

# EE1320: Measurement Science

## Lecture 3: Sensor Readout and Signal Conditioning

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May 7, 2013



Delft  
University of  
Technology

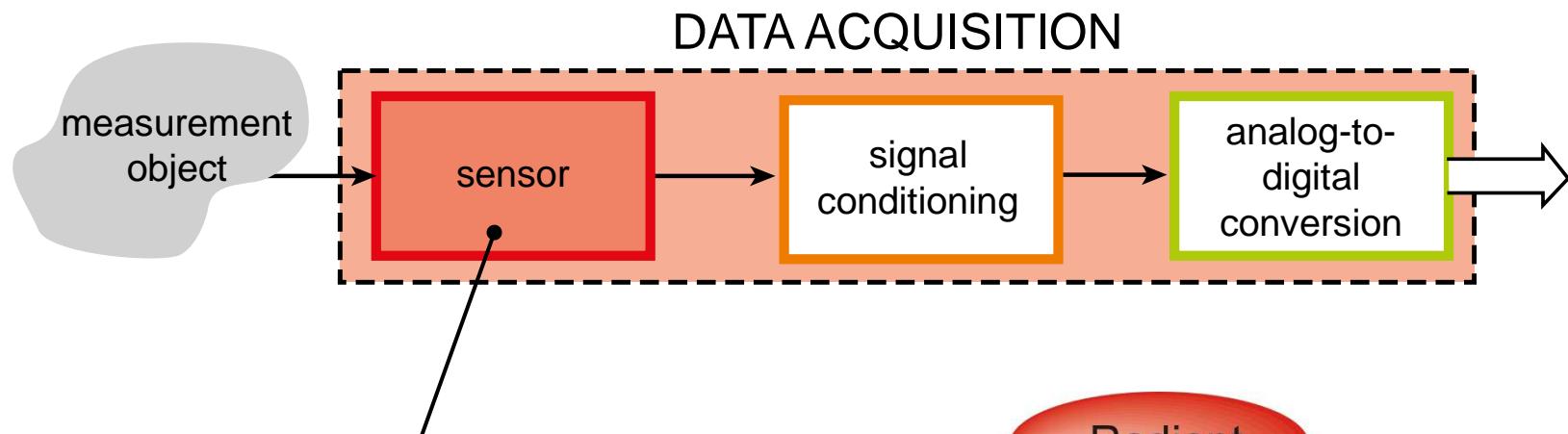
Challenge the future

# Course program 2013

week	date	topic
4.1	Tu 23/4 Fr 26/4	#1 intro measurements and meas. systems #2 sensors
4.3	Tu 7/5	#3 sensor readout and signal conditioning
4.4	Tu 14/5 We 15/5	#4 instrumentation amplifiers intermediate test
4.5	Tu 21/5	#5 analog-to-digital converters
4.6	We 29/5	#6 measurement instruments I
4.7	Tu 4/6 We 5/6	#7 measurement instruments II intermediate test
4.8	Tu 11/6	tutorial
4.11	We 3/7	final exam

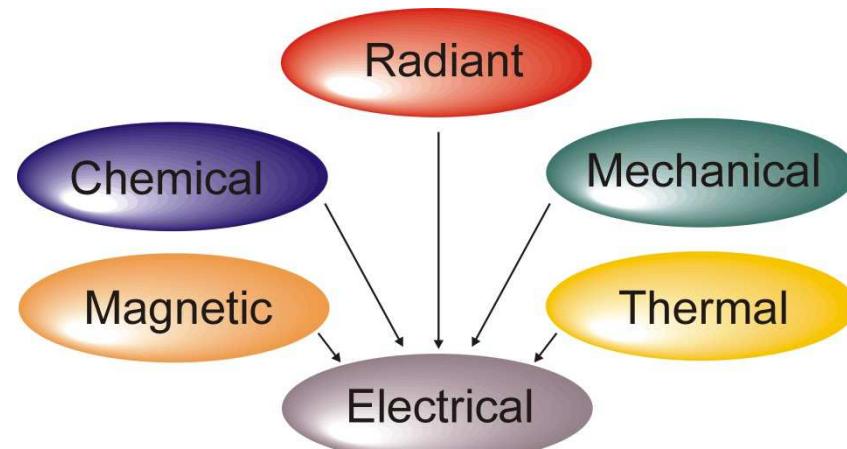
Lecturer: dr. ir. Michiel Pertijns  
room HB 15.050, M.A.P.Pertijns@tudelft.nl, 015-2786823

# Last time... Sensors

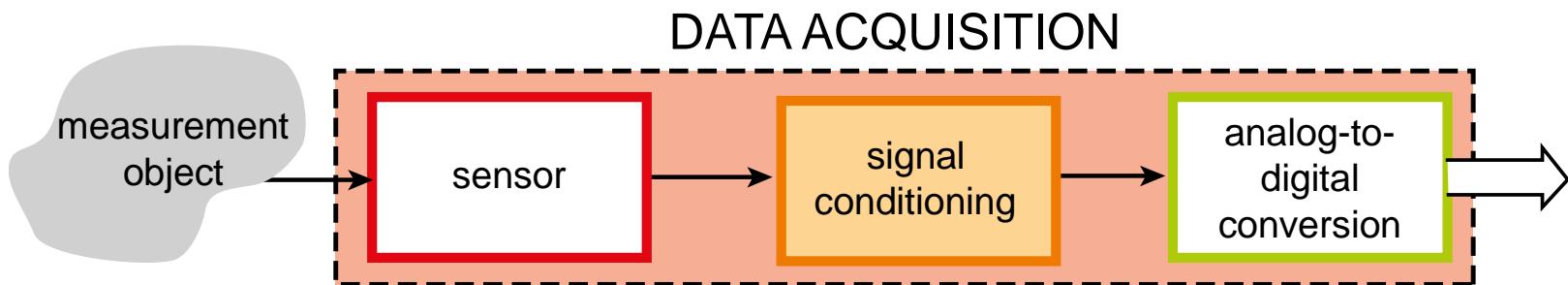


**transduction** of information  
from a (non-electrical) domain  
to the electrical domain

- self generating / modulating
- direct / tandem transduction



# Today: sensor readout and signal conditioning



- Why signal conditioning?
- Readout of
  - thermocouples with a non-inverting amplifier
  - photodiodes with a transimpedance amplifier
  - capacitive sensors with a charge amplifier
- Additionally: effects of non-ideal properties of opamps

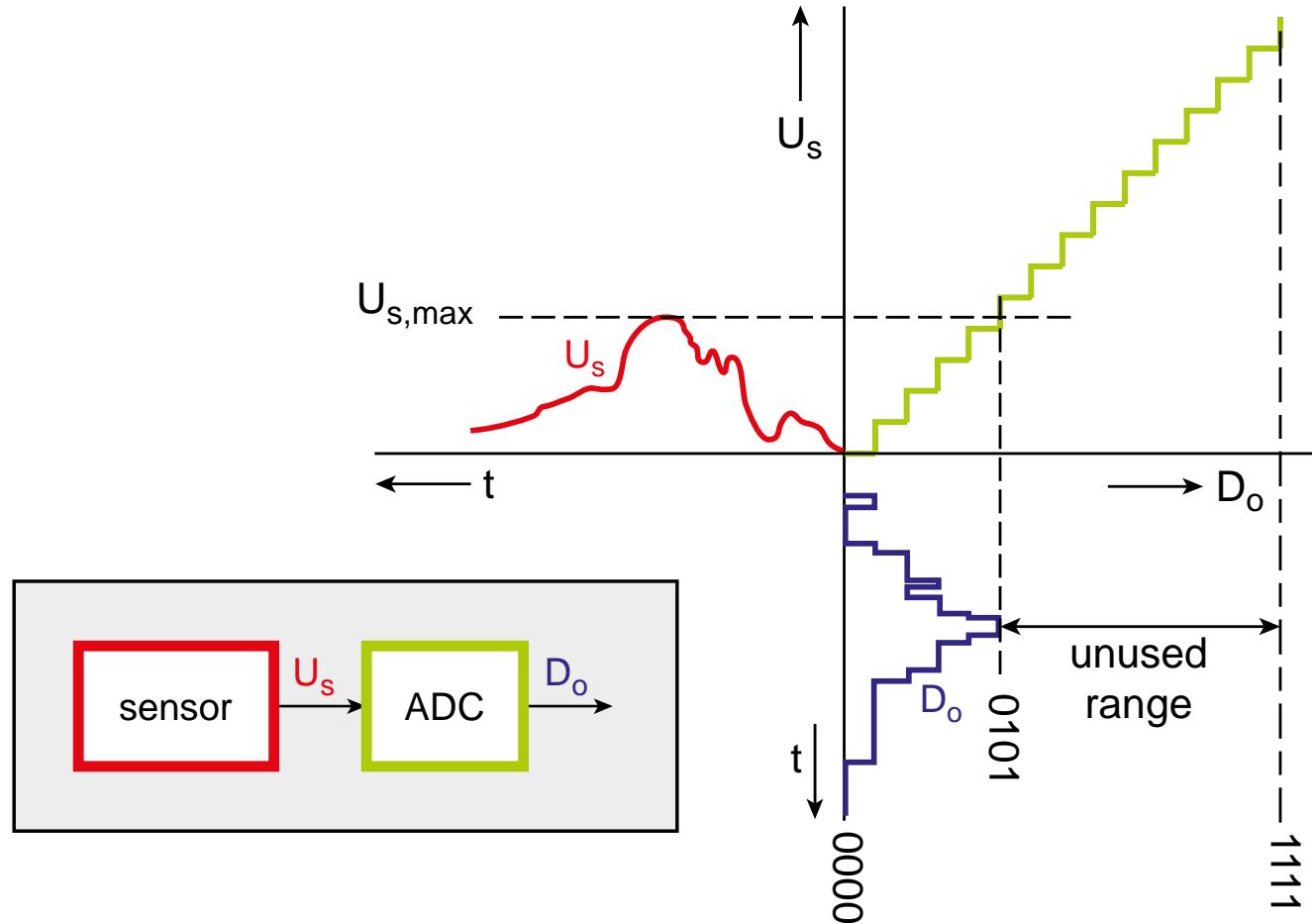
# Overview study material

- Regtien 12 (except 12.1.4, 12.1.5):
  - Properties of opamps and basic opamp circuits (recap)
  - Non-ideal properties of opamps
- Regtien 13.1.1, 13.1.2
  - Integrator en differentiator
- Regtien 5.2: Signal models – equivalent error sources

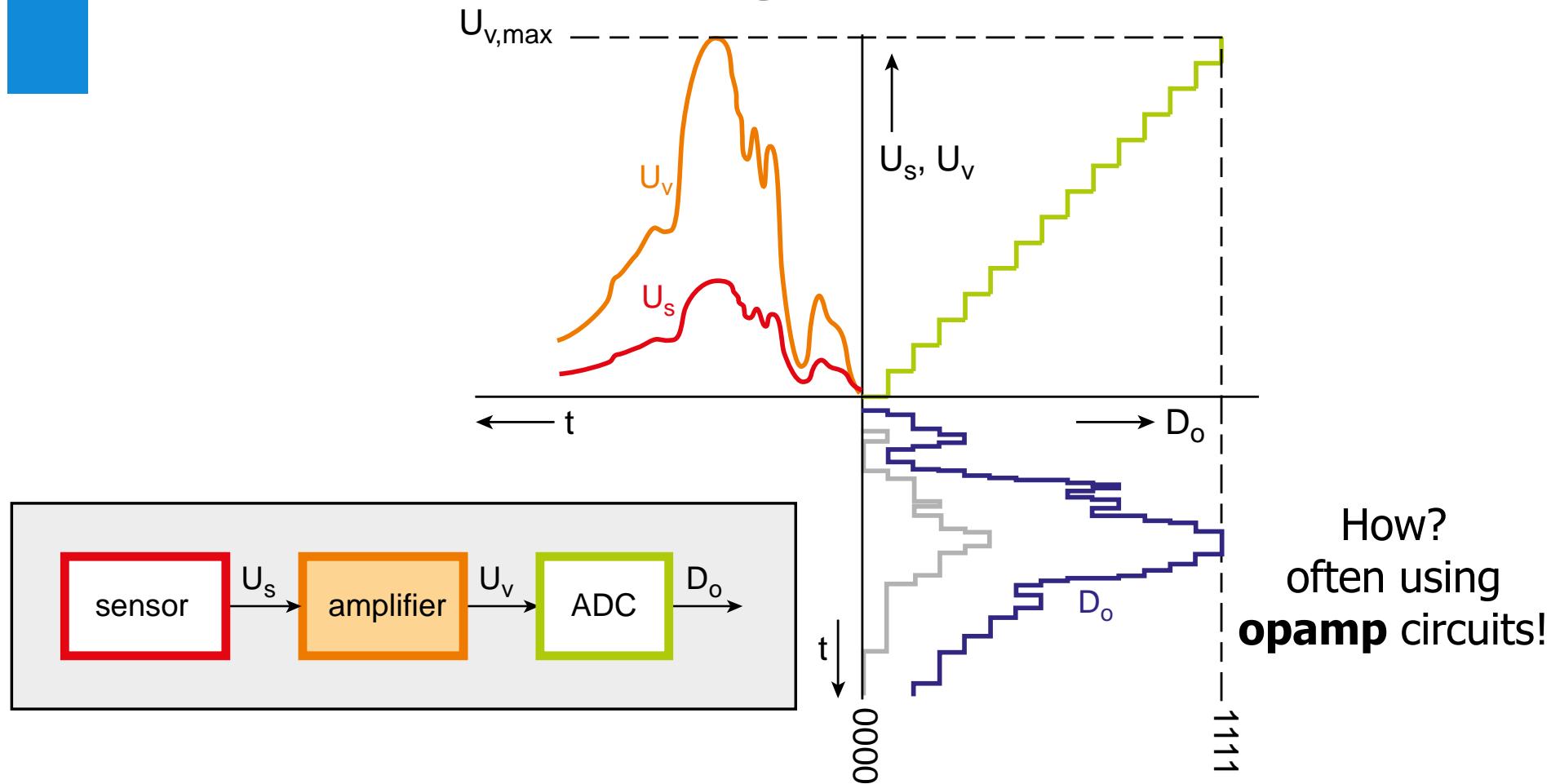
# Importance of signal conditioning

- Output signal of sensors is often not suitable for ADC input
  - too small
  - too sensitive
  - too much interference / noise
  - wrong format
  - input range ADC not used effectively
  - load of sensor by ADC yields errors
  - ADC saturates without filtering
  - e.g. resistive sensor on voltage-input
- Signal conditioning adapts the sensor signal to the ADC
  - amplification (scaling)
  - buffering
  - filtering
  - conversion

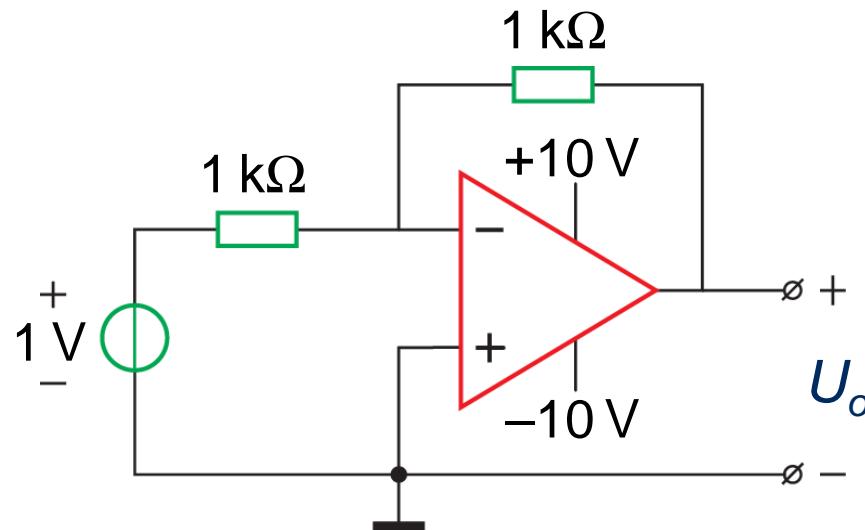
# Importance of signal conditioning - without scaling



# Importance of signal conditioning - with scaling



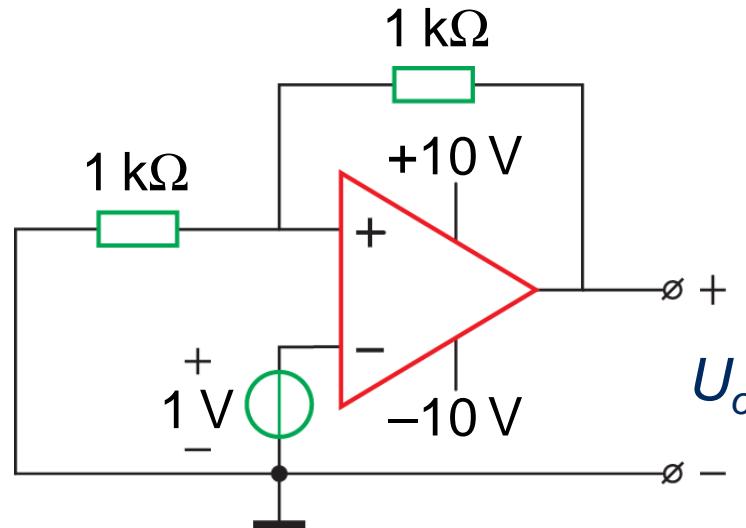
# Opamps – remember them?



The output voltage  $U_o$  is:

- A  $-1\text{ V}$
- B  $2\text{ V}$
- C  $-2\text{ V}$
- D  $-10\text{ V}$

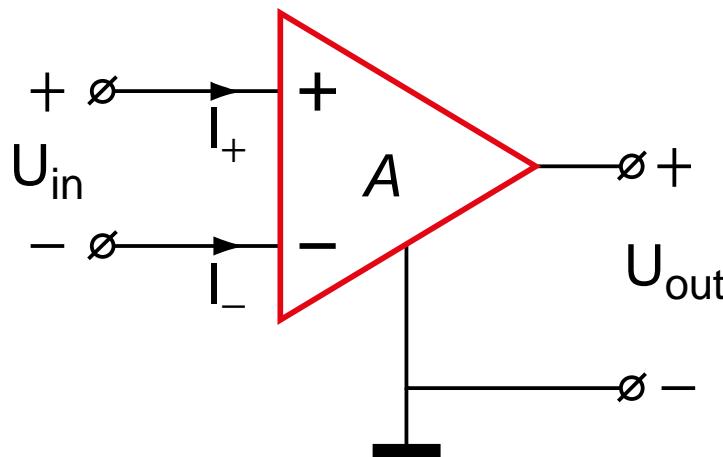
# Opamps – remember them?



The output voltage  $U_o$  is:

- A      1 V
- B      2 V
- C       $-2 \text{ V}$
- D       $-10 \text{ V}$

# Opamp – ideal behavior



- Amplifies differential input voltage with very high (ideally infinite) gain  $A$

$$U_{out} = A \cdot U_{in} = A \cdot (U_+ - U_-)$$

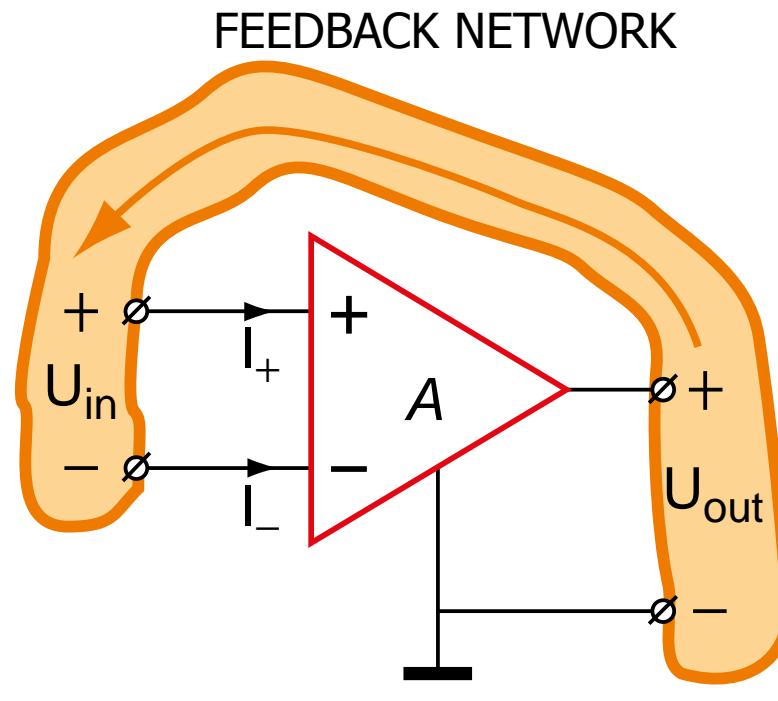
$$A \rightarrow \infty$$

- Input currents are zero:

$$I_+ \rightarrow 0$$

$$I_- \rightarrow 0$$

# Opamp – ideal behavior



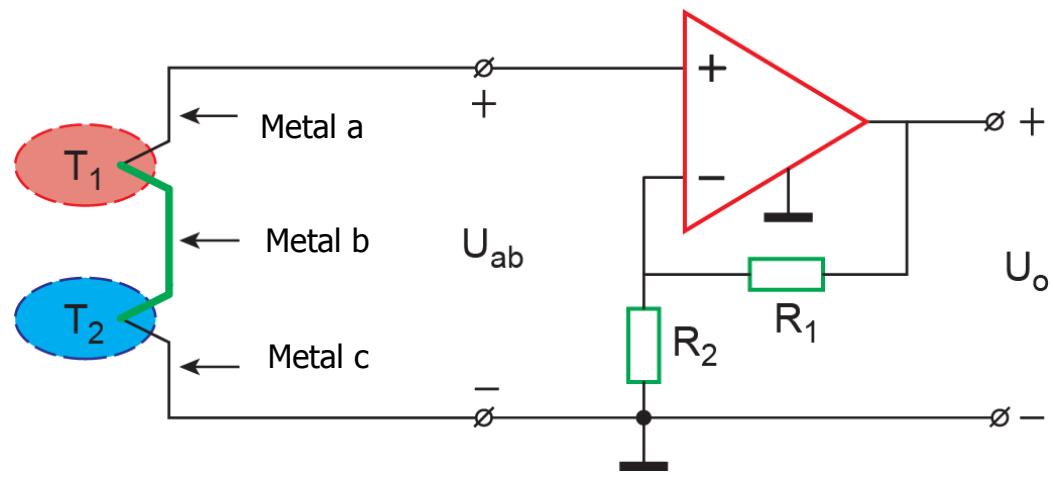
- Feedback network  
(with passive components)  
determines transfer
- Stable negative feedback  $\Rightarrow$   
 $U_{in} \rightarrow 0$  ("virtual ground")
- Zero-conditions at the input:

$$U_{in} = U_+ - U_- \rightarrow 0$$

$$I_+ \rightarrow 0$$

$$I_- \rightarrow 0$$

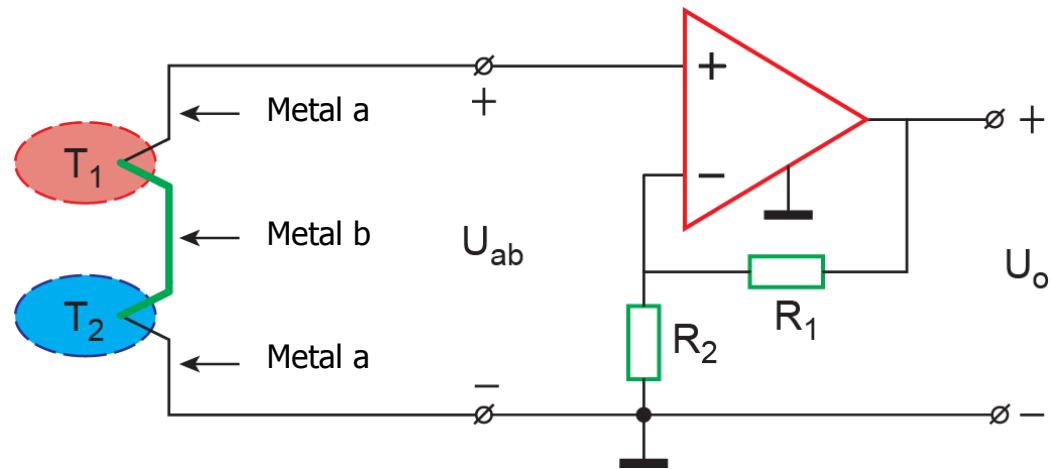
# Thermocouple readout using a non-inverting amplifier



- Thermocouple senses temperature difference:  
$$U_{ab} = \alpha_{ab} \cdot (T_1 - T_2)$$
- Sensitivity determined by Seebeck coefficients  $\alpha_a$  and  $\alpha_b$ :  
$$\alpha_{ab} = \alpha_a - \alpha_b$$
- Example: chromel/alumel ("type K" thermocouple)

$$\alpha_{ab} = 40 \mu\text{V/K}$$

# Thermocouple readout using a non-inverting amplifier



- Given:
  - measurement range  
 $0 \leq T_1 - T_2 \leq 100 \text{ K}$
  - ADC input range  
 $0 \leq U_o \leq 1 \text{ V}$
  - chromel/alumel couple  
 $\alpha_{ab} = 40 \mu\text{V/K}$

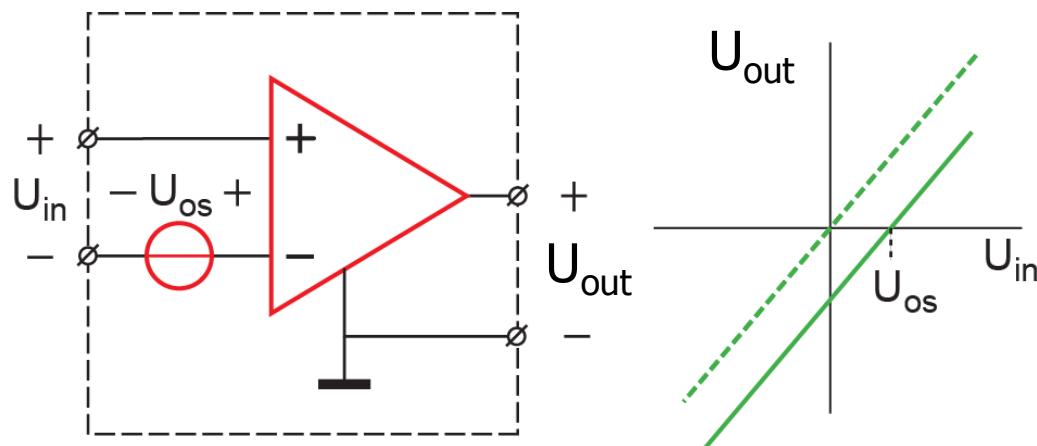
- Determine the required gain
- Dimension the resistors

$$G = \frac{1 \text{ V}}{40 \mu\text{V/K} \cdot 100 \text{ K}} = 250$$

$$G = \frac{R_1 + R_2}{R_2} \quad \text{e.g. } R_1 = 249 \text{ k}\Omega, \\ R_2 = 1 \text{ k}\Omega$$

# Opamp offset voltage

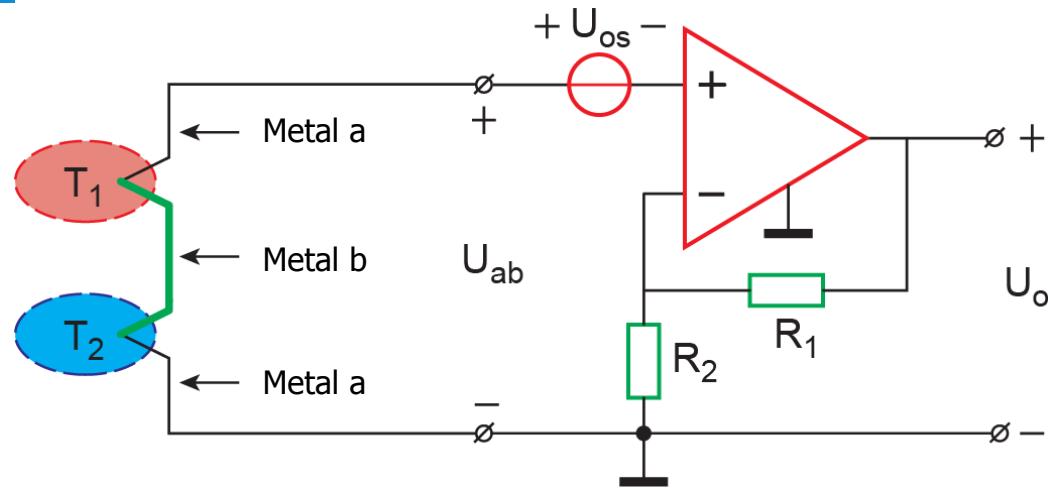
- Ideal opamp:  $U_{out} = 0$  when  $U_{in} = 0$
- Actual opamps have an **offset**:  $U_{out} \neq 0$  at  $U_{in} \neq 0$
- **Offset voltage  $U_{os}$** : input voltage  $U_{in}$  for which  $U_{out} = 0$



typical values:

- standard opamp:  $\pm 1 \text{ mV}$
- precision opamp:  $< \pm 10 \mu\text{V}$

# Thermocouple readout with offset



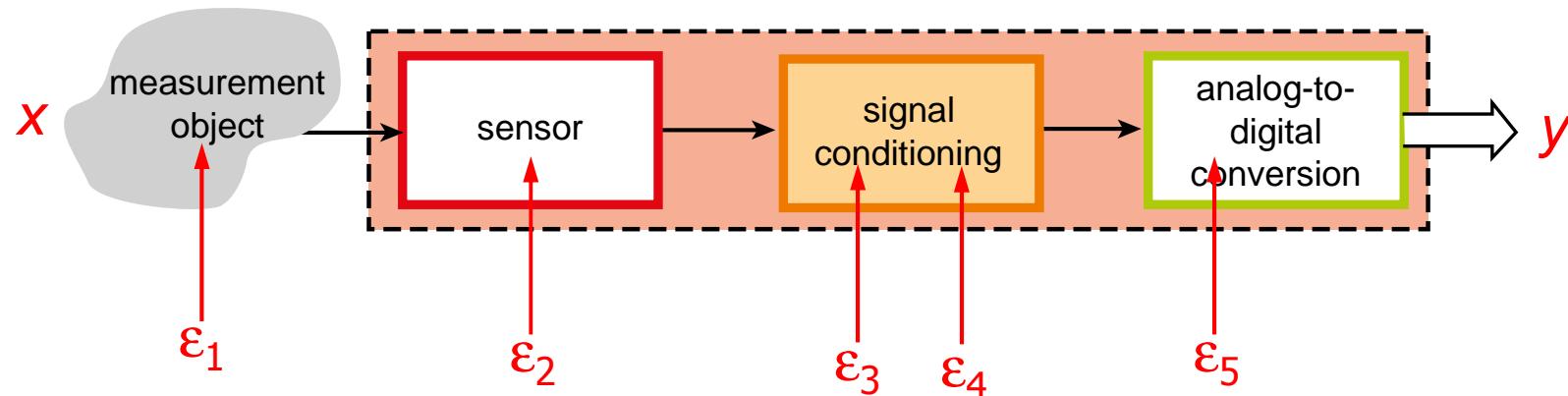
- Given:
  - opamp offset voltage  $|U_{os}| < 1 \text{ mV}$
  - chromel/alumel couple  $\alpha_{ab} = 40 \mu\text{V/K}$

- Determine the maximum measurement error due to the offset voltage



# Combining sources of error

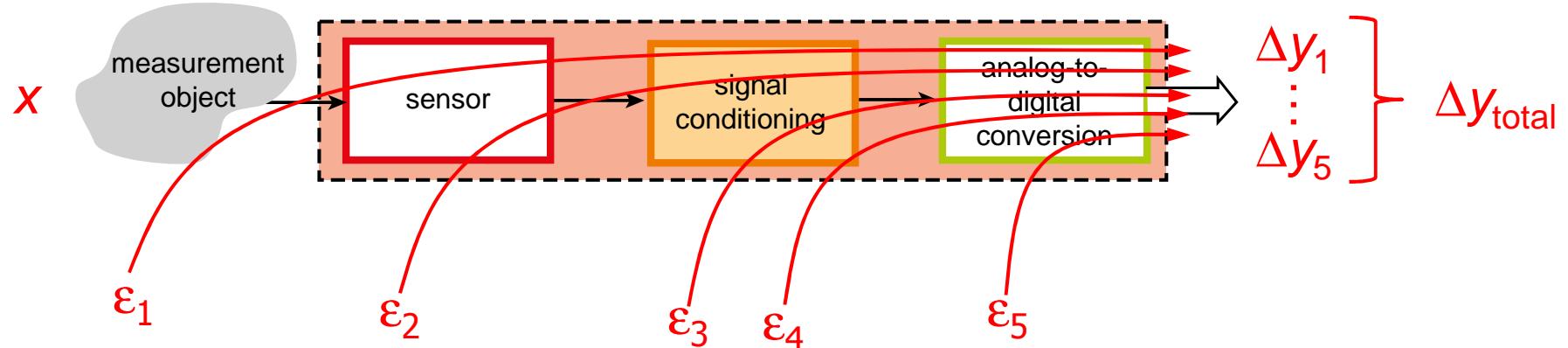
- Sources of error can occur at many positions in the chain



- For instance: offset, distortion, crosstalk, cross sensitivity
- How to determine their combined effect on the measurement?

# Combining sources of error

- Determine the effect of the individual sources on the output



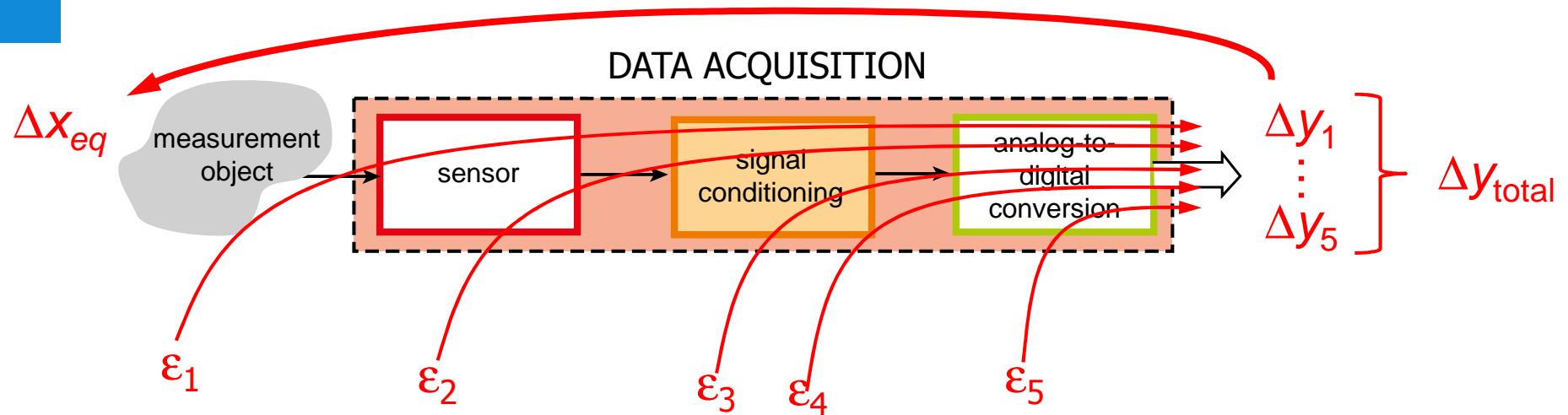
- If the system is linear (or can be linearized), then:

$$\Delta y_{\text{total}} = \sum \Delta y_i \quad \text{for systematic sources of error (e.g. offset)}$$

$$\Delta y_{\text{total}}^2 = \sum \Delta y_i^2 \quad \text{for uncorrelated stochastic sources of error (e.g. noise)}$$

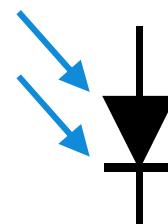
# Equivalent sources of error

- Translate the output-referred error back to the input



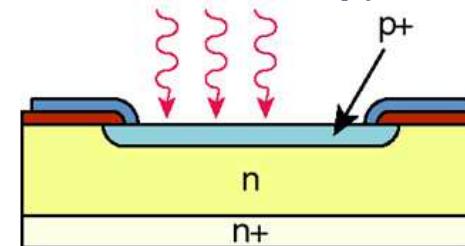
- $\Delta x_{eq}$  is called the equivalent input error
- Example: what's the effect of  $\varepsilon_3$  on the measurement?
  - Determine output error due to  $\varepsilon_3 \Rightarrow \Delta y_3$
  - Translate this back to the input  $\Rightarrow \Delta x_{eq,3}$
  - $\varepsilon_3$  causes an equally large error as an error  $\Delta x_{eq,3}$  at the input would

# Photo diode

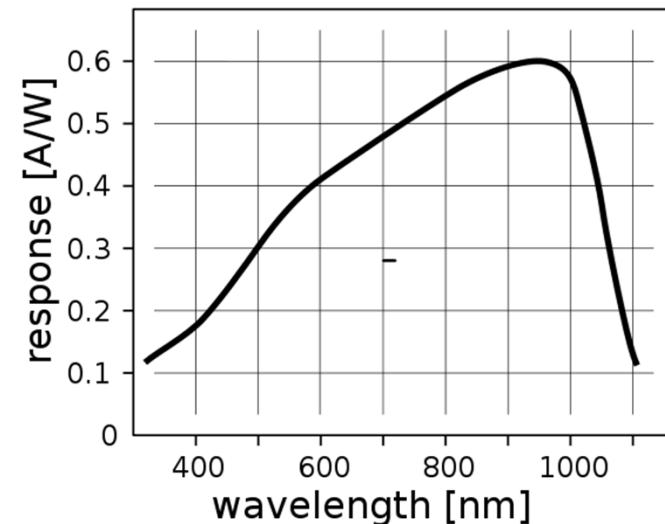


- Photons lead to a photocurrent  $I_{ph}$
- Characteristic properties:
  - spectral sensitivity  $R$  [A/W]
  - dark current  $I_{dark}$  [A]
  - quantum efficiency  $\eta$  [%]: electrons / photon

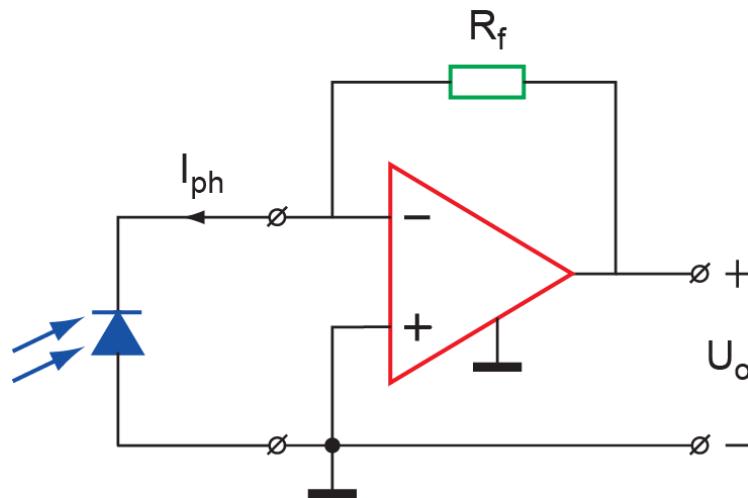
$$E = h \cdot v = \frac{h \cdot c}{\lambda}$$



Typical sensitivity  
of a Si photodiode



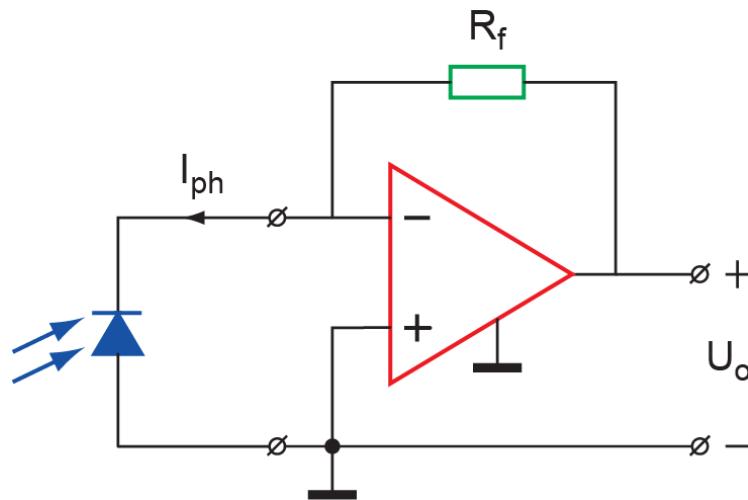
# Photodiode readout using a transimpedance amplifier



- transimpedance amplifier = current-voltage converter

$$U_o = R_f \cdot I_{ph}$$

# Photodiode readout using a transimpedance amplifier

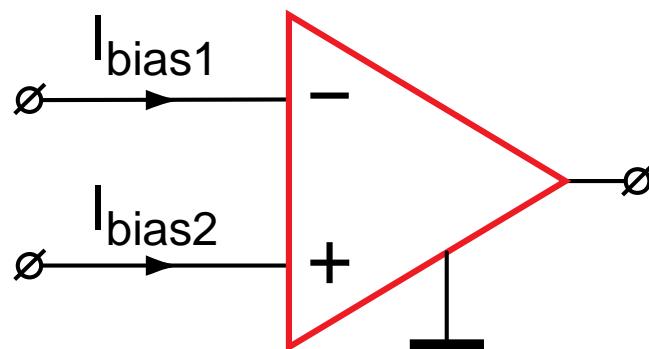


- Given:
  - spectral sensitivity  
 $R_{spec} = 0.5 \text{ A/W}$
  - sensitive area  
 $A = 1 \text{ mm}^2$
  - light intensity range  
 $0 \leq P \leq 1 \text{ W/m}^2$
  - ADC input range  
 $0 \leq U_o \leq 1 \text{ V}$
- Determine the required feedback resistance



# Opamp offset current and bias current

- Ideal opamp:  $I_+ \rightarrow 0, I_- \rightarrow 0$
- Practical opamps require **bias current**  $I_{bias}$
- Moreover, input currents are not exactly equal:  
**offset current:**  $I_{os} = I_{bias1} - I_{bias2}$

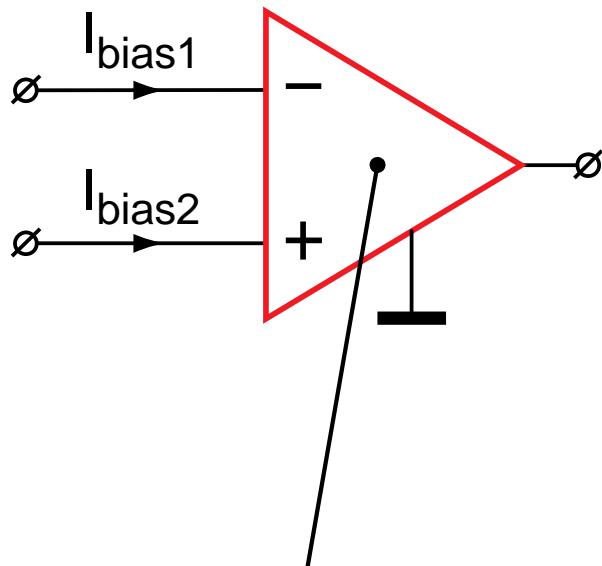


values vary strongly  
depending on opamp type

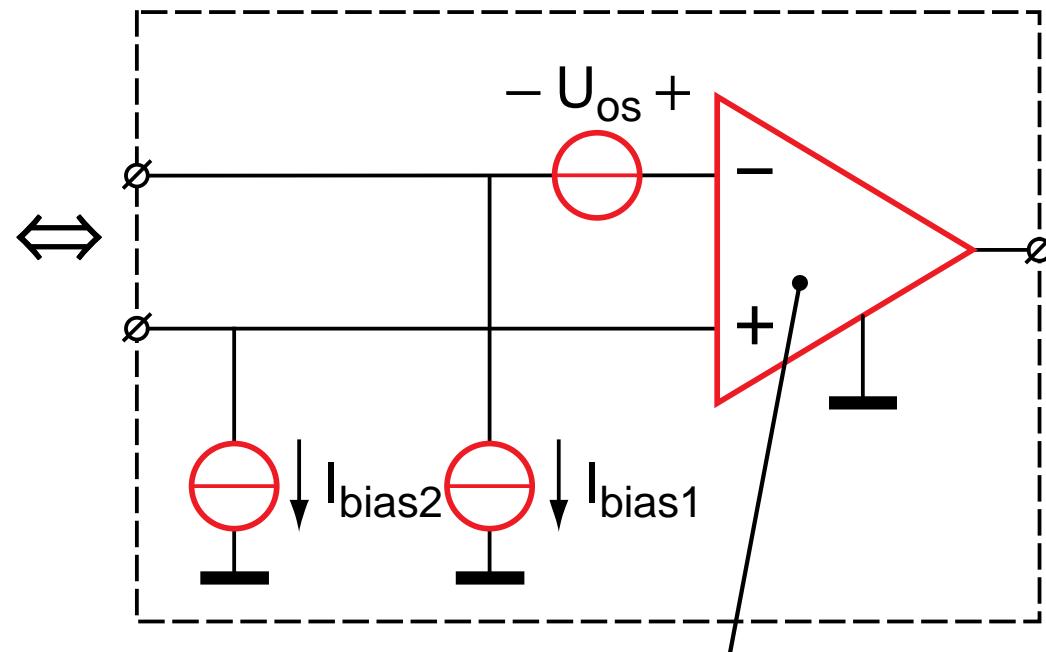
- MOS: pA ~ nA
- bipolar: nA ~  $\mu$ A

often highly  
temperature dependent!

# Modeling offset and bias current with equivalent sources

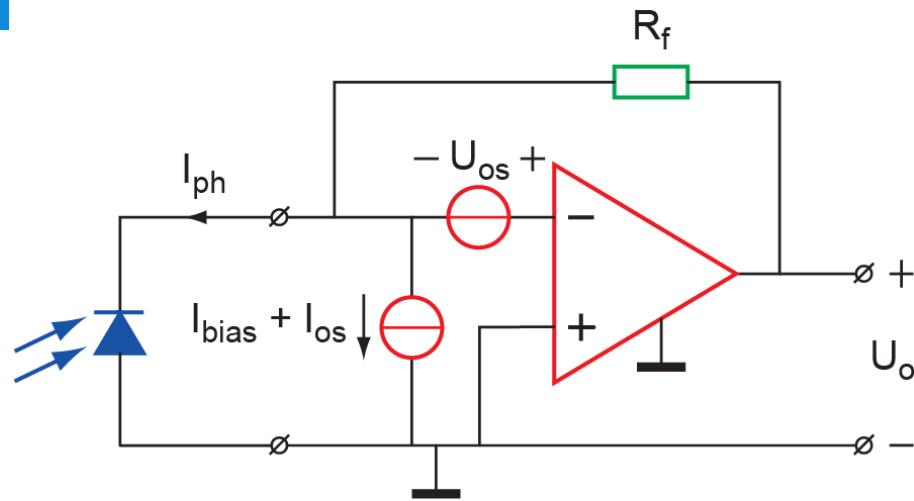


Practical opamp  
with offset and  
bias currents



Ideal opamp  
without offset and  
bias currents

# Photodiode readout with offset and bias current

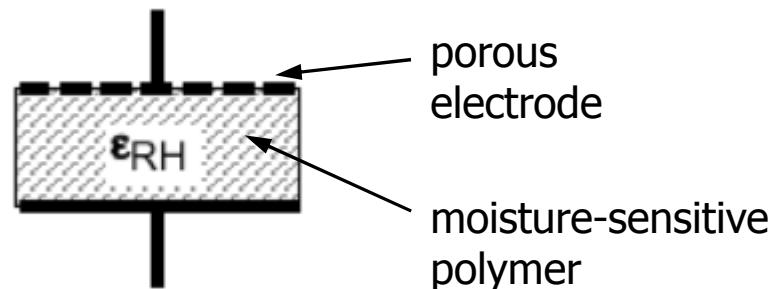
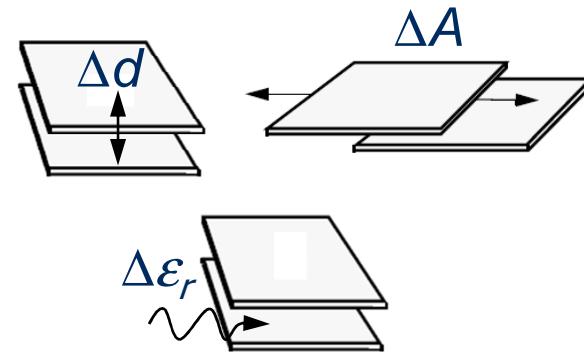


- Determine maximum offset voltage at the output (in mV)
- Determine the equivalent input offset in terms of the photocurrent (in nA)

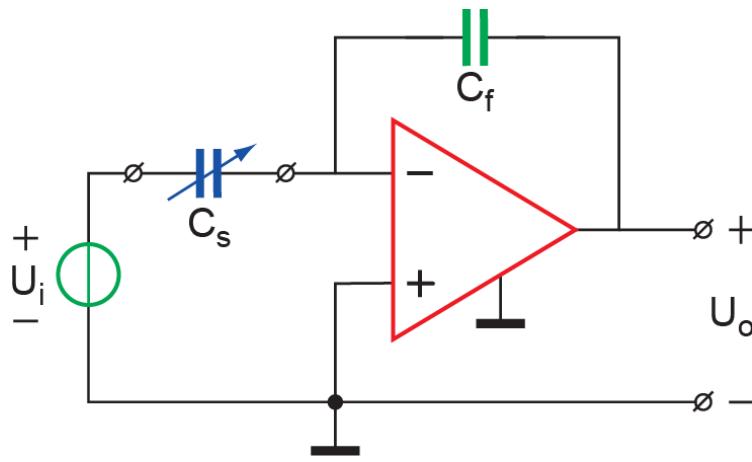
- Given:
  - dark current photodiode  $I_{dark} \leq 5 \text{ nA}$
  - opamp offset voltage  $|U_{os}| < 1 \text{ mV}$
  - opamp bias current  $I_{bias} < 10 \text{ nA}$
  - opamp offset current  $|I_{os}| < 1 \text{ nA}$
  - $R_f = 2M\Omega$

# Readout of capacitive sensors using a charge amplifier

- Capacitive sensor:  $C_s = \epsilon_0 \cdot \epsilon_r \cdot \frac{A}{d}$
- $C_s$  changes due to
  - displacement  $\Delta d, \Delta A$
  - change in dielectric constant
- Example: humidity sensor

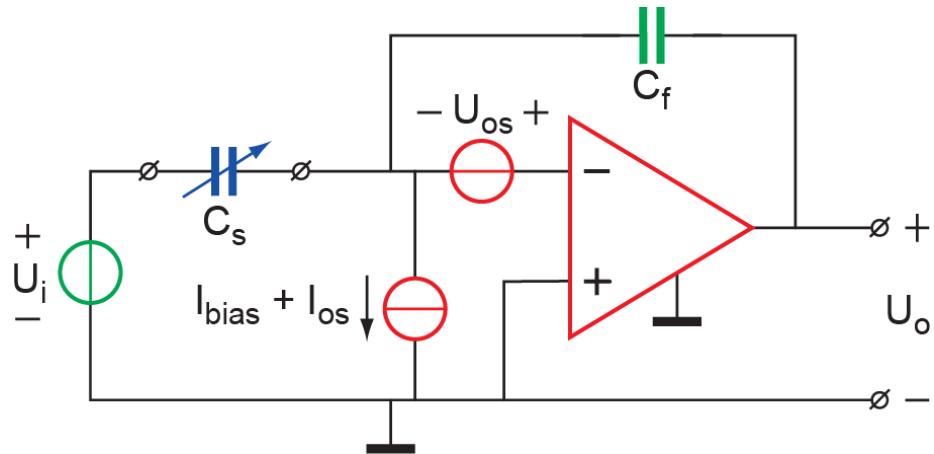


# Readout of capacitive sensors using a charge amplifier



- Charge amplifier
  - resembles an inverting amplifier
- Transfer:
$$U_o = -\frac{Z_f}{Z_s} U_i = -\frac{j\omega C_s}{j\omega C_f} U_i = -\frac{C_s}{C_f} U_i$$
- Requires AC voltage  $U_i$  ( $\omega > 0$ )

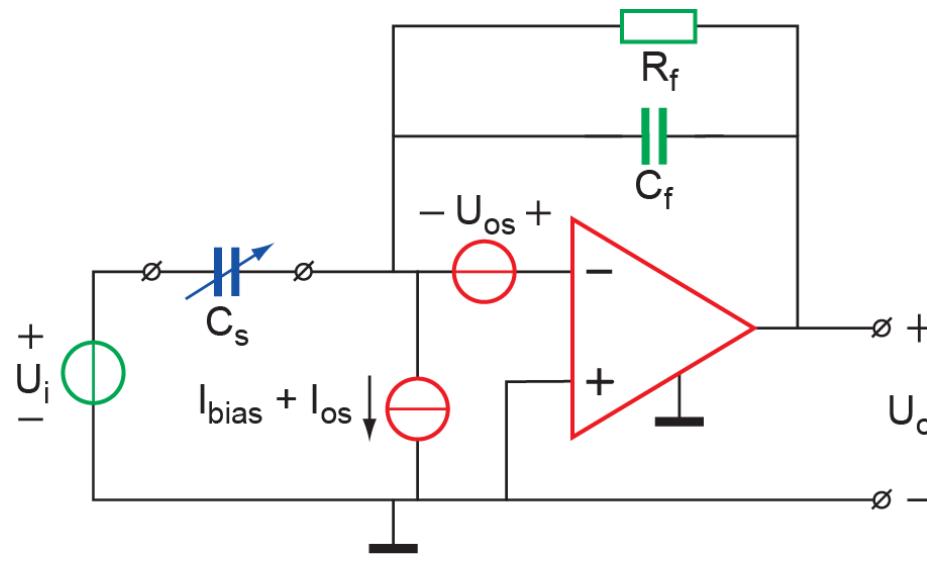
# Readout of capacitive sensors with offset and bias current



- What is wrong??



# Readout of capacitive sensors with offset and bias current



- “Tamed” integrator:  
feedback resistance  $R_f$
- DC transfer determined by  $R_f$ :

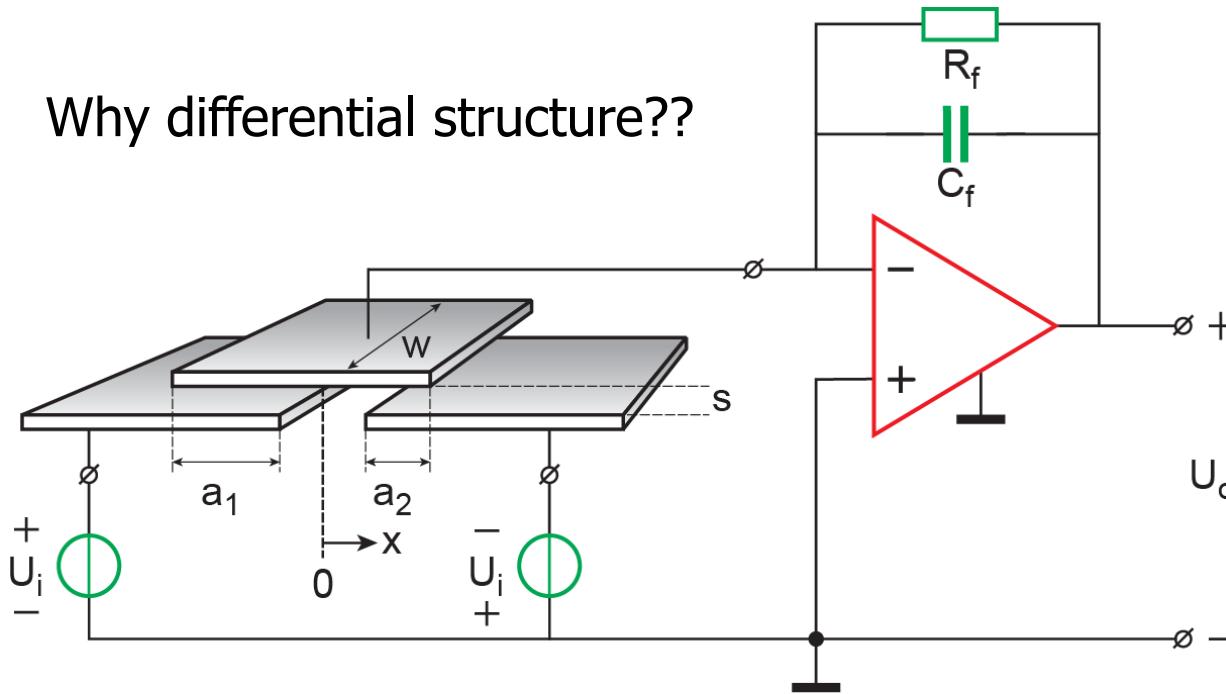
$$\Delta U_o = -U_{os} + (I_{bias} + I_{os}) \cdot R_f$$

- For  $\omega > \frac{1}{R_f C_f}$  transfer

determined by  $C_f$ :  $U_o = -\frac{C_s}{C_f} U_i$

# Differential readout of capacitive sensors

Why differential structure??



- Differential structure  $\Rightarrow U_o = 0$  for  $x = 0$
- Differential structures eliminate offsets and even-order non-linearities.

# Summary

- Signal conditioning needed to adjust sensor output signal to input of ADC
- Opamps are suitable building blocks for sensor readout
  - non-inverting amplifier (example: thermocouples)
  - transimpedance amplifier (example: photodiodes)
  - charge amplifier (example: capacitive sensors)
- Opamp's non-ideal properties influence the transfer
  - offset voltage, bias current, offset current
  - modeled with equivalent sources at input of opamp
  - can be translated to equivalent input- or output-referred errors

# What's next?

- Study:
  - Regtien chapter 12, sections 5.2, 13.1.1, 13.1.2
- Practice
  - See the exercises on Blackboard!
- Questions, things unclear? Let me know!  
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Next time:  
instrumentation amplifiers!