

- Useful formulae:

- $\cos(a + b) = \cos(a) \cdot \cos(b) - \sin(a) \cdot \sin(b)$
- $\sin(a + b) = \sin(a) \cdot \cos(b) + \cos(a) \cdot \sin(b)$

- Surface elevation for regular wave with propagation direction μ
 $\zeta(x, y, t) = \zeta_a \cos(kx \cos(\mu) + ky \sin(\mu) - \omega t)$

- Corresponding undisturbed wave potential for regular wave with propagation direction μ in deep

water: $\phi_0 = \frac{\zeta_a g}{\omega} e^{kz} \sin(kx \cos(\mu) + ky \sin(\mu) - \omega t)$

- Pressure from Bernoulli equation:

- $p = -\rho \frac{\partial \Phi}{\partial t} - \frac{1}{2} \rho (u^2 + w^2) - \rho g z$

- Forces/Moments from integrated pressures:

$$\bar{F} = - \iint_S (p \cdot \bar{n}) dS$$

$$\bar{M} = - \iint_S p \cdot (\bar{r} \times \bar{n}) dS$$

- Undisturbed wave potential for regular wave with propagation direction μ

in deep water: $\phi_0 = \frac{\zeta_a g}{\omega} e^{kz} \sin(kx \cos(\mu) + ky \sin(\mu) - \omega t)$

- Integrated Rayleigh distribution: $P(x > a) = e^{-\frac{a^2}{2m_{ox}}}$

- $e^{-ix} = \cos(x) - i \sin(x)$

- Relation source strength, potential and Green's Function :

$$\frac{\partial \phi_j}{\partial n}(x, y, z, \omega) = \frac{1}{4\pi} \iint_{S_0} \sigma_j(\hat{x}, \hat{y}, \hat{z}, \omega) \cdot \frac{\partial G}{\partial n}(x, y, z, \hat{x}, \hat{y}, \hat{z}, \omega) dS_0$$

- Internal shear vertical shear force:

$$Q(x_1) = \int_{stern}^{x_1} -F'_{w3}(x_b) - X'_{h3}(x_b) + m' \cdot (\ddot{z} + \ddot{\phi} \cdot y_m' - \ddot{\theta} \cdot x_b) dx_b$$

$$= \int_{stern}^{x_1} -q_z(x_b) + m' \cdot (\ddot{z} + \ddot{\phi} \cdot y_m' - \ddot{\theta} \cdot x_b) dx_b$$

- Internal bending moment:

$$M(x_1) = x_1 \cdot Q(x_1) + \int_{stern}^{x_1} x_b \cdot (q_z - m' \cdot (\ddot{z} + \ddot{\phi} \cdot y_m' - \ddot{\theta} \cdot x_b)) dx_b$$

NB: make sure you know how to determine the distributed load q_z !