

# Offshore Hydromechanics

## **Module 1 :       Hydrostatics                       Constant Flows                       Surface Waves**

**OE4620 Offshore Hydromechanics**

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**November 2007**

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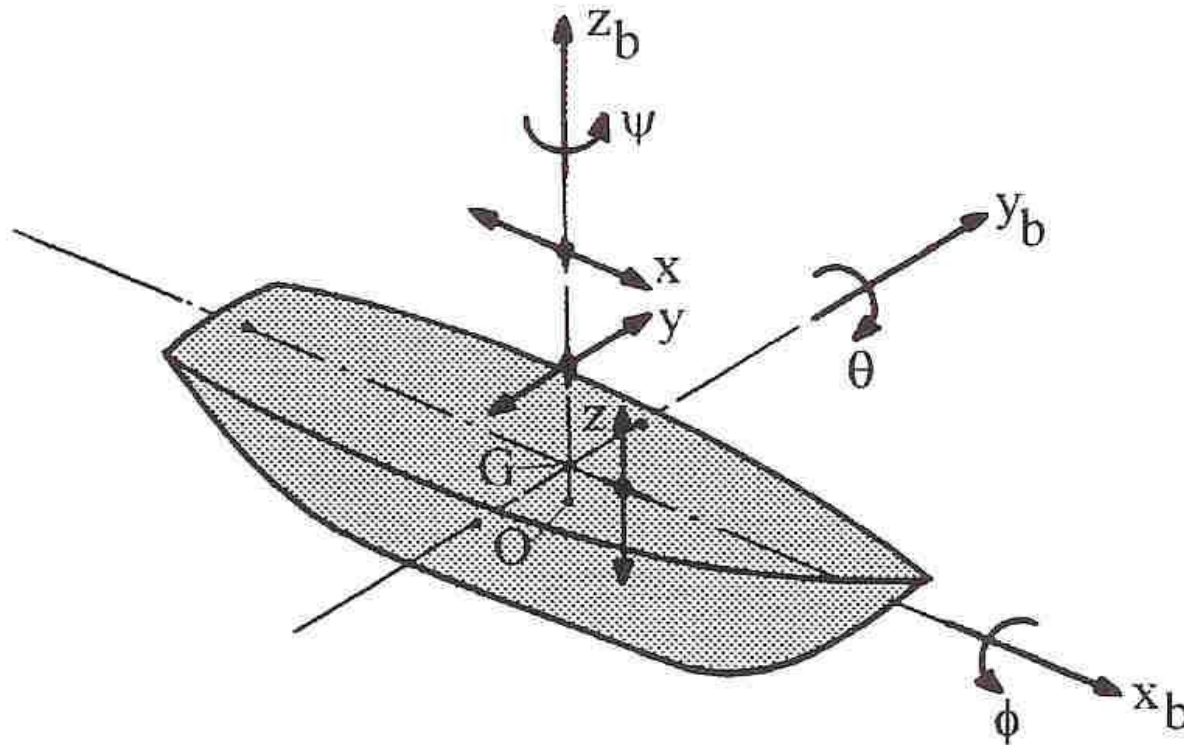
# 1. INTRODUCTION

- Some definitions
- Floater types
- Relevance of hydromechanics

# Floater motions

	static	dynamic	symbol
X :		surge	x
Y :		sway	y
Z :		heave	z
Around X :	heel, list	roll	$\phi$
Around Y :	trim	pitch	$\theta$
Around Z :	course angle	yaw	$\psi$

# Axes convention



# Application

Nearly every offshore design or problem

- DP vessel design
- Semi submersible optimization
- Jacket launch
- FPSO mooring
- Etc. etc.

# 2. HYDROSTATICS

- Equilibrium situations  
or
- Quasi-static situations

Law of Archimedes : Ευρεκα !!

# Archimedes Law

The weight of a floating body is equal to the weight of the displaced fluid.

The term “displacement” of a floater refers to its weight.

$$D = \rho g \nabla \text{ [N]}$$

$\nabla$  = submerged volume [m<sup>3</sup>]

$\rho$  = specific density of the fluid

seawater :  $\rho = 1025 \text{ kg/m}^3$

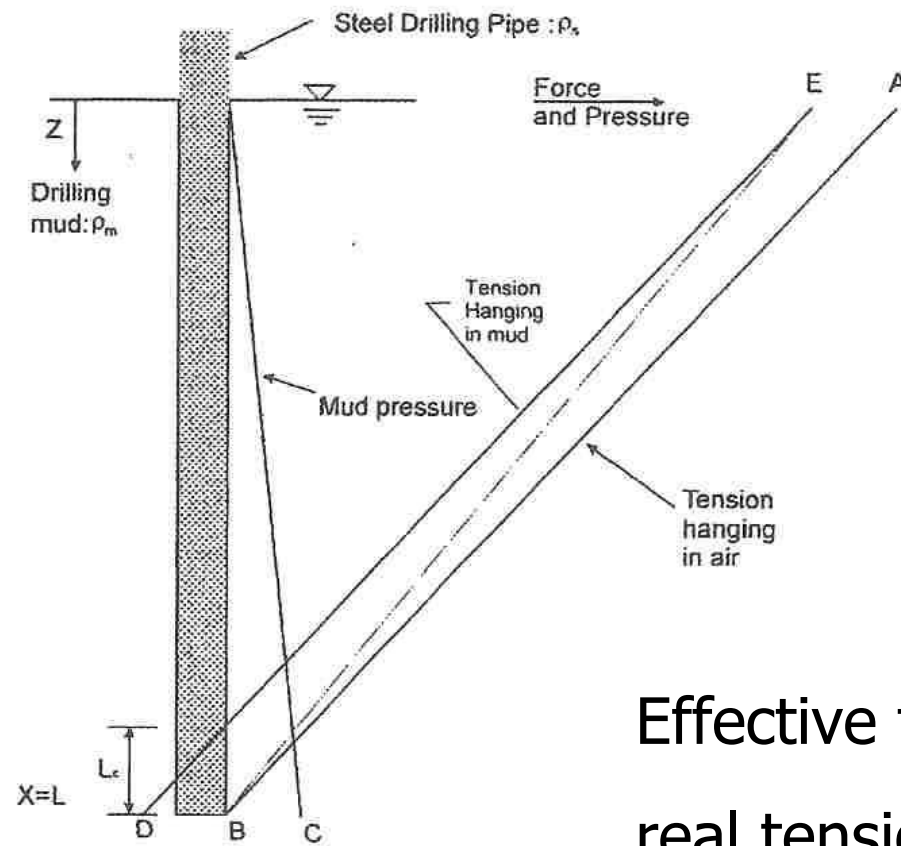
# Static internal forces, stresses

Consider external (and internal) pressures and the local loads or weights.

Archimedes applies to complete bodies, not to internal forces.

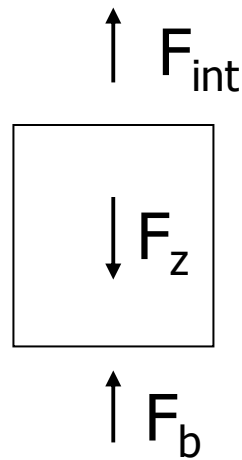


# Example : drillstring in mud



Effective tension versus  
real tension

# Example : drillstring in mud



Effective tension versus = 0 when  $F_z = F_b$

$$\rho_s g A \Delta L = \rho_m g A L \quad \Delta L = \frac{\rho_m}{\rho_s} L$$

# Floating Stability

The property of floating bodies that keeps them upright.

Offshore : quiet motion behaviour, in particular in roll.

*These two definitions are to some extent contradictory !*

# Floating Stability

## Applications:

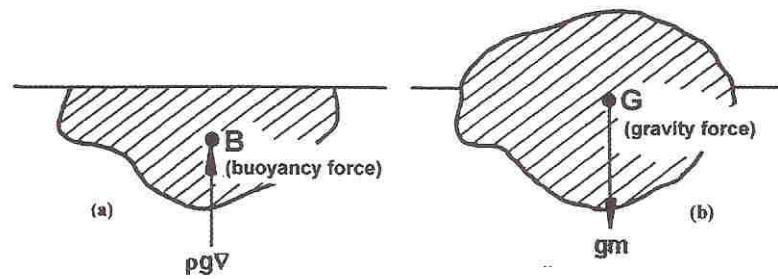
- Determine angle of heel due to heeling moment
- Determine shift of center of gravity due to additional mass
- Find center of gravity (inclining experiment)
- Determine static stability curve

# Floating Stability

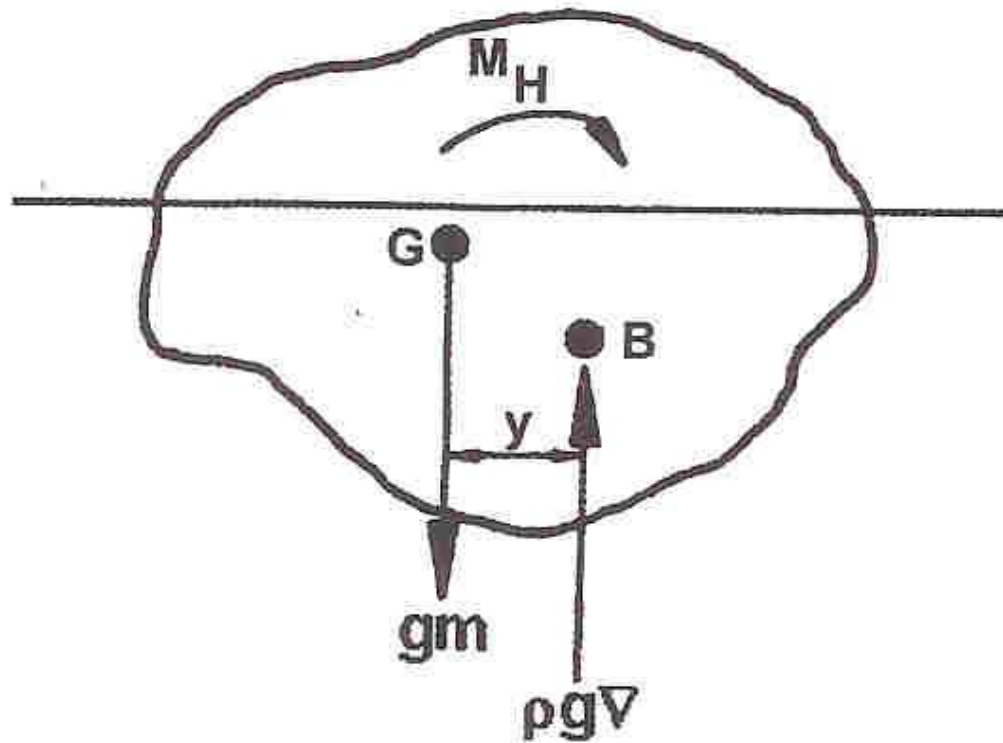
A floating structure at rest is in:

- *Horizontal equilibrium*
- *Vertical equilibrium*
- *Rotational equilibrium (!)*

# Weight and buoyancy

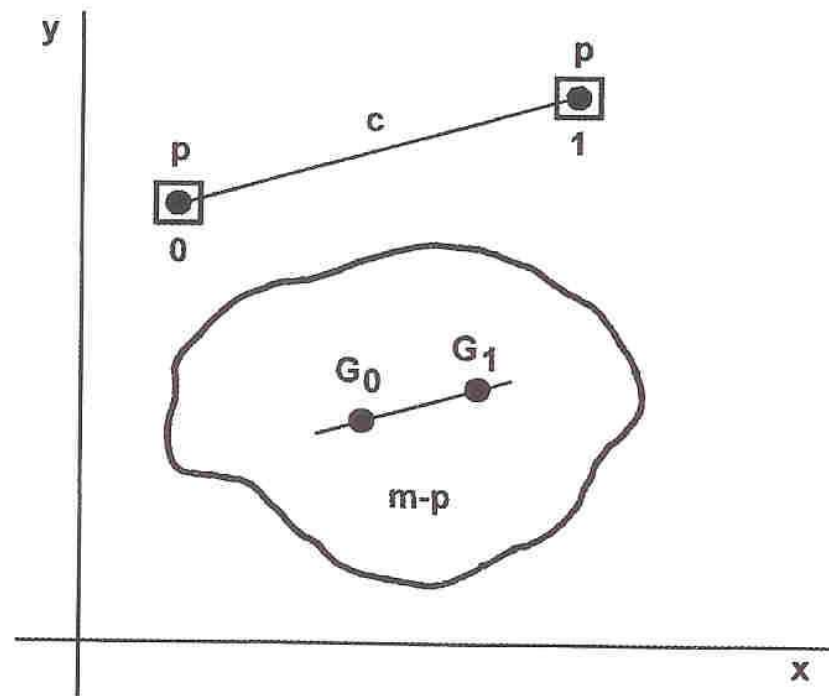


# Heeling Moment



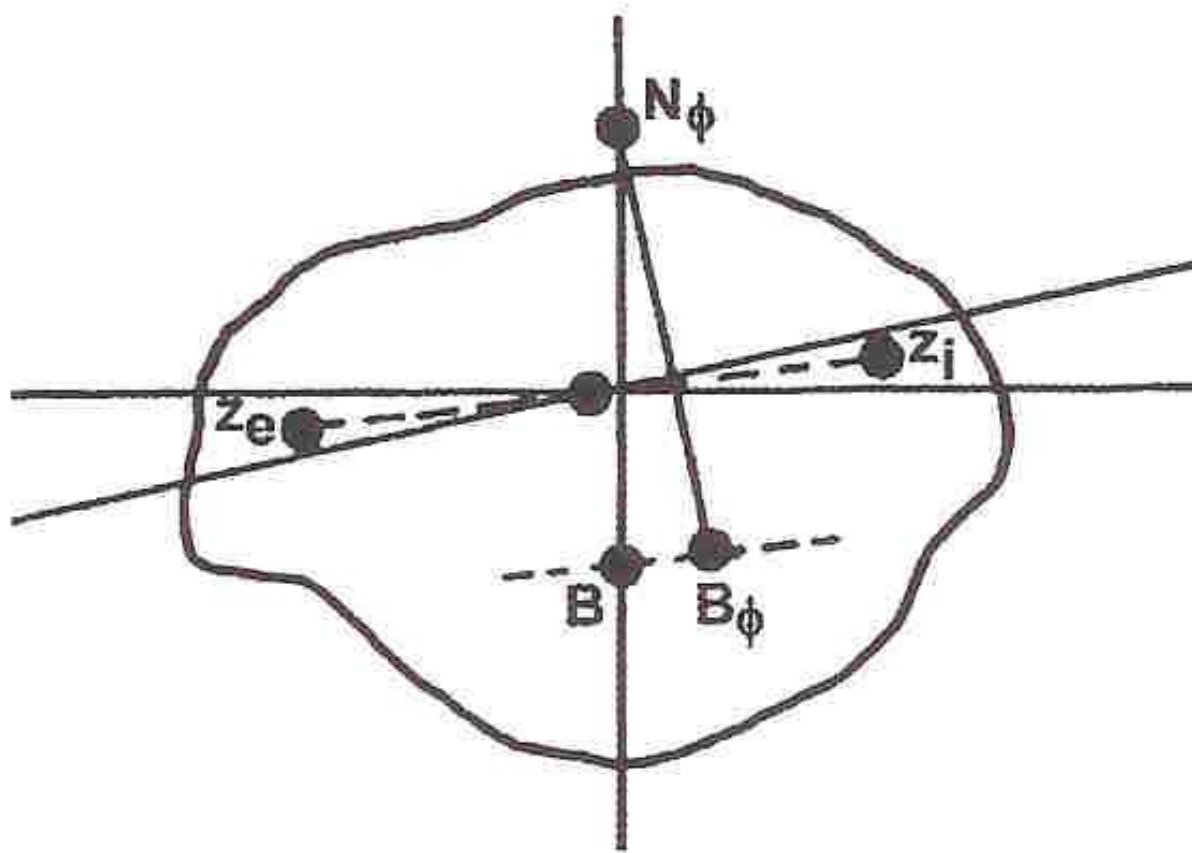
# Shifting loads

$$\overline{G_0G_1} = \frac{p \cdot c}{m}$$





# Shifting buoyancy



# Stabilizing Moment

$$M_S = \rho g \nabla GN_\phi \sin \phi$$

$$= D.GZ$$

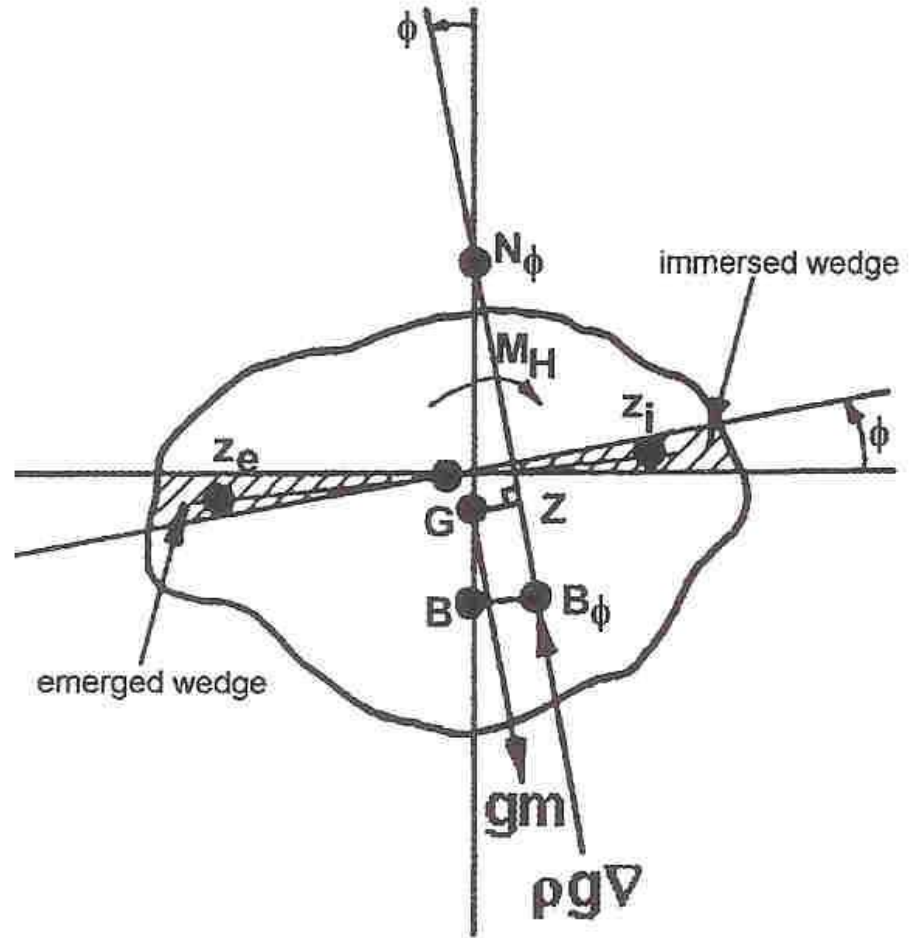
Equilibrium :

$$M_S = M_H$$

Small angle of heel :

$$\sin \phi \approx \phi$$

$$GZ = GN_\phi \cdot \phi = GM \cdot \phi$$



# Stabilizing Moment

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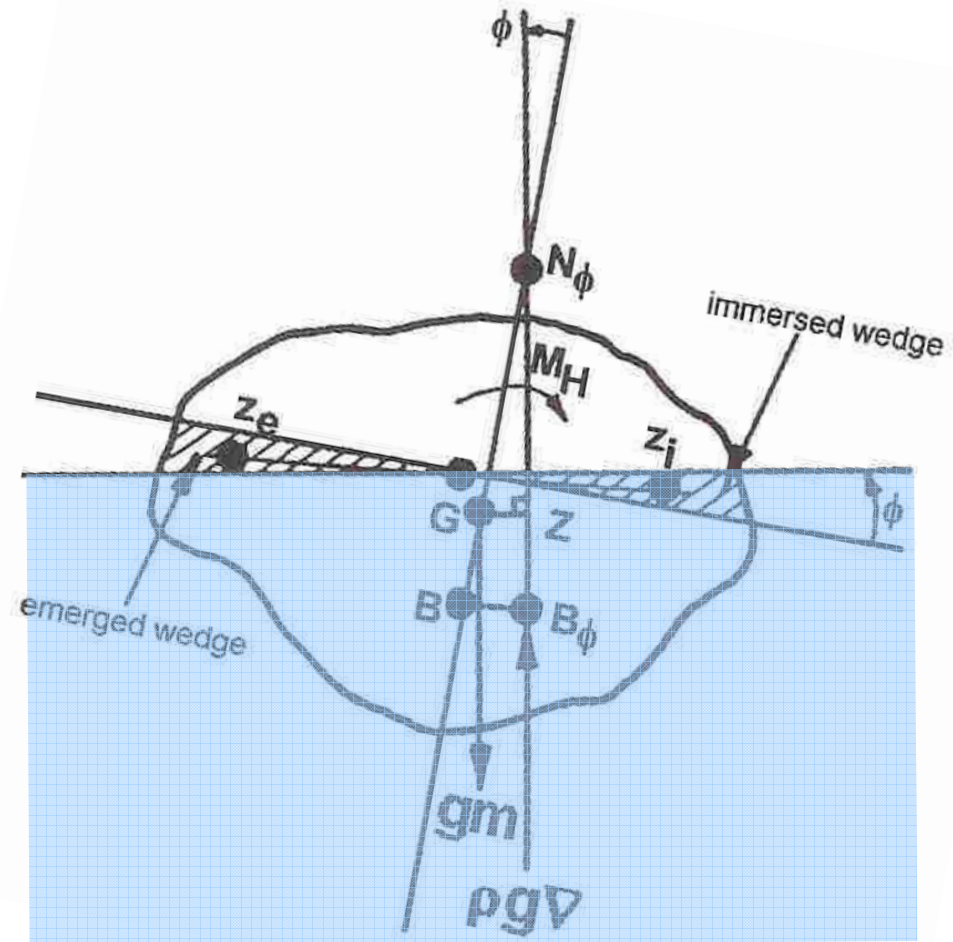
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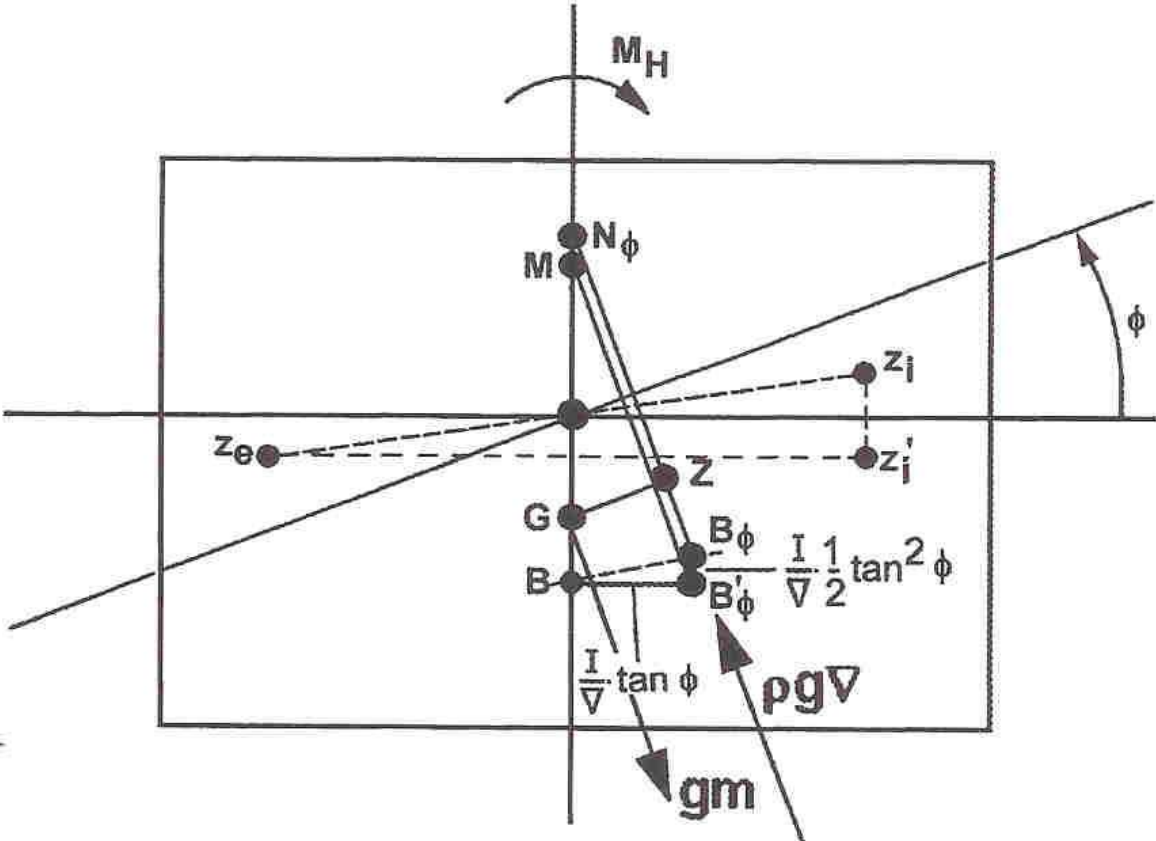
# Rectangular barge

$$\overline{BB'_\phi} = \overline{BM} \cdot \tan \phi$$

$$\boxed{\overline{BM} = \frac{I_T}{\nabla}}$$

$$\overline{B'_\phi B_\phi} = \overline{MN_\phi}$$

$$\boxed{\overline{MN_\phi} = \frac{I_T}{\nabla} \cdot \frac{1}{2} \tan^2 \phi}$$



# Arbitrarily shaped floater

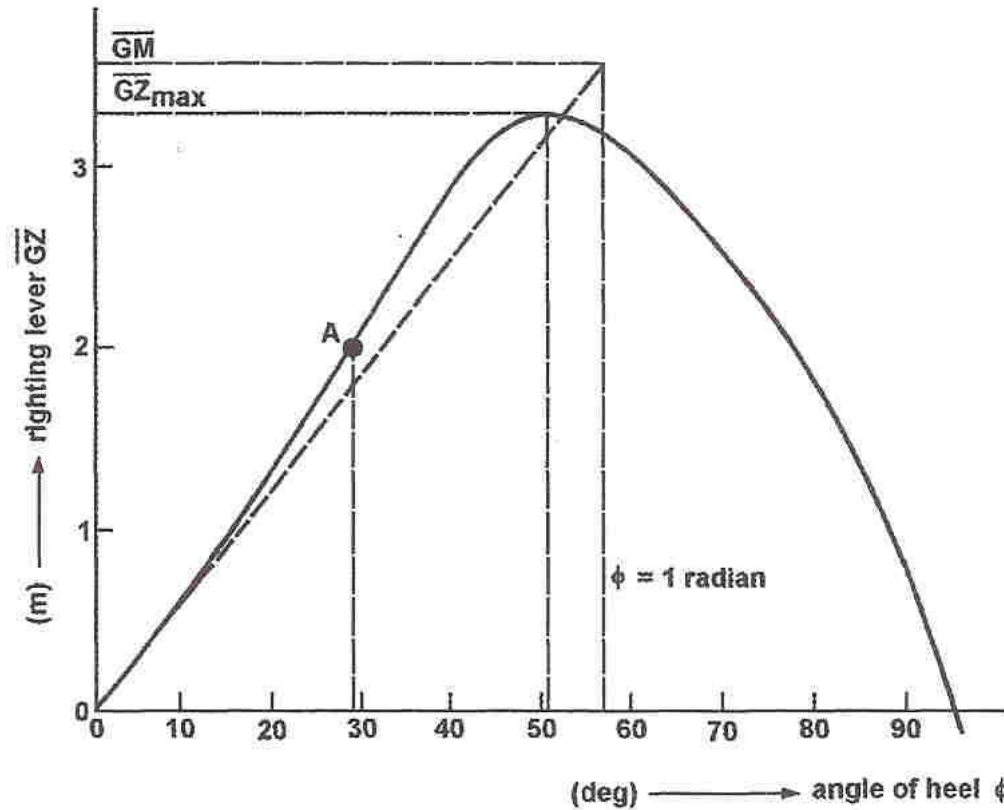
•At very small angles of heel :  $\overline{BM} = \frac{I_T}{\nabla}$

•If side walls are vertical when the unit is floating upright :

$$\overline{BN}_\phi = \frac{I_T}{\nabla} \left(1 + \frac{1}{2} \tan^2 \phi\right) \quad (\text{Scribanti Formula})$$

•Otherwise : compute the position of B in every heeled position

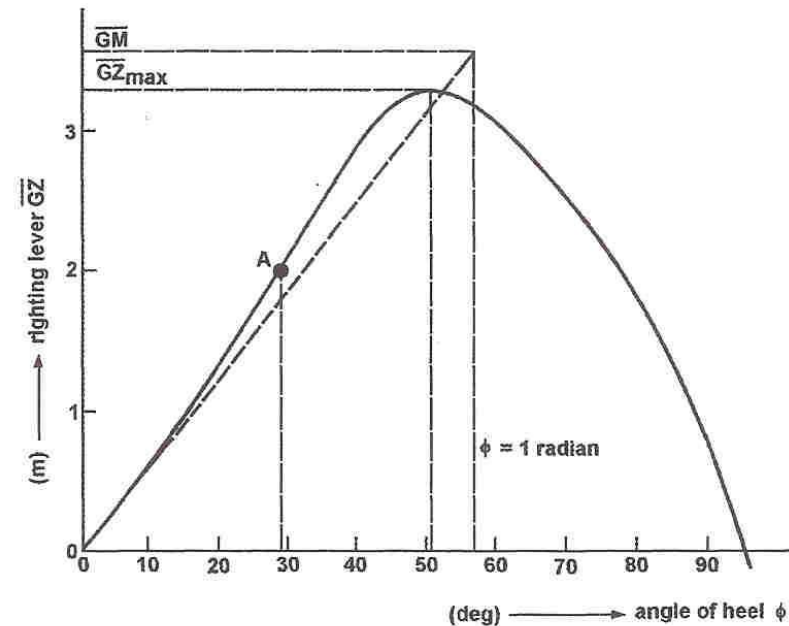
# Static Stability Curve



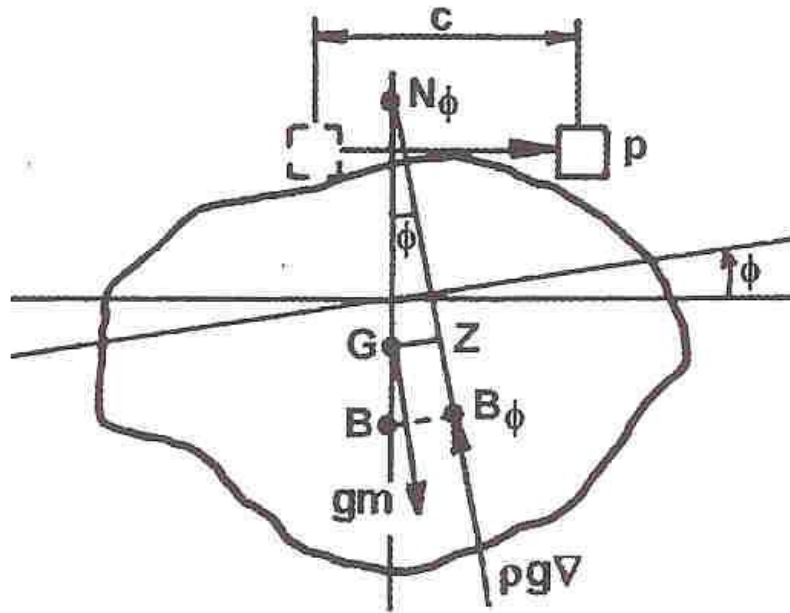
# Static Stability Curve

## Characteristics

- Slope at origin = GM
- Maximum GZ value
- Range of stability
- Angle of deck immersion
- Area under the curve



# Shifting a load



$$\phi = \arccos \left\{ \frac{\rho \nabla \cdot \overline{GN_\phi} \cdot \sin \phi}{p \cdot c} \right\}$$

$$\left[ \frac{1}{2} \overline{BM} \cdot \tan^3 \phi + \overline{GM} \cdot \tan \phi = \frac{p \cdot c}{\rho \nabla} \right]$$



# Liquid loads with free surface

$$\overline{GG''} = \frac{\rho' i}{\rho \nabla} \cdot \left( 1 + \frac{1}{2} \tan^2 \phi \right)$$

