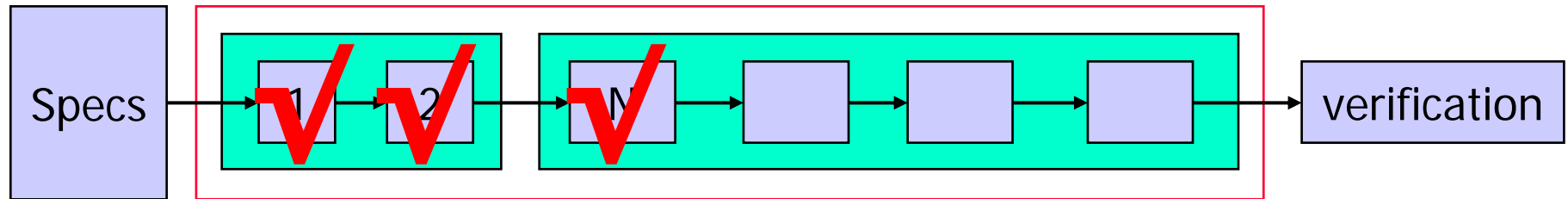


# Structured Electronic Design

Building the nullor: **Distortion**



Topology

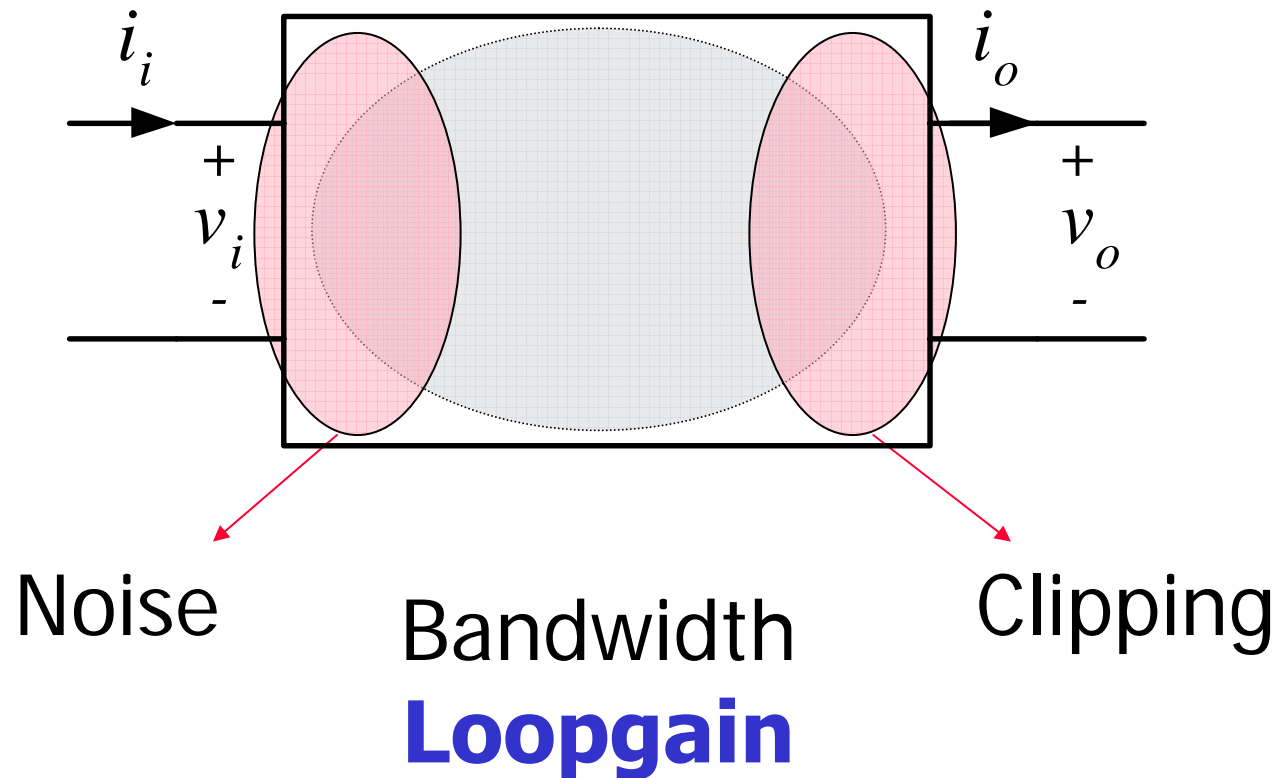
Best nullor implementation

Voltage and current swing

Power consumption

**FINAL** Noise level

All stages maximal gain (CE CS)  
Most orthogonal order: N, D, B



bandwidth – noise – distortion

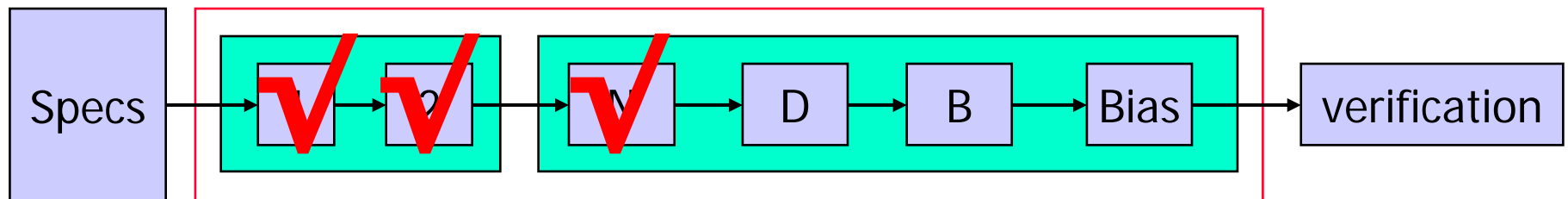
bandwidth – distortion - noise

noise - bandwidth – distortion

noise – **distortion** - bandwidth

distortion - noise – bandwidth

distortion – bandwidth - noise



When optimizing bandwidth:

Small-signal models (no non-linearity)

No noise

When optimizing noise behavior:

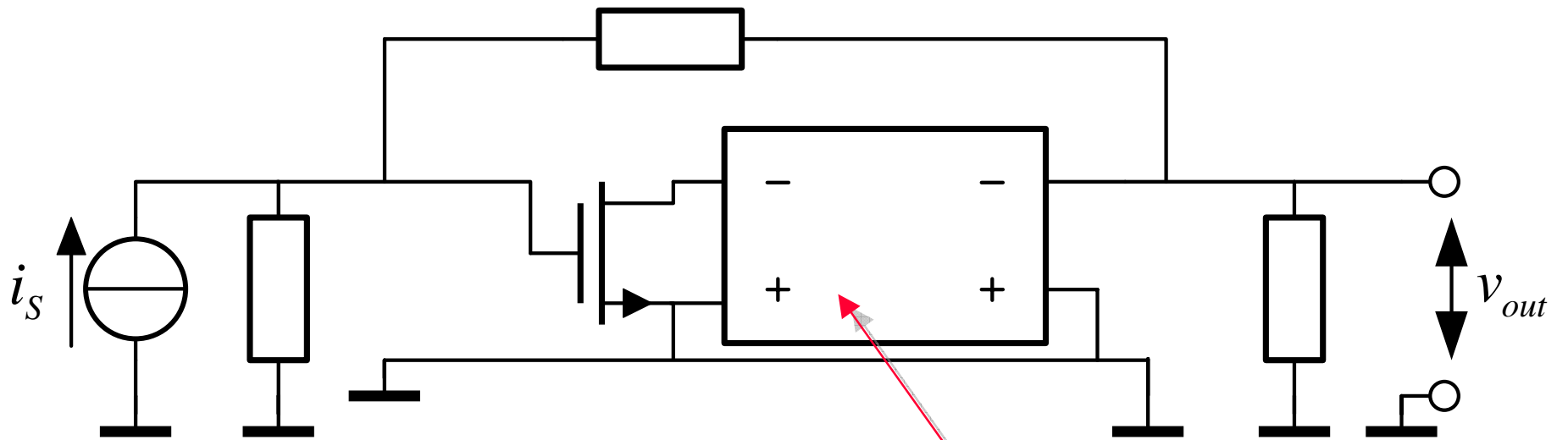
Small-signal models (no non-linearity)

No bandwidth details

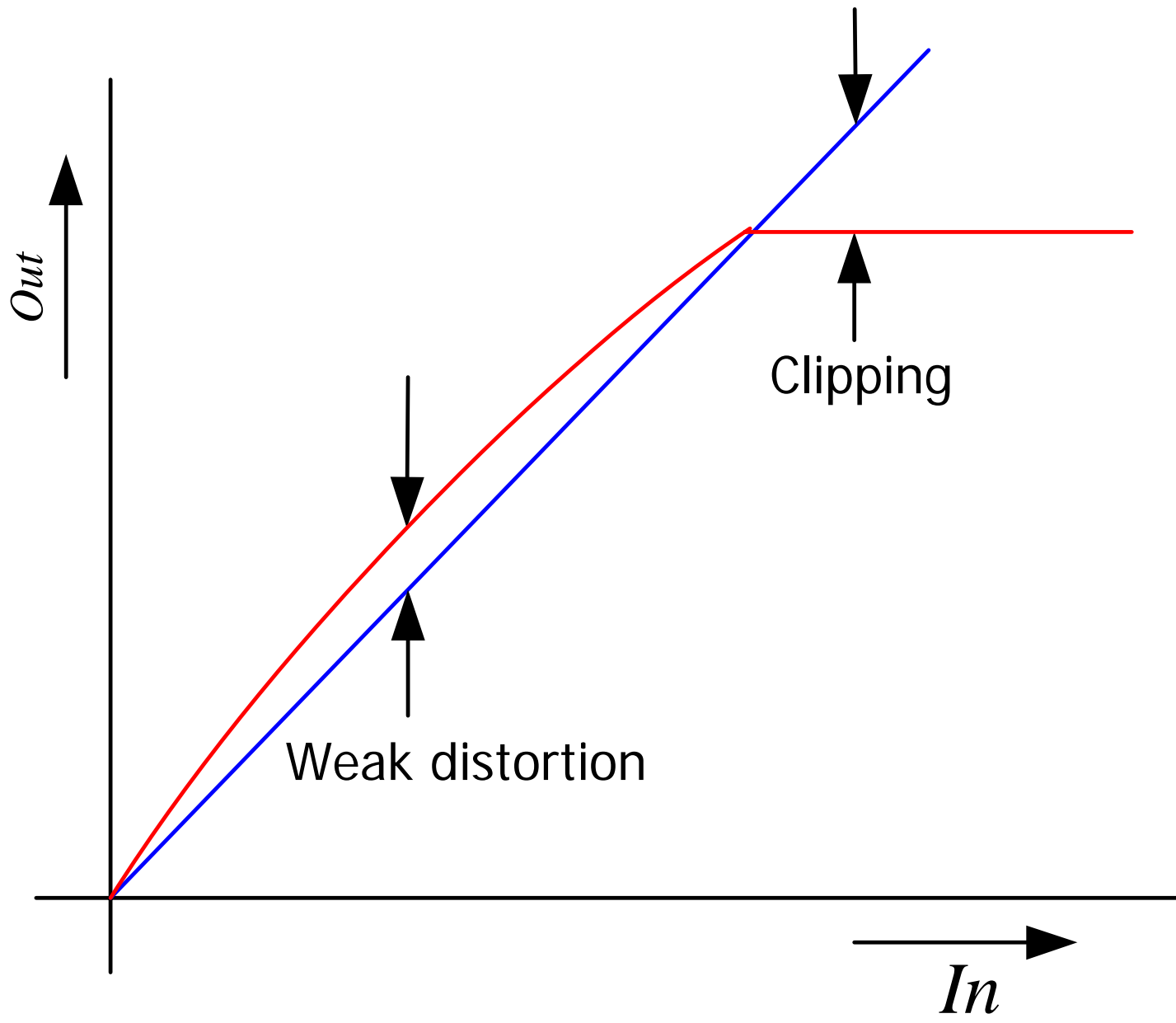
**When optimizing non-linear behavior:**

**No dynamic effects**

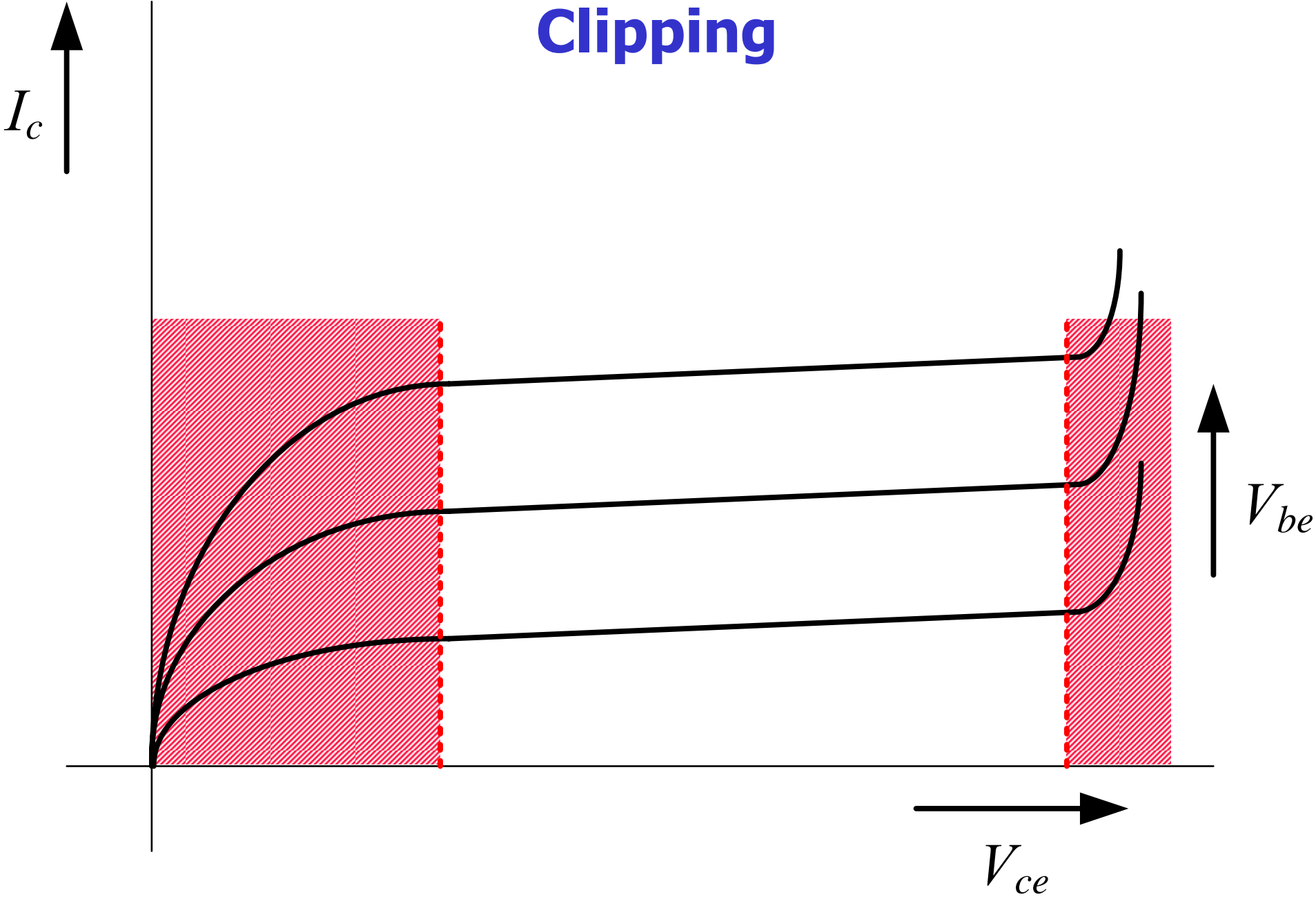
**No noise**



Non-dynamic active circuit  
(Not a nullor anymore)

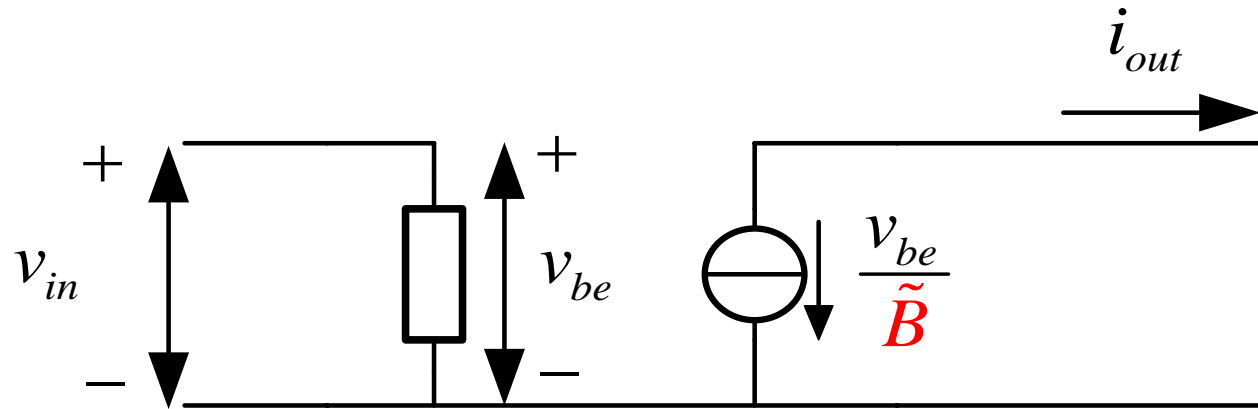


# Clipping





# Weak distortion

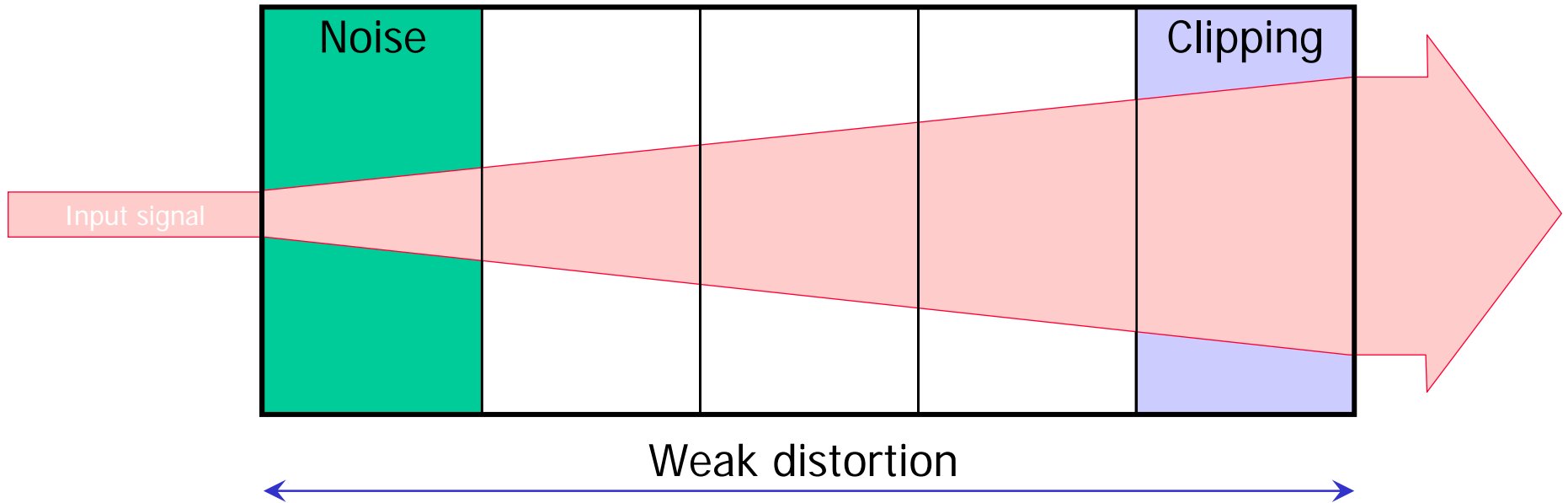


**Simplest model that suffices**

$$i_{out} = -I_s \left( e^{\frac{v_{in}}{V_T}} - 1 \right)$$

$$V_T = \frac{kT}{q}$$

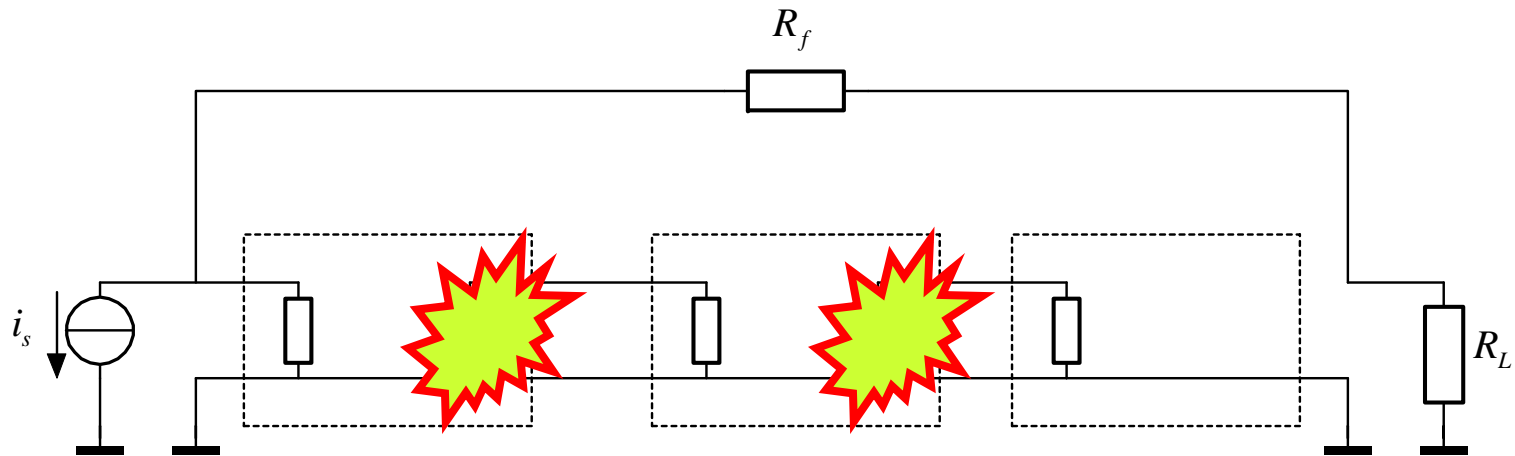
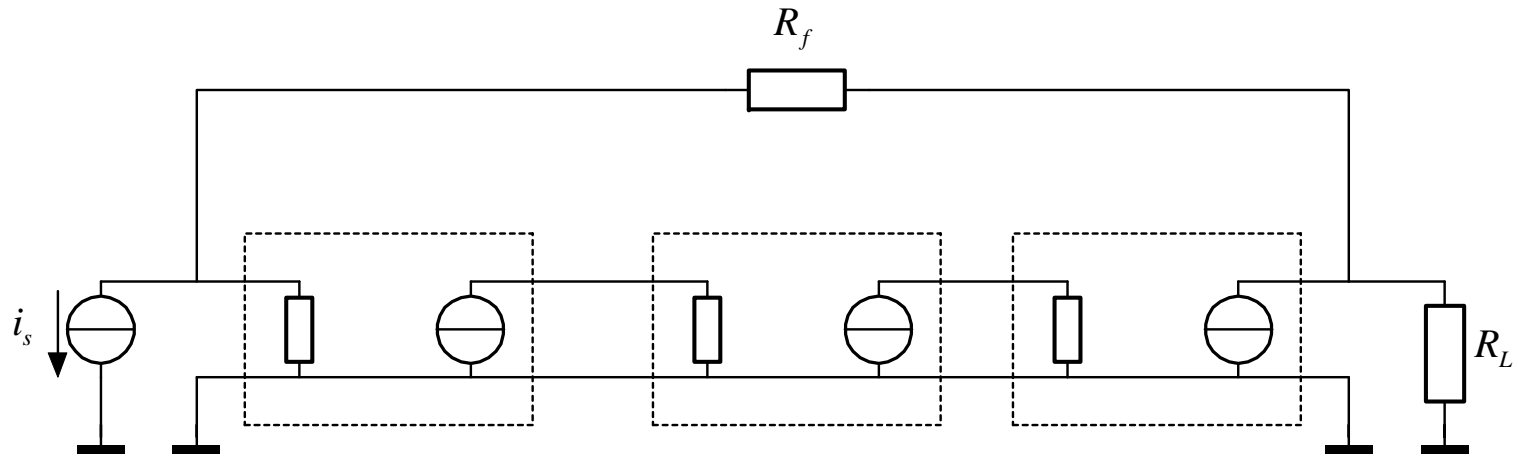
# Strategy



**2 distortion types**

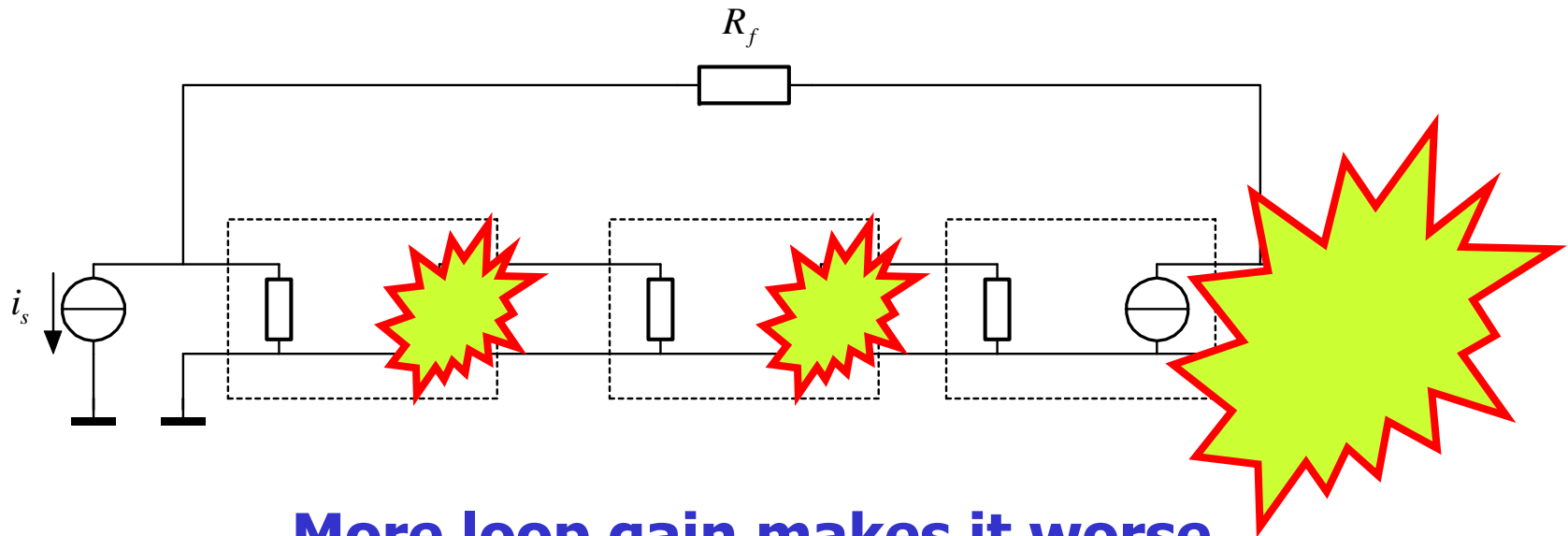
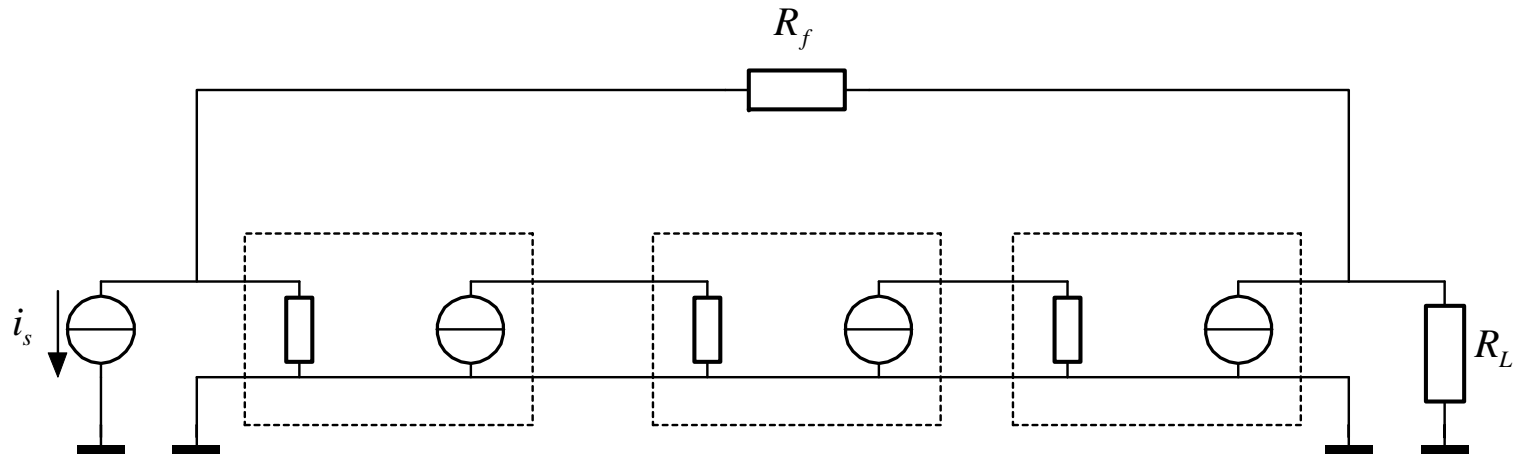
**Completely different approach**

# Clipping breaks the loop



**More loop gain does not repair this**

# Clipping breaks the loop



**More loop gain makes it worse**

# Strategy

Clipping breaks the loop

**local** problem

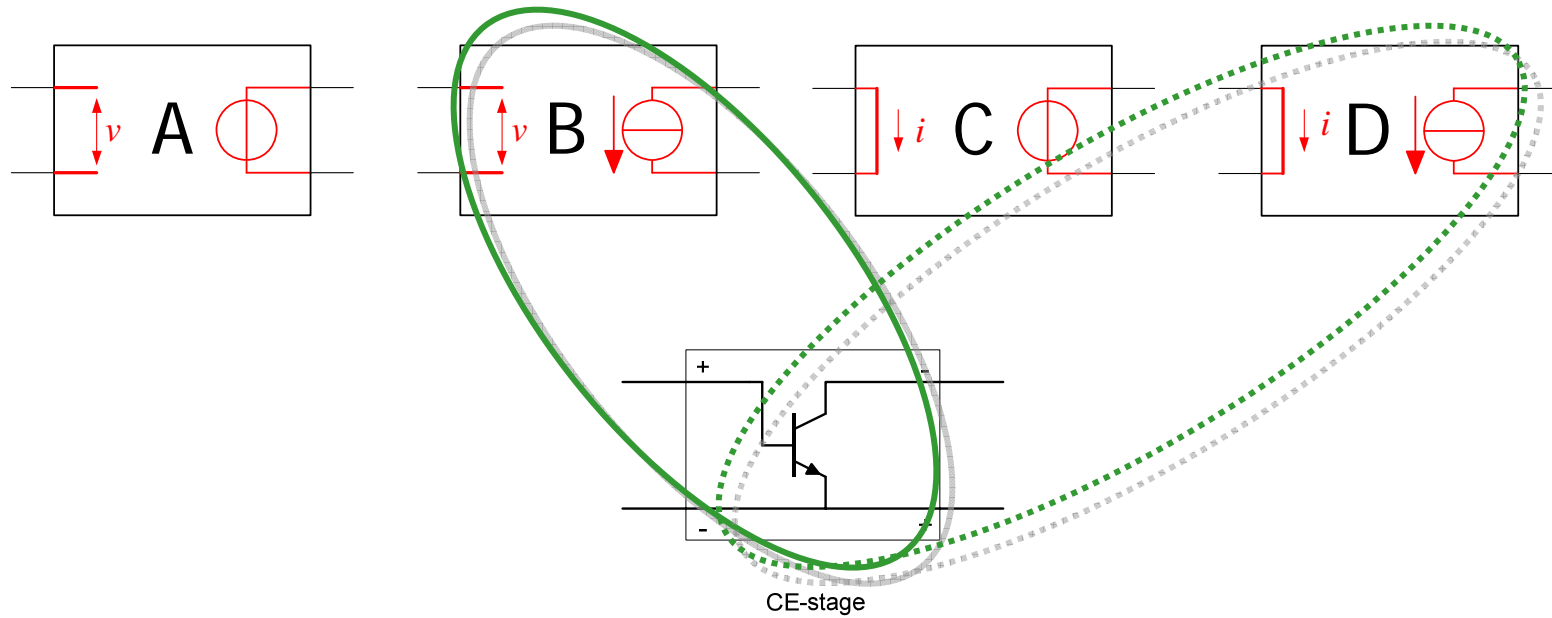
**local** solution

Weak distortion does not break the loop

can be in **any stage**

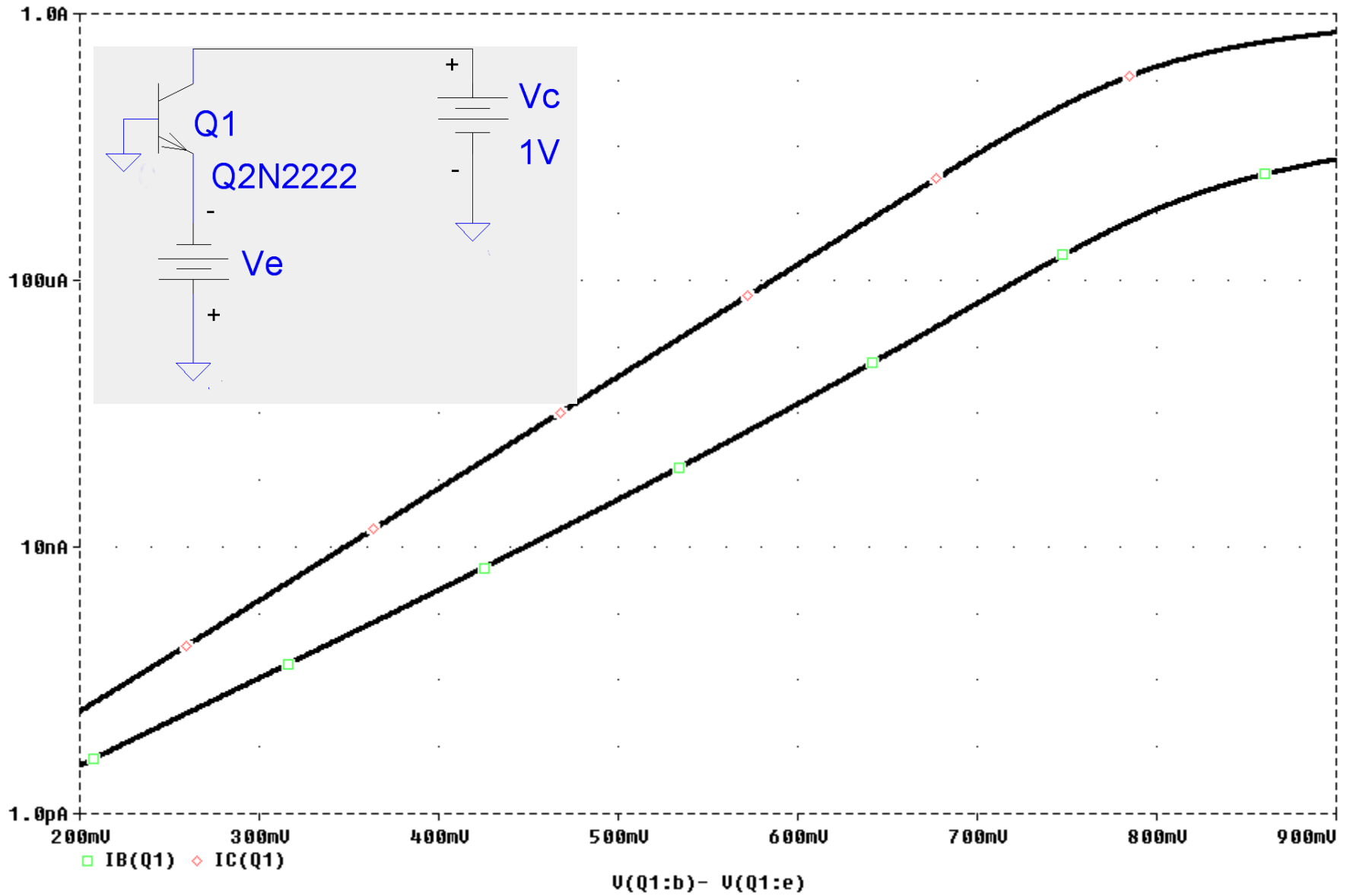
reduced by **the loop** (everywhere)

# The bipolar transistor model

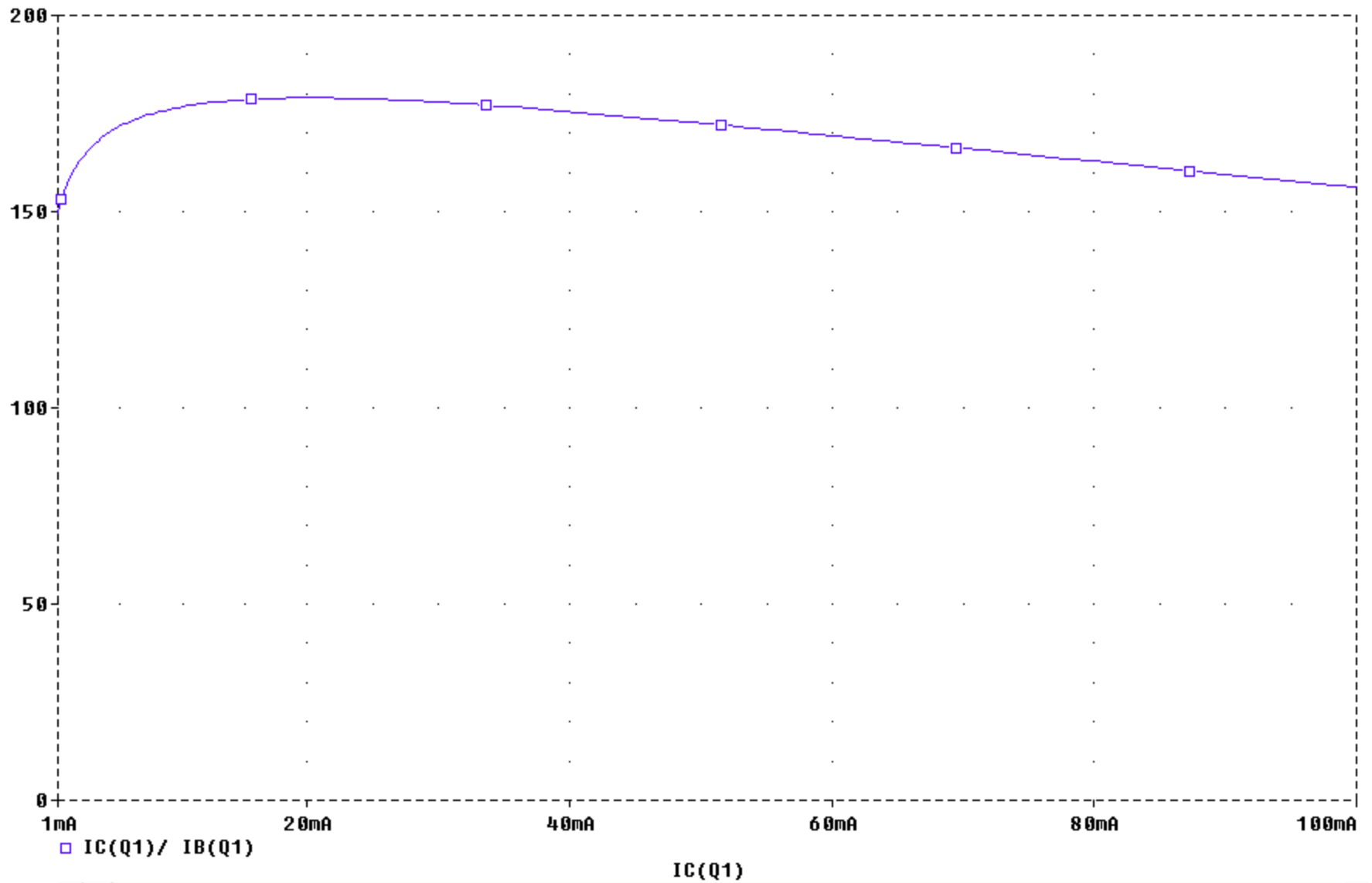


$$\begin{pmatrix} \tilde{A} & \tilde{B} \\ \tilde{C} & \tilde{D} \end{pmatrix}$$

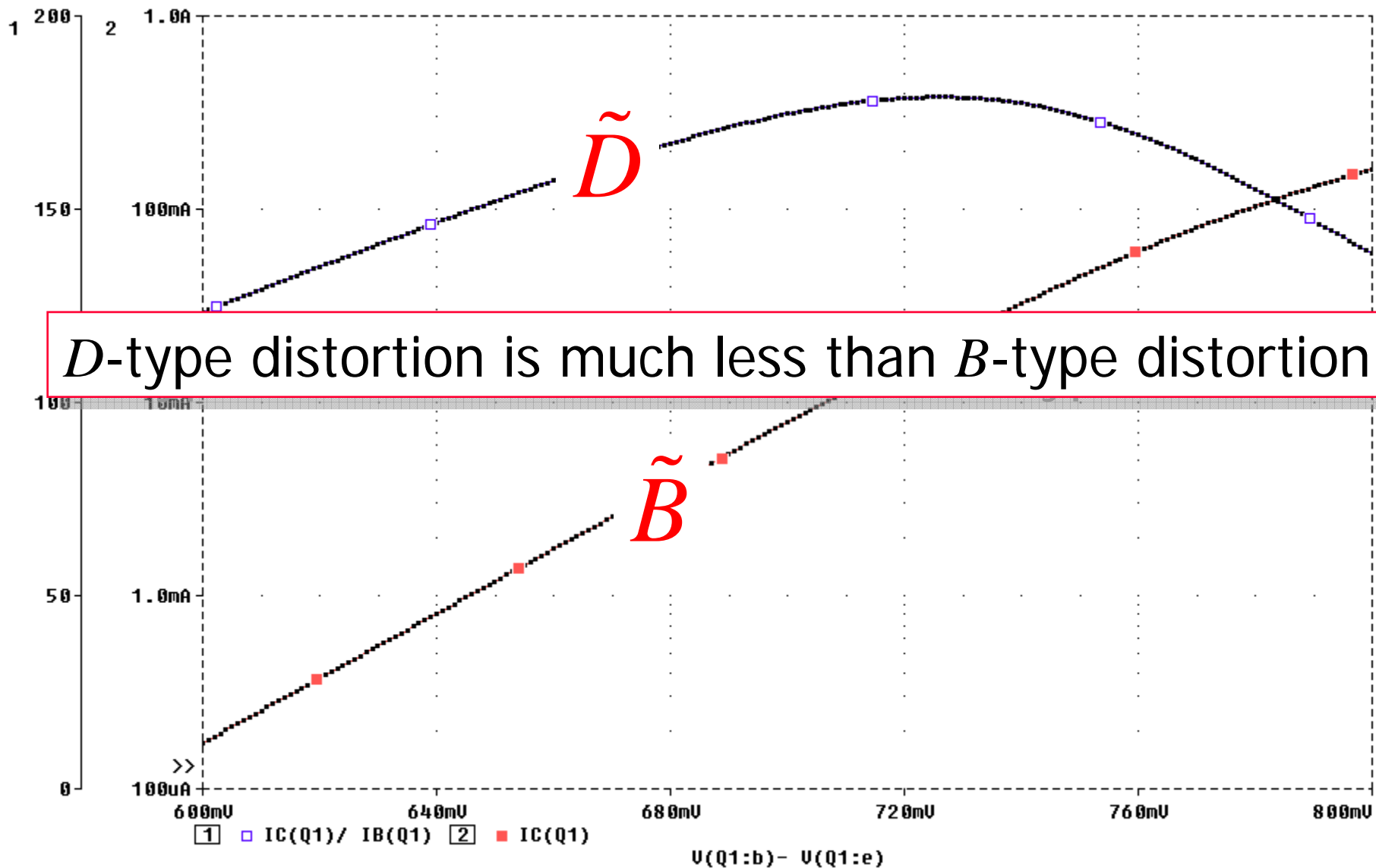
# Simulation of $B$



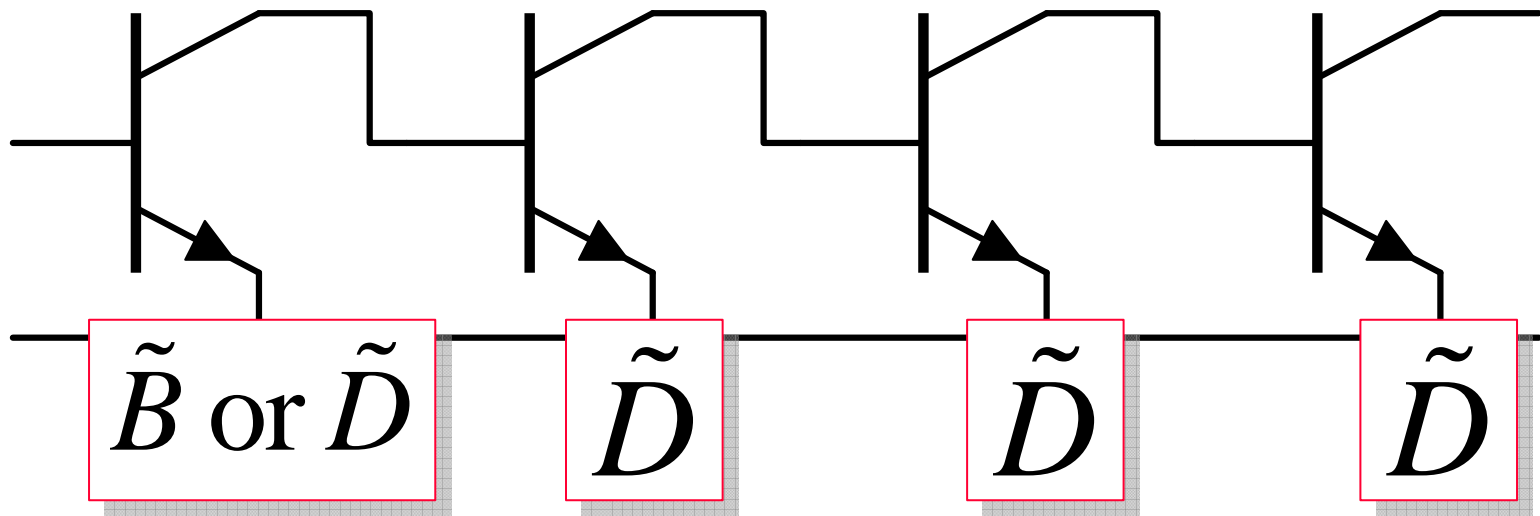
# Simulation of $D$



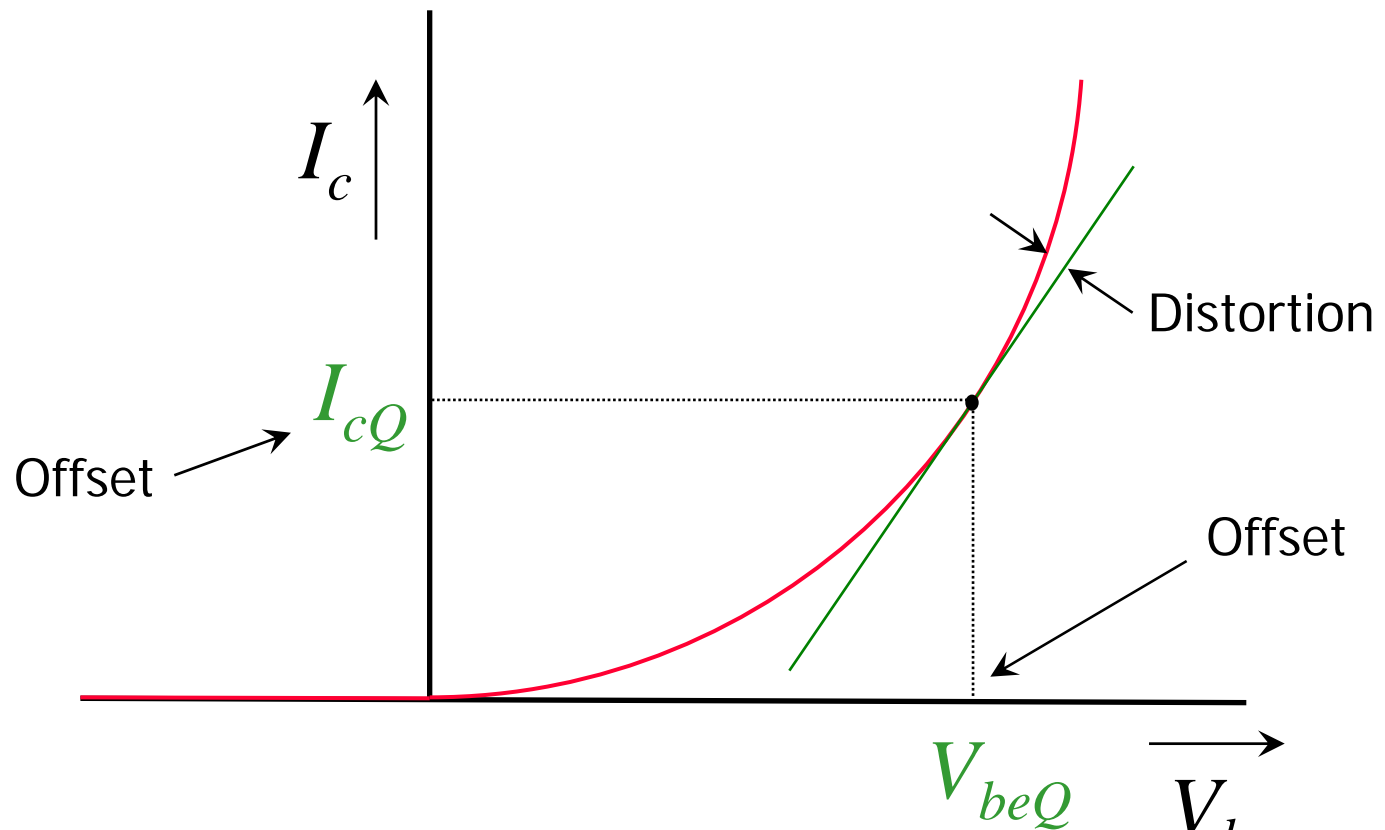




# Location

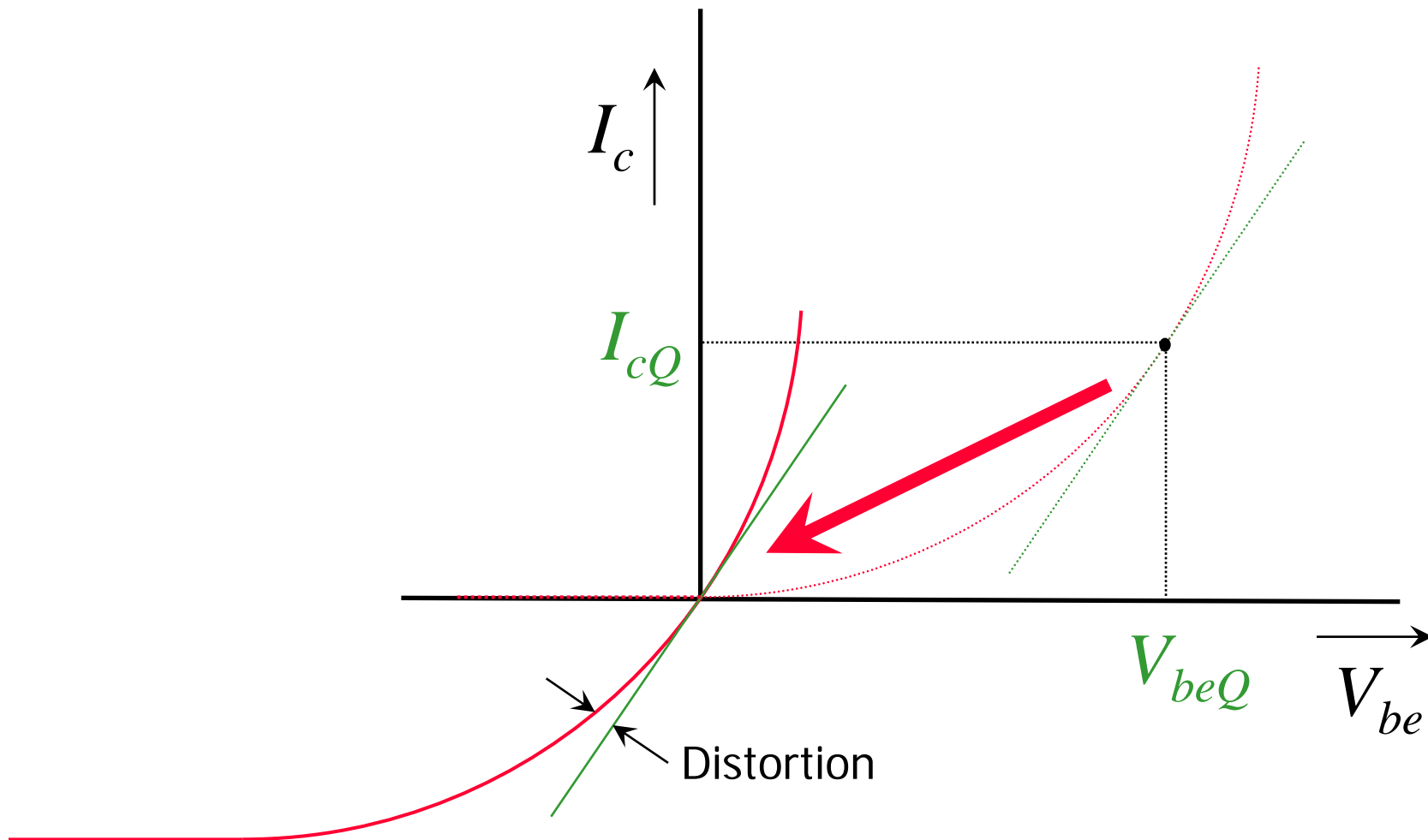


# Select a suitable tangent



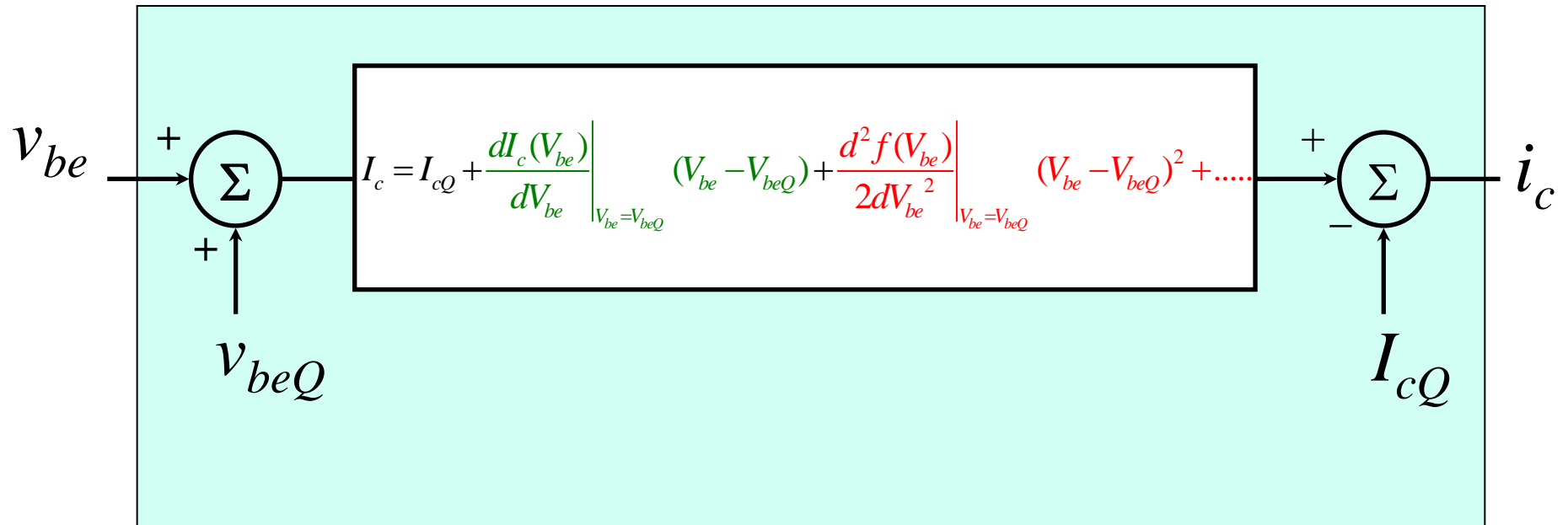
$$I_c = I_{cQ} + \left. \frac{dI_c(V_{be})}{dV_{be}} \right|_{V_{be}=V_{beQ}} (V_{be} - V_{beQ}) + \left. \frac{d^2 f(V_{be})}{2dV_{be}^2} \right|_{V_{be}=V_{beQ}} (V_{be} - V_{beQ})^2 + \dots$$

# Translation to the origin (Biasing)

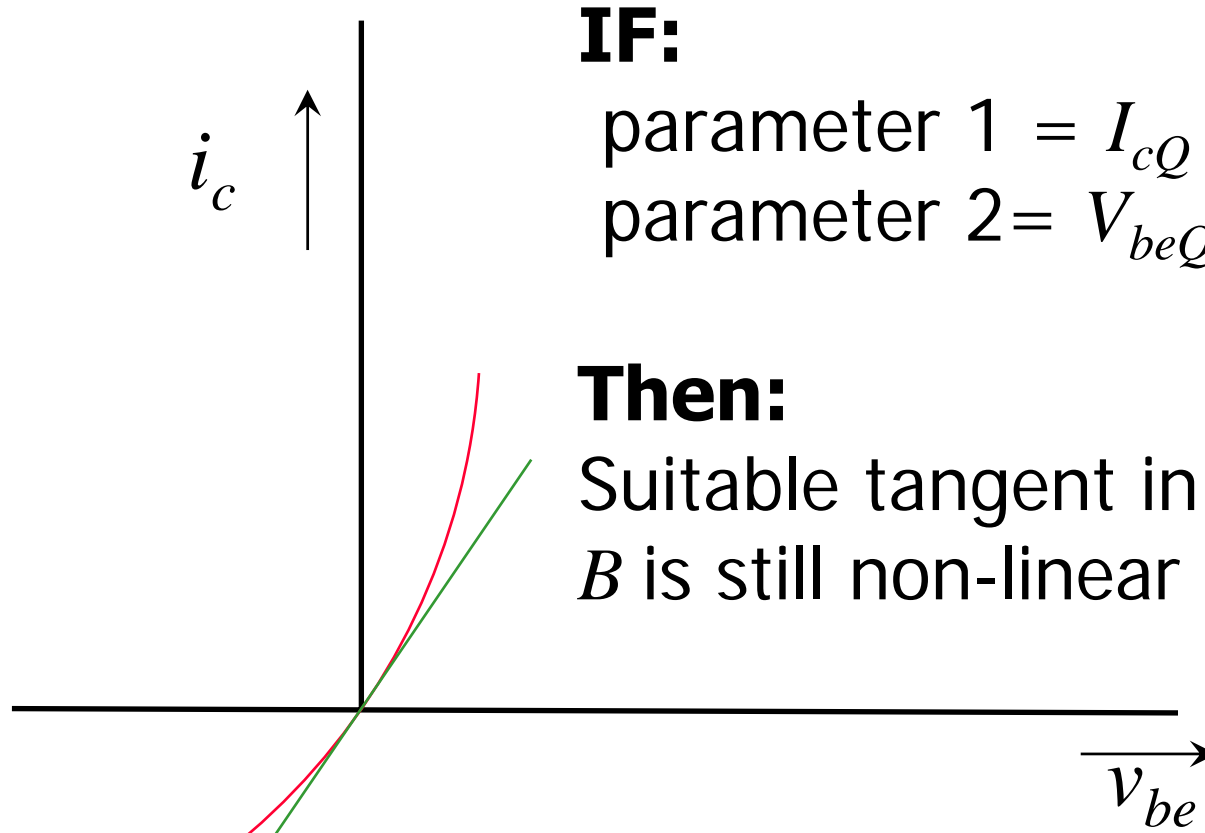


# Adding and subtracting offsets = Biasing

$$i_c = \frac{1}{B_{V_{beQ}}} v_{in} + \left. \frac{d^2 f(V_{be})}{2dV_{be}^2} \right|_{V_{be}=V_{beQ}} v_{be}^2 + \dots$$



# Bias parameters for transfer $B$



**IF:**

parameter 1 =  $I_{cQ}$

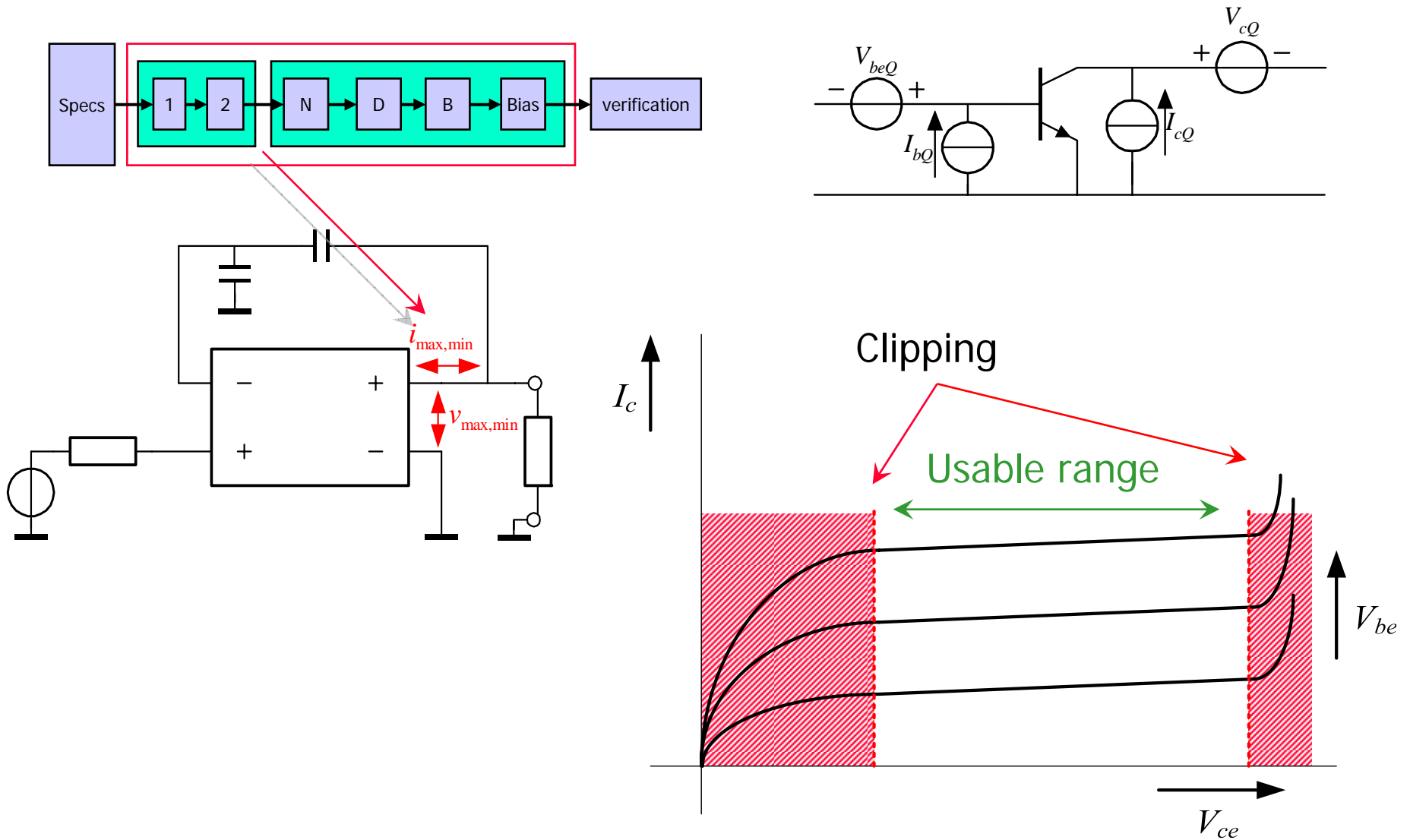
parameter 2 =  $V_{beQ}$

**Then:**

Suitable tangent in origin  
 $B$  is still non-linear

$$i_c = \frac{1}{B_{V_{beQ}}} v_{be} + \left. \frac{d^2 f(V_{be})}{2dV_{be}^2} \right|_{V_{be}=V_{beQ}} v_{be}^2 + \dots$$

# More bias parameters



# 4 bias parameters

**IF:**

*parameter 1* =  $I_{cQ}$

*parameter 2* =  $V_{beQ}$

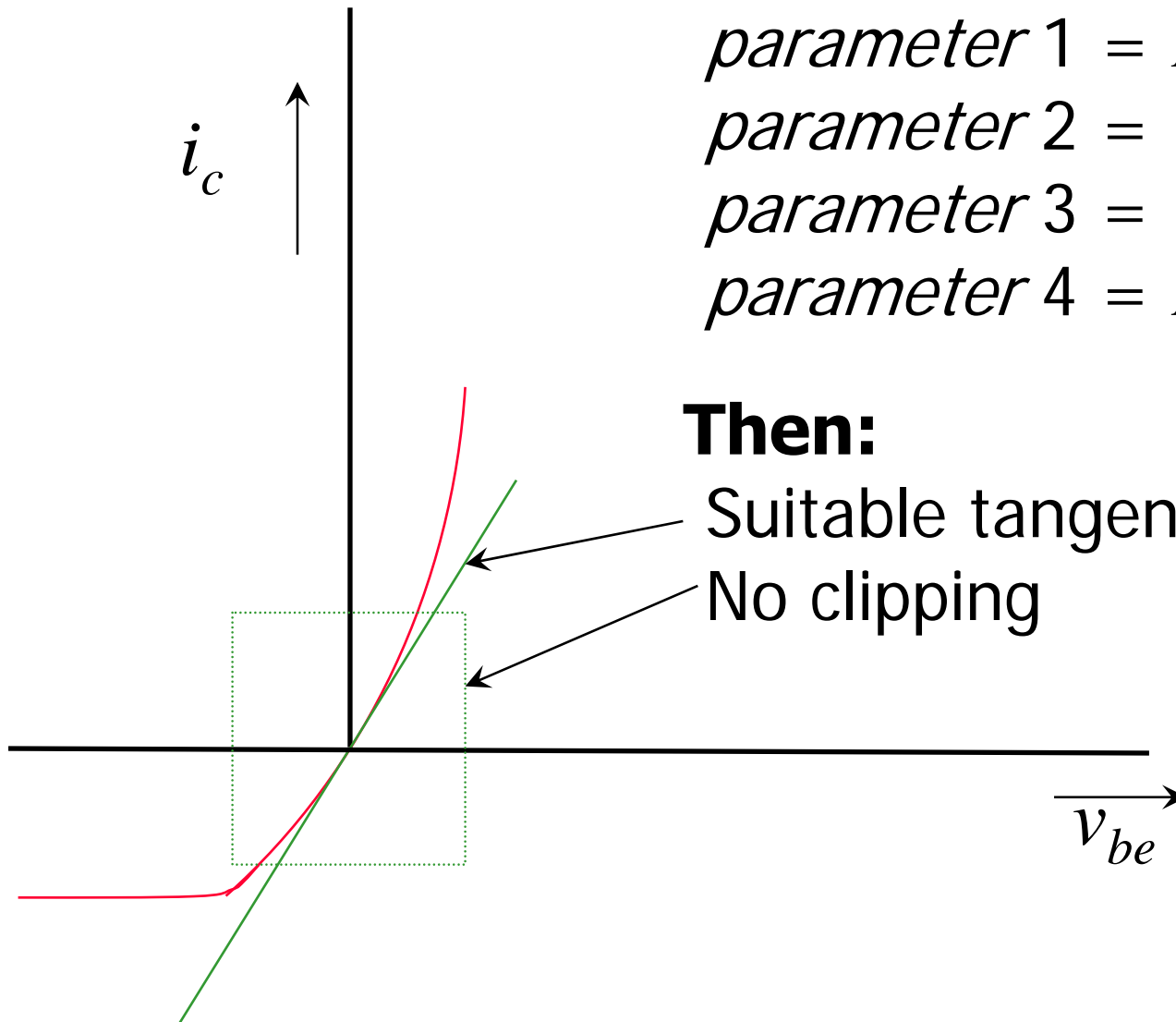
*parameter 3* =  $V_{cQ}$

*parameter 4* =  $I_{bQ}$

**Then:**

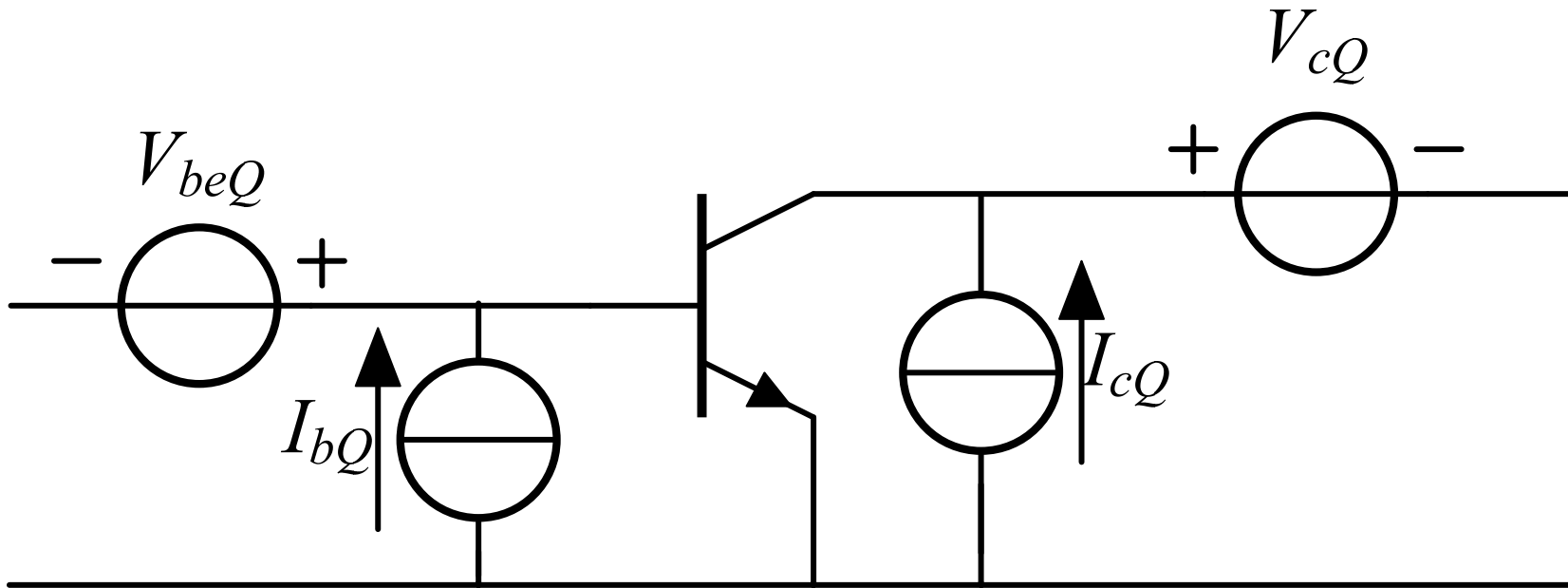
Suitable tangent in origin

No clipping





## 4 bias sources needed for the translations



Implementation will be **done later** in the biasing step

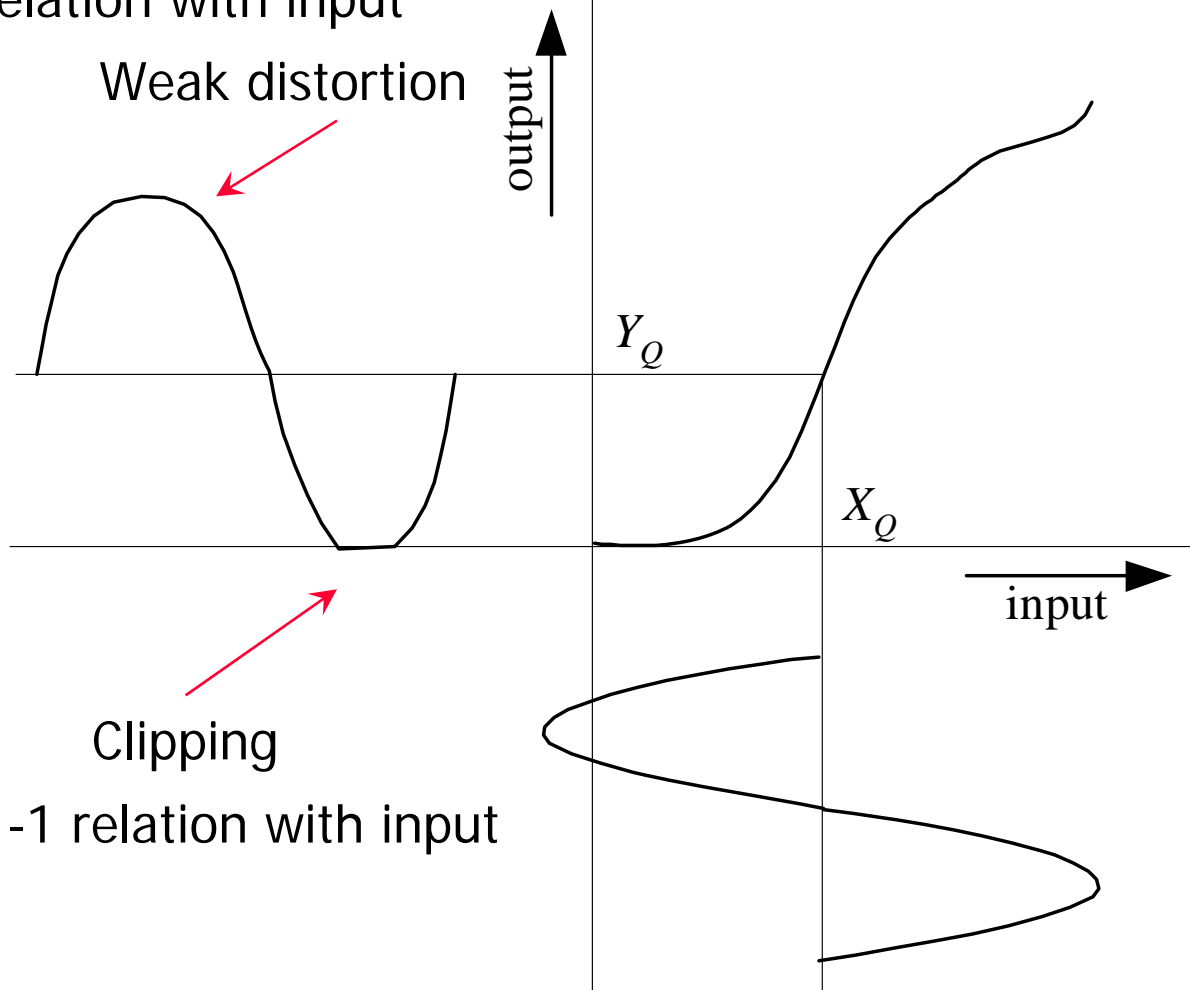
Now biasing quantities are **just parameters**

Biasing does **not** make the circuit linear

# Summary : Clipping and weak distortion

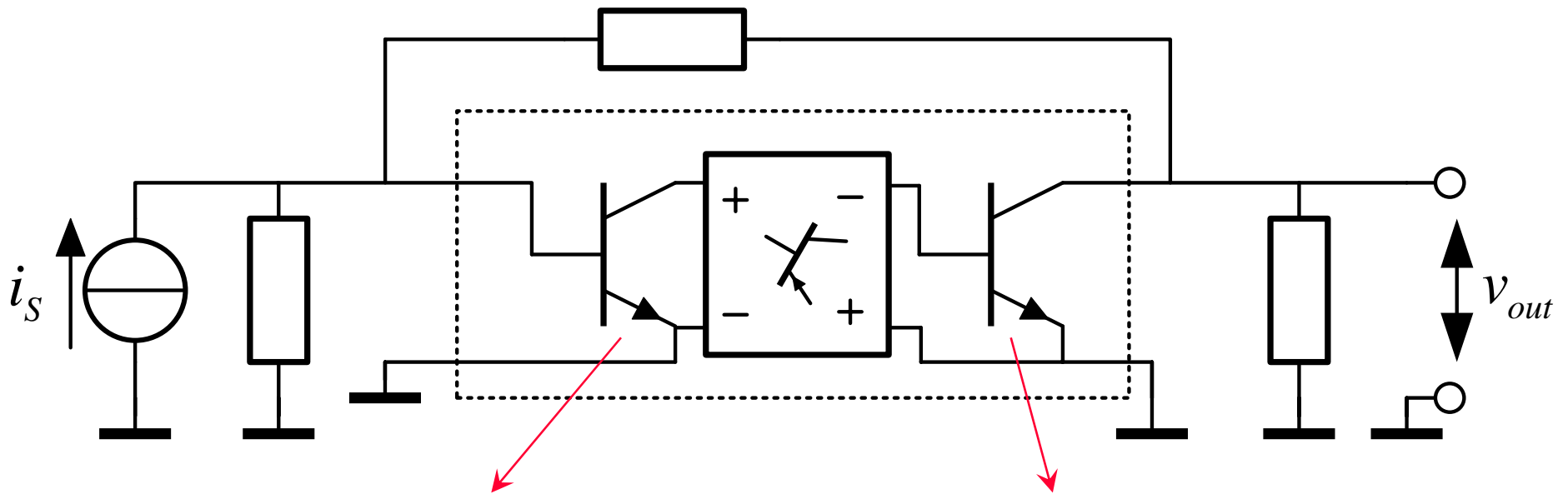
Still 1-1 relation with input

Weak distortion



# Design the last stage: clipping

$V_{beQ}$  and  $I_{bQ}$  not independent



$$V_{cQ} \Rightarrow V_{\min} < v_c < V_{\max}$$

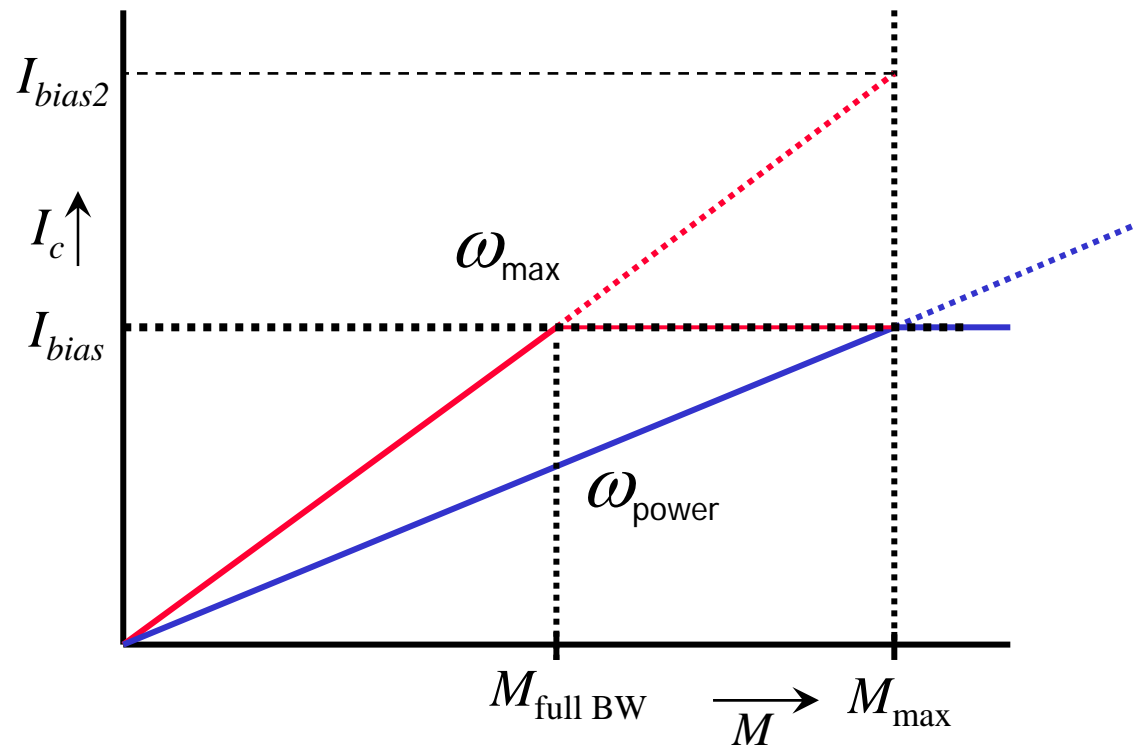
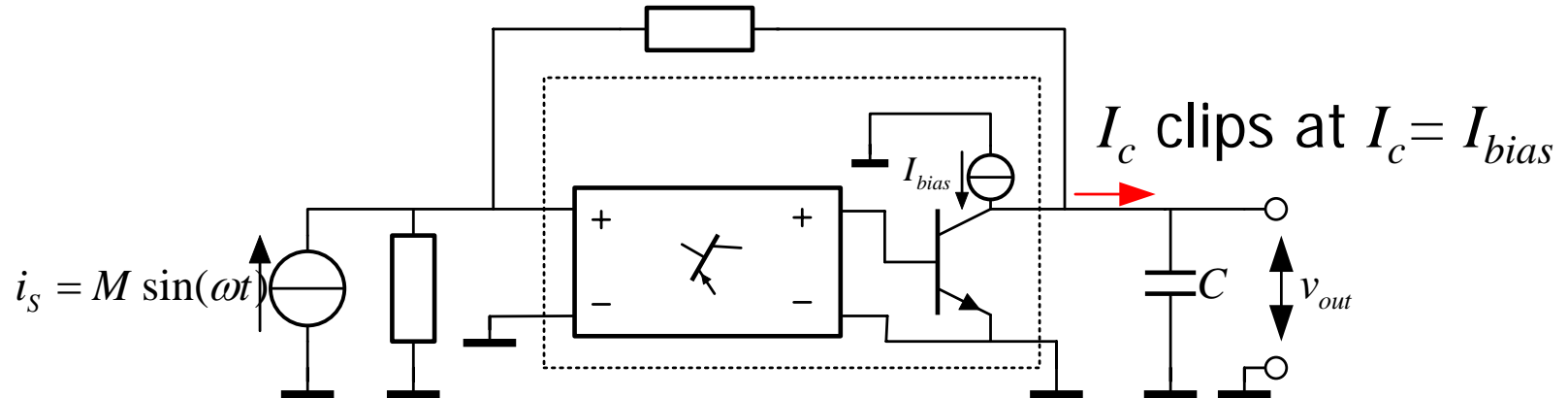
$$I_{cQ} \Rightarrow I_{\min} < i_c < I_{\max}$$

Slewing

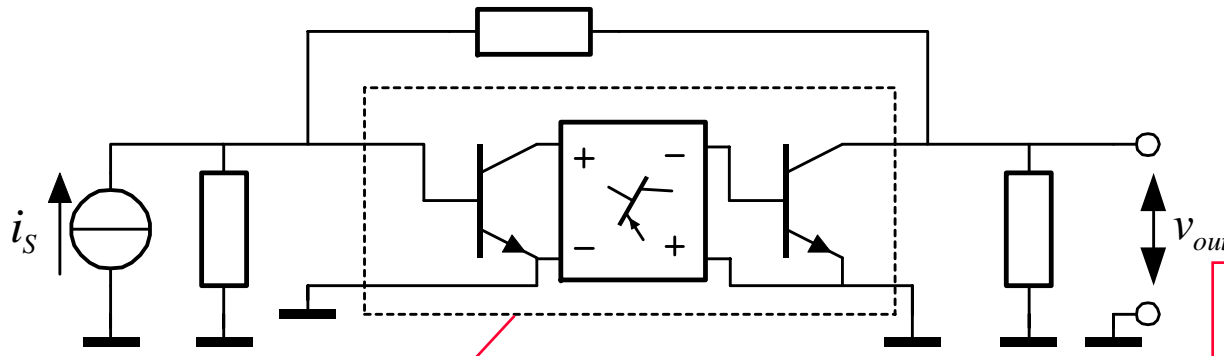
$$V_{cQ} \Rightarrow V_{\min} < v_c < V_{\max}$$

$$I_{cQ} \Rightarrow I_{\min} < i_c < I_{\max}$$

# Power bandwidth $\omega_{\max} > \omega_{\text{power}}$



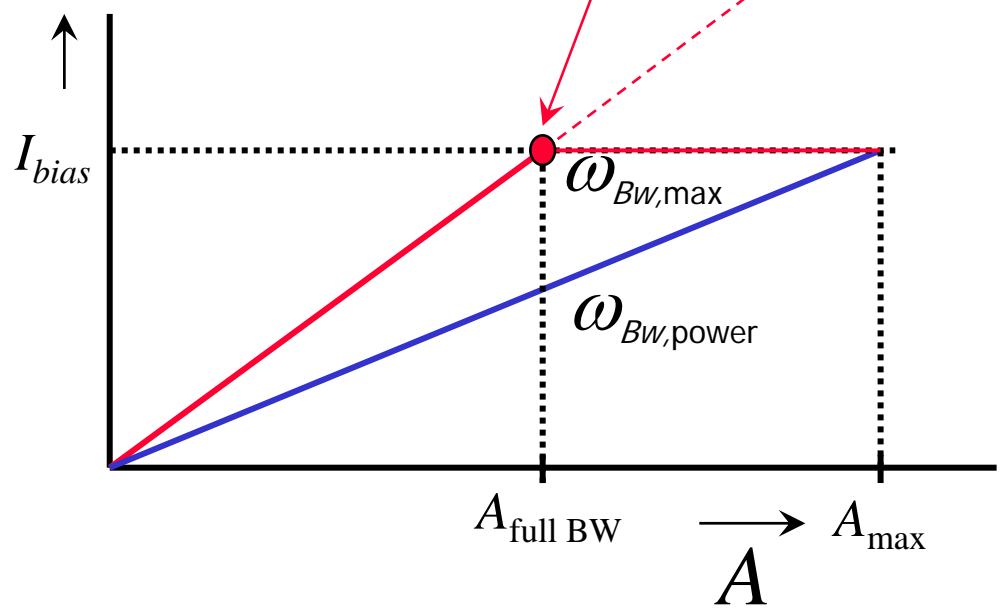
# Check all stages



Can be verified with small-signal models (AC analysis)

$$V_{cQ} \Rightarrow V_{\min} < v_c < V_{\max}$$

$$I_{cQ} \Rightarrow I_{\min} < i_c < I_{\max}$$



## Conclusions: Clipping

The loop is broken!

**Loop gain does not help** (Disaster)

Can only be prevented locally

### **Last stage large gain**

Clipping in last stage

Dominant criterion for last stage

Dominant influence on power consumption

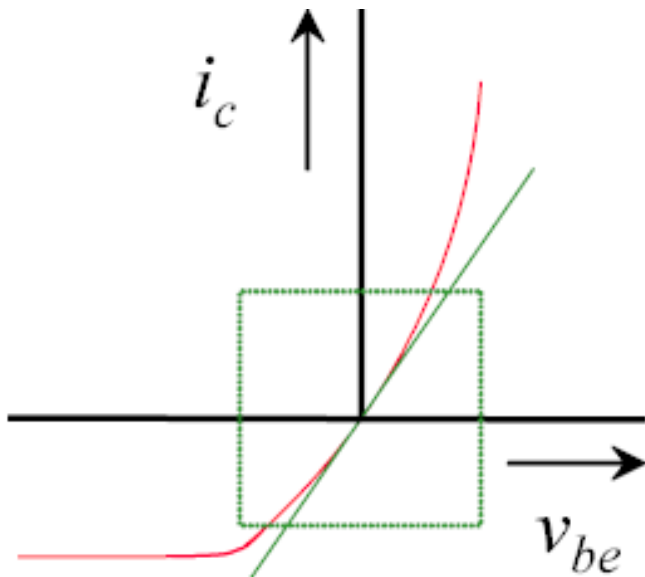
Clipping of other stages should not be a problem

# Weak distortion

Proper bias signals added (no offsets)

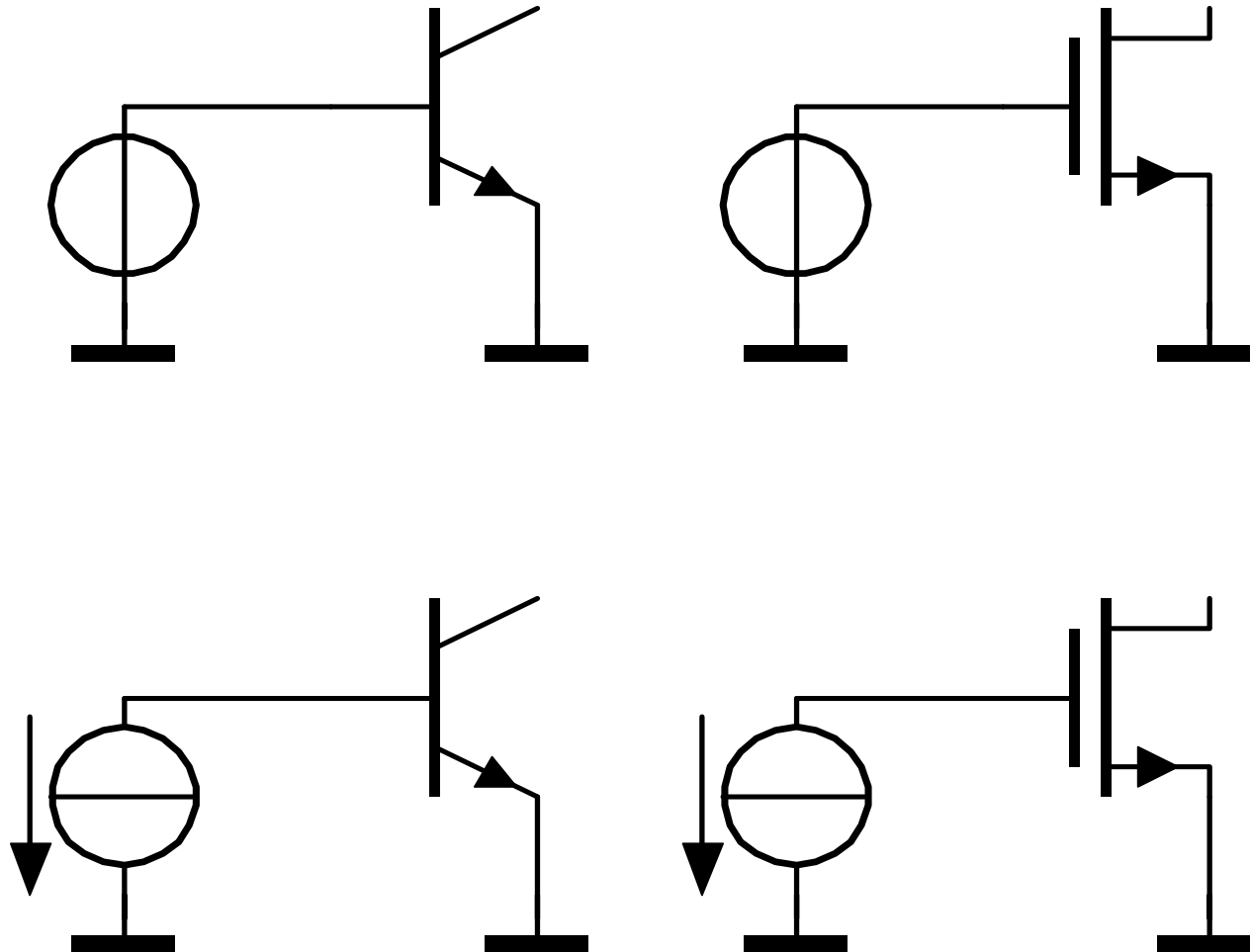
**No** clipping

Small distortion components → Third order is enough



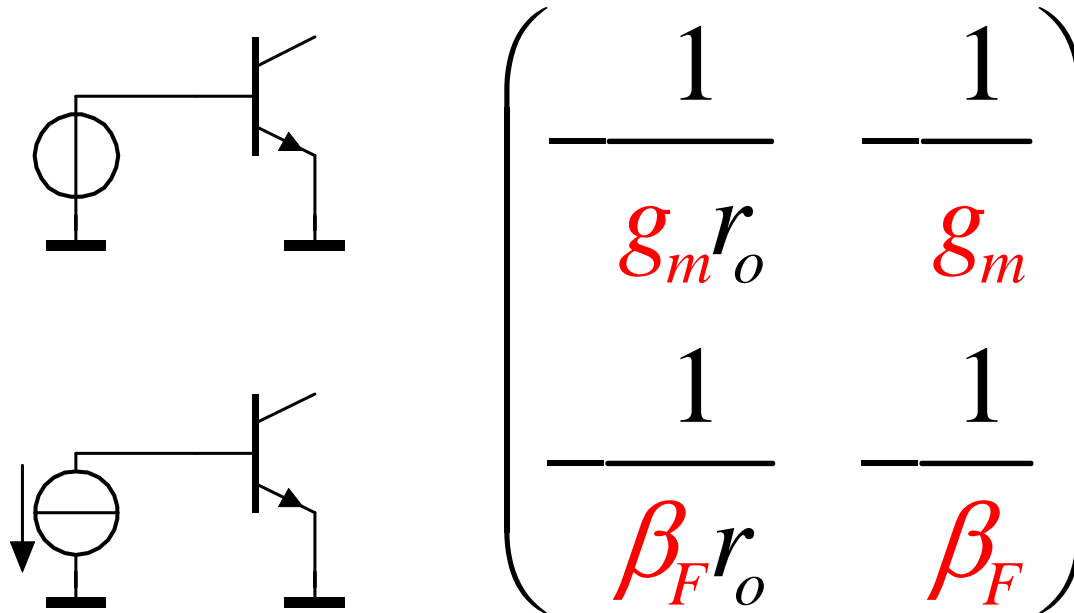
$$i_c = G_t v_{be} + G_{t2} v_{be}^2 + G_{t3} v_{be}^3$$

# Weak distortion, 4 cases





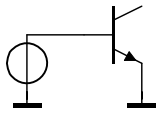
# Weak distortion, Bipolar transistor



$g_m$  or  $B$  –type distortion

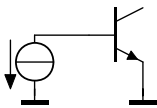
$\beta$  or  $D$  –type distortion

# Weak distortion, bipolar transistor



$g_m$  or  $B$  –type distortion

$$i_c = \frac{1}{B} v_{be} + \frac{d^2 f(V_{be})}{2dV_{be}^2} \Big|_{V_{be}=V_{beQ}} v_{be}^2 + \frac{d^3 f(V_{be})}{6dV_{be}^3} \Big|_{V_{be}=V_{beQ}} v_{be}^3$$

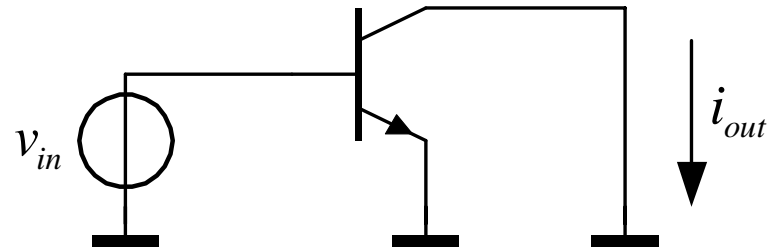


$\beta$  or  $D$  –type distortion

$$i_c = \frac{1}{D} i_b + \frac{d^2 f(I_b)}{2dI_b^2} \Big|_{I_b=I_{bQ}} i_b^2 + \frac{d^3 f(I_b)}{6dI_b^3} \Big|_{I_b=I_{bQ}} i_b^3$$

# B –type distortion

$$I_c = I_s \left( e^{\frac{V_{be}}{V_T}} - 1 \right)$$



$$\frac{dI_c}{dV_{be}} = \frac{1}{V_T} I_s e^{\frac{kT}{q} V_{be}} = \frac{I_c}{V_T} = \frac{1}{B}$$

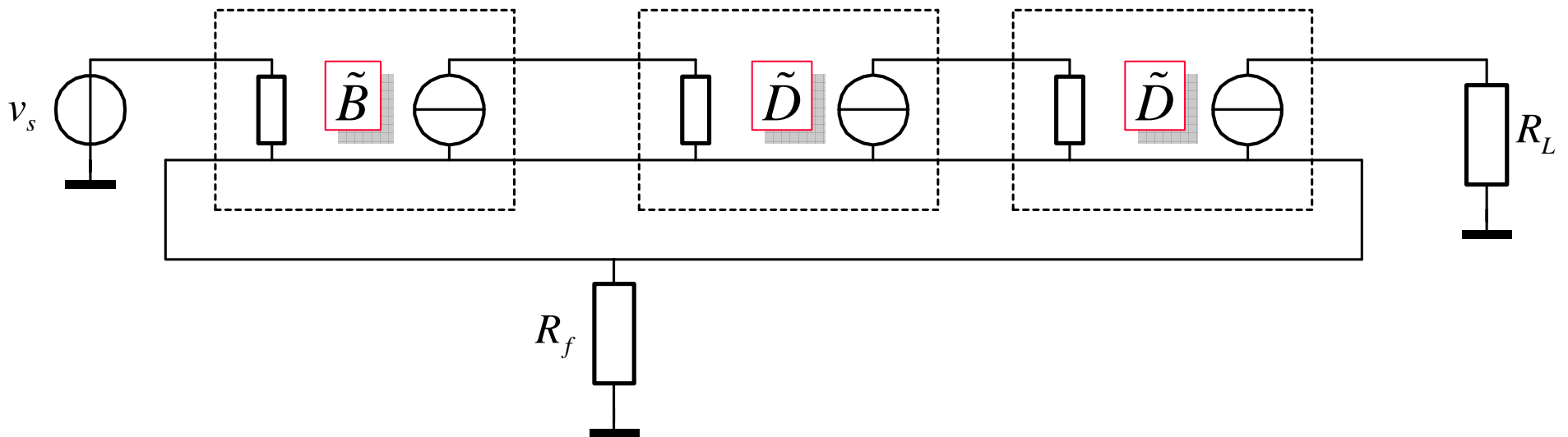
$$\frac{d^2 I_c}{dV_{be}^2} = \frac{1}{V_T^2} I_s e^{\frac{kT}{q} V_{be}} = \frac{I_c}{V_T^2} = \frac{1}{BV_T}$$

$$\frac{d^3 I_c}{dV_{be}^3} = \frac{1}{V_T^3} I_s e^{\frac{kT}{q} V_{be}} = \frac{I_c}{V_T^3} = \frac{1}{BV_T^2}$$

$$i_{out} = -\frac{1}{B} \left( v_{in} + \frac{v_{in}^2}{2V_T} + \frac{v_{in}^3}{6V_T^2} \right)$$

# ***B* –type distortion is bias independent**

$$i_{out} = -\frac{1}{B} \left( v_{in} + \frac{v_{in}^2}{2V_T} + \frac{v_{in}^3}{6V_T^2} \right)$$

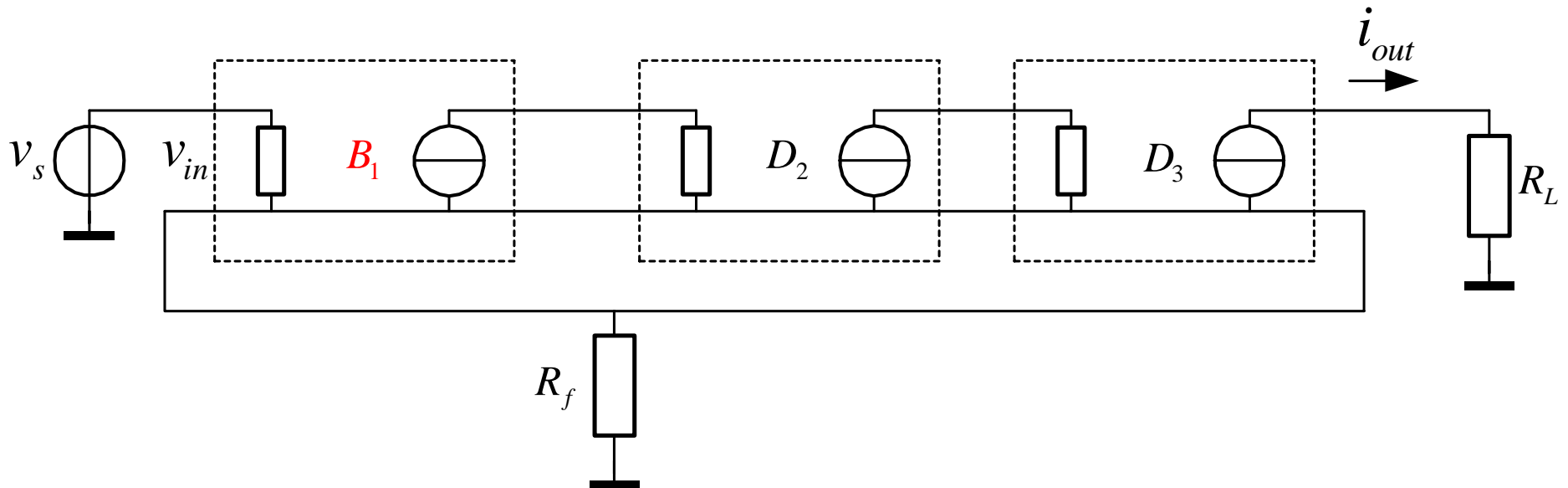


*B* –type at the **input**, when the nullator is a voltage sensor

**Reduce via loopgain** (no interference with noise optimum)

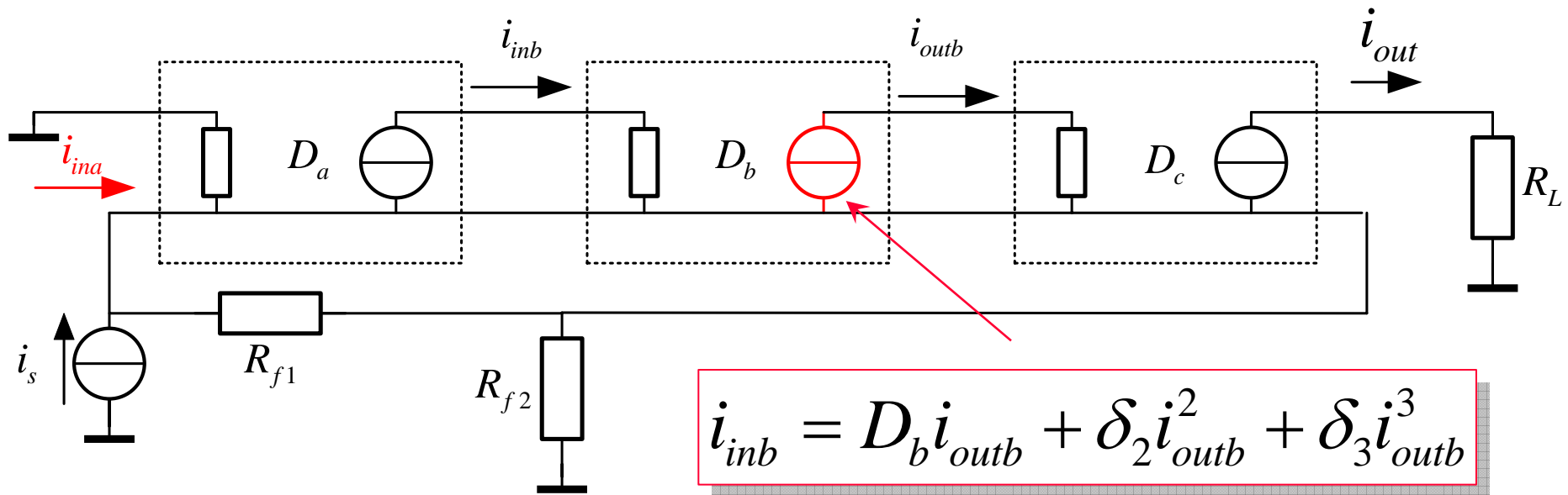
# Reduction of $B$ –type distortion

$$i_{out} = -\frac{1}{B_1 D_2 D_3} \left( v_{in} + \frac{v_{in}^2}{2V_T} + \frac{v_{in}^3}{6V_T^2} \right)$$



Secondary effect : Increase bias first stage  $\rightarrow B_1$  smaller  $\rightarrow$  more loopgain  
 Without feedback, increasing bias first stage does not help

# Influence of location of distortion



$$i_{ina} = D_a \left[ D_b D_c i_{out} + \delta_2 (D_c i_{out})^2 + \delta_3 (D_c i_{out})^3 \right]$$

$D_a$  has a linear effect on distortion

$D_c$  has a **quadratic** and **cubic** effect on distortion

## Gain after non-linear stage is best

$$i_{ina} = D_a \left[ D_b D_c i_{out} + \delta_2 (D_c i_{out})^2 + \delta_3 (D_c i_{out})^3 \right]$$

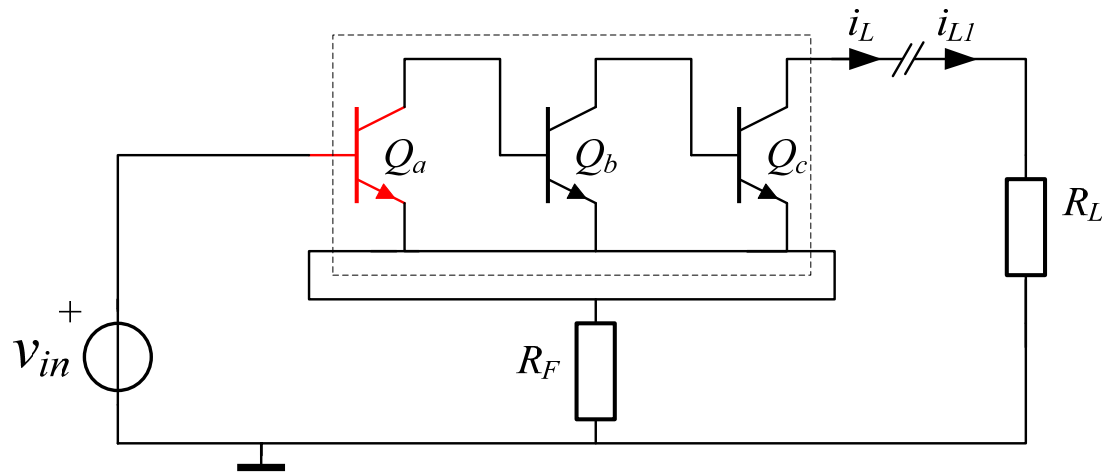
Gain **last stage** important!

Insert **extra gain after** distorting stage

Maximum gain all stages

Worst distortion often at input (*B* –type)

# Distortion caused by first transistor



$$i_L = L i_{L1} + l_2 i_{L1}^2 + l_3 i_{L1}^3$$

$$L = \frac{R_F}{B_a D_b D_c}$$

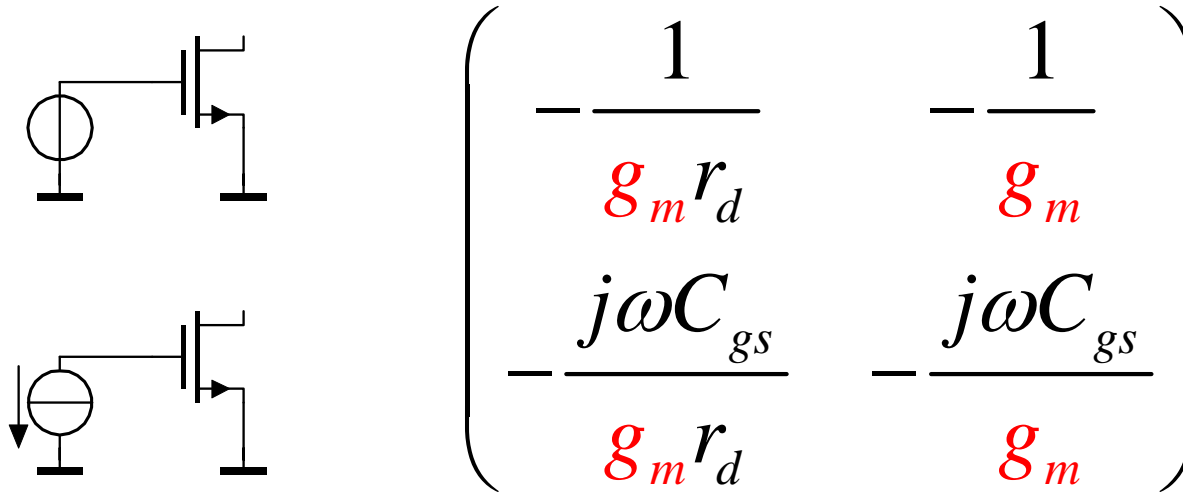
$$l_2 = -\frac{1}{2V_T} \frac{B_a^2 D_b^2 D_c^2}{R_F} = \frac{1}{2V_T} \frac{1}{L} B_a D_b D_c$$

$$l_3 = -\frac{1}{3V_T^2} \frac{B_a^3 D_b^3 D_c^3}{R_F} = \frac{1}{3V_T^2} \frac{1}{L} B_a^2 D_b^2 D_c^2$$

Gain of stage itself works as if it's after its non-linearity



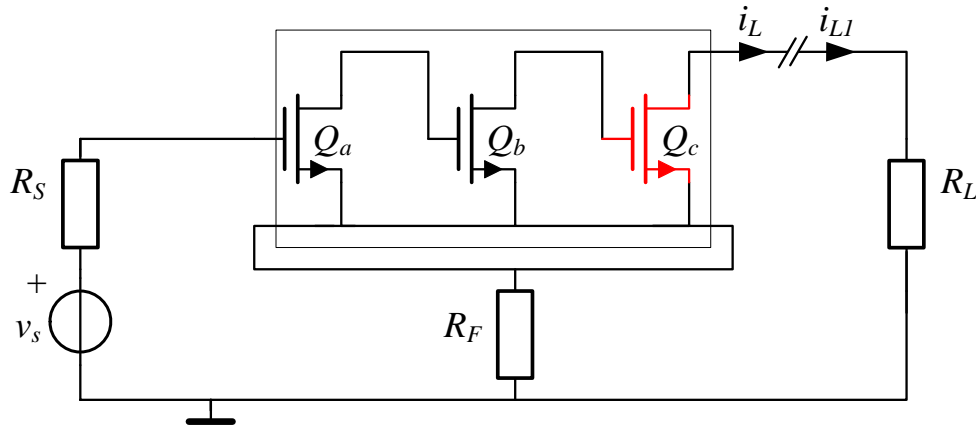
# Weak distortion, FET



Always  $g_m$  distortion

$$\left( \begin{array}{cc} -\frac{1}{g_m r_o} & -\frac{1}{g_m} \\ -\frac{1}{\beta_F r_o} & -\frac{1}{\beta_F} \end{array} \right)$$

# Distortion caused by last transistor



$$i_L = L i_{L1} + l_2 i_{L1}^2 + l_3 i_{L1}^3$$

$$L = \frac{R_F}{A_a A_b B_c}$$

$$l_2 = -\frac{1}{4} \frac{A_a A_b B_c}{R_F I_{dQc}} = -\frac{1}{4} \frac{1}{L} \frac{1}{I_{dQc}}$$

$$l_3 = -\frac{1}{8} \frac{A_a A_b B_c}{R_F I_{dQc}^2} = -\frac{1}{8} \frac{1}{L} \frac{1}{I_{dQc}^2}$$

$$A \propto (\text{Channel length})^{-1}$$

Longer transistor  $\Rightarrow$  lower distortion

# Bipolar versus FET

$$l_2 = -\frac{1}{2V_T} \frac{B_a^2 D_b^2 D_c^2}{R_F} = \frac{1}{2V_T} \frac{1}{L} B_a D_b D_c$$

Distortion from first stage

$$l_3 = -\frac{1}{3V_T^2} \frac{B_a^3 D_b^3 D_c^3}{R_F} = \frac{1}{3V_T^2} \frac{1}{L} B_a^2 D_b^2 D_c^2$$

Reduce via bias, loopgain

$$l_2 = -\frac{1}{4} \frac{A_a A_b B_c}{R_F I_{dQc}} = \frac{1}{4} \frac{1}{L} \frac{1}{I_{dQc}}$$

Distortion from last stage

$$l_3 = -\frac{1}{8} \frac{A_a A_b B_c}{R_F I_{dQc}^2} = \frac{1}{8} \frac{1}{L} \frac{1}{I_{dQc}^2}$$

Reduce via bias, loopgain, **layout**

# Local feedback

Reduces non-linearity of stage

Impedance in active part ☠

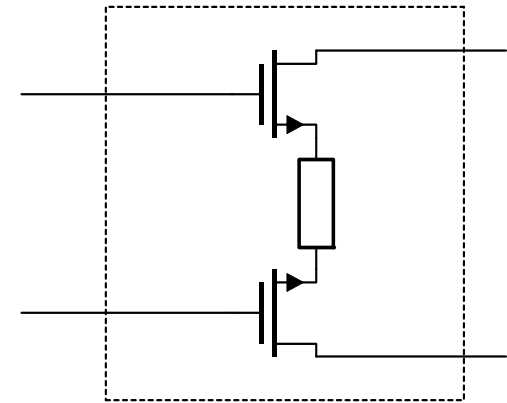
Reduces the overall loopgain

**Never** better than overall loop

**Increases distortion** other stages

Especially for last stage not a good idea

Only when non-linearity makes variation of loopgain too large



# Conclusions weak distortion

$B$  –type distortion (only at nullor input)

$D$ –type distortion (for bipolar)

## Increase the loopgain

Via biasing ( $B(I_Q)$ )

Via Layout (FET)

Extra stage (preferably after distortion source)

**No** local feedback

Use high gain last stage (also reduces clipping preceding stage)

# Dynamic distortion

Volterra series

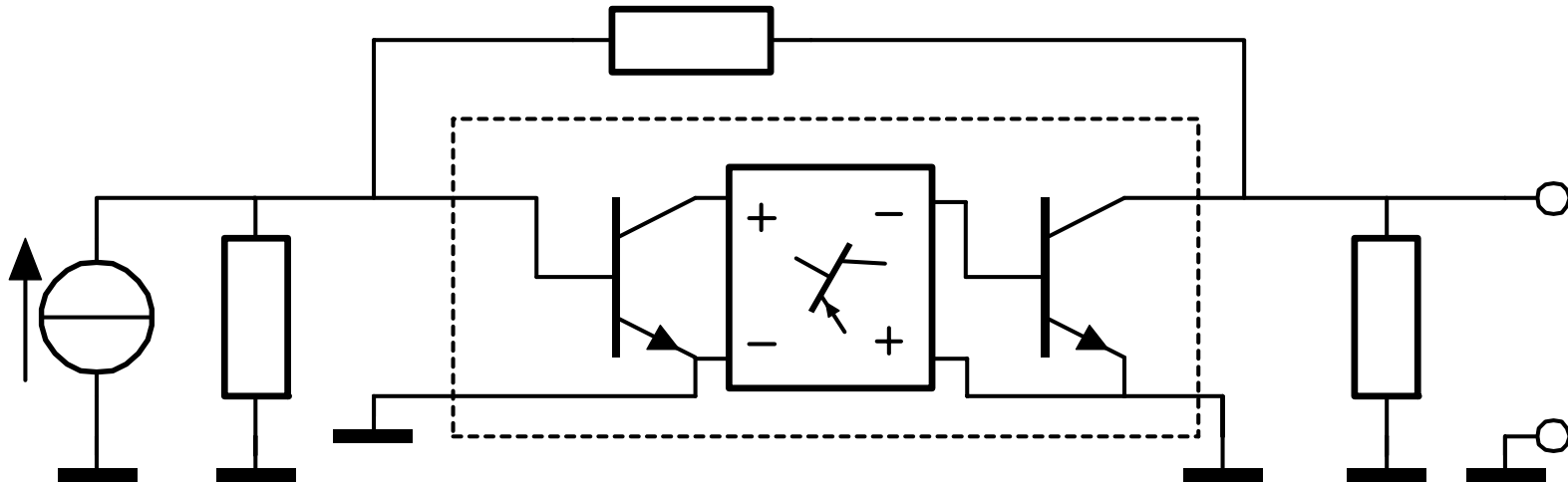
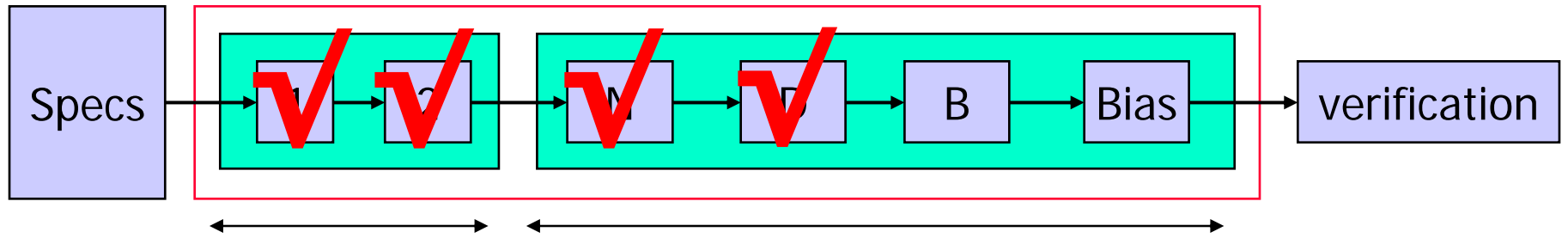
Dynamic eigenvalues



**Loopgain helps**

Still research

# Conclusions



# Specifications

- Harmonic distortion
- Intercept points
- Compression point
- Intermodulation
- Power bandwidth

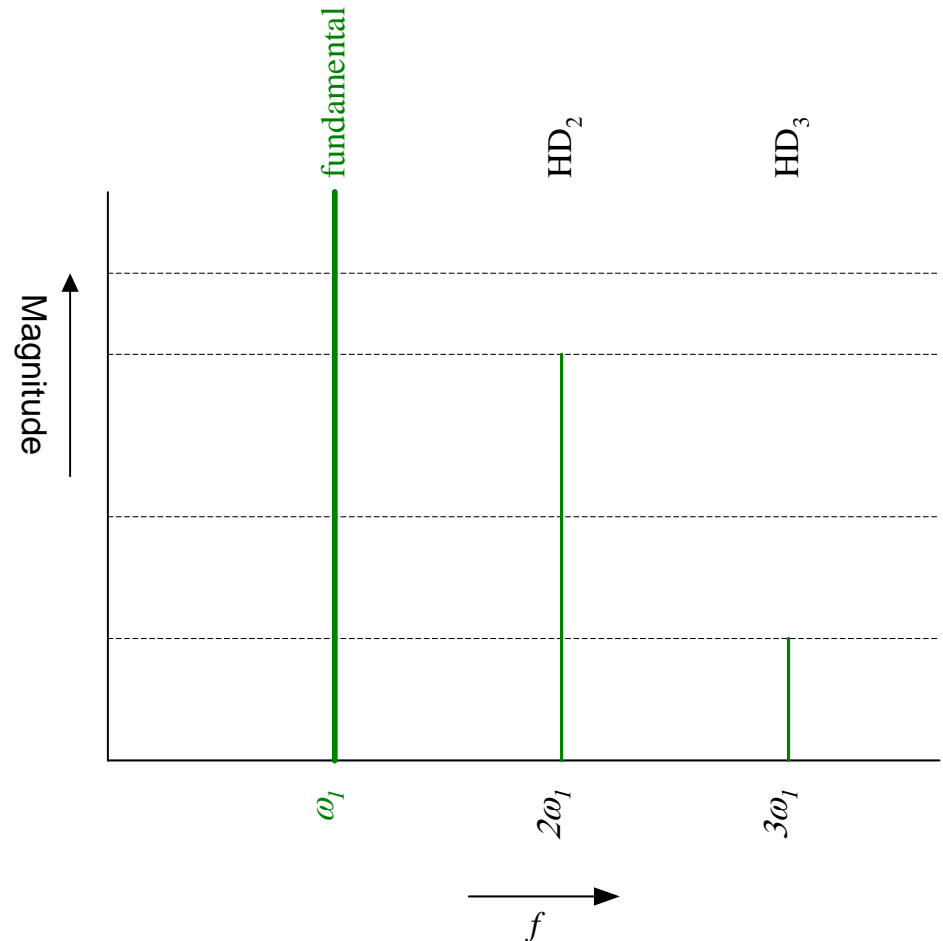


# Harmonic distortion

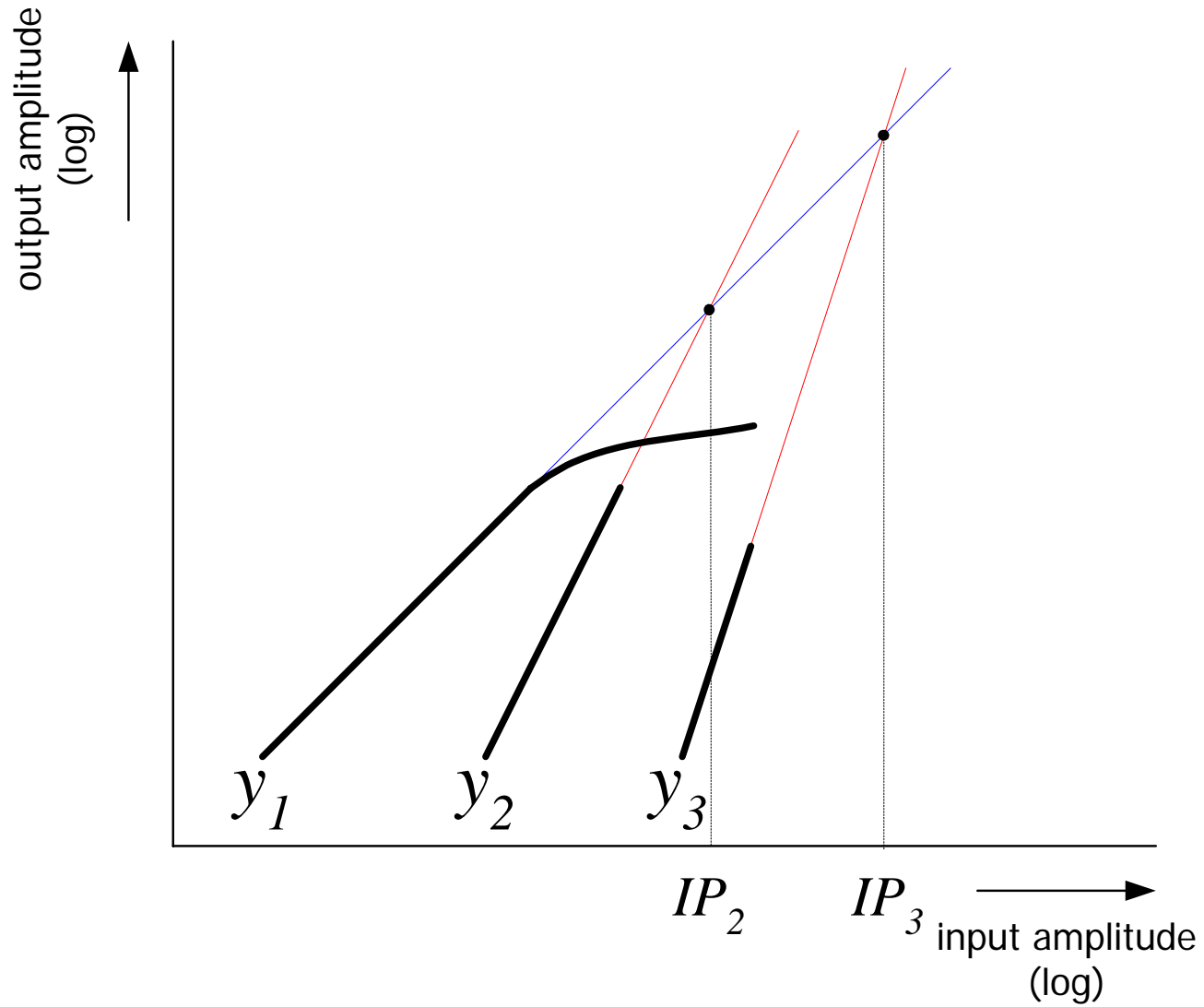
Compare amplitudes fundamental harmonic with  $n^{\text{th}}$  order harmonic

$$HD_n \hat{=} \frac{y_n}{y_1}$$

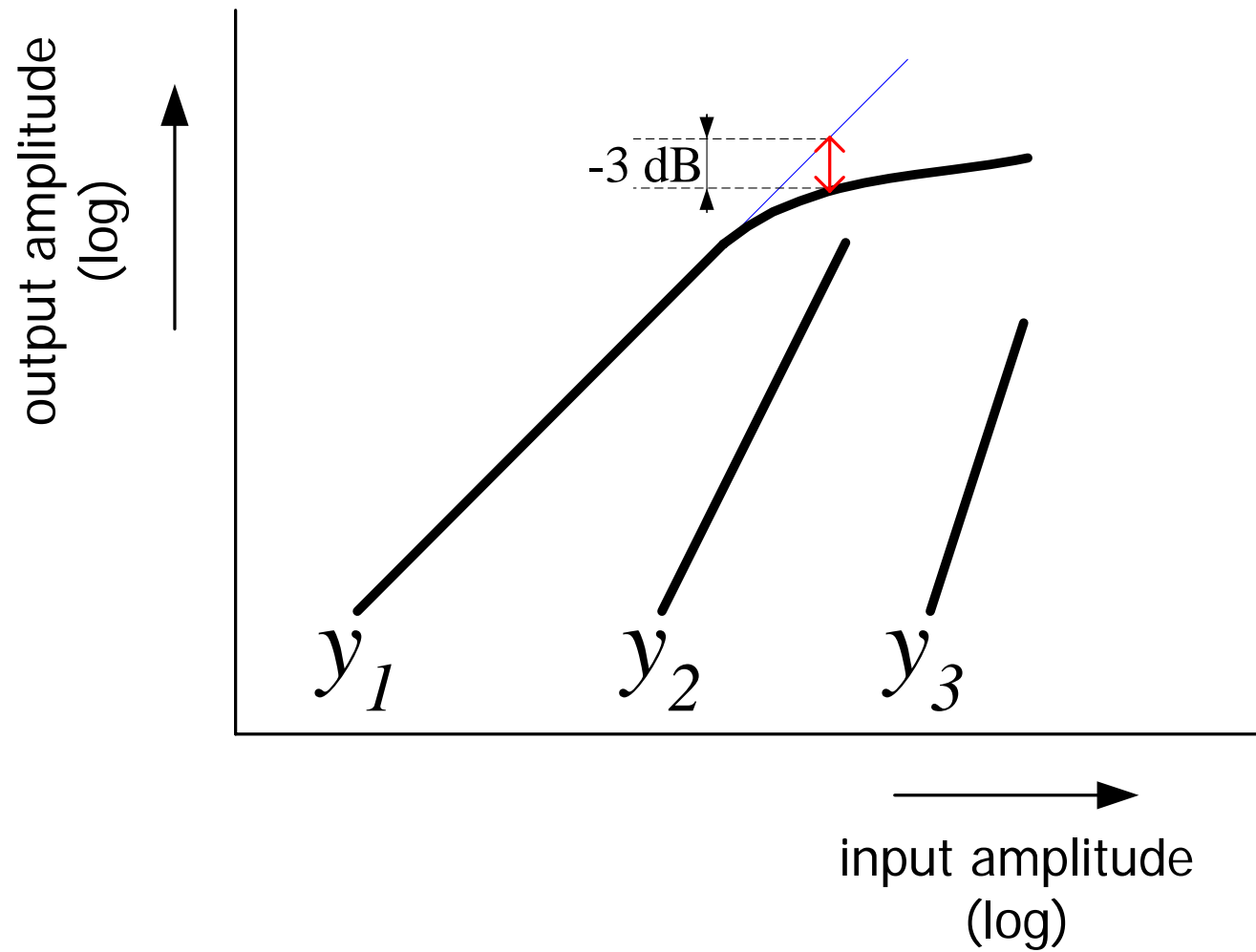
$$THD = \sqrt{\sum_{n=2}^m |HD_n|^2}$$



# Intercept points



# Compression point



# Intermodulation

