

# Flow, loads

## Chapter 2

### ct4310 Bed, Bank and Shoreline protection

H.J. Verhagen

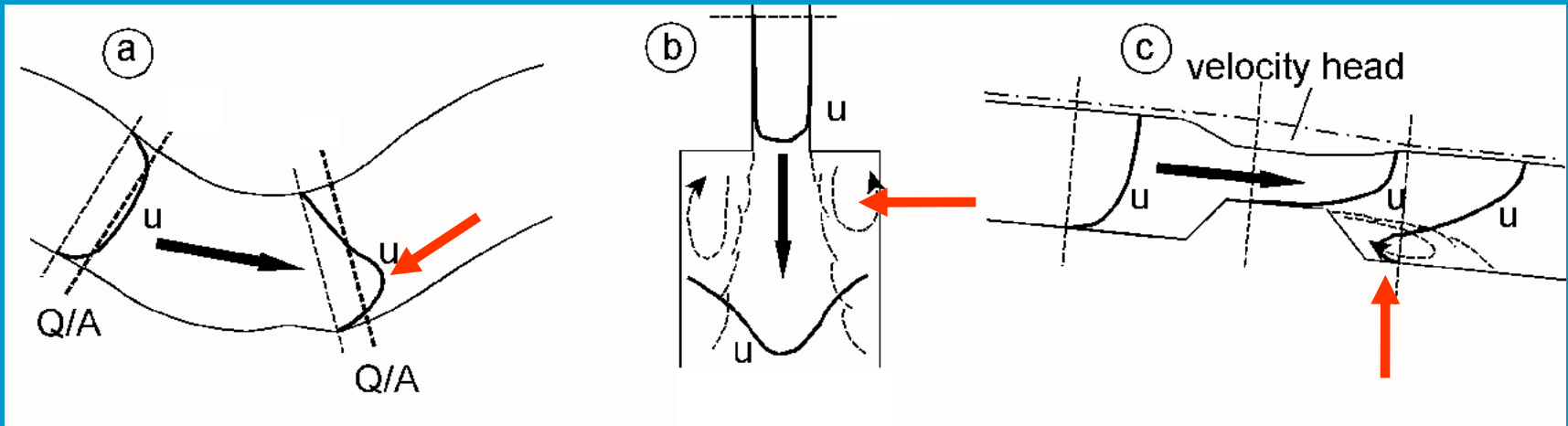
5 November 2009

1

# Introduction

- we have forces on protection elements
- forces are caused by flow
- flow can be regular and fluctuating
- fluctuations can be in the order of:
  - hours                      tide
  - seconds                     short waves
  - milliseconds                turbulence

# velocity fields in various situations



# Demonstration Reynolds number

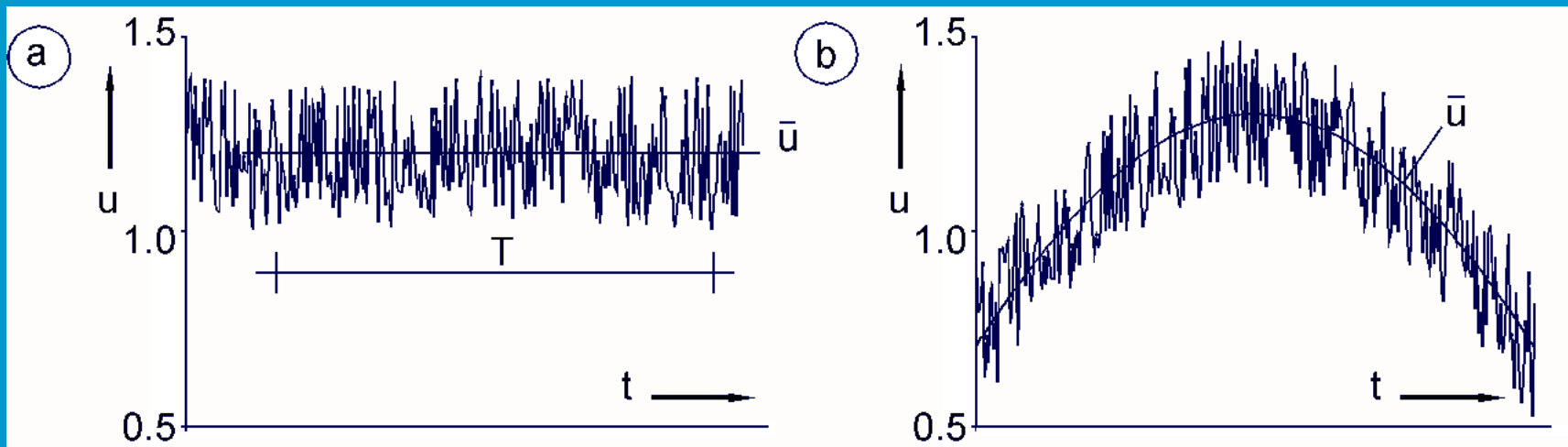
Flume with  
uniform flow  
velocity is approx.  
0.5 m/s

turbulent in case  $Re > 2000$

$$Re = \frac{u \rho D}{\mu}$$



# velocity registration in turbulent flow



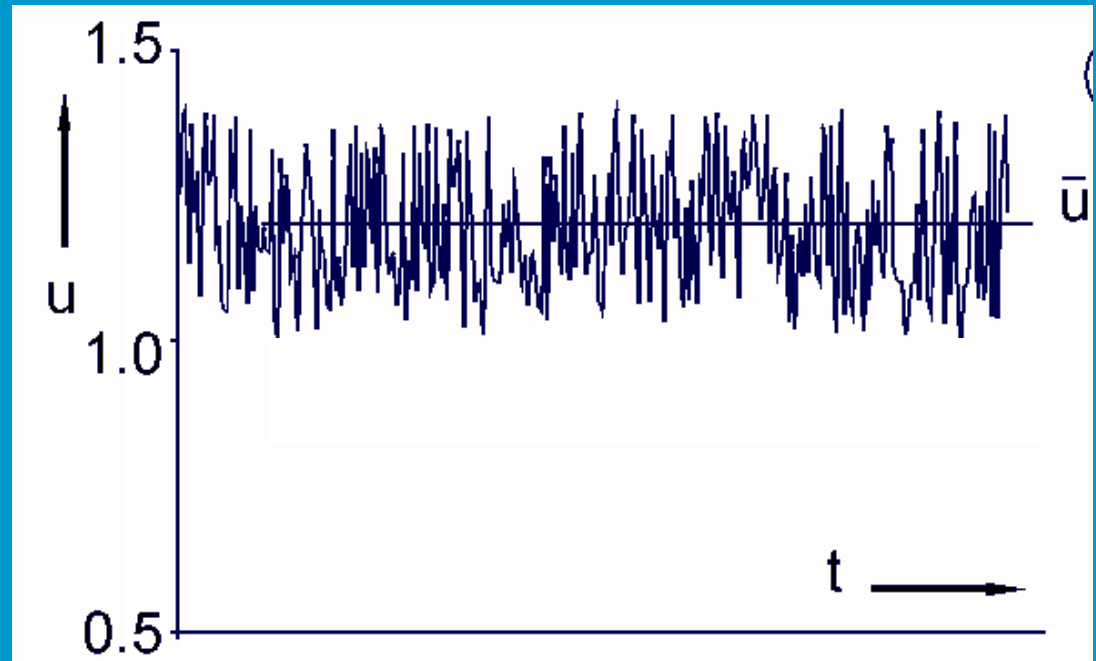
# turbulent variations

$$u = \bar{u} + u'$$

$$v = \bar{v} + v'$$

$$w = \bar{w} + w'$$

$$p = \bar{p} + p'$$



# how to express turbulence ?

$$k = \frac{1}{2} \left( \overline{u'^2} + \overline{v'^2} + \overline{w'^2} \right)$$

$k$  is the total kinetic energy in turbulent flow

$$r_u = \frac{\sqrt{\overline{u'^2}}}{\overline{u}}, \quad r_v = \frac{\sqrt{\overline{v'^2}}}{\overline{u}}, \quad r_w = \frac{\sqrt{\overline{w'^2}}}{\overline{u}}$$

$r$  is relative fluctuation intensity in turbulent flow



# Reynolds stresses

$$m^* \quad a \quad = \quad F$$

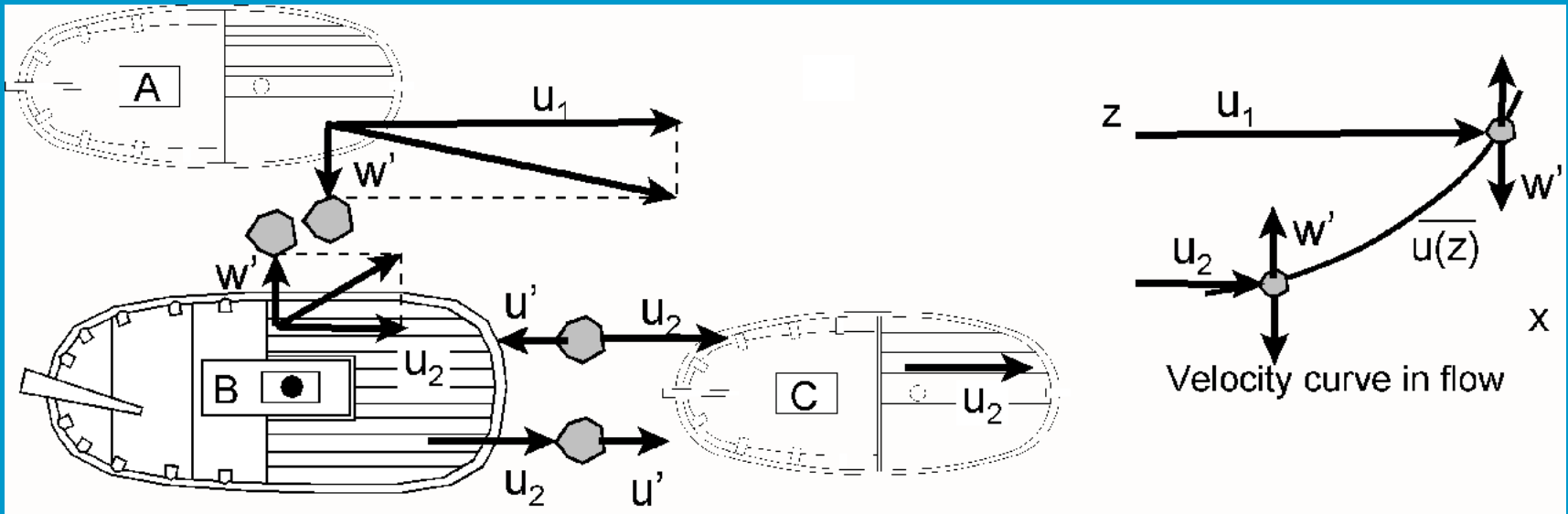
$$\rho \left( \frac{\partial \bar{u}}{\partial t} + \bar{u} \frac{\partial \bar{u}}{\partial x} + \bar{w} \frac{\partial \bar{u}}{\partial z} \right) = - \frac{\partial \bar{p}}{\partial x} + \mu \frac{\partial^2 \bar{u}}{\partial z^2} - \rho \left( \frac{\partial \overline{u'^2}}{\partial x} + \frac{\partial \overline{u'w'}}{\partial z} \right)$$

inertia
press.
visc.
Reynolds stresses

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mean values
turb. fluctuations

# exchange of momentum

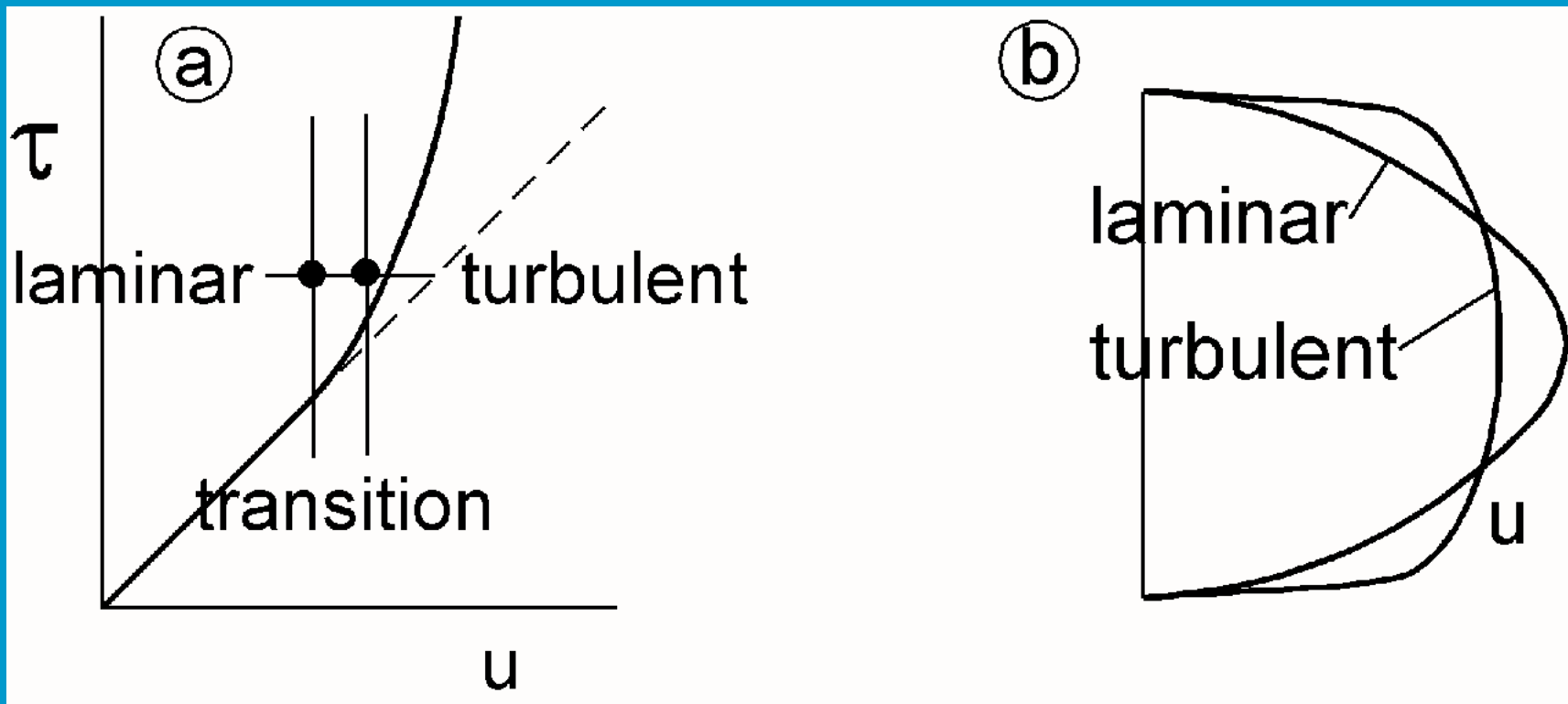


# Flow resistance

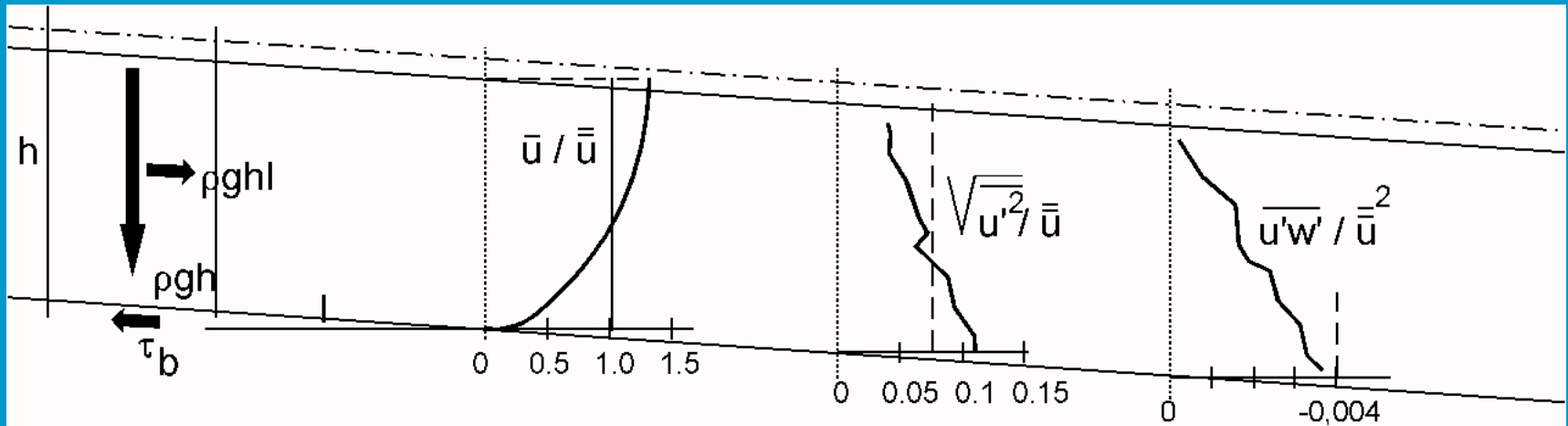
$$\tau = c_f \rho u^2$$

**In turbulent flow quadratic terms become dominant and relation between  $\tau$  and  $u$  becomes quadratic**

# resistance in laminar and turbulent flow



# uniform wall flow



# wall flow

$$\tau_b = \rho g h I = c_f \rho \bar{u}^2 (= \rho u_*^2 = \rho \overline{u'_b w'_b}) \Rightarrow \bar{u} = \frac{1}{\sqrt{c_f}} \sqrt{g h I}$$

$u_*$  is the shear “velocity”

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Chezy:  $\bar{u} = C \sqrt{R I}$  with:  $C = \sqrt{\frac{g}{c_f}}$

Manning:  $\bar{u} = \frac{1}{n} R^{2/3} \sqrt{I}$  with:  $n = R^{1/6} \sqrt{\frac{c_f}{g}}$

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Nikuradse-Colebrook roughness:

$$C = \frac{\sqrt{g}}{\kappa} \ln \frac{12 R}{k_r} \approx 18 \log \frac{12 R}{k_r} \quad (k_r \text{ is equivalent roughness})$$

$$u_* = \bar{u} \sqrt{g / C}$$

# Cress

## Coastal and River Engineering Support System

- Simple program to solve hydraulic engineering equations
- Downloadable from:  
<http://www.cress.nl>
  - English, Spanish and Dutch
  - extended help
  - focus on dikes and related structures
- Requires Administrator rights for installation
- Also available on citg-network (?)



## Coastal and River Engineering Support System

A cooperation project of the Netherlands Ministry of Public Works (Rijkswaterstaat), IHE-Delft and TU-Delft



### Introduction

This program is intended as a support for design and planning of coastal and river projects and is not intended to replace the judgement of a qualified engineer on a particular project. The contents of CRESS are not to be used for advertising, publication or promotional purposes. Citation of trade names does not constitute an official endorsement or approval of the use of such commercial products. The issuing partners do not accept liability for interpretations or implementations made by users of this program.

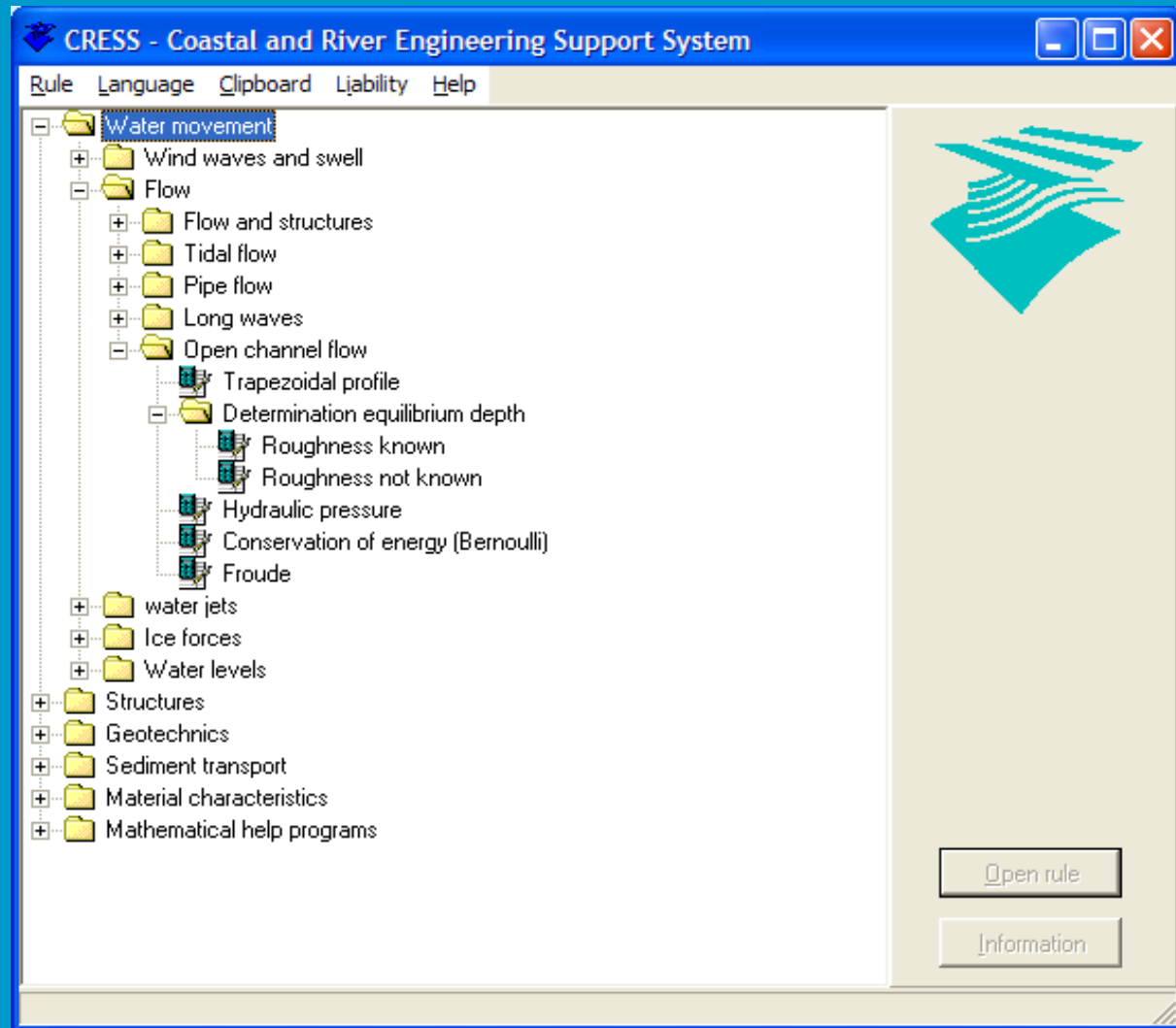
				<p><a href="#">Latest Cress version (RWS-Cress)</a>, (version 4.0.5) in English, Dutch, French and Spanish. This version contains extensive help. For installation administrator rights are required (installation includes a registration procedure of the dll's in the registry of your computer).          The French version is only available as test version. To activate the French version, download <a href="#">menu.zip</a> and replace the files in your directory .../cress/menu by the files from this zipfile.</p>
	<p><a href="#">Seperate link to helpfiles of Cress (RWS-Cress)</a></p>			
	<p><a href="#">Download IHE-version of Cress</a> (old version, does not require writing in the registry of your computer)          Remark: Help in program does not work any more. <a href="#">Download</a> separate helpfiles.</p>			
	<p><a href="#">Chinese version of Cress (IHE-Cress)</a></p>			
	<p><a href="#">DOS-version of Cress</a></p>			
	<p><a href="#">DOS-ersion of Cress in Bahasa Indonesia</a></p>			
<p>Older versions of Cress (windows):</p> <ul style="list-style-type: none"> <li>• <a href="#">Cress 2007</a></li> <li>• <a href="#">Cress 2005</a></li> <li>• <a href="#">Cress 2004</a></li> </ul>				

In case of problems, you may consult the [faq-list](#).

Cress is not able to compute the shallow water wave parameters  $T_{m-1,0}$  and  $H_{2\%}$ , because then you need to enter depth profile information. These parameters can be calculated with Swan. The full Swan code can be downloaded from the [Swan-homepage](#). However, also a practical Graphical User Interface, SwanOne is available free of charge. With the use of [SwanOne](#) you may calculate  $T_{m-1,0}$  and  $H_{2\%}$  without detailed knowledge of the Swan computational system.



# Cress (3)



# example

## Cress

Given: discharge  $q=20 \text{ m}^3/\text{s}$   
bed slope  $i=1/1000$

channel width  $b_b=10 \text{ m}$   
roughness  $0.2 \text{ m}$

side slope  
vertical  $m=0$

calculate  $h$  and  $u$

assume  $h=1$

$$R = bh / (b + 2h) = 0.83$$

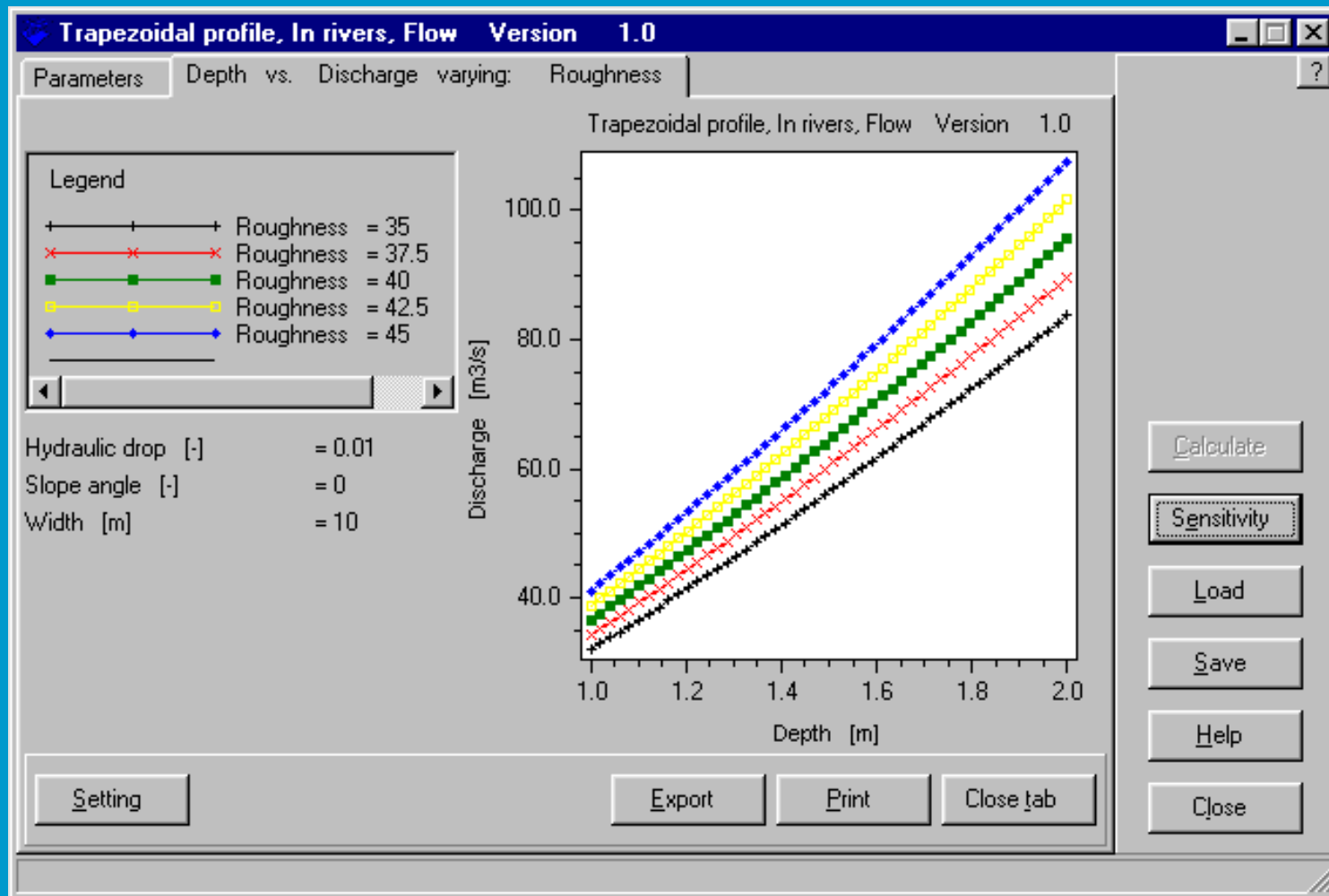
$$C = 18 \log(12 * 0.83 / 0.2) \\ = 30.6$$

$$Q = bh C \sqrt{Ri} \\ = 10 * 1 * 30 * \sqrt{0.3 * .001} \\ = 8.83 \text{ m}^3/\text{s} \\ \Rightarrow \text{too low, increase } d$$

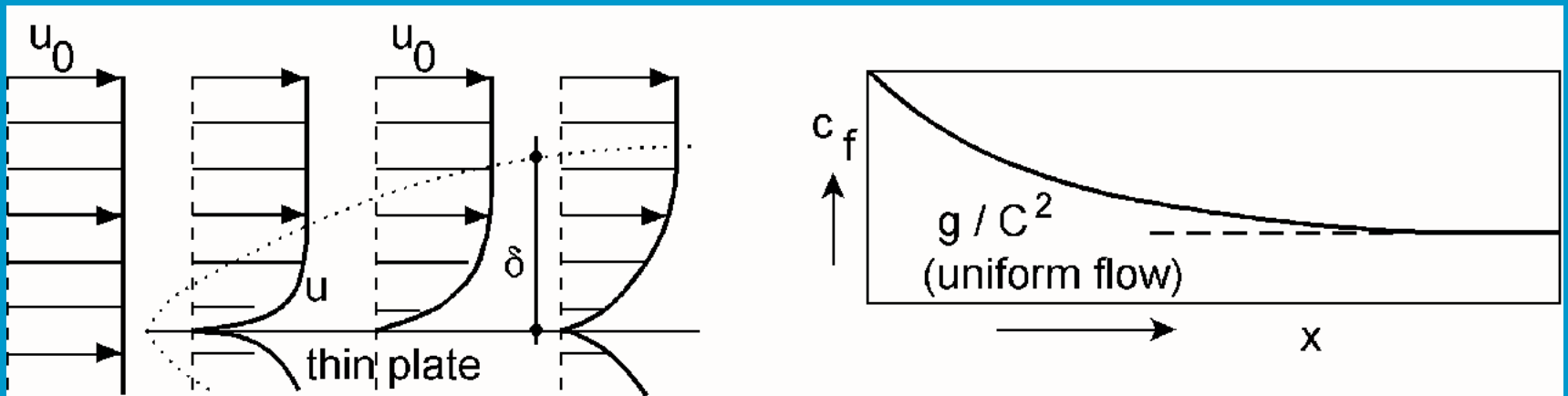
Input		Output	
<input type="radio"/> m	0.00	u	3.49 m/s
<input type="radio"/> h	1.00 m	R	0.83 m
<input type="radio"/> $b_b$	10.00 m	A	10.00 $\text{m}^2$
<input type="radio"/> i	0.01		
<input type="radio"/> C	38.2 $\text{m}^{1/2}/\text{s}$		
<input checked="" type="radio"/> Q	34.87 $\text{m}^3/\text{s}$		

Buttons: Calculate, Sensitivity, Load, Save, Help, Close

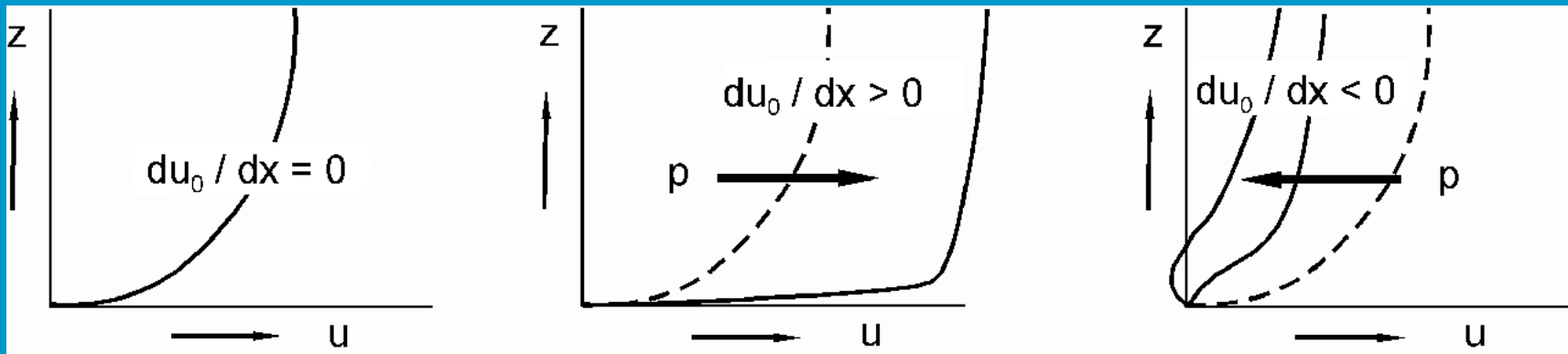
# output of program



# growth of boundary layer



# influence of pressure gradient on velocity profile

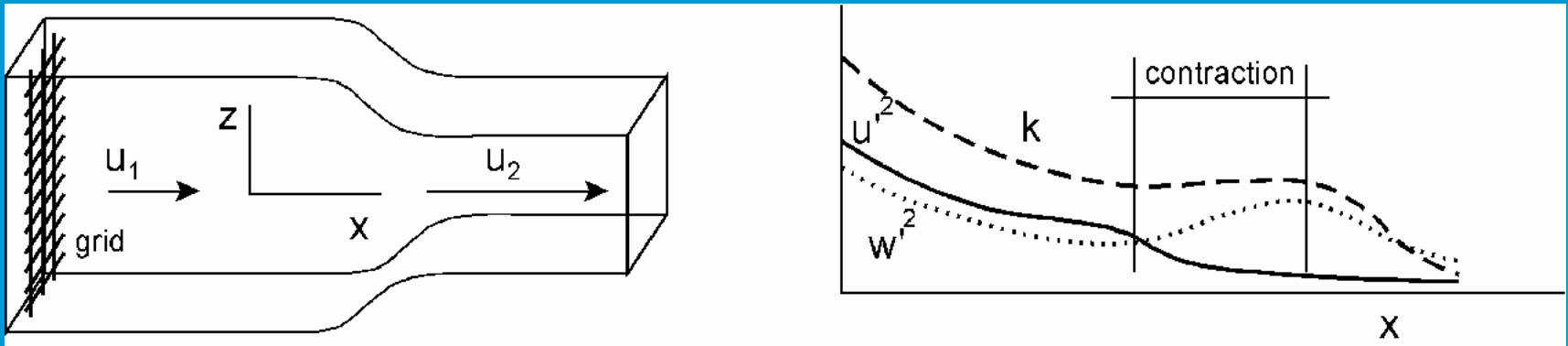


uniform

accelerated

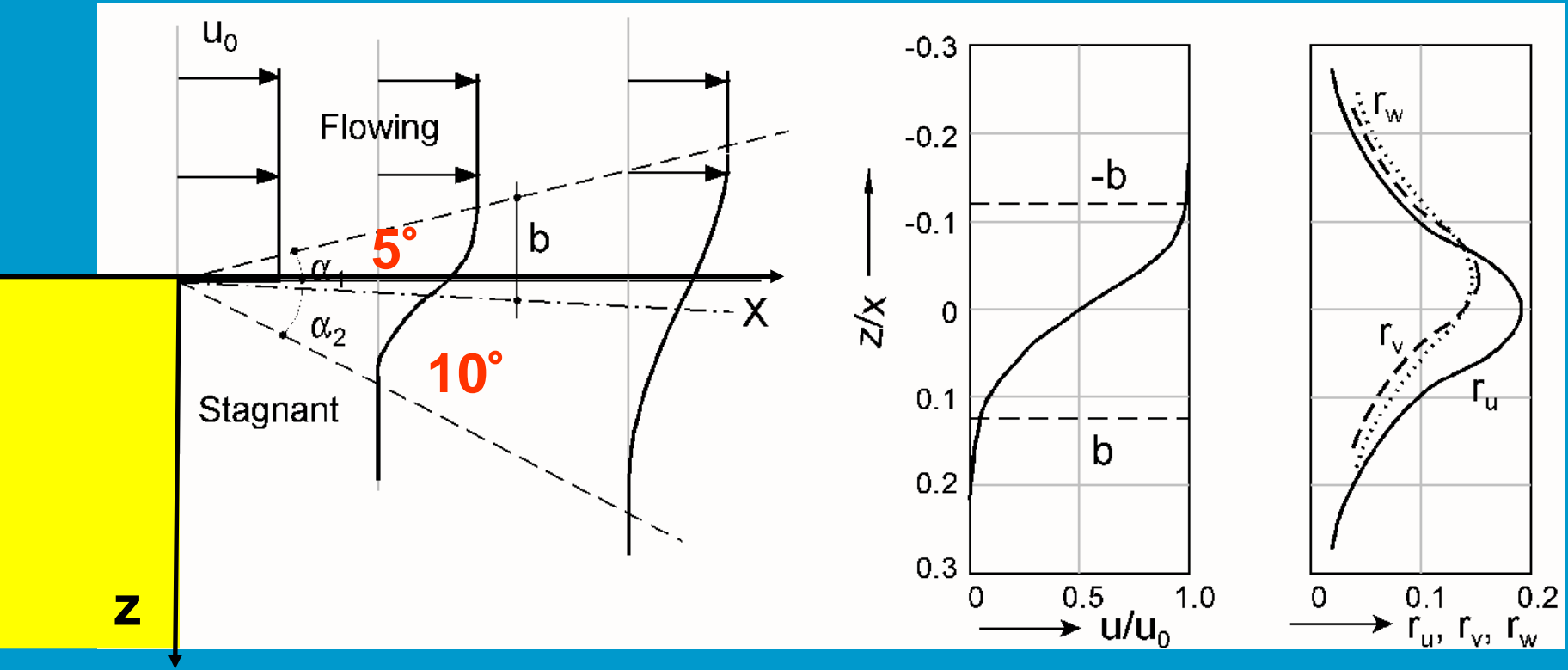
decelerated

# turbulence in windtunnel contraction



the fluctuations in x-direction decrease due to acceleration

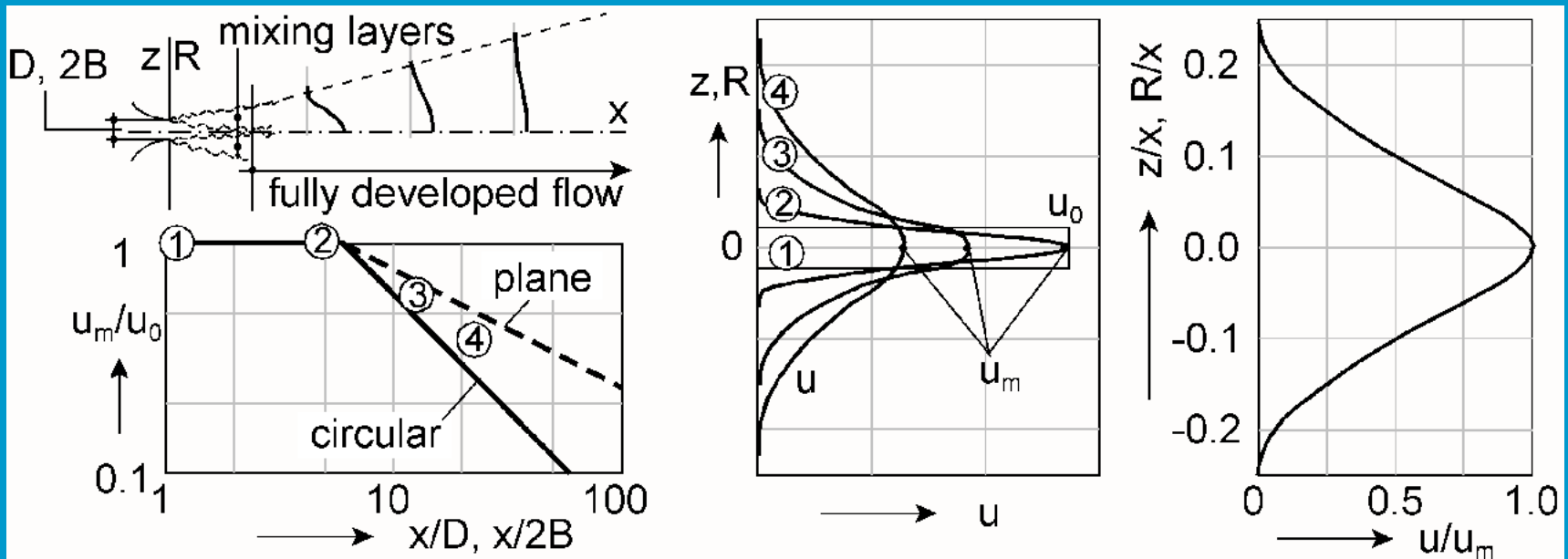
# flow, velocities and turbulence in mixing layer



ct4310/01overzichtstroming  
BB: 4310V2-MixingZone



# flow and velocities in jets



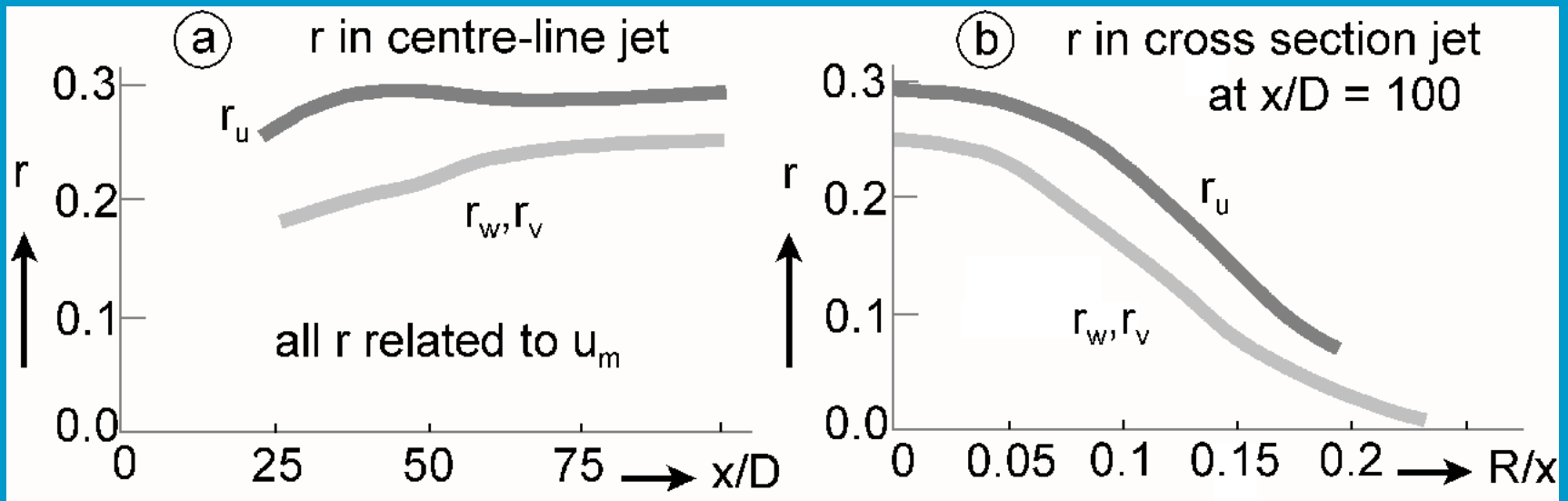


# jet equations

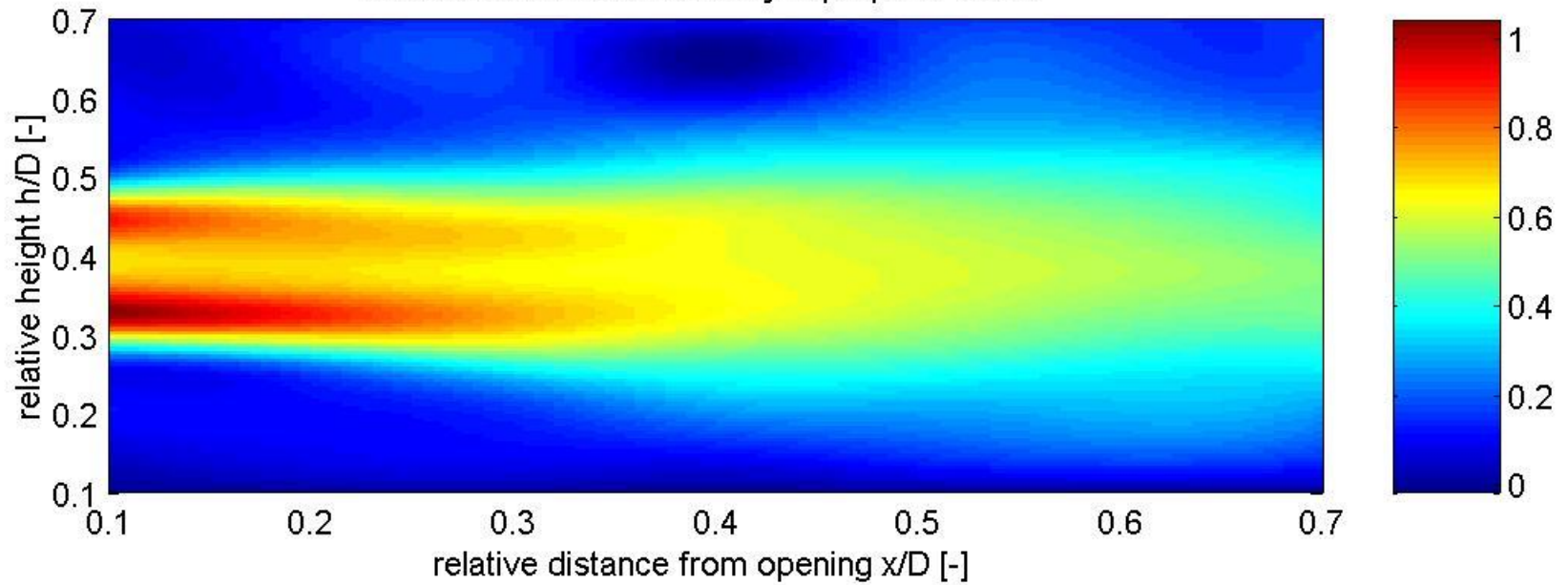
$$\text{Plane jets : } u_m = \frac{3.5 u_0}{\sqrt{x/B}} \quad b = 0.1 x \quad u = u_m e^{\left(-0.693 \left(\frac{z}{b}\right)^2\right)}$$

$$\text{Circular jets : } u_m = \frac{6.3 u_0}{x/D} \quad b = 0.1 x \quad u = u_m e^{\left(-0.693 \left(\frac{R}{b}\right)^2\right)}$$

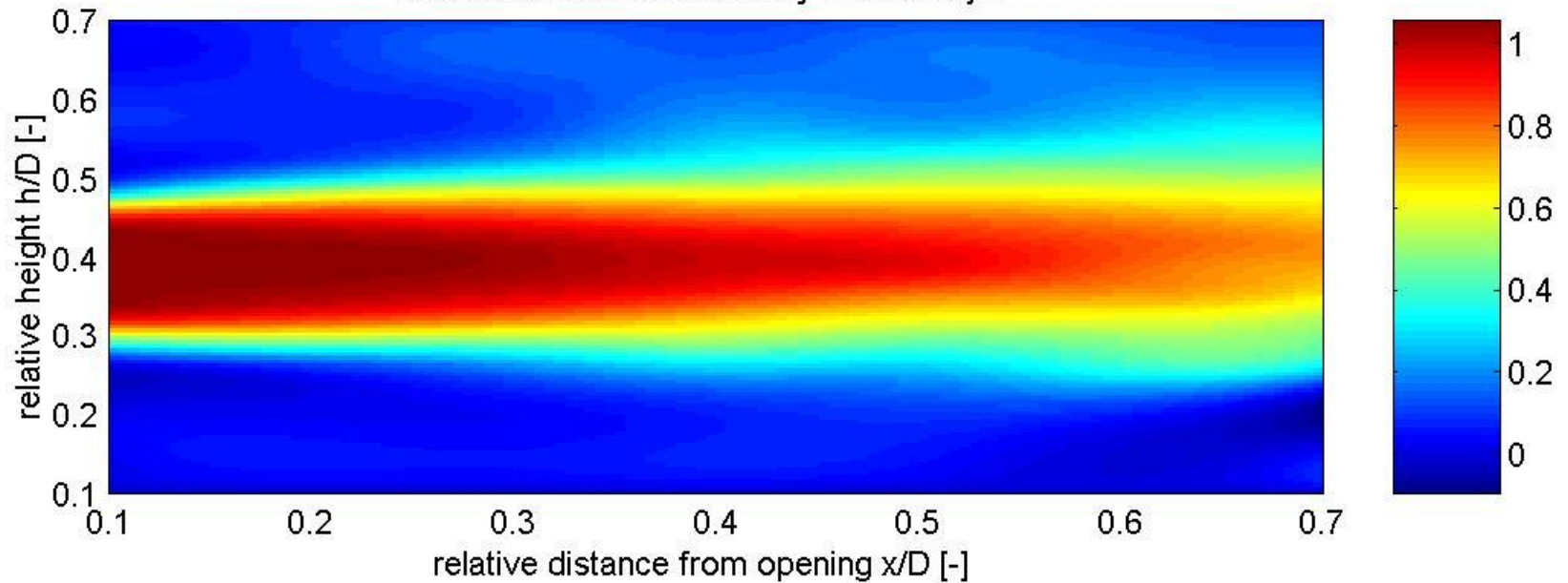
# turbulent fluctuations in circular jet



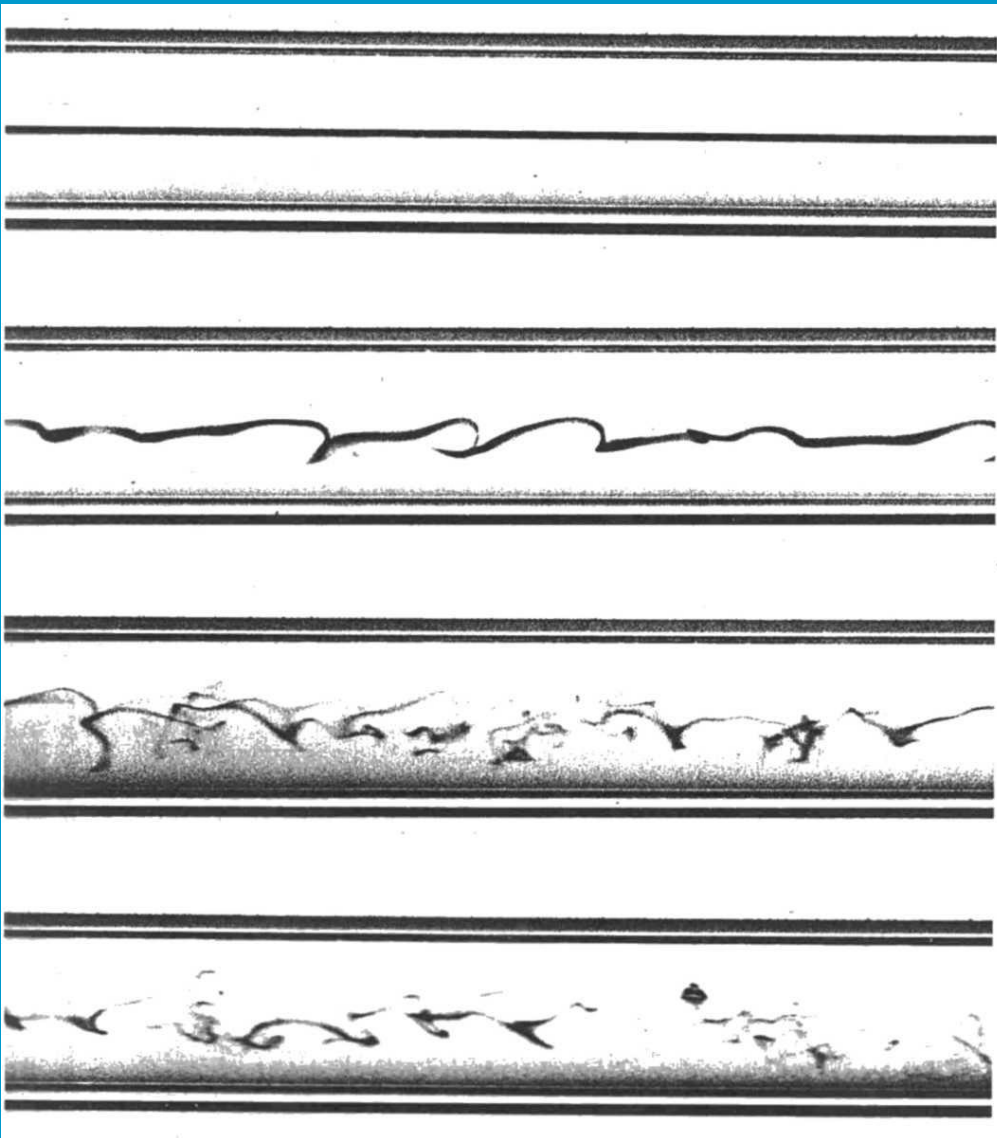
Relative streamwise velocity in propeller wash



Relative streamwise velocity in circular jet



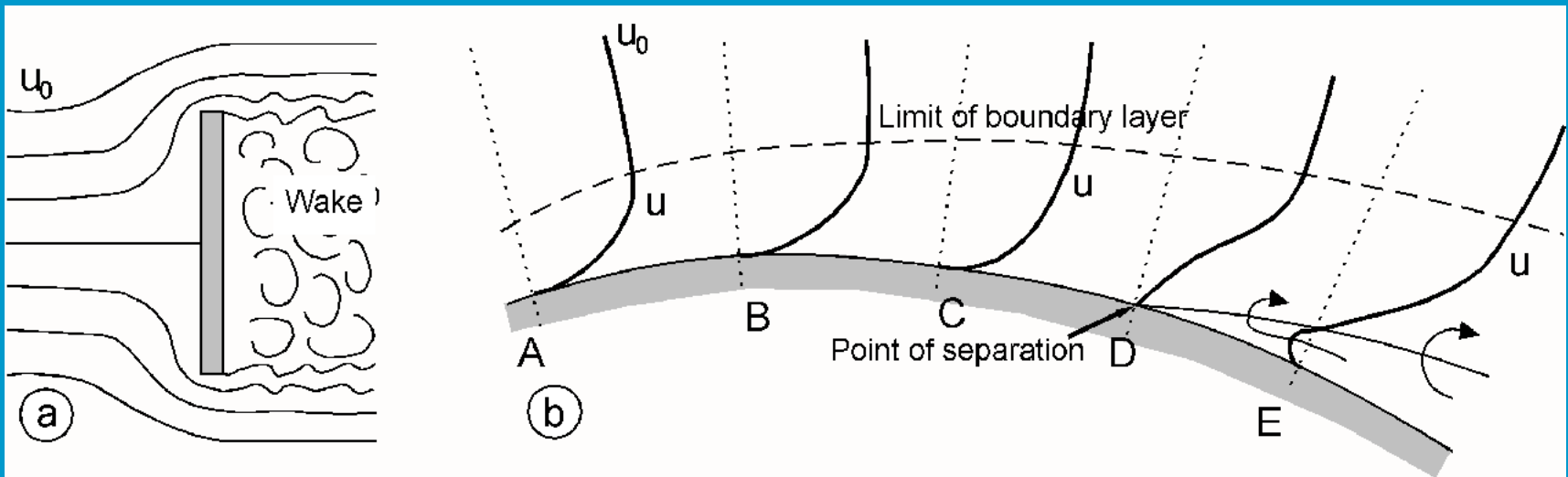
# Reynolds dye experiment



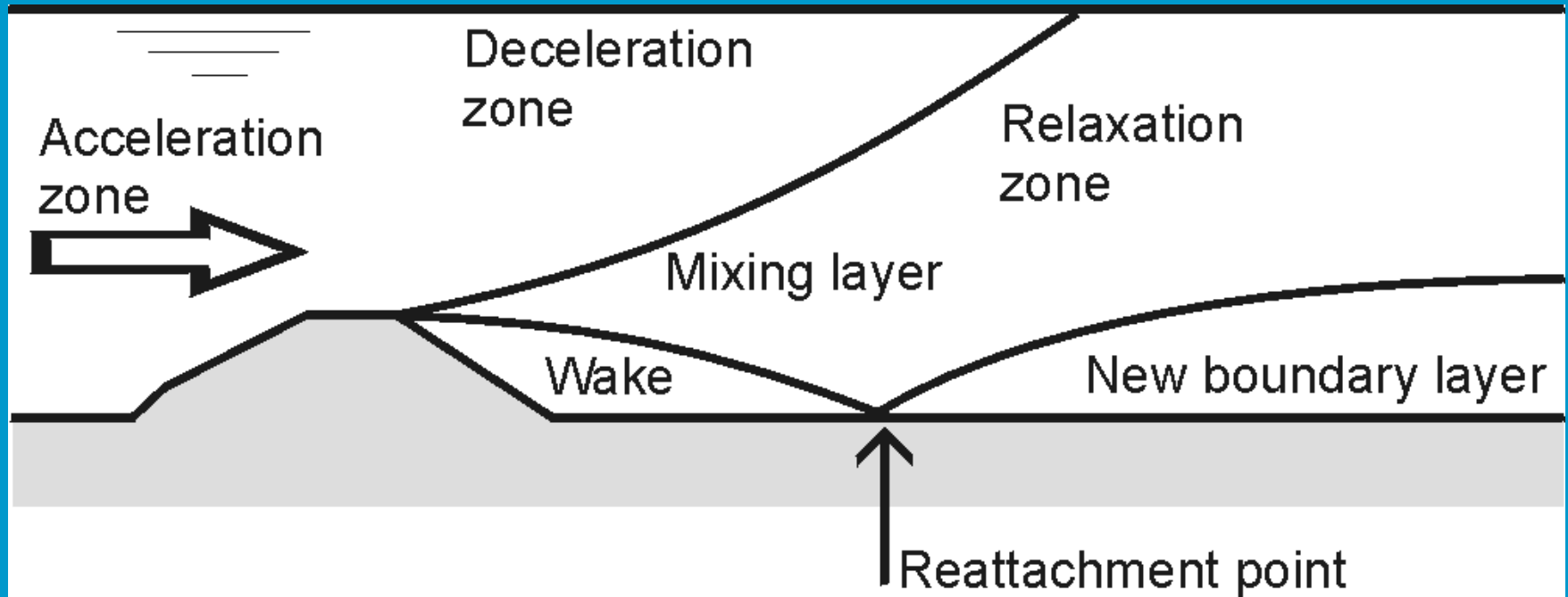
# Video on Turbulence

- Presented by Robert W Stuart  
University of British Columbia
- Produced by the national committee for fluid  
mechanics films, national science foundations
- Downloadable from:  
<http://web.mit.edu/fluids/www/Shapiro/ncfmf.html>

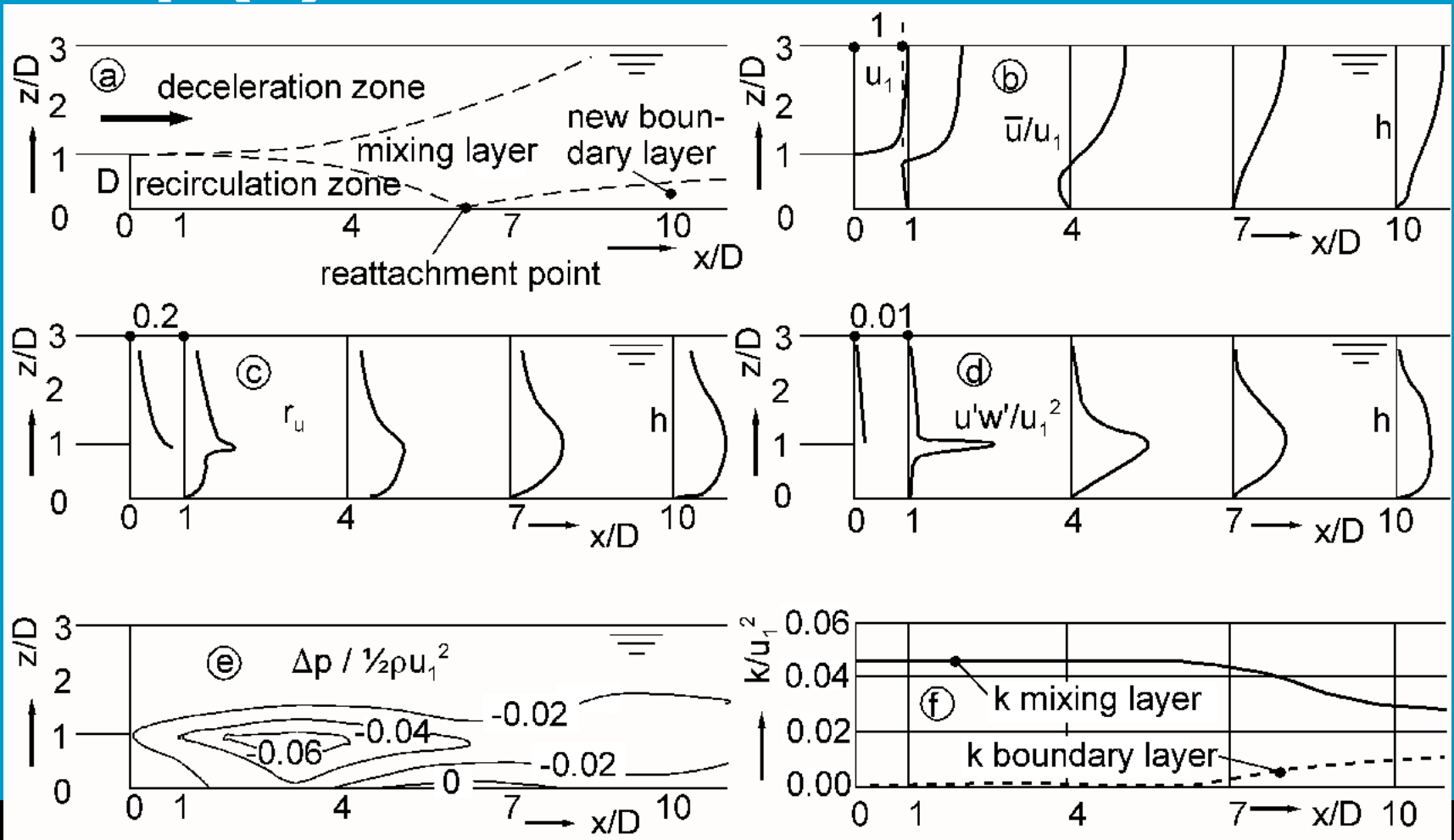
# flow separation around blunt and round body



# flow phenomena in backwater-facing step (1)

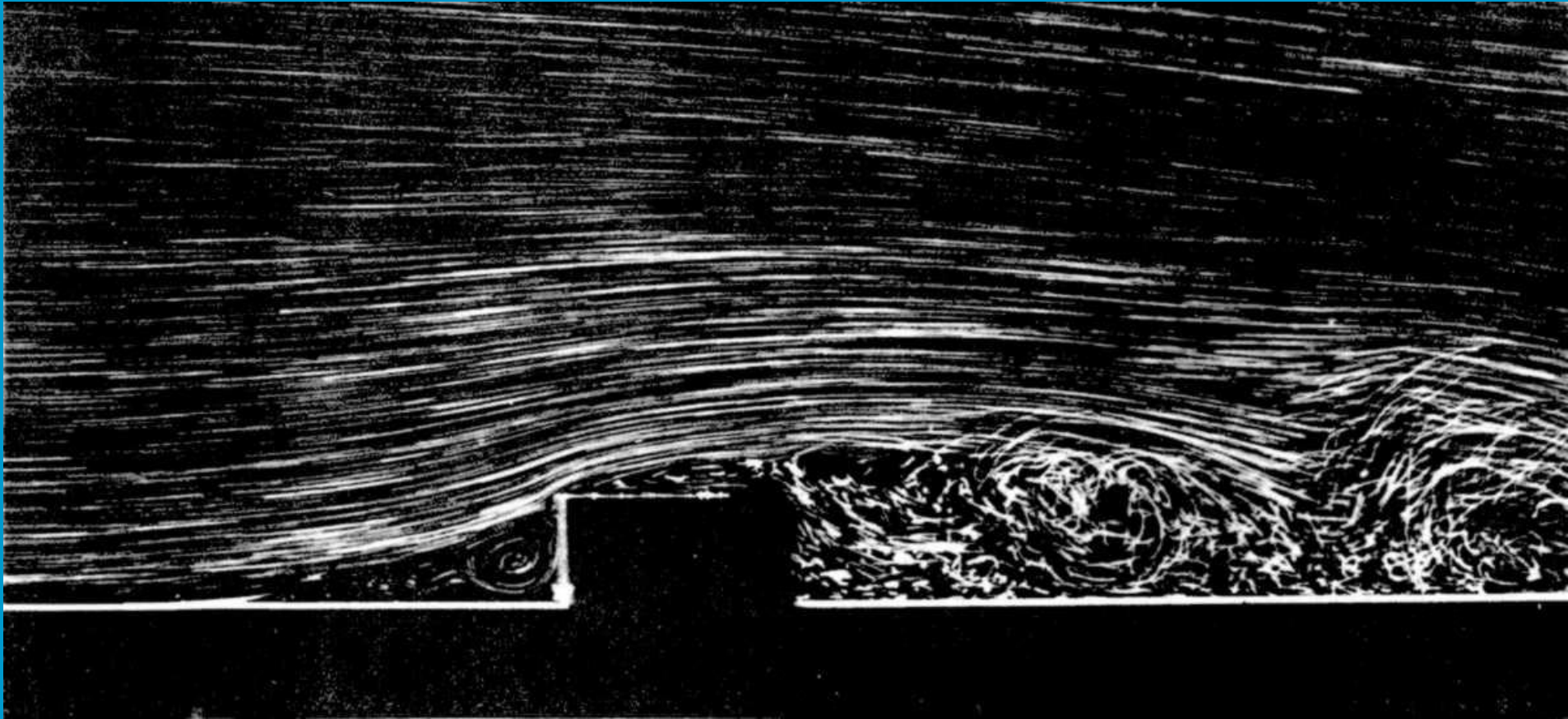


# flow phenomena in backwater-facing step (2)

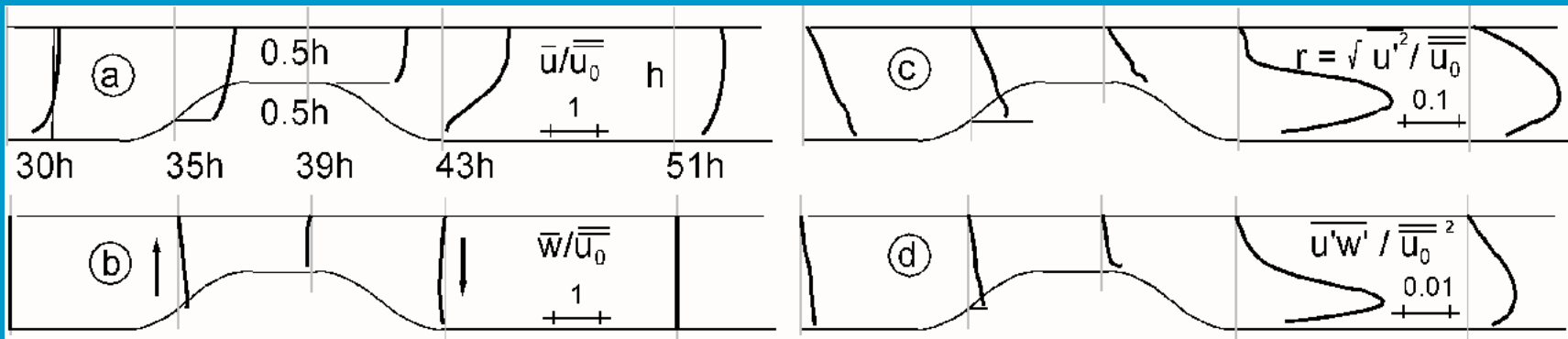




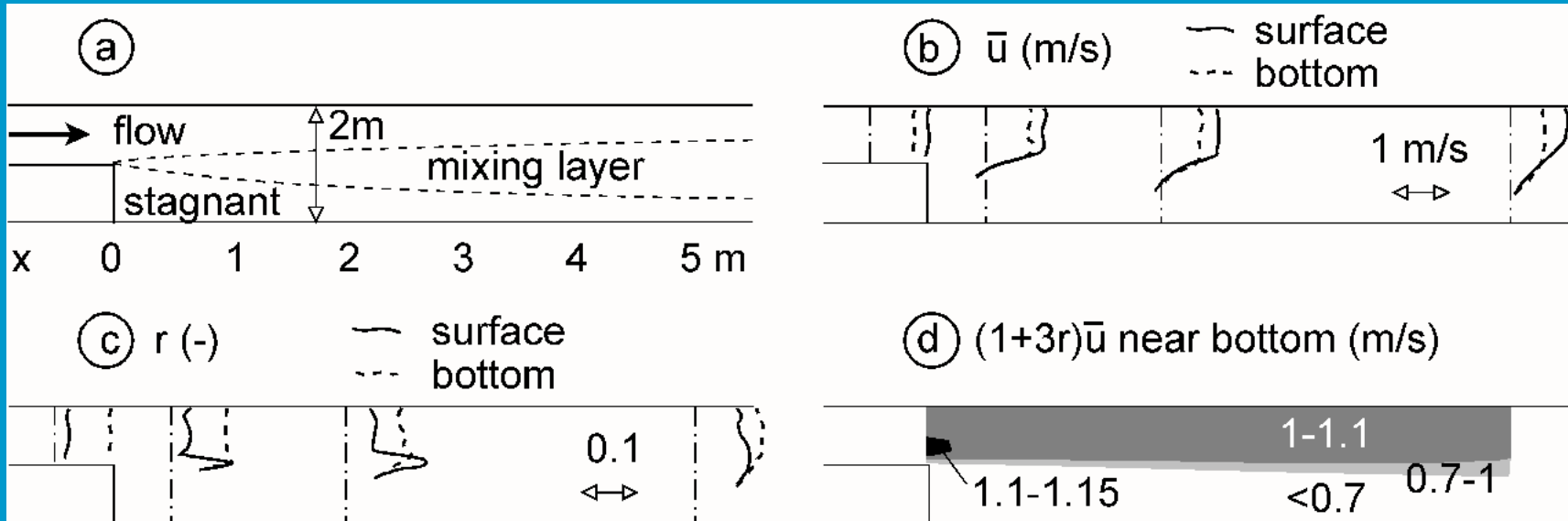
# turbulent separation over a rectangular block



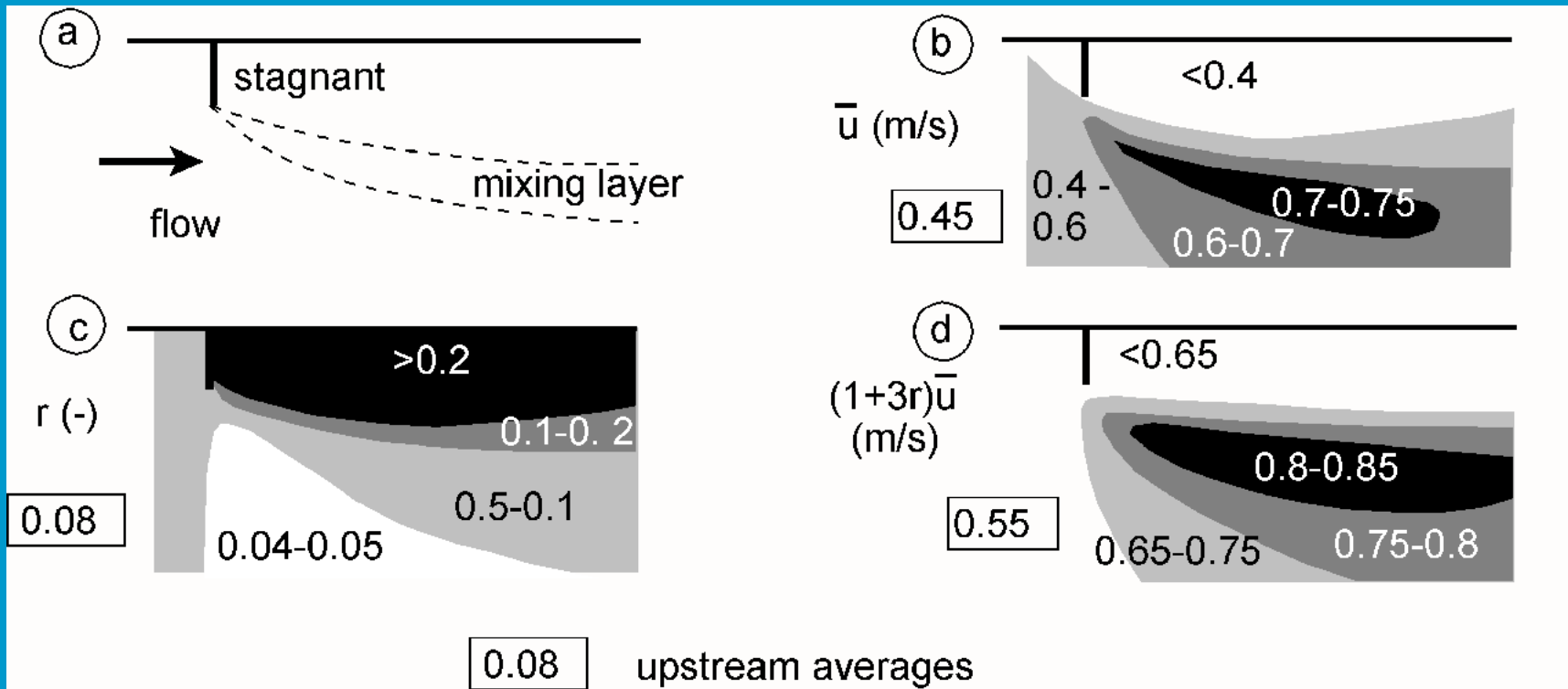
# flow characteristics around a sill



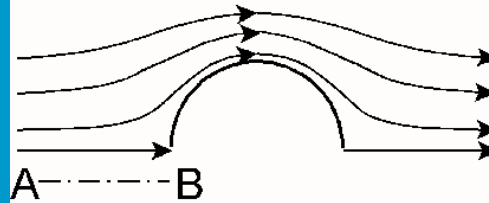
# flow characteristics in a horizontal expansion



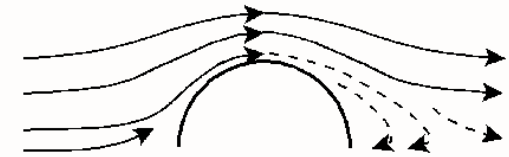
# flow characteristics for a horizontal constriction



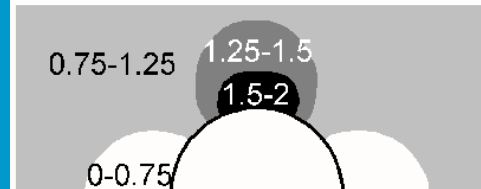
# flow around cylinder



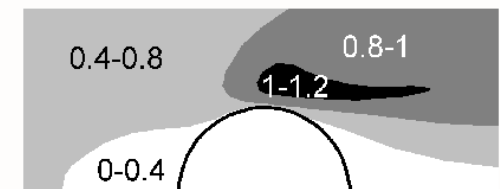
(a) streamlines potential flow



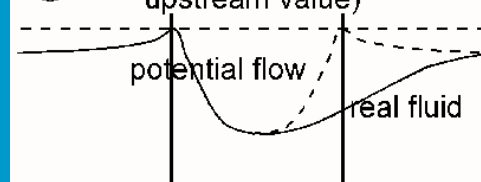
(b) streamlines measured near bottom



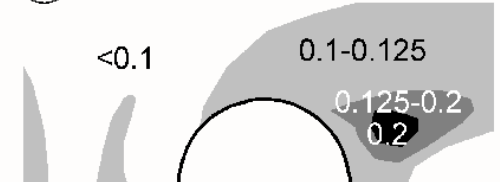
(c) velocities potential flow (relative to upstream value)



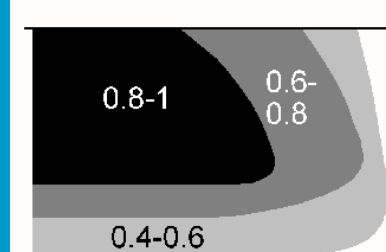
(d) velocities measured near bottom



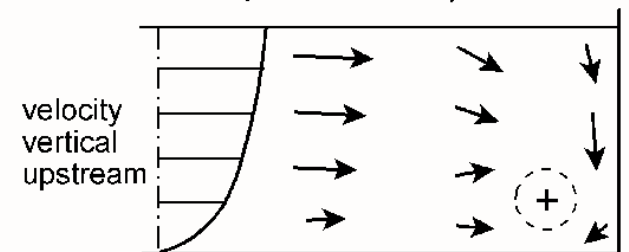
(e) water surface in cross-section A-B-A



(f) turbulence relative to upstream velocity

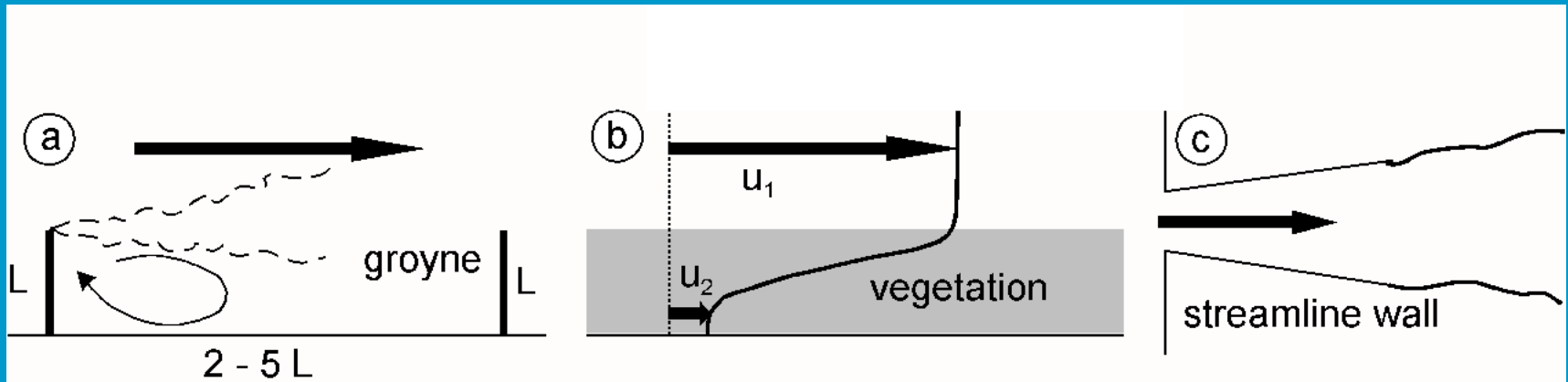


(g) velocity contours cross section A-B



(h) flow directions cross section A-B

# possible load reduction of flow induced loads



# appendix

# basic equations

# turbulence

5 November 2009

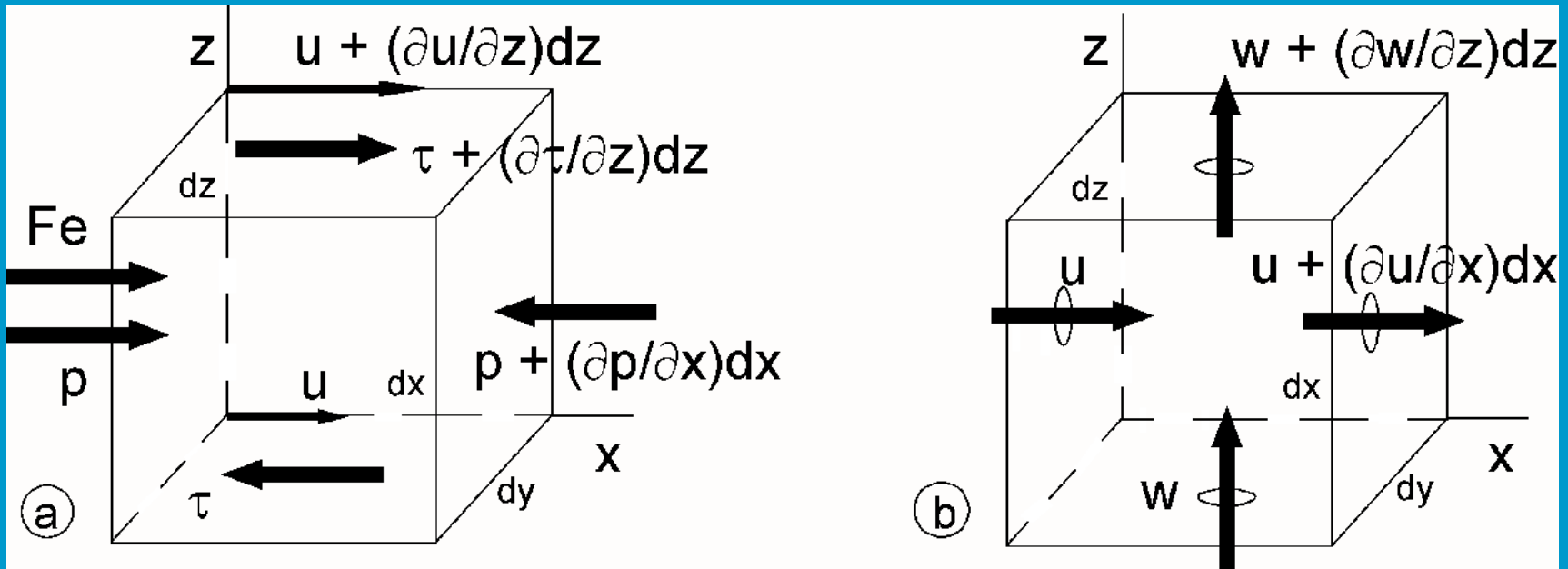
39

# basic equations

$$F_x = - \frac{\partial p}{\partial x} dx (dy dz) + \frac{\partial \tau}{\partial z} dz (dx dy) + Fe(x)$$



# forces and flow with regards to $dx dy dz$



# simplified Navier-Stokes equation

$$\rho \left( \frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + w \frac{\partial u}{\partial z} \right) = - \frac{\partial p}{\partial x} + \mu \frac{\partial^2 u}{\partial z^2}$$

<i>local</i>	<i>convective</i>	<i>pressure</i>	<i>viscous</i>
<i>inertia</i>	<i>inertia</i>	<i>gradient</i>	<i>shear</i>

# continuity equation

$$\frac{\partial u}{\partial x} + \frac{\partial w}{\partial z} = 0$$

# after some mathematics...

$$\rho \left( \frac{\partial \bar{u}}{\partial t} + \overline{u \frac{\partial \bar{u}}{\partial x}} + \overline{w \frac{\partial \bar{u}}{\partial z}} + \overline{u' \frac{\partial u'}{\partial x}} + \overline{w' \frac{\partial u'}{\partial z}} \right) = - \frac{\partial \bar{p}}{\partial x} + \mu \frac{\partial^2 \bar{u}}{\partial z^2}$$

*local conv.inertia conv.inertia press. visc.*  
*inertia by mean vel. by fluct.vel. grad. shear*

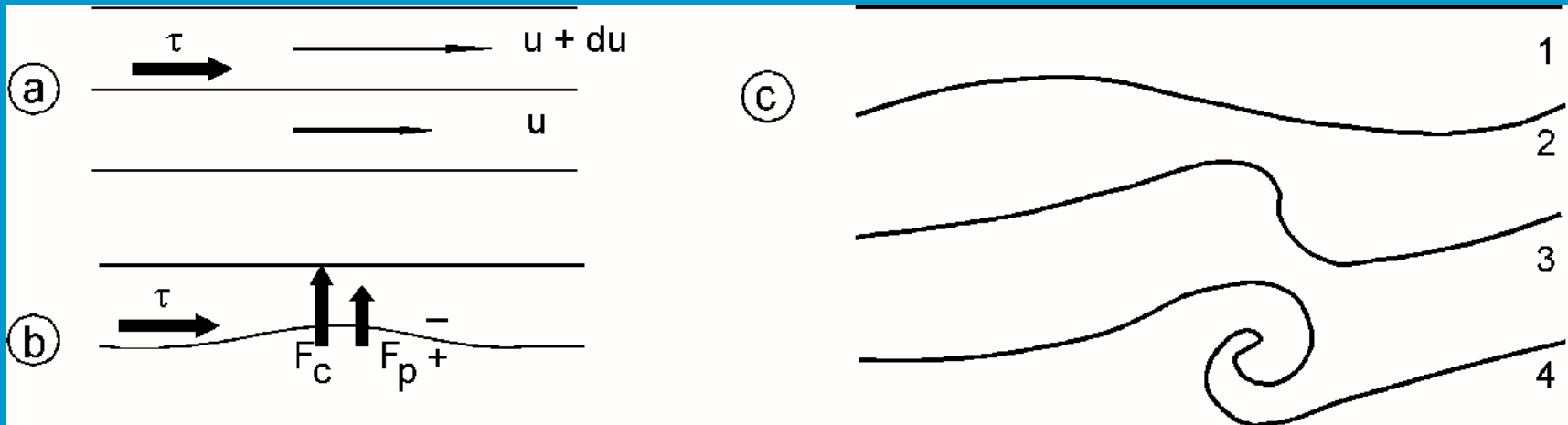
# Reynolds equation

$$\rho \left( \frac{\partial \bar{u}}{\partial t} + \bar{u} \frac{\partial \bar{u}}{\partial x} + \bar{w} \frac{\partial \bar{u}}{\partial z} \right) = - \frac{\partial \bar{p}}{\partial x} + \mu \frac{\partial^2 \bar{u}}{\partial z^2} - \rho \left( \frac{\partial \overline{u'^2}}{\partial x} + \frac{\partial \overline{u'w'}}{\partial z} \right)$$

*inertia*                      *press.*    *visc.*                      *Reynolds - stresses*

-----|-----|-----  
*mean values*                      *turb. fluct.*

# (in)stability of laminar flow



# The Reynolds number

$$Re = \frac{\rho \cdot U^2 / L}{\mu \cdot U / L^2} = \frac{U \cdot L}{\nu}$$

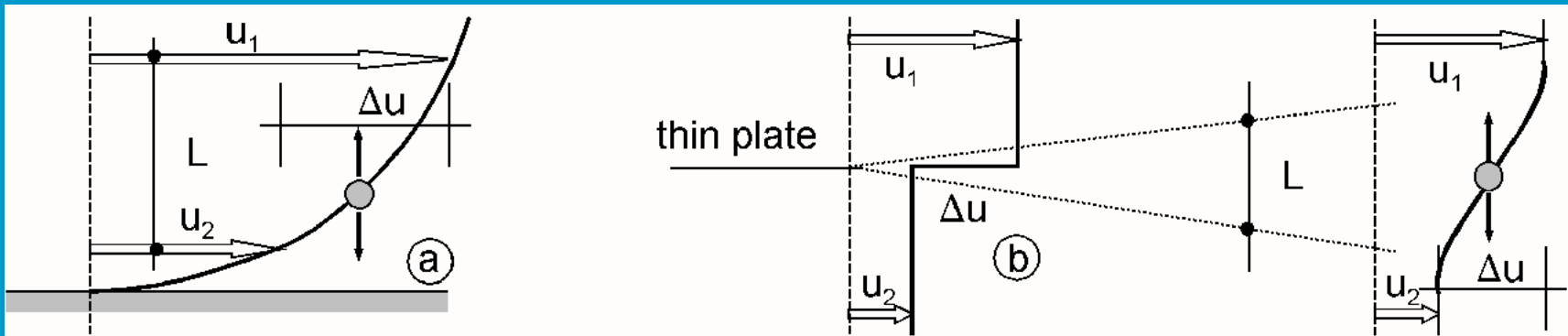
transition from laminar to turbulent flow:

$Re \approx 1000 - 2000$

$\mu$  = dynamic viscosity

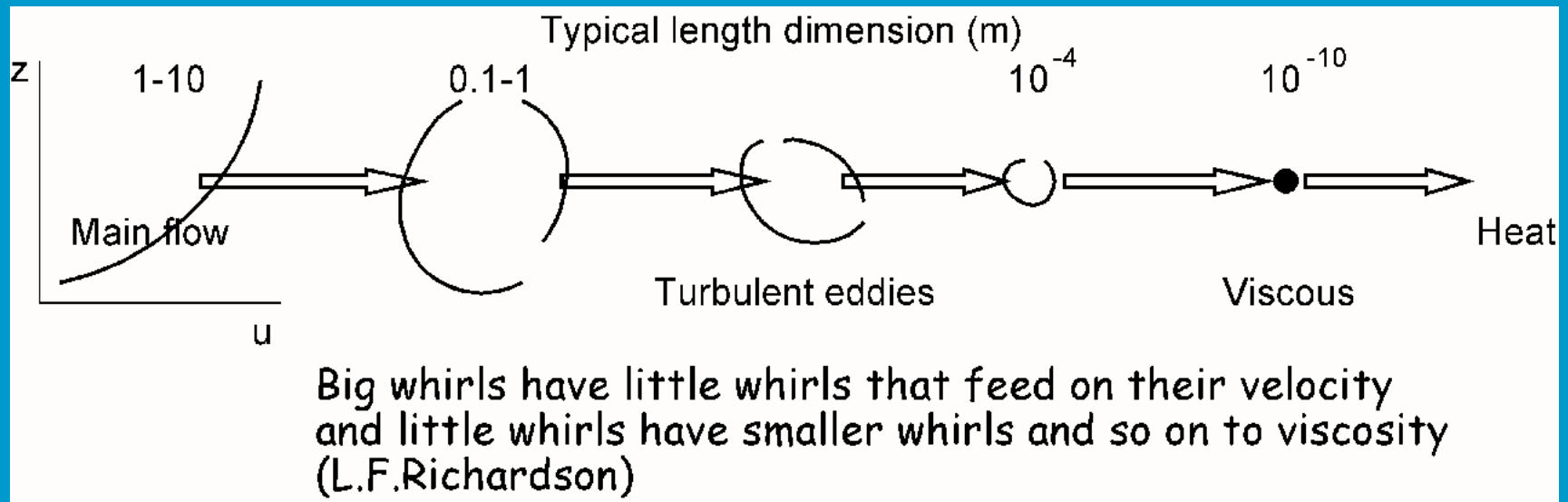
$\nu$  = kinematic viscosity ( $\nu = \mu/\rho$ )

# wall turbulence and free turbulence





# energy cascade in turbulent motion



# flow and turbulence in hydraulic jump

