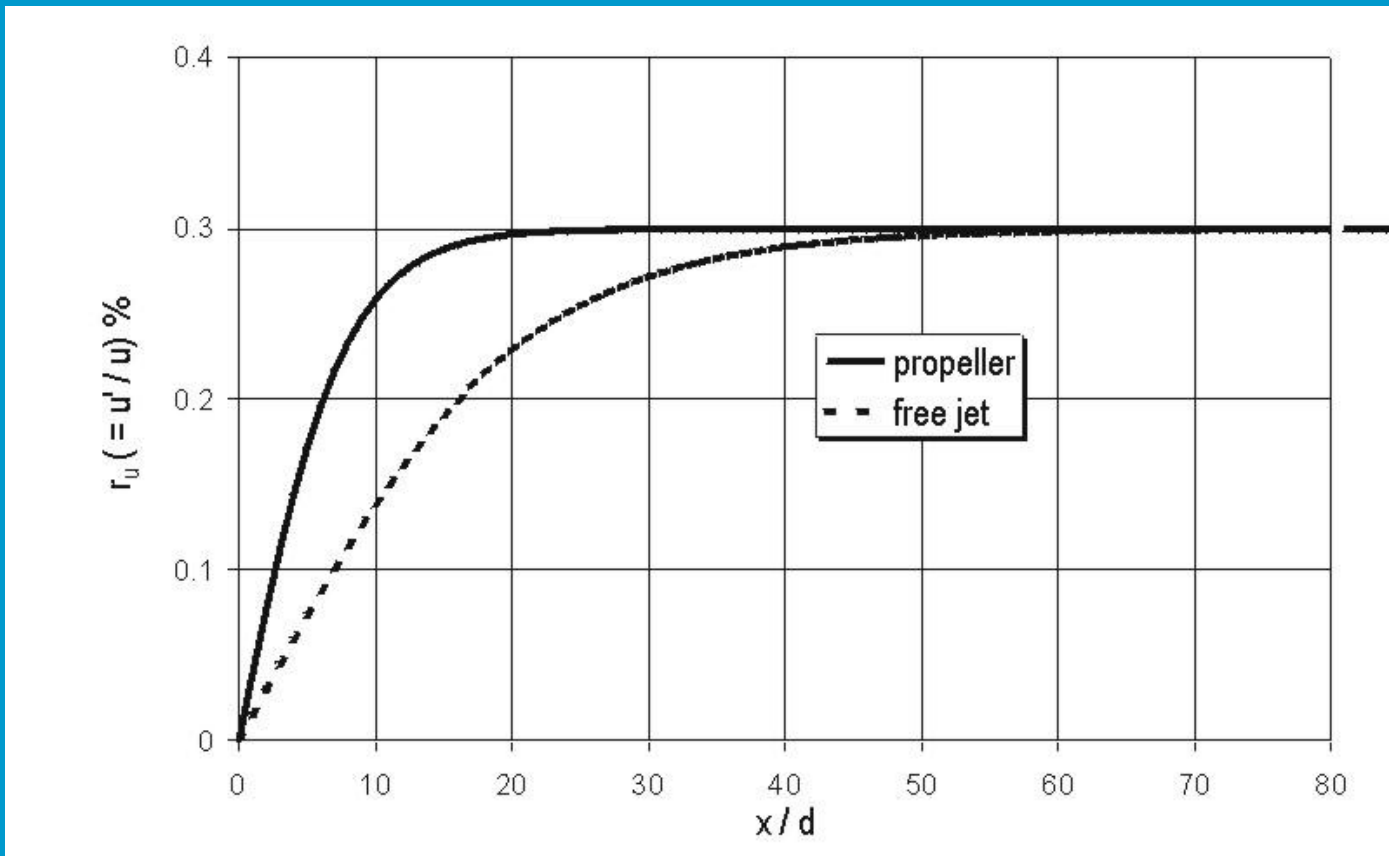
Data from CUR 197  
“Breuksteen in de praktijk”

# Propeller action

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# turbulence in propeller wash and in free circular jet

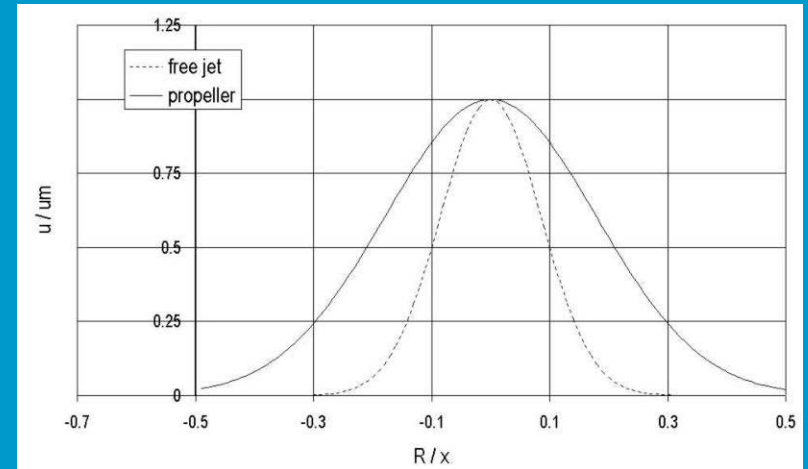
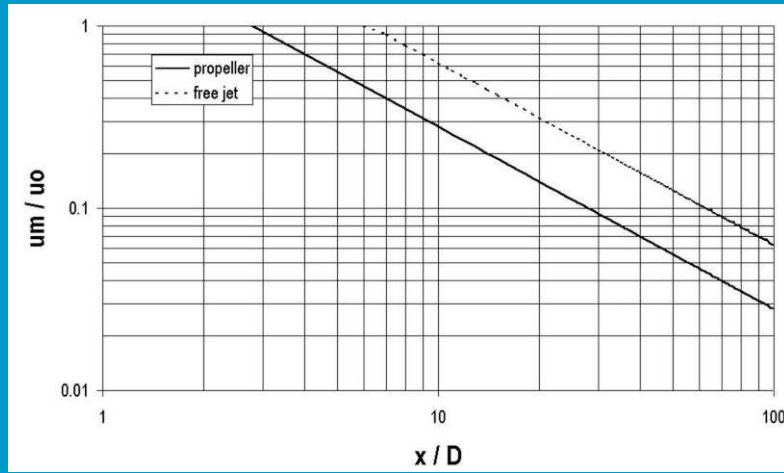


# equations for propeller jets

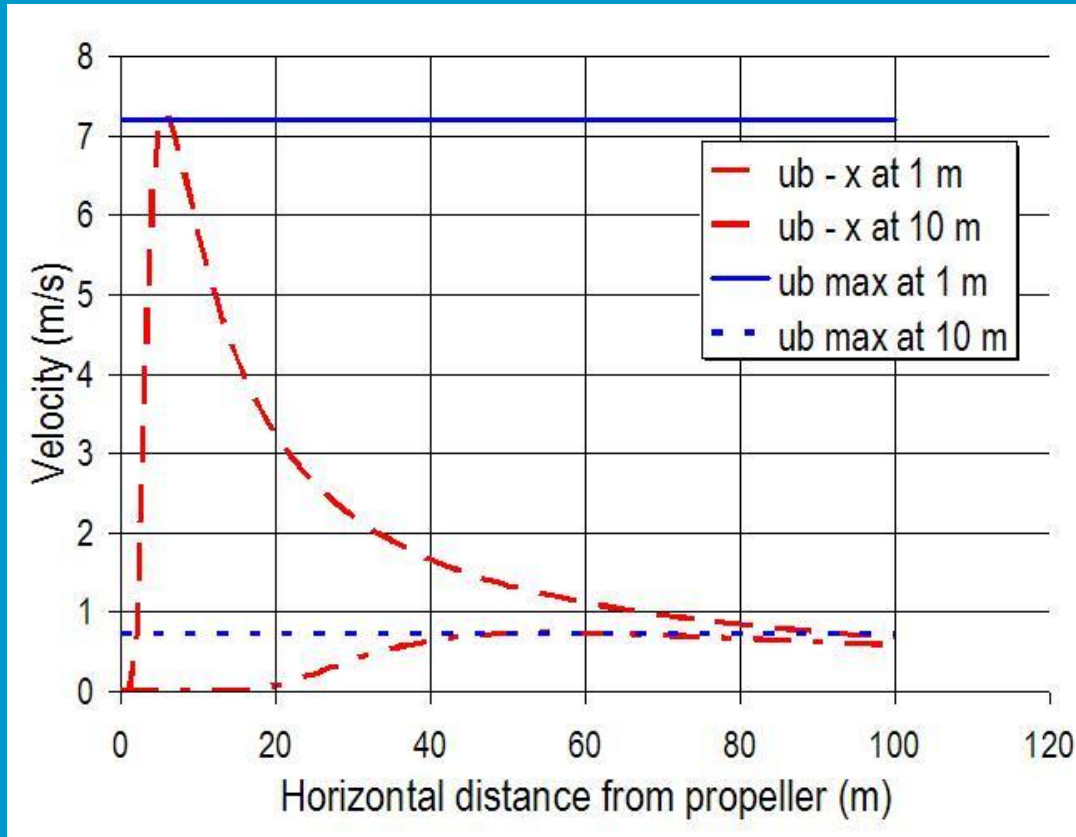
$$\left. \begin{aligned} u_m &= \frac{2.8u_0}{x/d} \\ b &= 0.21x \\ u &= u_m e^{-0.69\left(\frac{r}{b}\right)^2} \end{aligned} \right\} u = \frac{2.8u_0}{x/d} e^{-15.7\left(\frac{r}{x}\right)^2}$$



# velocity distribution in propeller wash and free jets



# velocities behind propeller

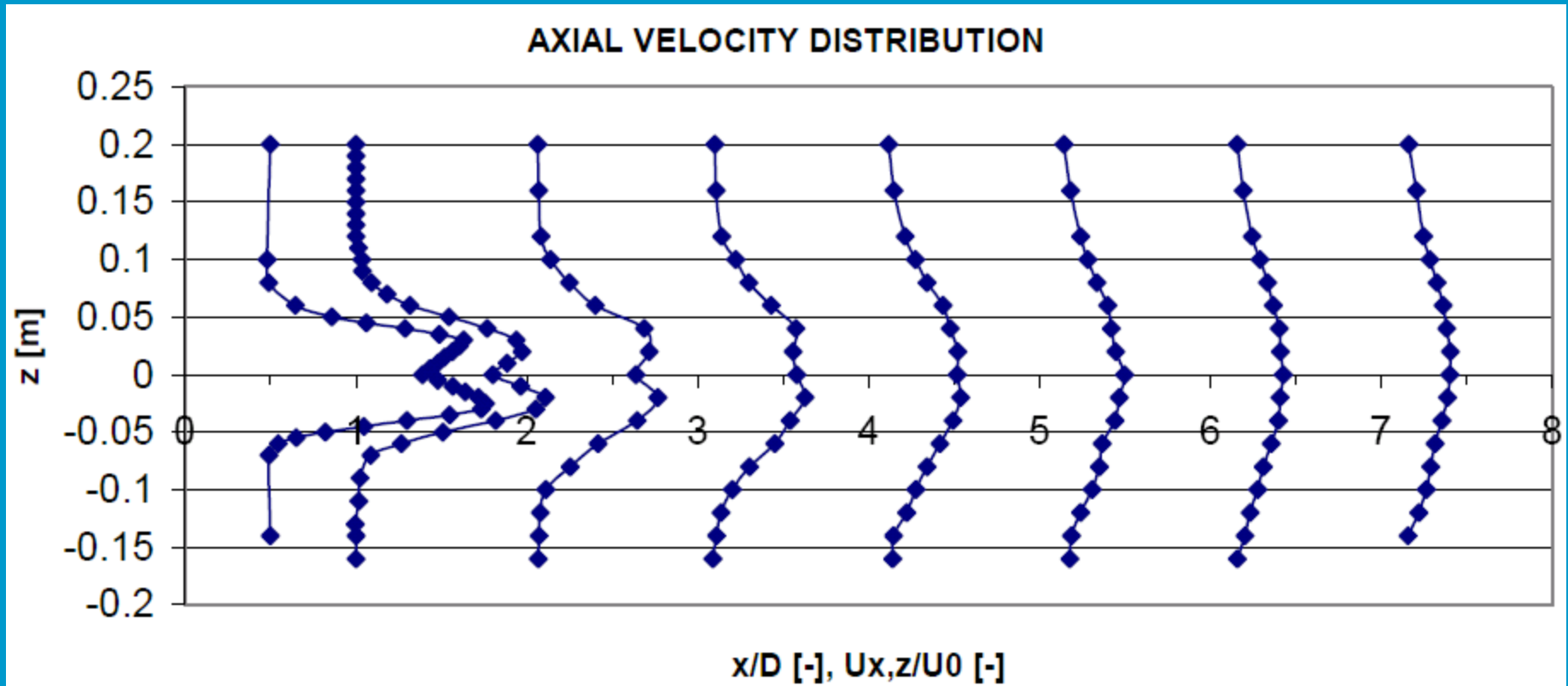


$$u_0 = 1.15 \left( \frac{P}{\rho d^2} \right)^{1/3}$$

$$u_{b-\max} = 0.3u_0 \frac{d}{z_b}$$

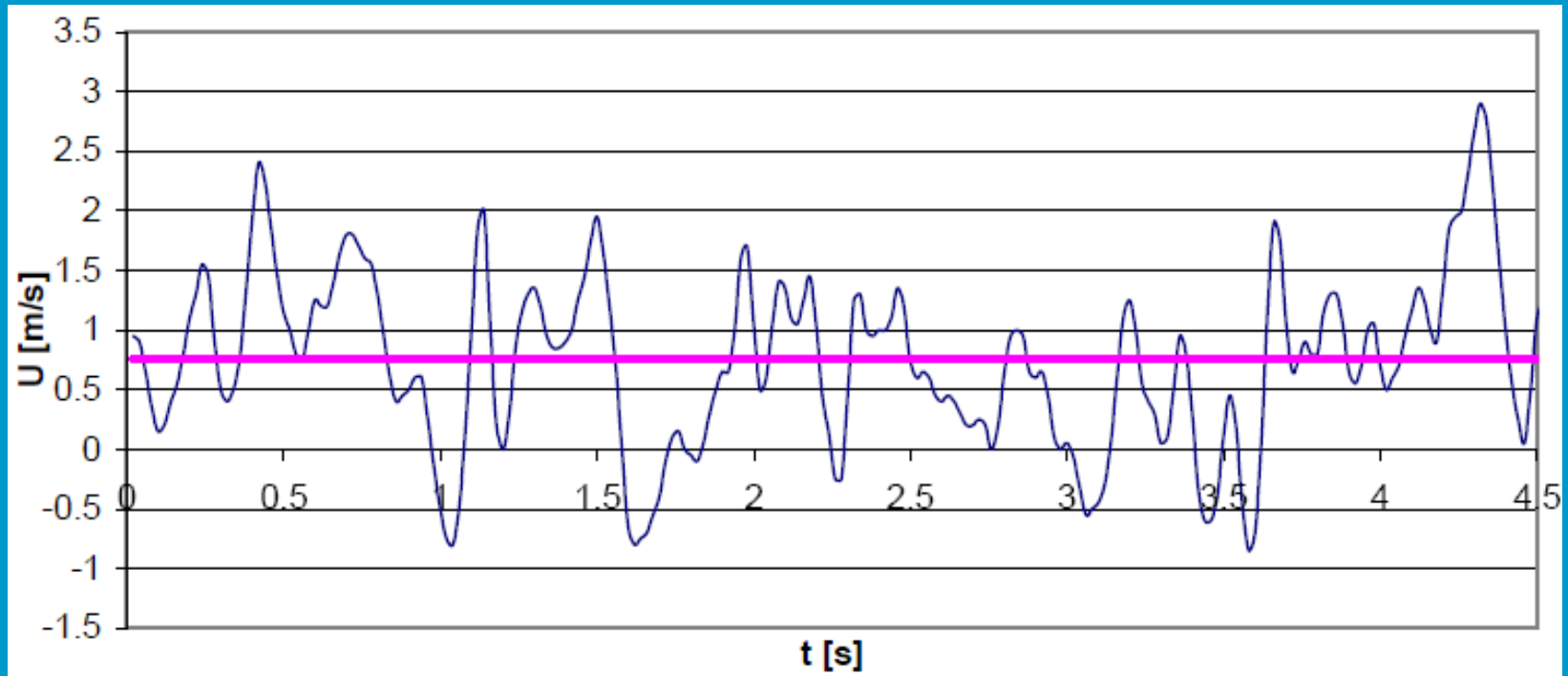
see also section 2.4.2.

# measured flow in a propeller jet



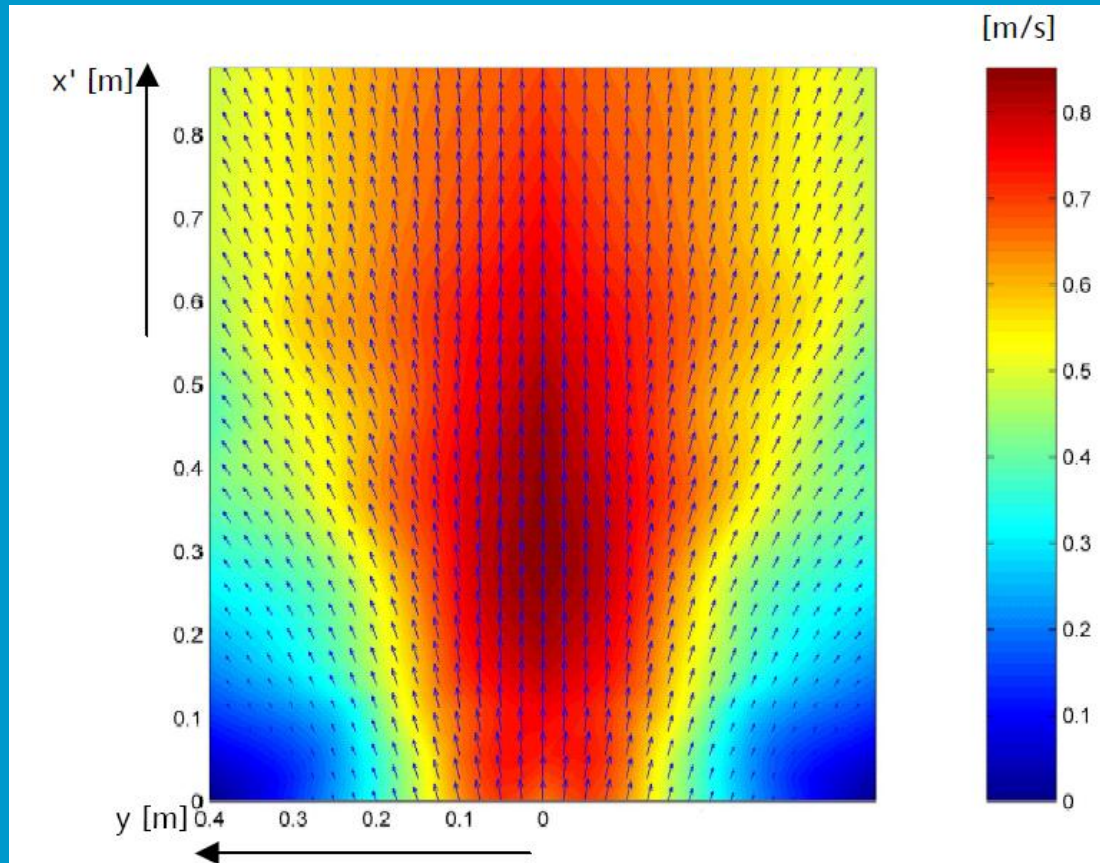
data from thesis Schokkink, 2003

# Turbulence in a propeller jet



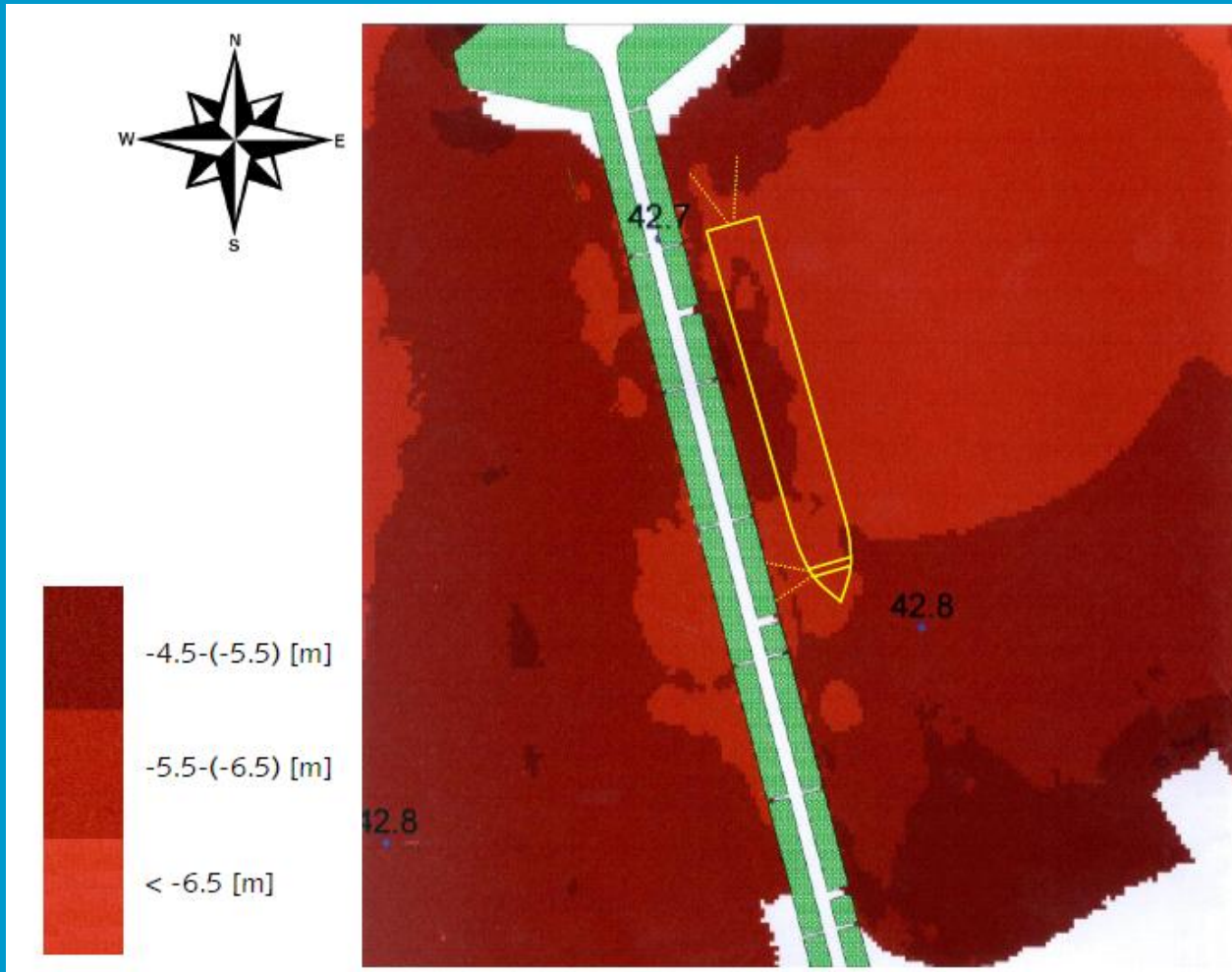
data from thesis Schokkink, 2003

# Flow caused by a propeller on an inclined slope



data from thesis Schokkink, 2003

# erosion due to bowthrusters

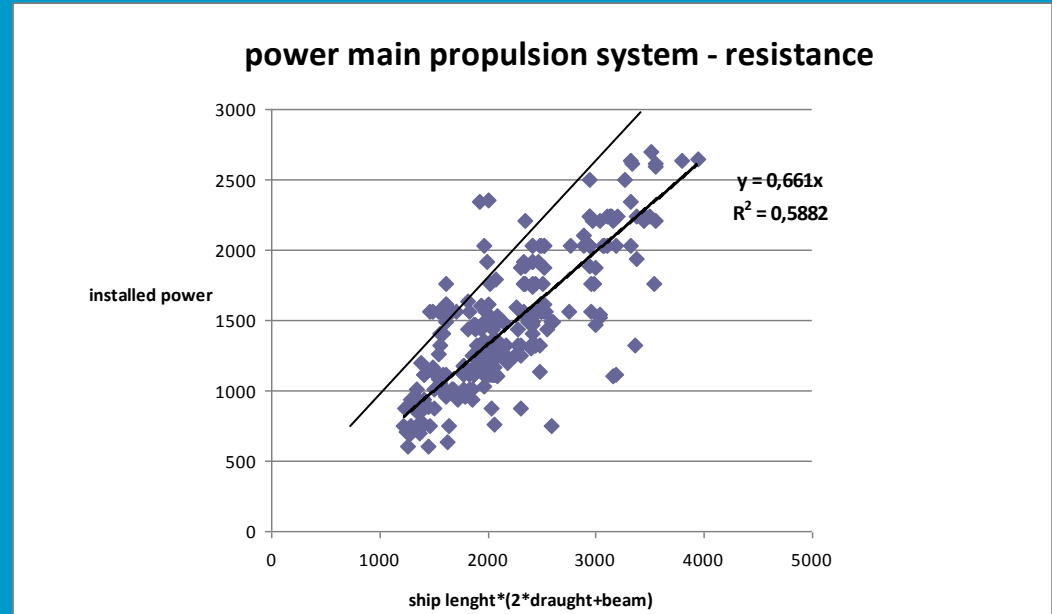


data from thesis Schokkink, 2003  
Plofsluis, Amsterdam Rijn kanaal

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# Ship engines

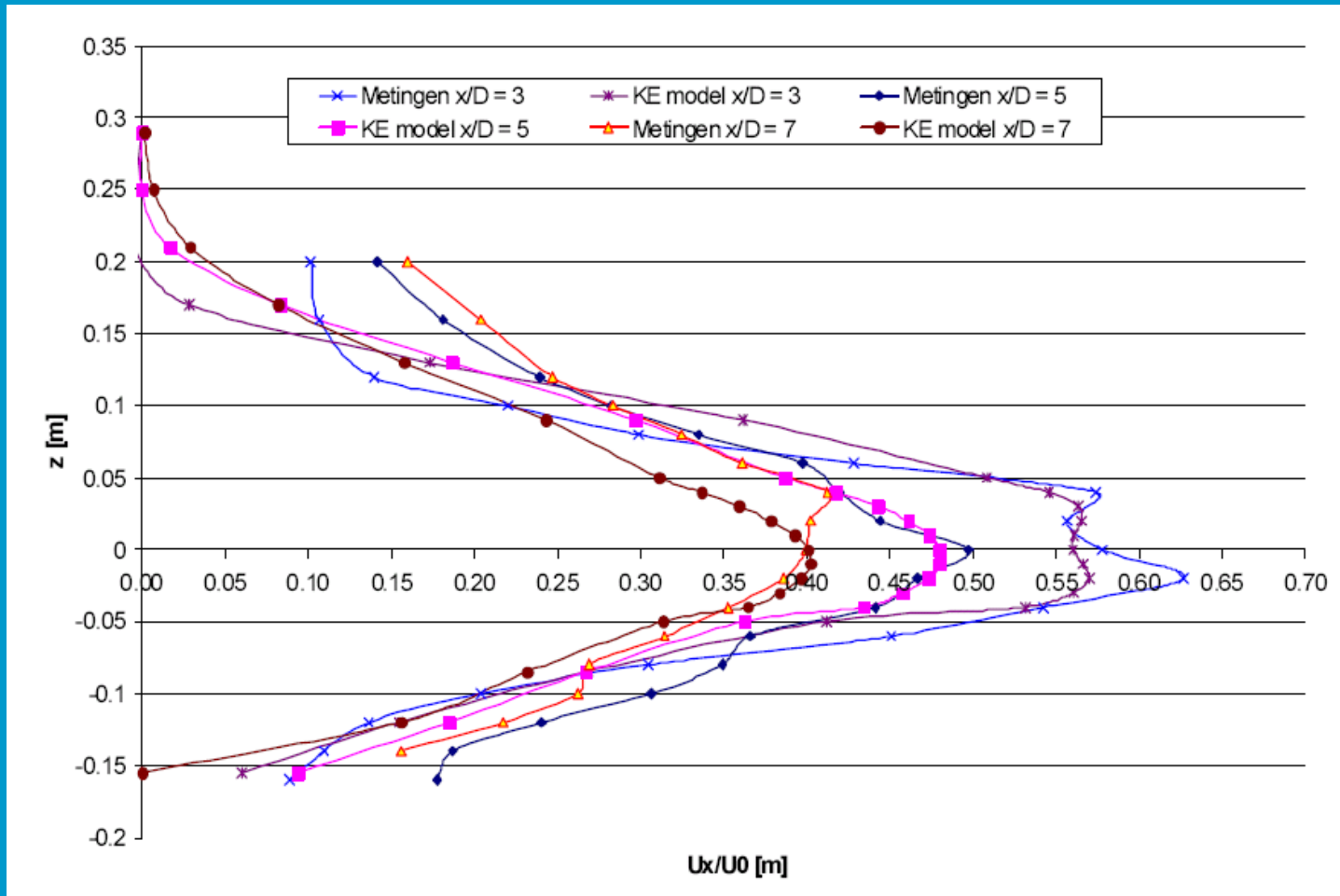


Type of ship	Power of engine (kW)
Small ships	100
Spits	200
Kempenaar	350
Dortmund-Ems Kanal	500
Rhein-Herne Kanal	700
Large Rhine vessel	1400
2 barge pushboat	1500

$$P_{\text{mean}} = 0.66L(2D+B)$$

$$P_{10\%} = 1.25 P_{\text{mean}}$$

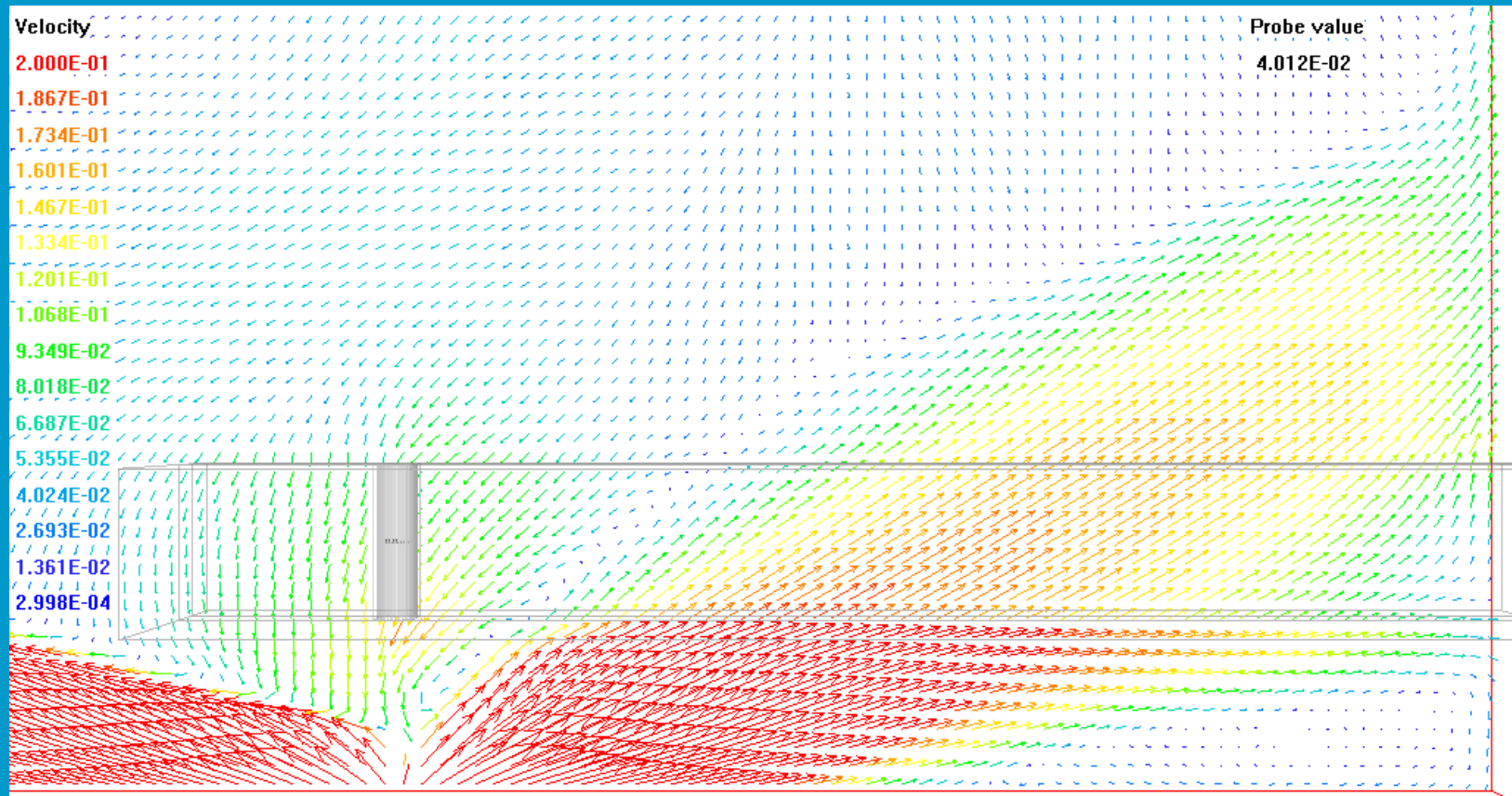
# Simulation of a propeller jet



Model by De Jong [2003], measurements by Schokking [2002]



# Model simulation with Phoenicx



Data from Van der Laan [2005]

# The physical model

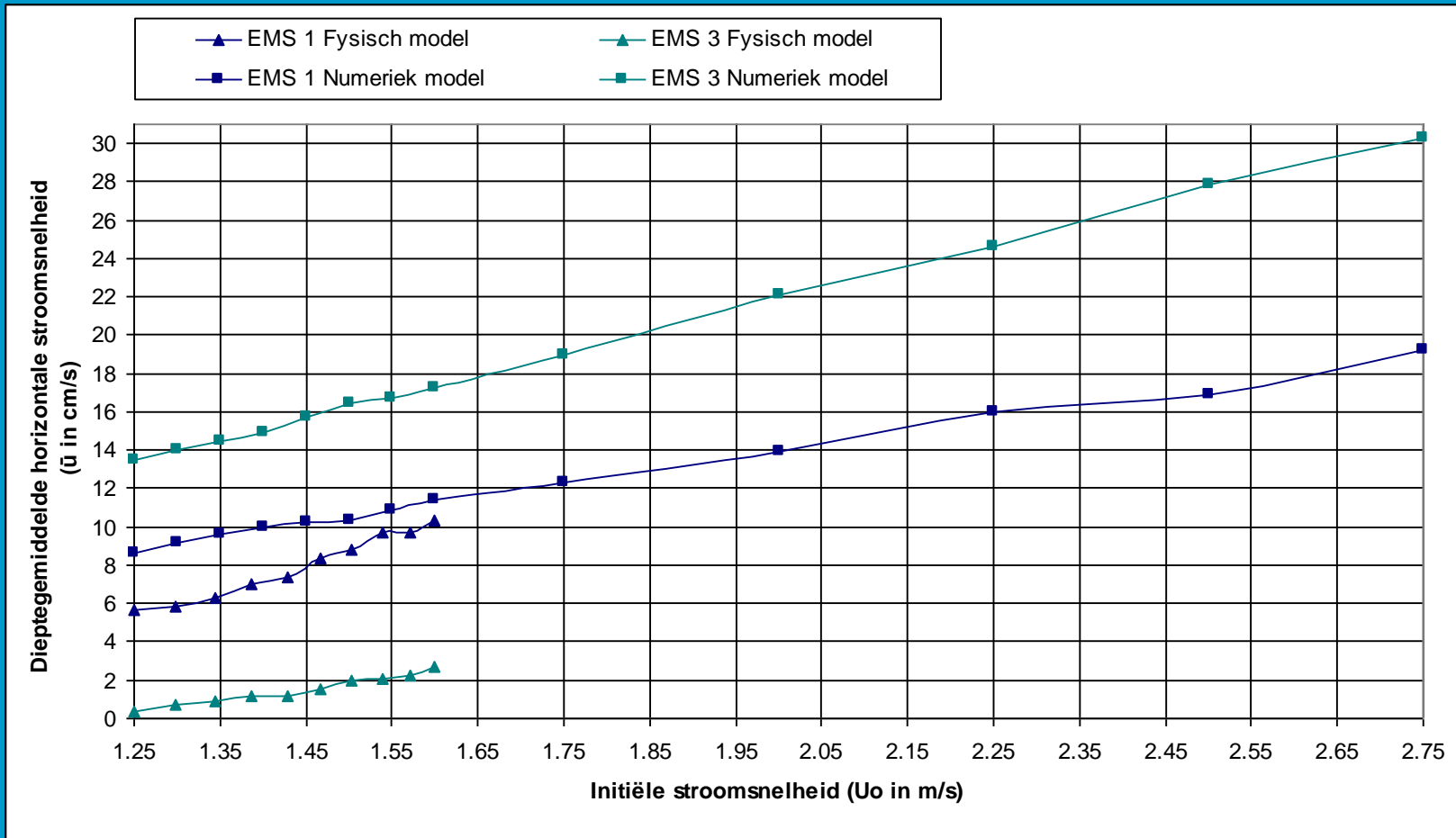


Van der Laan [2005]

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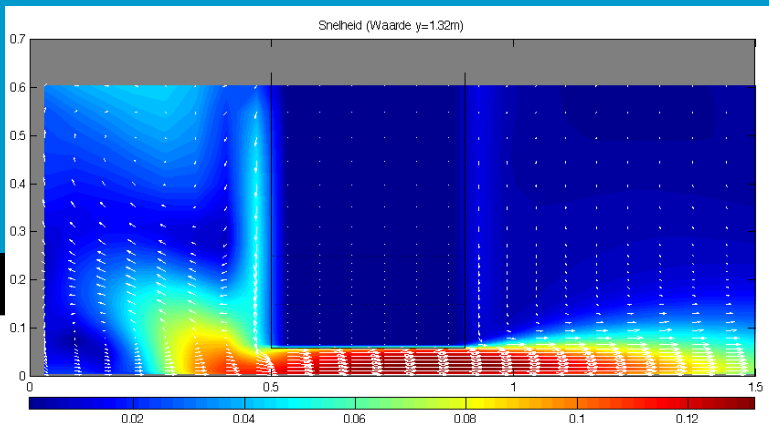
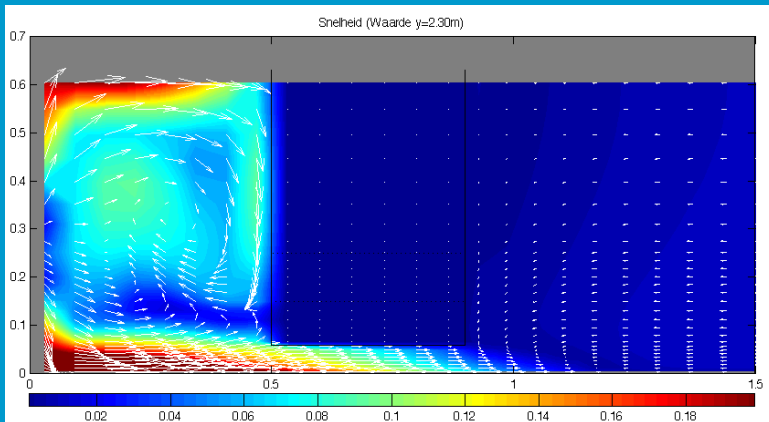
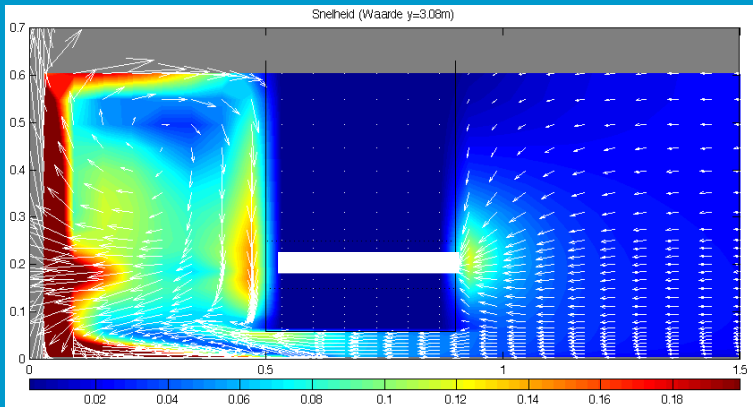
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# Mathematical vs. Physical model



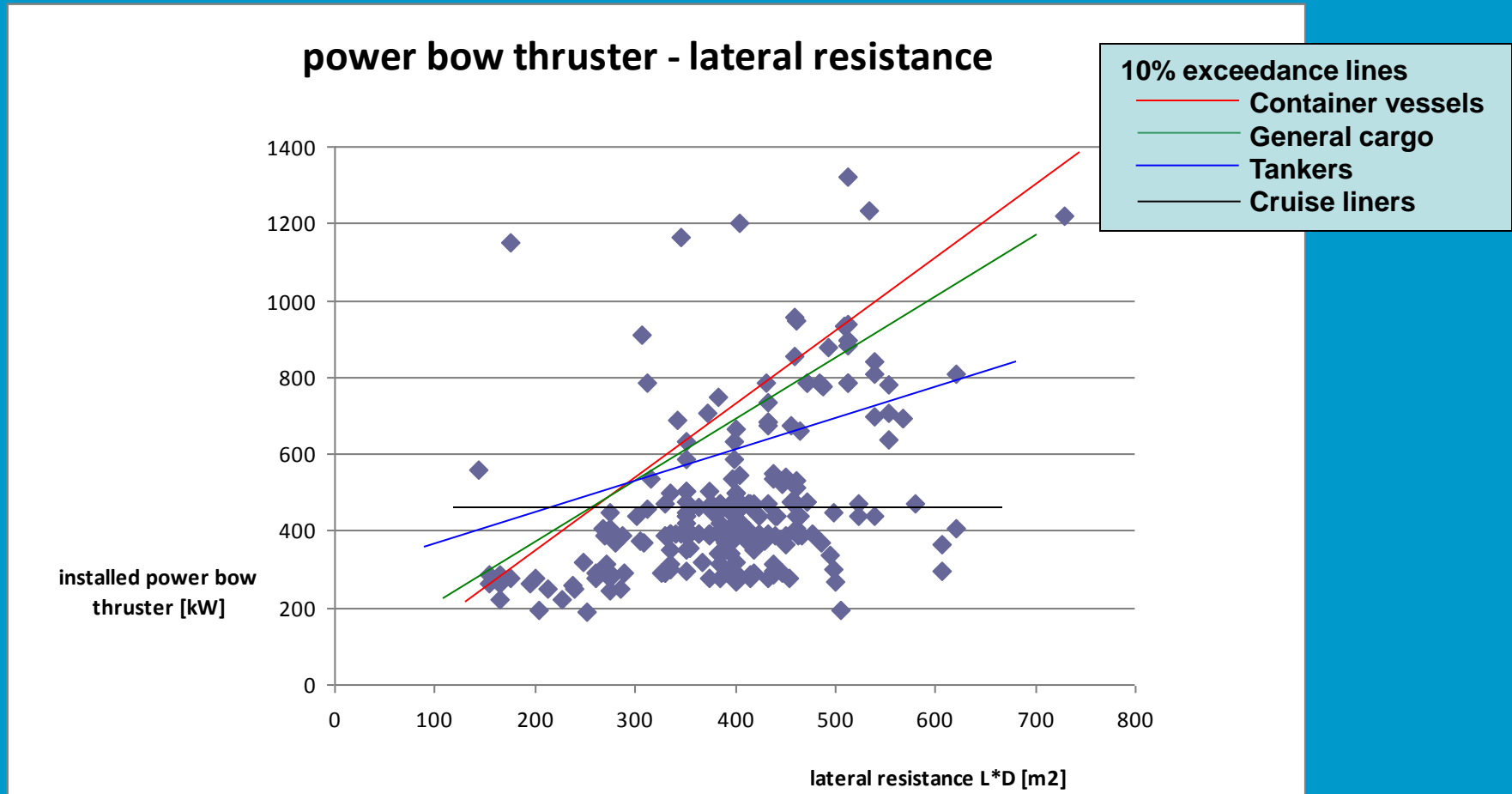
Van der Laan [2005]

# flow under ship



Egbert van Blaaderen, 2006

# Data of all inland vessels - $P_{\text{mean}} = A_1 L D + A_2$



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Data from Verheij (2010)

# stability of bed protection

- important are:
  - return flow
  - stern wave (depression)
  - secondary waves
  - propeller wash
- Relations based on Izbash + experimental data
- Hartelkanaal tests provided good data
  - M1115 1980-1988
  - Q908 1990
- Dipro

# bow thrusters

$$P_d = A_1(LD) + A_2$$

$$D_0 = 0.068P_d^{0.5}$$

$$v_p = 1.15\zeta \left( \frac{P_d}{D_0^2} \right)^{1/3}$$

$$v_b = 1.03v_p \frac{D_0}{z_p}$$

$P_d$  = Power of engine

$L$  = length of ship

$D$  = draught of ship

$D_0$  = diameter of propeller

$v_p$  = velocity behind thruster

$v_b$  = velocity near the bed

$\zeta$  = loss factor = 0.9

$z_p$  = distance propeller axis  
and bottom of channel

The axis of the thruster is  $\alpha D_p$  above the bed, but for  $\alpha$  there is no default given.

# stability (primary waves)

$$\Delta d_{n50} = 1.2 \frac{u_r^2}{2g} \frac{1}{\sqrt{1 - \frac{\sin^2 \alpha}{\sin^2 \phi}}}$$

$$\frac{z_{\max}}{\Delta d_{n50}} = 1.8 \cot \alpha^{0.33}$$



# stability (secondary waves)

$$\frac{H\sqrt{\cos 55^\circ}}{\Delta d_{n50}} = 2.7 \xi^{-0.5} \quad \rightarrow \quad \frac{H}{\Delta d_{n50}} = 3.6 \xi^{-0.5}$$

# stability (propeller wash)

$$\Delta d_{n50} = 2.5 \frac{u_b^2}{2g} \frac{1}{\sqrt{1 - \frac{\sin^2 \alpha}{\sin^2 \phi}}}$$

given: depression = 0.78 m

$$H = 0.27, \quad T = 1.8 \text{ s}$$

$$u_r = 1.17 \text{ m/s} \quad \tan \alpha = 1/3$$

## example (2)

stern wave effect:

$$\frac{z_{\max}}{\Delta d_{n50}} = 1.8 \cot \alpha^{0.33}$$

$$d_{n50} = \frac{0.78}{1.65 * 1.8 * 3^{0.33}} = 0.18 \text{ m}$$

return flow effect:

$$\Delta d_{n50} = 1.2 \frac{u_r^2}{2g} \frac{1}{\sqrt{1 - \frac{\sin^2 \alpha}{\sin^2 \phi}}}$$

$$d_{n50} = \frac{1.2 * 1.17^2}{1.65 * 2 * 9.81 * \sqrt{1 - 0.31^2}} = 0.06 \text{ m}$$

secondary wave effect:

$$\frac{H}{\Delta d_{n50}} = 3.6 \xi^{-0.5}$$

$$d_{n50} = \frac{0.27 \sqrt{\xi}}{1.65 * 3.6} = 0.06 \text{ m}$$

# example (3)

- stern wave dominates problem
- action of stern wave only at waterline
- at deeper water return flow dominates
- at more spacious water bodies secondary waves become dominant

## example (4)

Ship 10 m wide, d3 m draught, 1000 kW engine (1370 hp), propeller diameter 1.4 m, propeller 1.5 m above bed

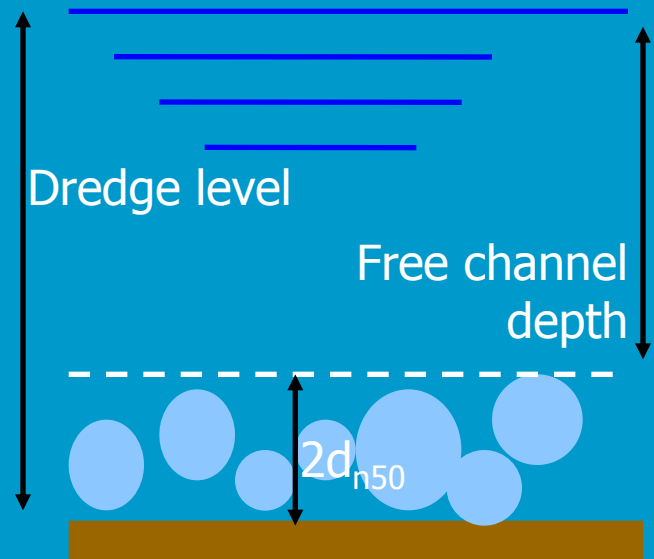
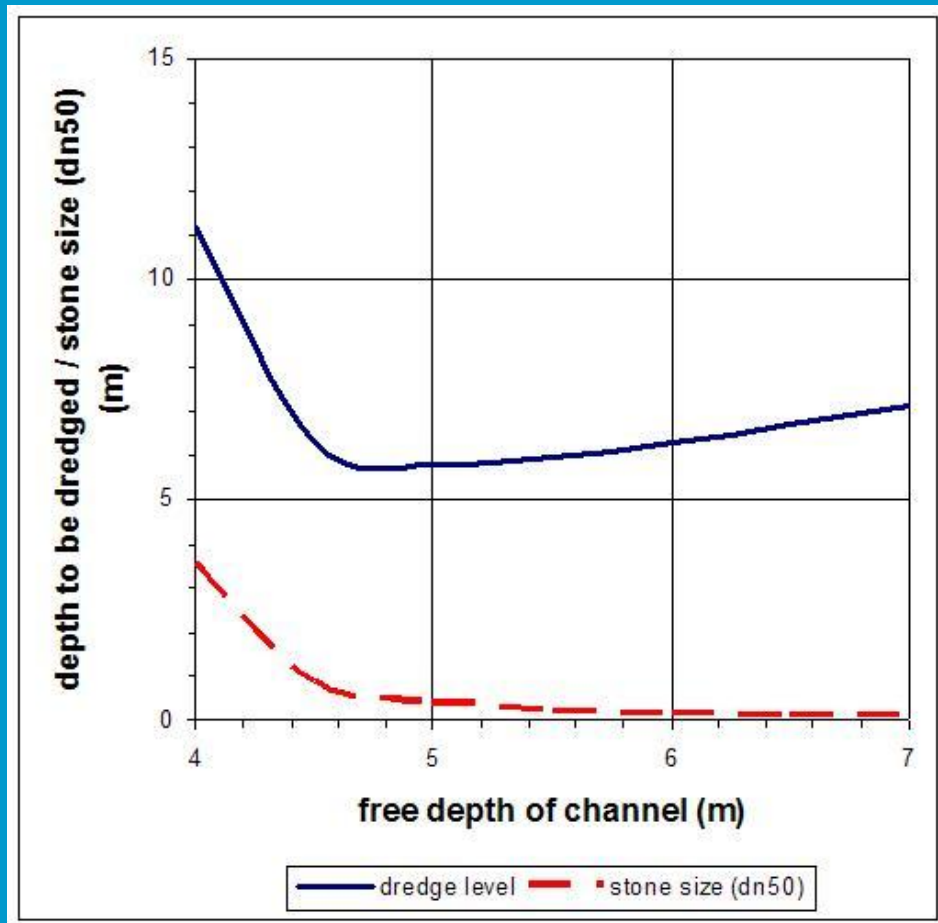
Effective jet = 70% of real diameter, so  $d = 1$  m

$$u_0 = 1.15 \left( \frac{P}{\rho d^2} \right)^{1/3} \qquad u_0 = 1.15 \left( \frac{10^6}{1000 * 1^2} \right)^{0.33} = 11.2 \text{ m/s}$$

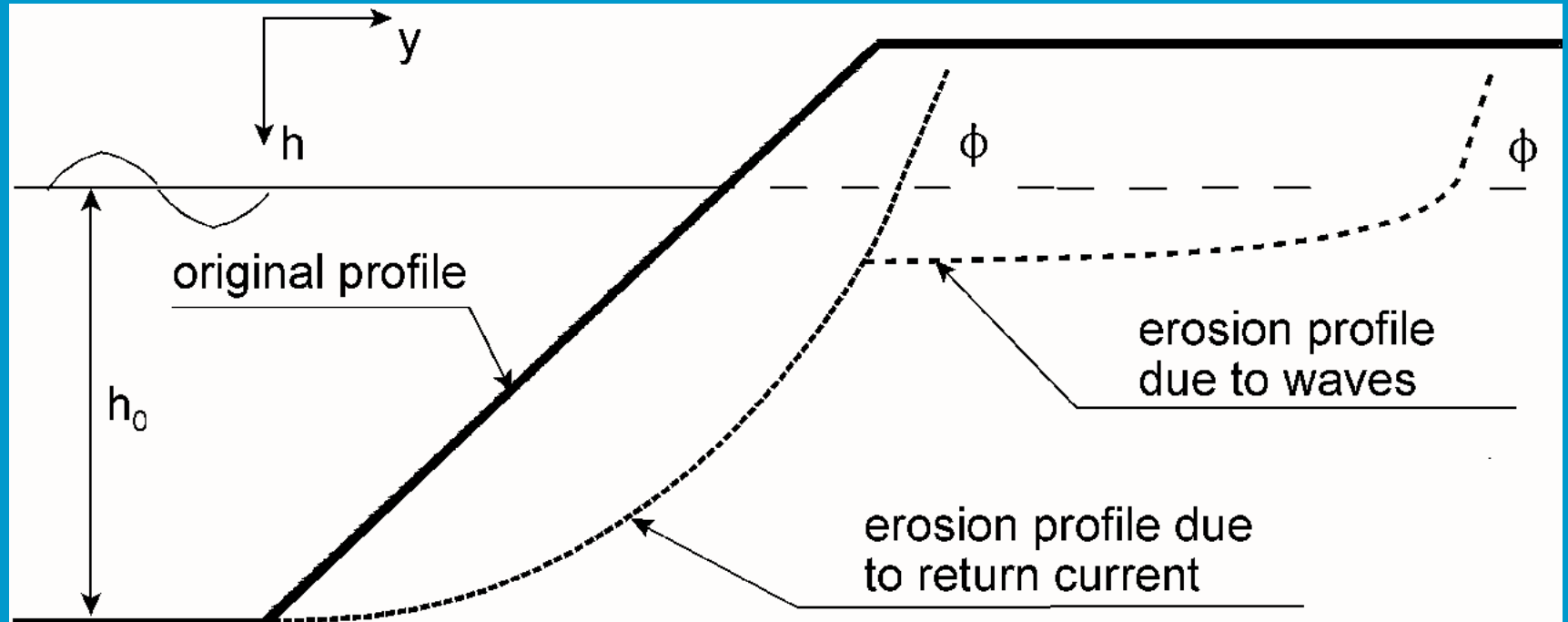
$$u_{b-\max} = 0.3u_0 \frac{d}{z_b} \qquad u_b = 0.3 * 11.2 \frac{1}{1.5} = 2.25 \text{ m/s}$$

$$\Delta d_{n50} = 2.5 \frac{u_b^2}{2g} \frac{1}{\sqrt{1 - \frac{\sin^2 \alpha}{\sin^2 \phi}}} \qquad d_{n50} = \frac{2.5 * 2.25^2}{1.65 * 9.8} = 0.4 \text{ m (60/300kg)}$$

# Optimal depth of a channel

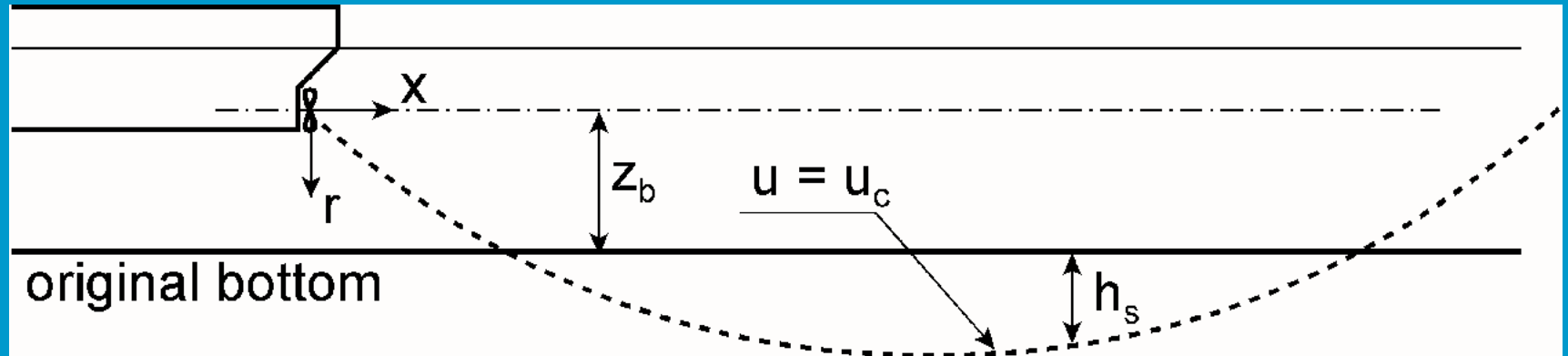


# erosion



$$h = h_0 \cos \left( \tan(\phi) \frac{y}{h_0} \right)$$

# bed erosion due to propeller wash



$$h_s = x \sqrt{\frac{-\ln\left(\frac{u_c x}{5.6 u_0 d}\right)}{15.7}} - z_b$$



# Dipro - Cress

