

Hydrogen and Electrical Energy Storage



12 March 2013

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Radiation, Radionuclides and Reactors

Program Batteries

Lecture 1: History, Applications, basic Electrochemistry and thermodynamics of batteries: Redox reactions, Gibbs free energy, chemical potential, Nernst.
Feb 27

Lecture 2: Solid state electrode reaction mechanisms, phase diagrams, phase rule, Gibbs Free energy, voltage profiles, capacities and energy densities. Li-ion batteries
March 6

Lecture 3: Continue topics Lecture 2.
March 13
Electrolyte stability: Pourbaix diagram, band structure solids, Cycle life.

Lecture 4: Kinetics, Butler-Volmer, diffusion, solid state diffusion
March 20
Discussion on Science paper 6 seconds discharge.

Lecture 5: Super capacitors
March 27
Future systems: Li-air, Li-sulphur
Flow-cells
Costs and Performance comparison batteries/systems
Material Abundance

Practical Issues

Book chapters, scientific literature and sheets will be available on BB

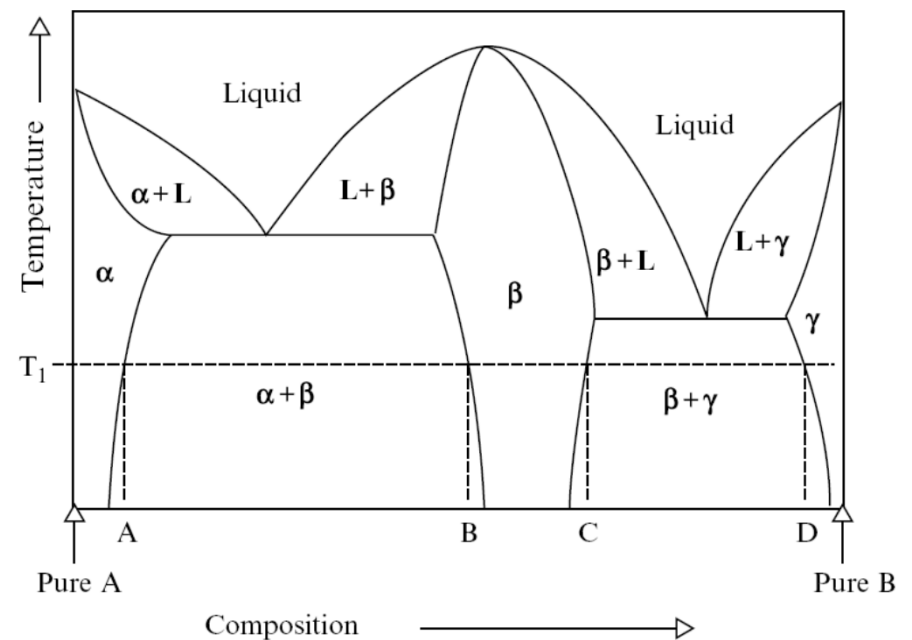
- Lecture 1: Electrochemistry 2.3-2.5
- Lecture 2: Advanced Batteries: Chapter 1, 2 and 3.1-3.3
- Lecture 3: Advanced Batteries Chapter 14.1,14.2,14.B1-4, 16.1-2,16B,
Review Goodenough et al. Chemistry of Materials and lecture sheets
- Lecture 4: Electrochemistry 3.1-3.3, Lecture sheets
- Lecture 5: Lecture sheets, Review Bruce et al. Li-air/Li-sulphur

Home assignment

Consider the following phase diagram for a cathode, and assume that the anode has a constant voltage independent of the composition and that T and p are constant:

a) Apply the Gibbs Phase Rule along T_1 in the regions $\alpha+\beta$ and β , is the potential constant?

b) Sketch the voltage diagram



Gibbs Phase Rule

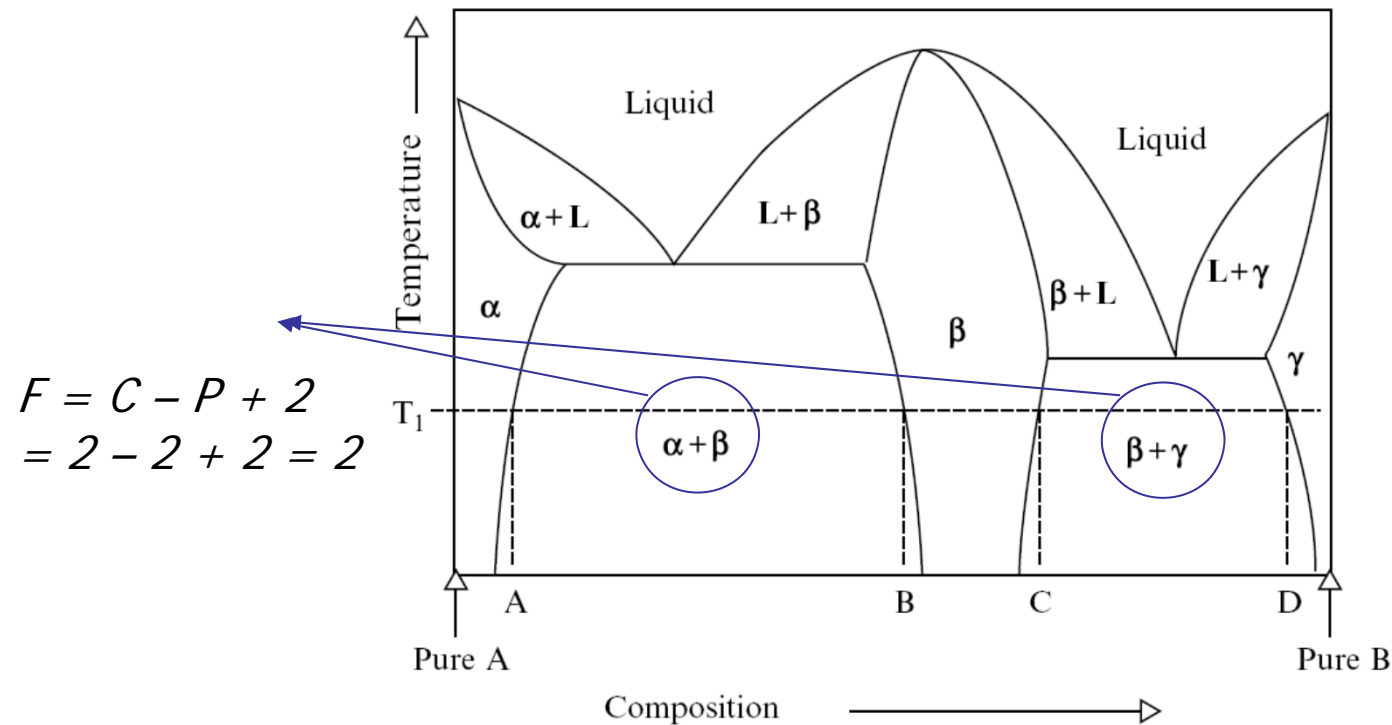
$$F = C - P + 2$$

- F : Number of degrees freedom
 C : Number of components (e.g. elements)
 P : Number of phases present in this system

Number of degrees freedom: Number of intensive thermodynamic parameters (T , p , μ , x) that must be specified to define the system (if true other intensive parameters are constant, if not they vary)

Example: suppose $F=1$ and T is specified $\Rightarrow p$, μ and x are fixed

Example: suppose $F=3$ and p, T is specified $\Rightarrow \mu$ will vary (depending on x)



$F=2$ and p, T is specified \Rightarrow other intensive variables are fixed/constant
 μ is constant \Rightarrow voltage is constant.

Note, composition of phases (ratio A/B) at points, A, B, C and D is also constant (also intensive variable)

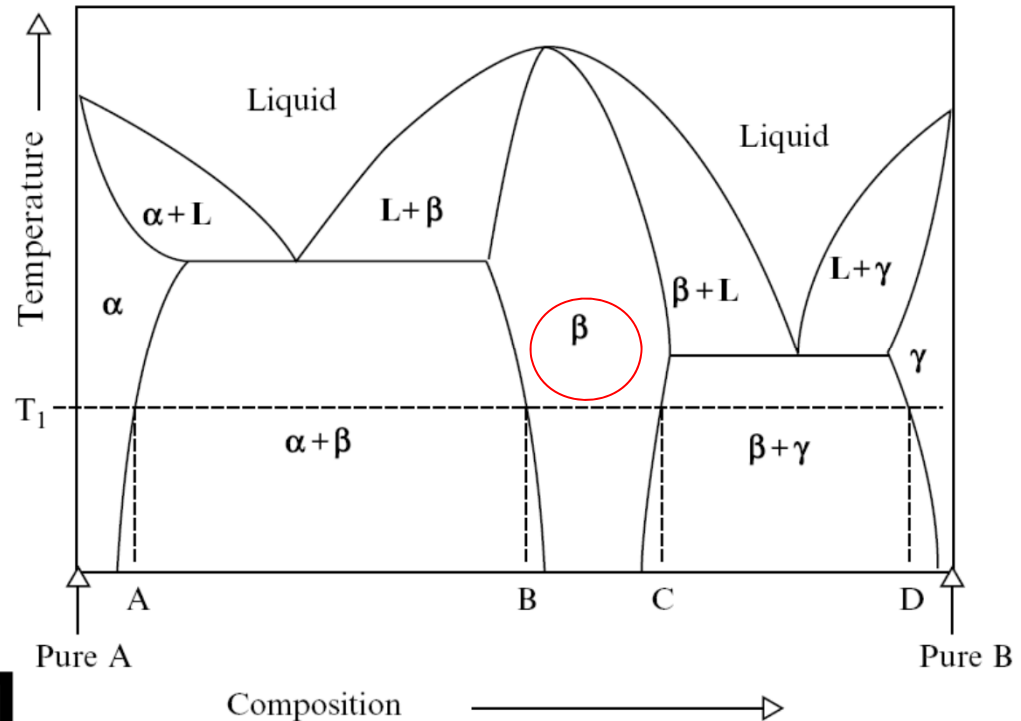
Question Gibbs Phase Rule 3

19. What is the number of degrees of Freedom, $F=C-P+2$, in the red circle?

- a) 1
- b) 2
- c) 3
- d) no clue

20. What does this mean assuming constant p, T ?

- a) constant voltage
- b) variable voltage
- d) no clue



<http://www.edupinion.nl/c548>



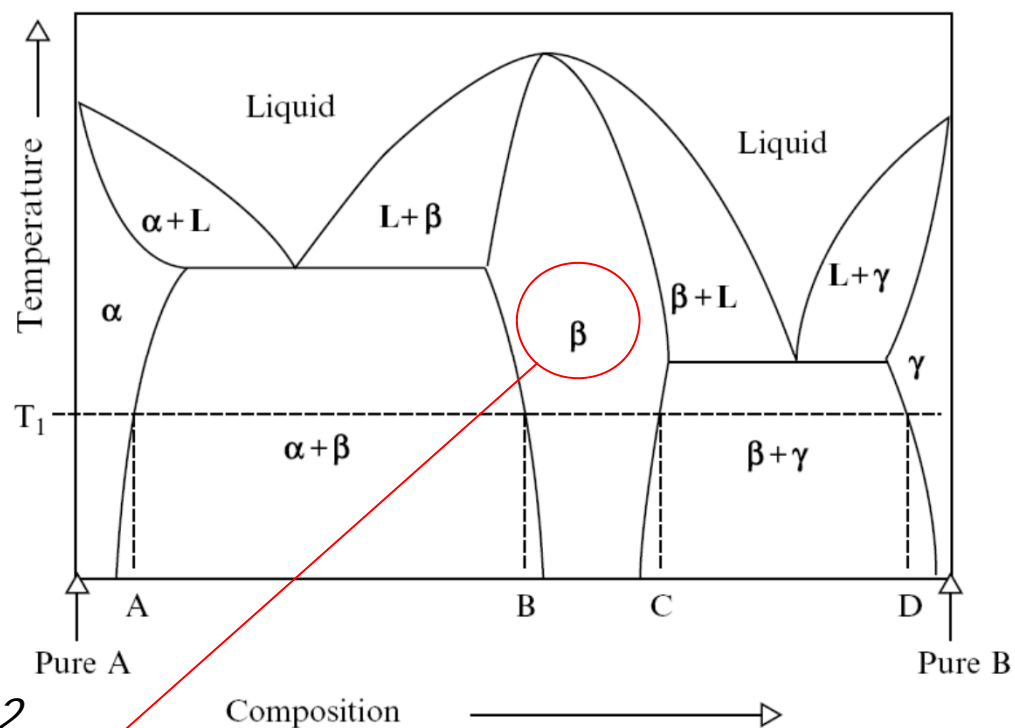
Question Gibbs Phase Rule 3

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- a) 1
- b) 2
- c) 3
- d) No clue

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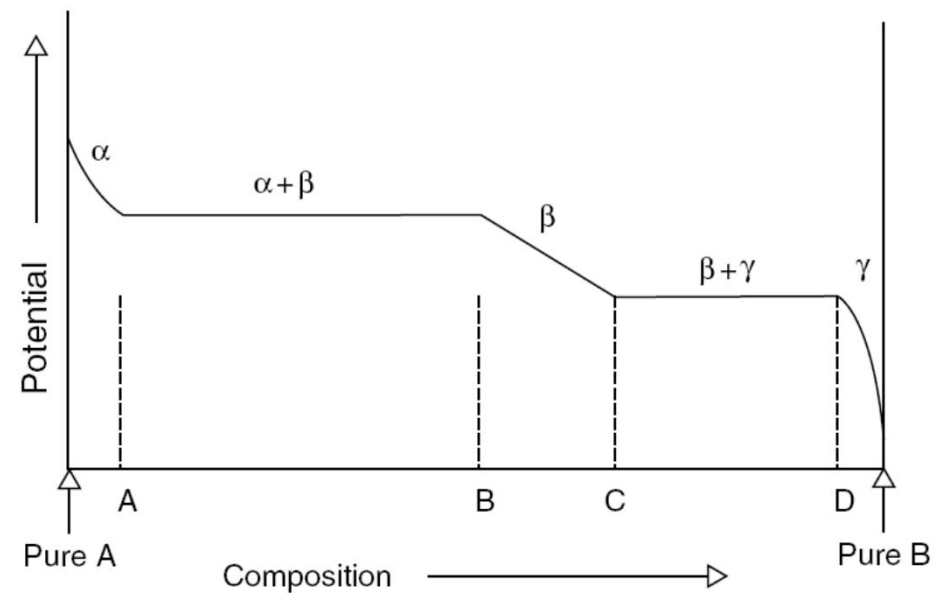
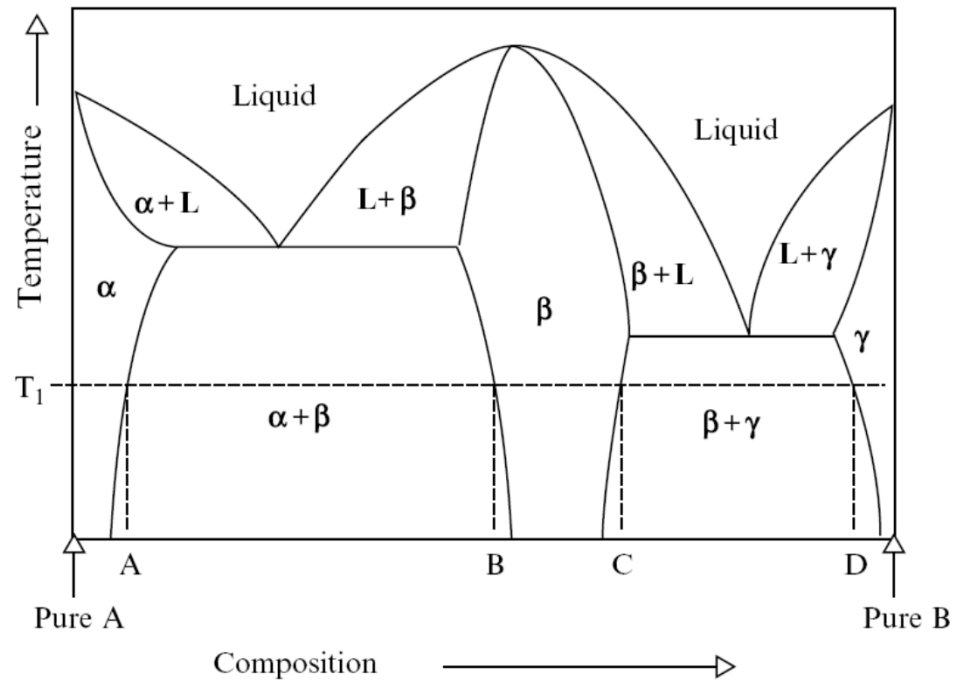
- a) Constant voltage
- b) variable voltage
- c) no clue



$$F = C - P + 2$$

$$= 2 - 1 + 2 = 3$$

E_{cell} = variable (depends on composition)! => 19c) and 20b)



Question Lithium storage in Antimony

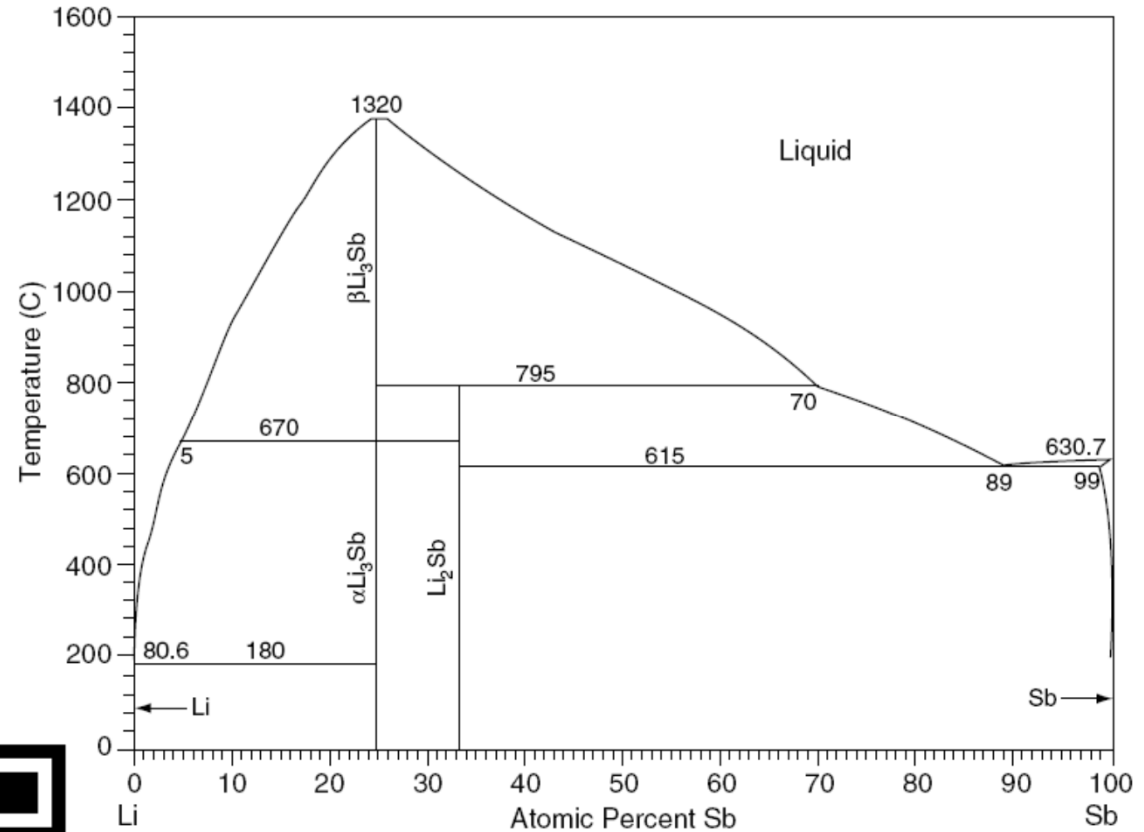
21. What kind of reaction is this?

- a) Reconstitution-displacement
- b) Reconstitution-formation
- c) Insertion
- d) No clue

22. If the maximum composition is Li_3Sb how many voltage plateau's do you expect?

Assume room temperature

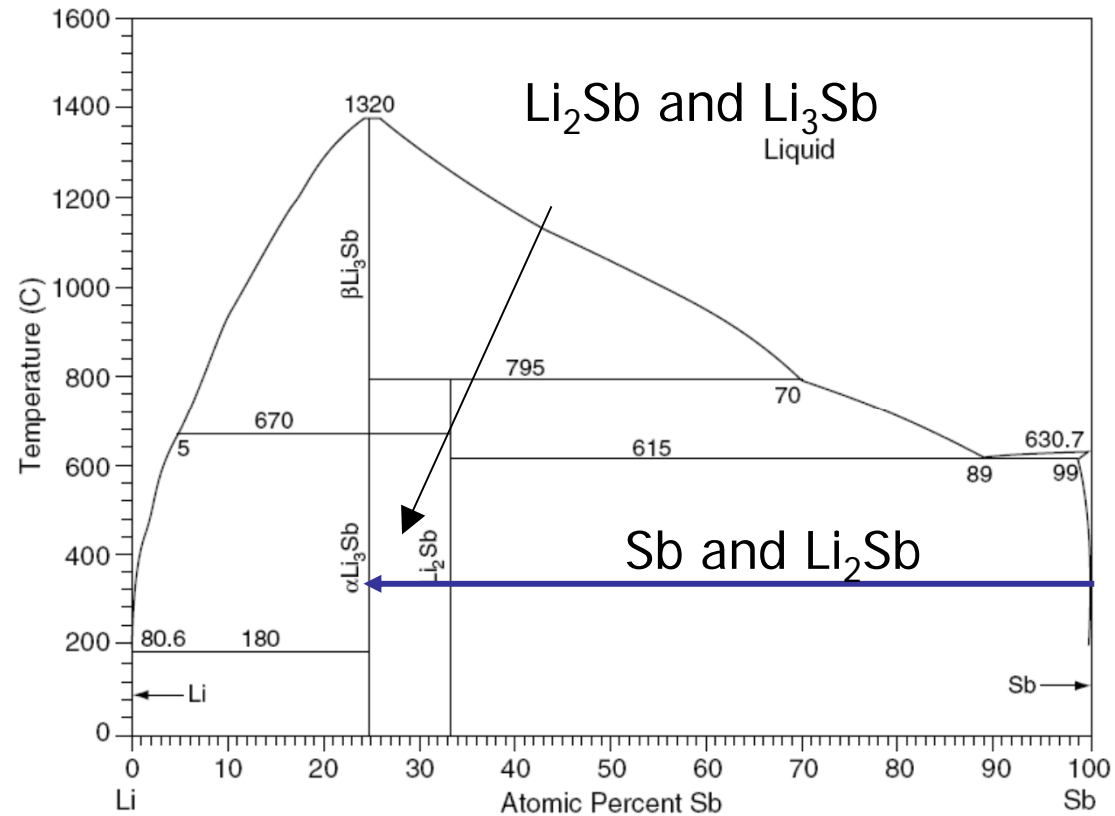
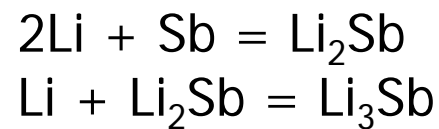
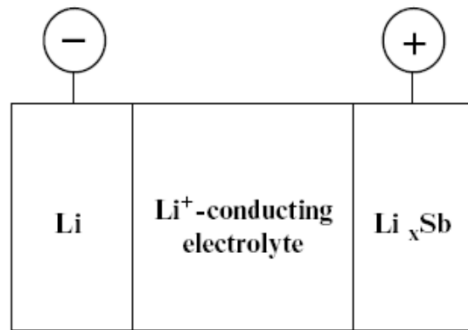
- a) 0
- b) 1
- c) 2
- d) No clue



<http://www.edupinion.nl/c043>



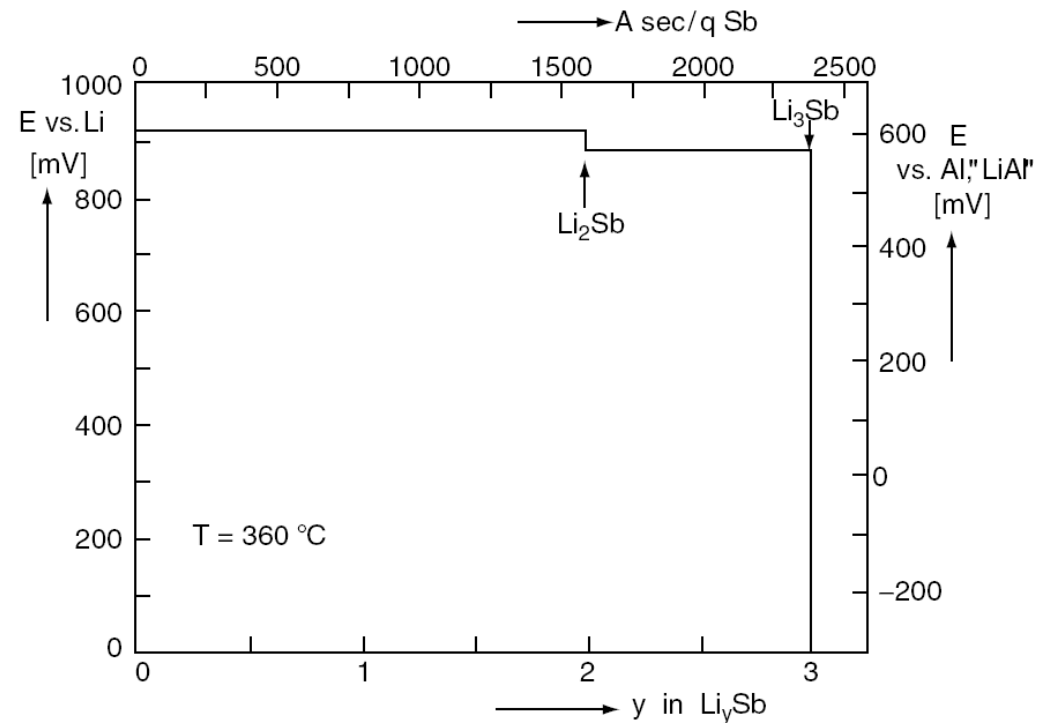
Question Lithium storage in Antimony



Type: A+B=AB: Reconstitution-formation => 21b)

Question Lithium storage in Antimony

Two two phase regions
 => two voltage plateau's
 => 22c)



$$E_{Cell}^1 = -\frac{\Delta G_r^0(Li_2Sb)}{2F} = 0.912 \text{ V versus Li-metal}$$

$$E_{Cell}^2 = \frac{\Delta G_r^0(Li_3Sb)}{F} - \frac{\Delta G_r^0(Li_2Sb)}{2F} = 0.871 \text{ V versus Li-metal}$$

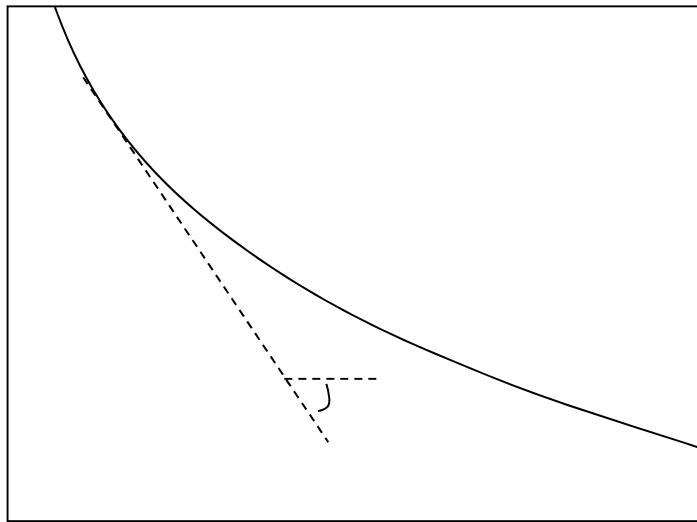
A different view, Voltage profile from the Gibbs Free Energy

Gibbs Free Energy

$$dG = Vdp - SdT + \sum_j \mu_j dn_j \quad \text{Constant p and T} \quad = \quad \sum_j \mu_j dn_j \Rightarrow \left. \frac{\partial G(x)}{\partial n} \right|_{T,p} = \mu_{\text{Electrode}}^{\text{Li}}$$

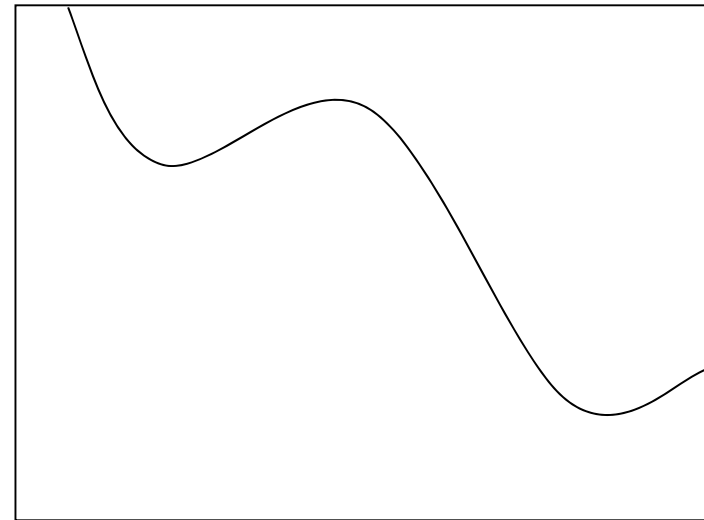
ΔG determines the direction of the reaction (and W_{chem}).
The shape of $G(x)$ how it gets there

Gibbs free energy $g(x)$ J/mol



Composition x , Li_xFePO_4

Gibbs free energy $g(x)$ J/mol

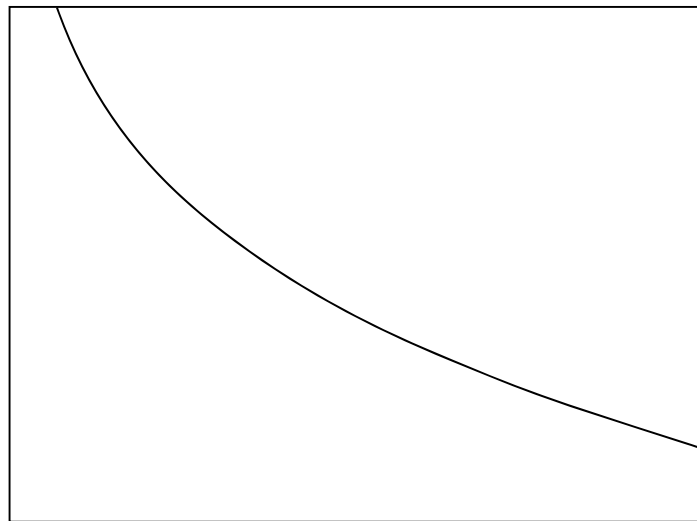


Composition x , Li_xFePO_4

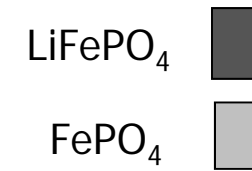
Gibbs Free Energy

Gradual compositional change: solid solution

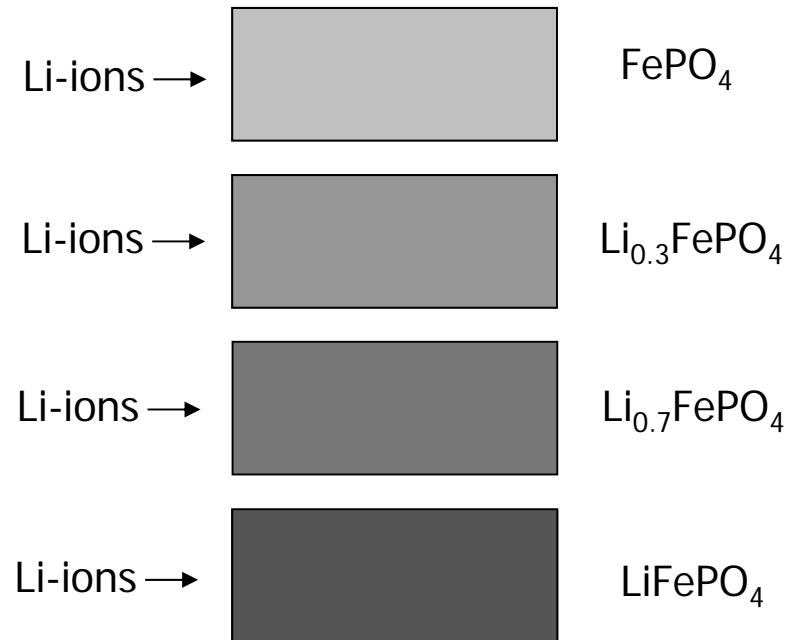
Gibbs free energy $g(x)$ J/mol



Composition x , Li_xFePO_4

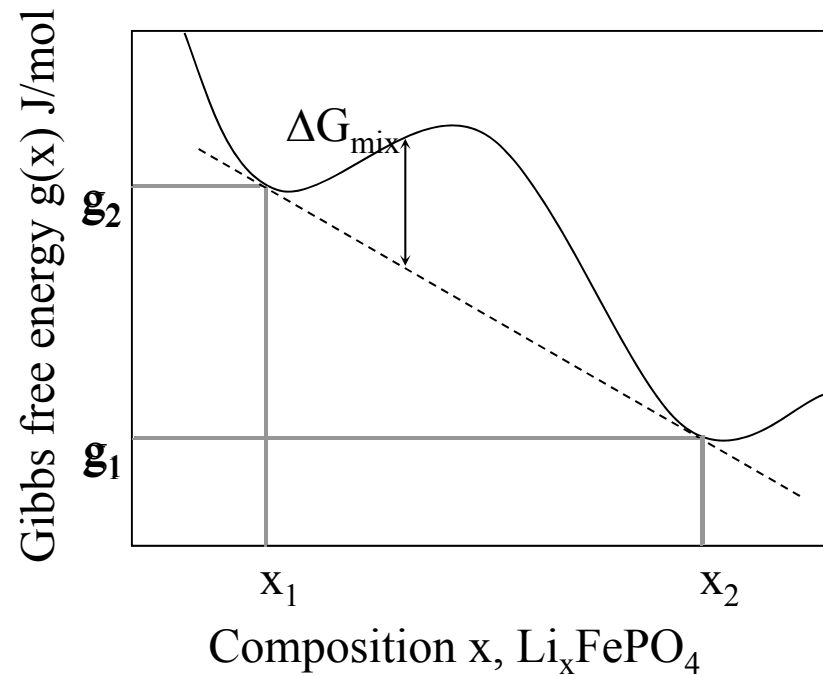


Overall composition

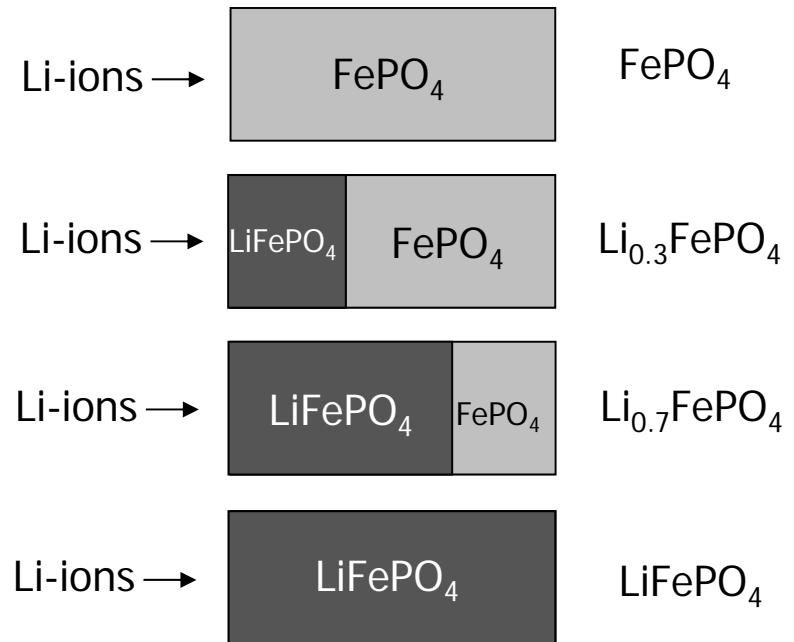


Gibbs Free Energy

Segregation: Phase transition

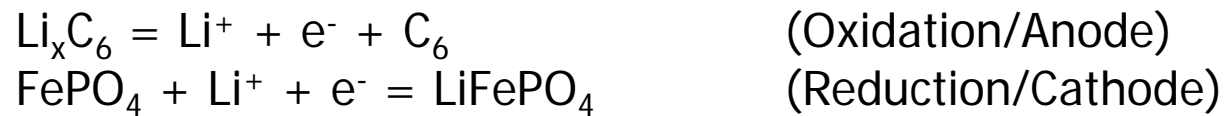


Overall composition

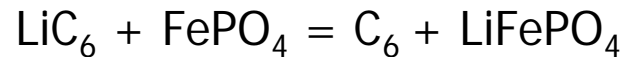


From the Gibbs Free energy to voltage

Discharge of Li-ion battery:



Overall reaction:



$$\begin{aligned} E_{\text{Cell}} dQ &= E_{\text{Cell}} zF dn = - \sum_j \mu_j dn = \left(\mu_{\text{LiFePO}_4}^{\text{Li}} - \mu_{\text{LiC}_6}^{\text{Li}} \right) dn \\ \Rightarrow E_{\text{Cell}}(x) &= - \frac{\mu_{\text{LiFePO}_4}^{\text{Li}} - \mu_{\text{LiC}_6}^{\text{Li}}}{F} = - \frac{\mu_{\text{Cathode}}^{\text{Li}}(x) - \mu_{\text{Anode}}^{\text{Li}}}{F} \end{aligned}$$

Assume $\mu_{\text{Anode}}^{\text{Li}} = \text{constant}$

From the Gibbs Free energy to voltage

In order to know the Voltage profile $E_{Cell}(x)$ we need $\mu_{Cathode}(x)$, which will depend on the Gibbs free energy $G(x)$ of the cathode.

We know: $\mu_{Cathode}^{Li} = \frac{dG_{Cathode}(x)}{dn}$ where dn is the number of moles of Li

It is more convenient to work with the Gibbs free energy per mole host material $g(x)$.

Suppose we have N mole of Cathode C and n moles of interstitial Li ions in the Cathode

such that: $n = xN$, then $g(x) = \frac{G(x)}{N}$

$$\mu_{Cathode}^{Li} = \left. \frac{\partial G(x)}{\partial n} \right|_{T,p,N} = \left. \frac{\partial (Ng(x))}{\partial n} \right|_{T,p,N} = \left. \frac{N \partial g(x)}{N \partial x} \right|_{T,p,N} = \left. \frac{\partial g(x)}{\partial x} \right|_{T,p,N} \quad \text{Slope in } g(x) \text{ plot!}$$

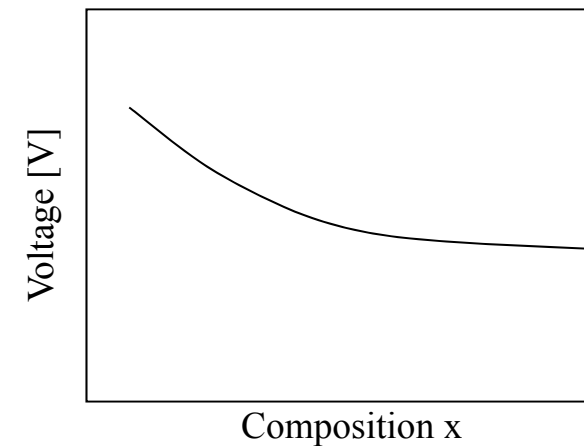
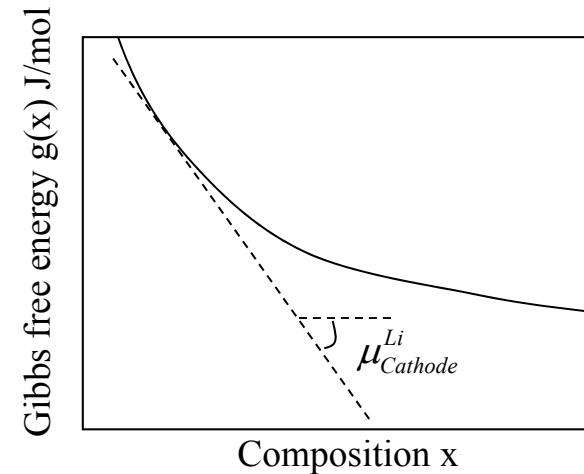
From the Gibbs Free energy to voltage

Solid solution

$$\mu_{Cathode}^{Li} = \frac{\partial g(x)}{\partial x}$$

$$E_{Cell}(x) = -\frac{\mu_{Cathode}^{Li}(x) - \mu_{Anode}^{Li}}{zF}$$

Open cell voltage is changing with composition:



From the Gibbs Free energy to voltage

Two phase decomposition

$$g(x)_{\text{common tangent}} = \frac{g_2 - g_1}{x_2 - x_1} x + \frac{g_1 x_2 - g_2 x_1}{x_2 - x_1}$$

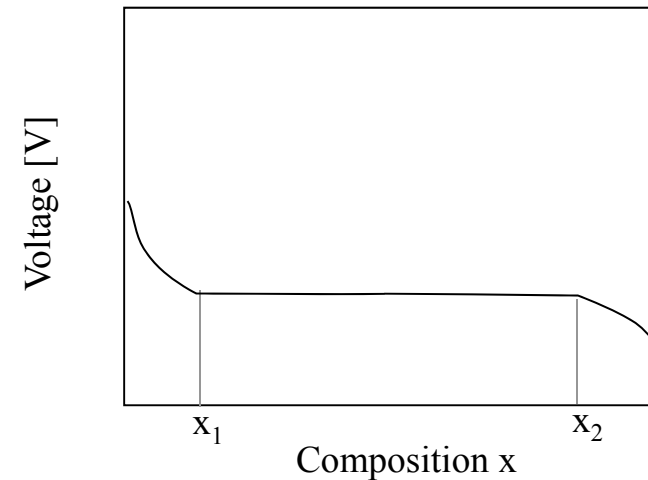
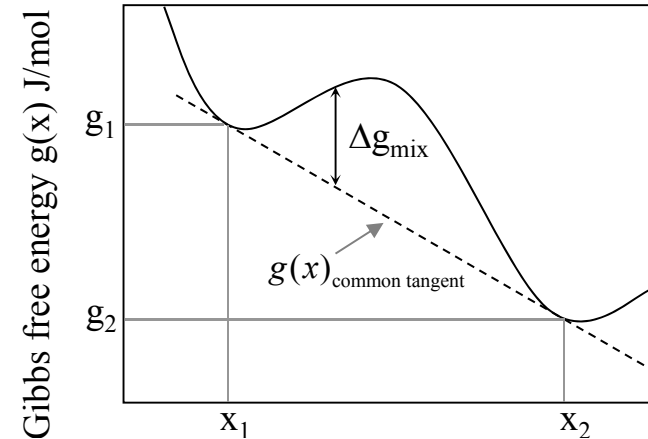
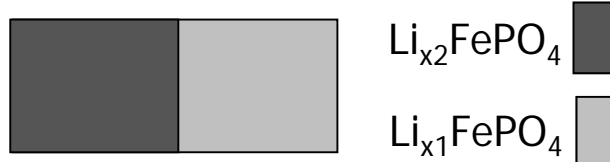
$$\Delta g_{\text{mix}} = g(x)_{\text{common-tangent}} - g(x)_{\text{solid-solution}}$$

$$\mu_C = \frac{\partial g}{\partial x} = \frac{g_2 - g_1}{x_2 - x_1} = \text{constant } (x_1 < x < x_2)$$

$$E_{\text{Cell}} = -\frac{\mu_{\text{Cathode}}^{\text{Li}}(x) - \mu_{\text{Anode}}^{\text{Li}}}{zF} = \text{constant } (x_1 < x < x_2)$$

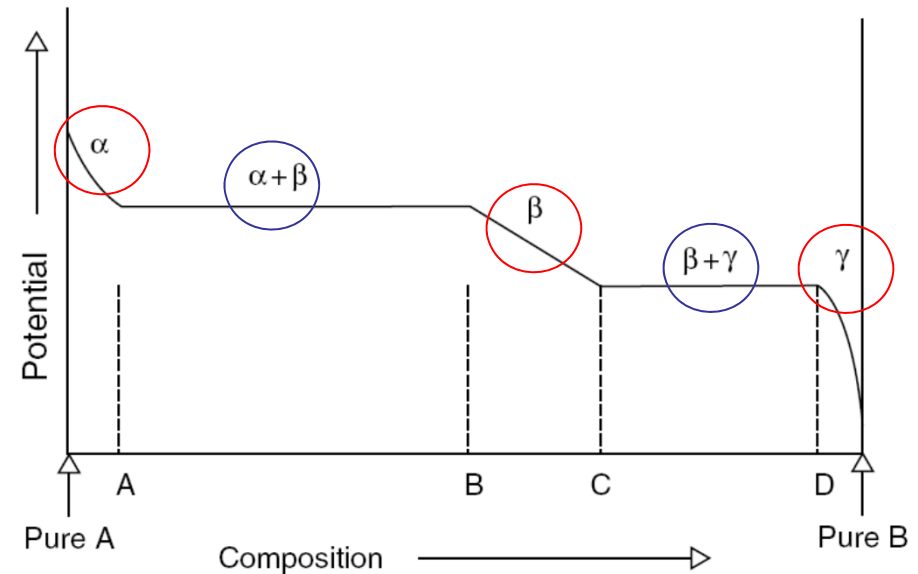
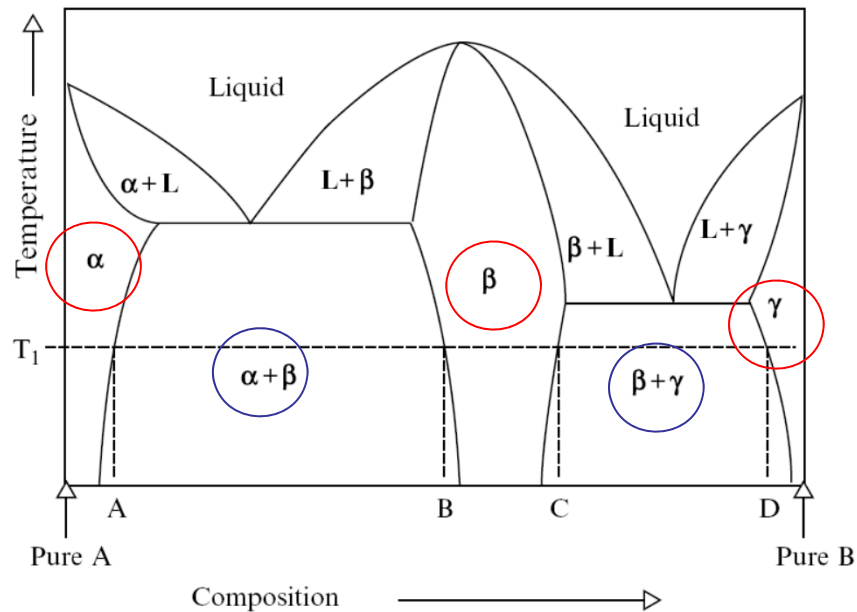
Open cell voltage is constant between x_1 and x_2

Overall
Composition
 Li_xFePO_4 $x_1 < x < x_2$



From the Gibbs Free energy to voltage

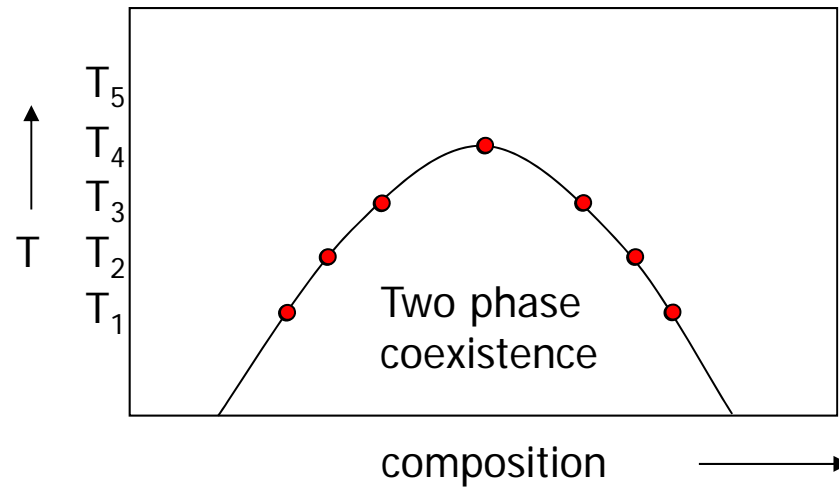
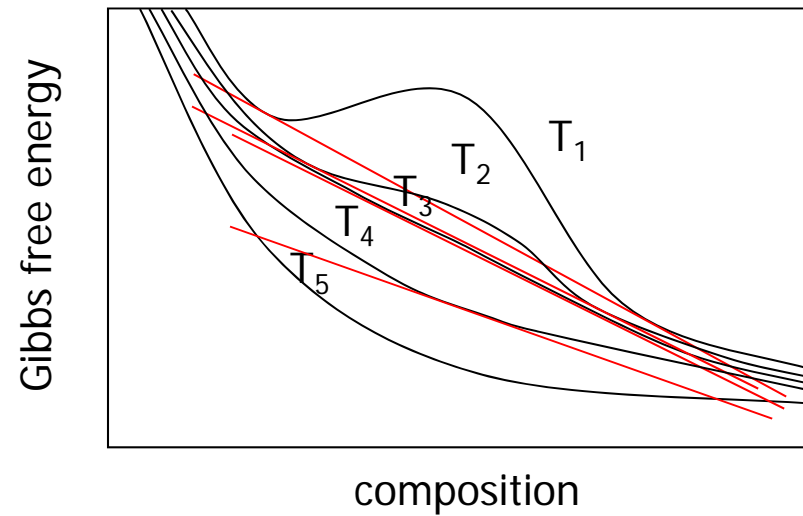
Gibbs phase rule \leftrightarrow Shape Gibbs Free energy



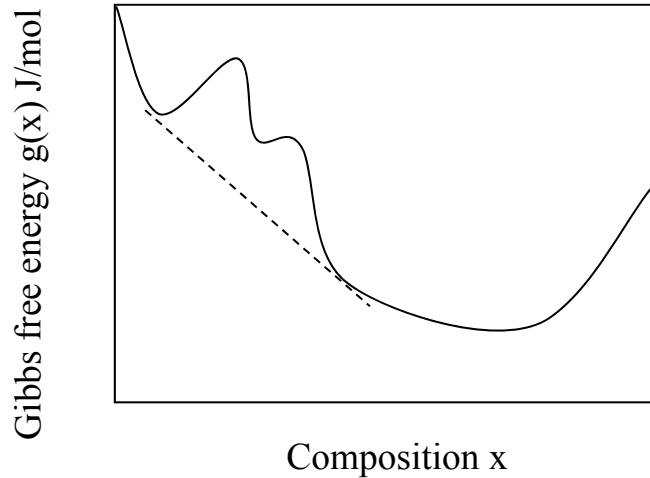
- Solid solution phase \rightarrow Variable composition \rightarrow variable potential
- Phase transition \rightarrow constant composition \rightarrow constant potential

Li-ion batteries, relation Gibbs and phase diagram

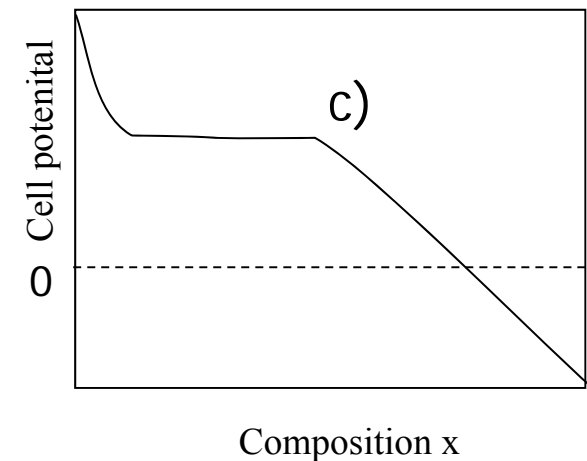
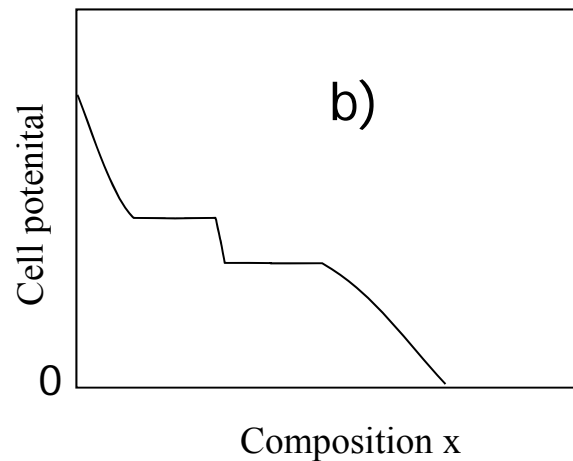
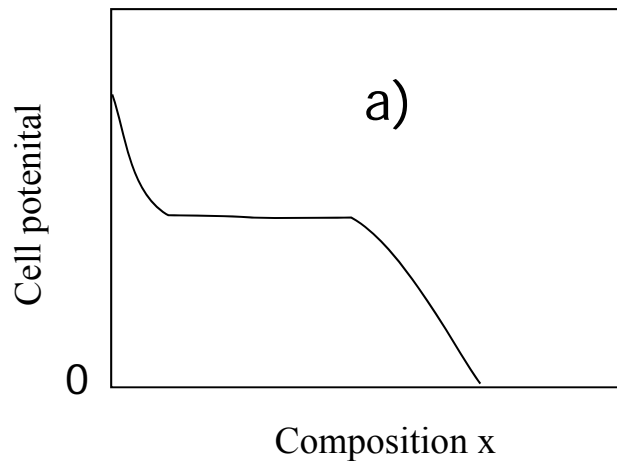
Construction
phase diagram:



Question Gibbs Free Energy 1



23. Based on the Gibbs Free Energy of the cathode, and assuming Li metal as anode, how does the voltage profile look like?



d) no clue

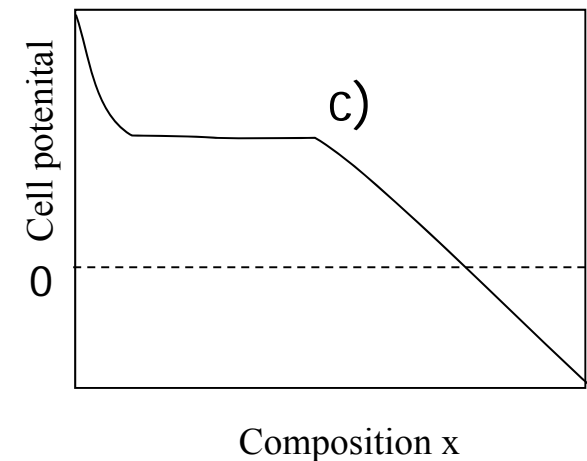
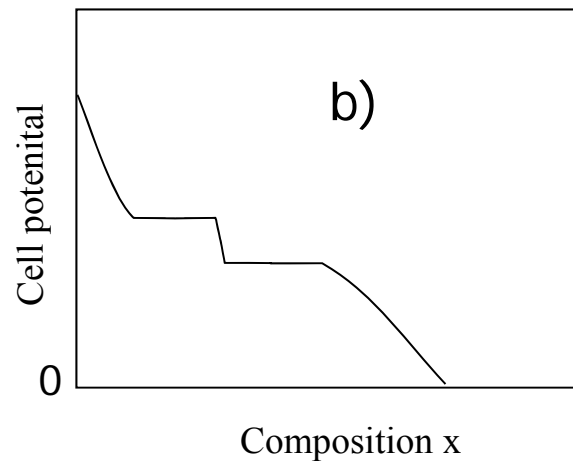
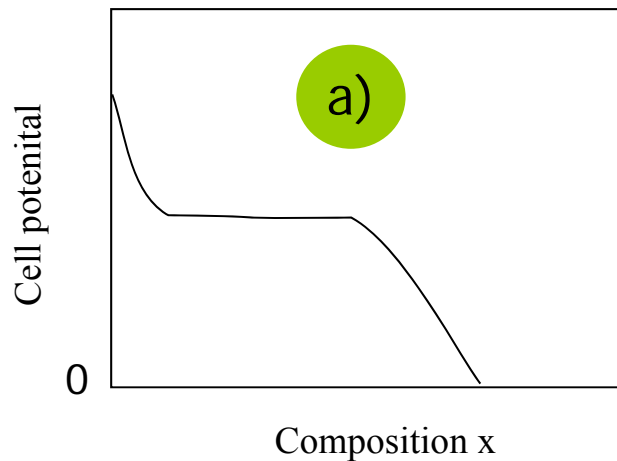
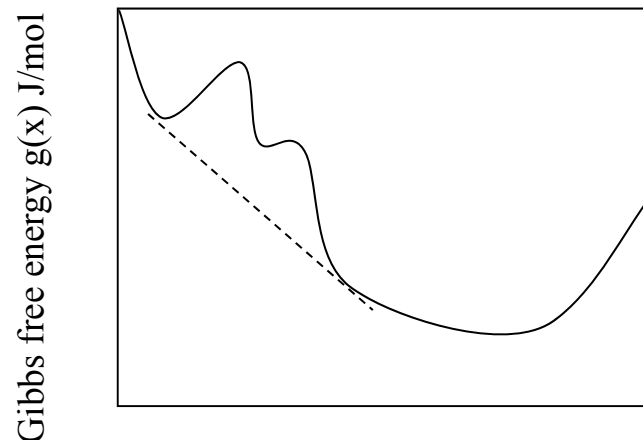
<http://www.edupinion.nl/c037>

Result



Question Gibbs Free Energy 1

23. Based on the Gibbs Free Energy of the cathode, and assuming Li metal as anode, how does the voltage profile look like?



Practical questions



What is the direction of a redox reaction?

What is the voltage that a redox reaction can deliver?

What is the energy density of a battery?

What determines the cycle life of a battery

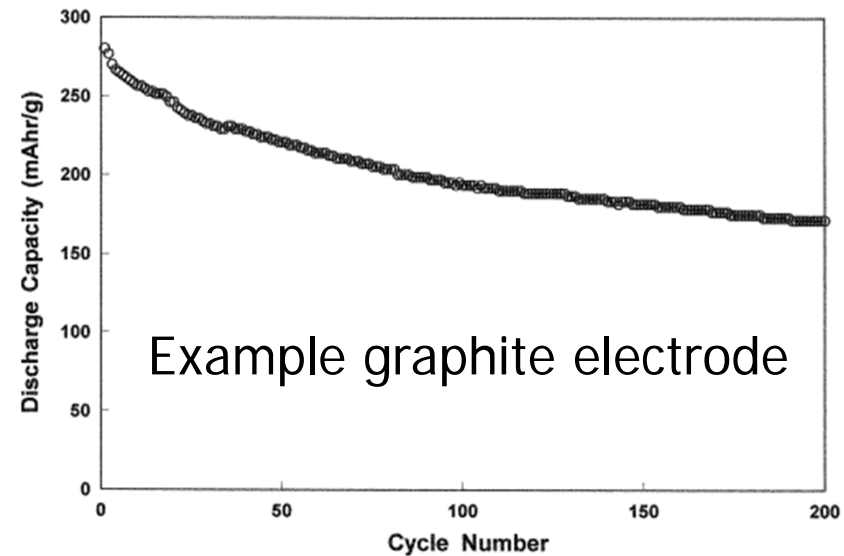
What is the power density of a battery? -> kinetics

Cycle Life of Batteries

Cycle Life of Batteries

Reduced cycle life:

Energy loss due to increasing cell impedance and due loss of active material



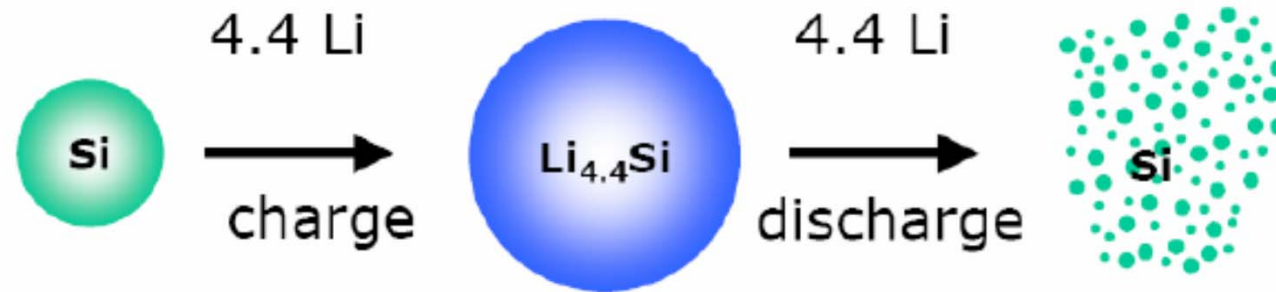
Reasons for reduced cycle life:

- (1) Structural changes in the electrodes upon (dis)charge
- (2) Thermodynamic instability electrode-electrolyte leading to decomposition of the electrolyte

-1-

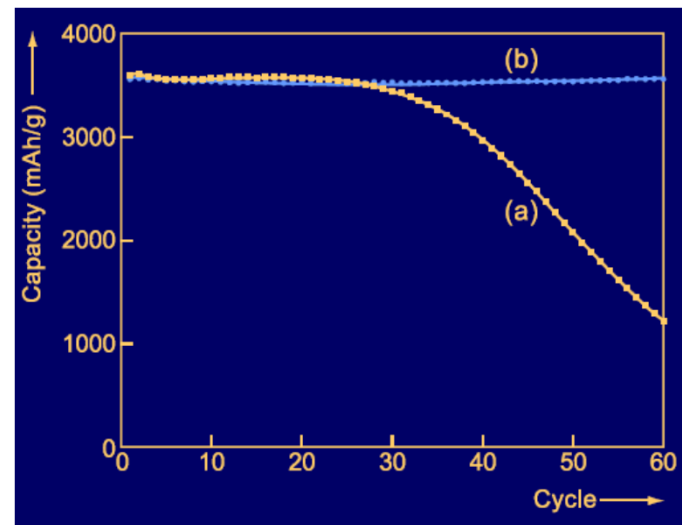
Structural changes of the electrodes upon (dis)charge

Structural changes of the electrode Reconstitution-Formation reactions



Volume expansion almost 400%
Leads to mechanical failure ->
Loss in capacity.

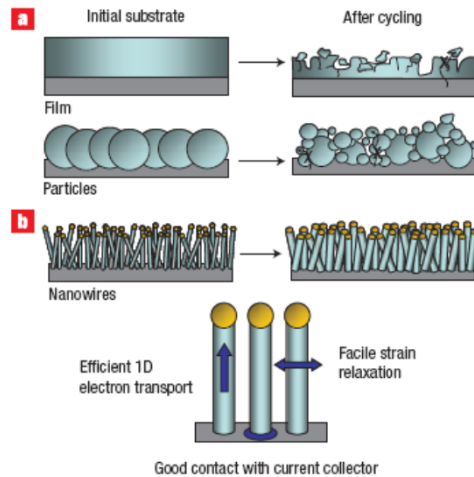
Rule of thumb, less than 10%
Volume expansion will lead to good
mechanical cycle life



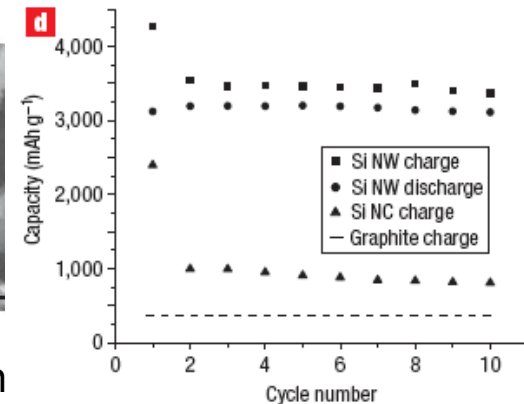
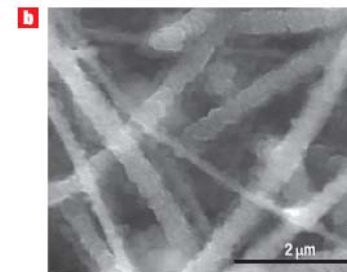
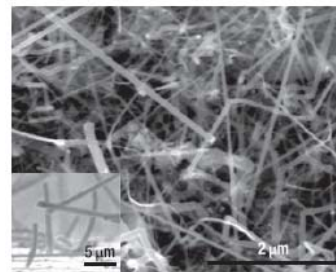
(b) Graphite x 15
(a) Si

Intermezzo: Strategies Alloy anode

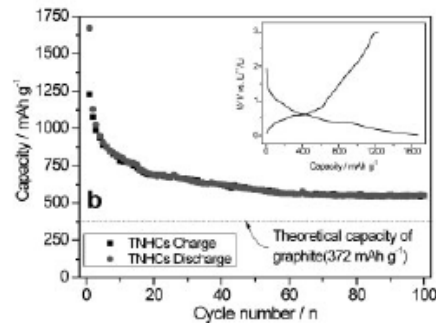
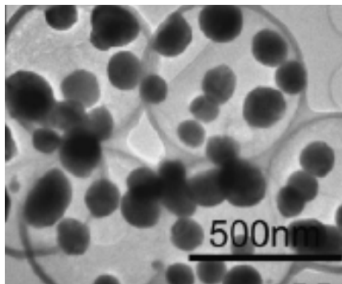
(1) Nano Si wires



- Space for $\text{Li}_{4.4}\text{Si}$ volume expansion
- Only 10 cycles reported



(2) Nano sized Sn particles encapsulated in hollow carbon sph



- Space for $\text{Li}_{4.4}\text{Sn}$ volume expansion
- No loss of contact due to confinement in Carbon sphere

Structural changes of the electrode

Reconstitution-Displacement reactions



(Li-insertion, see later)



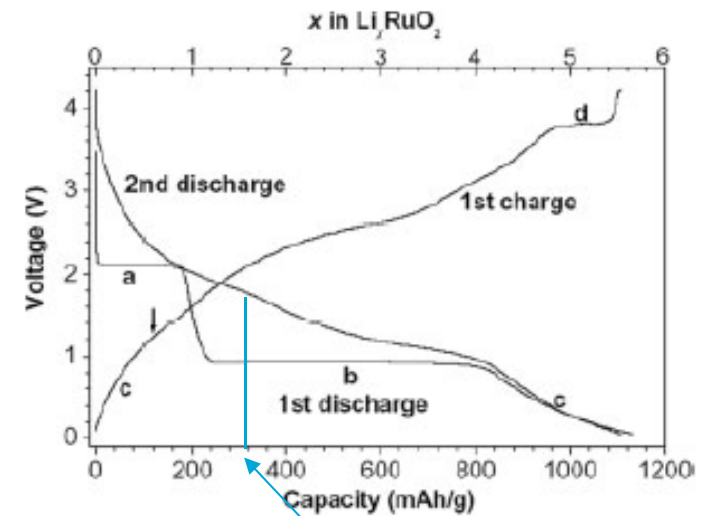
(reconstitution-displacement)



(supercapacitive behavior, later)

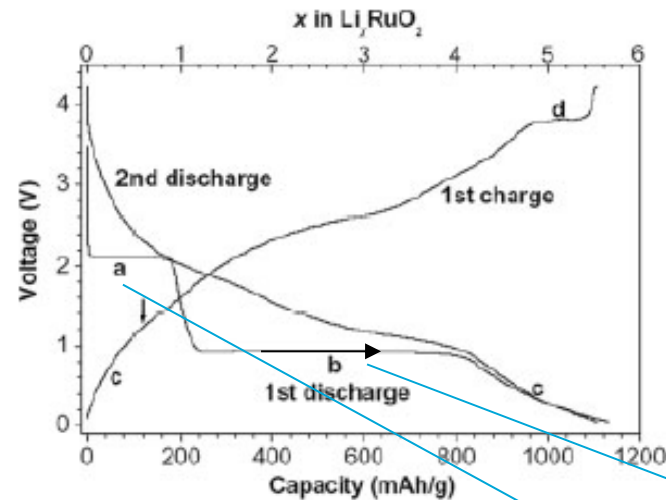
Host material decomposes in Li_2O and metal

SEI: Solid electrolyte interface: forms during first (dis)charge cycles, decomposed electrolyte (later)



Capacity of graphite

Structural changes of the electrode Reconstitution-Displacement reactions

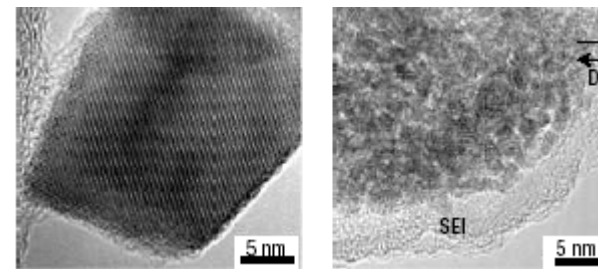


Host transforms in new compound
 ⇒ Extra capacity
 ⇒ Huge structural changes (after first cycle it remains nano-structured)
 ⇒ Only reversible because of nano distances Ru-O in Li₂O/Ru mixture

Nano structured RuO₂



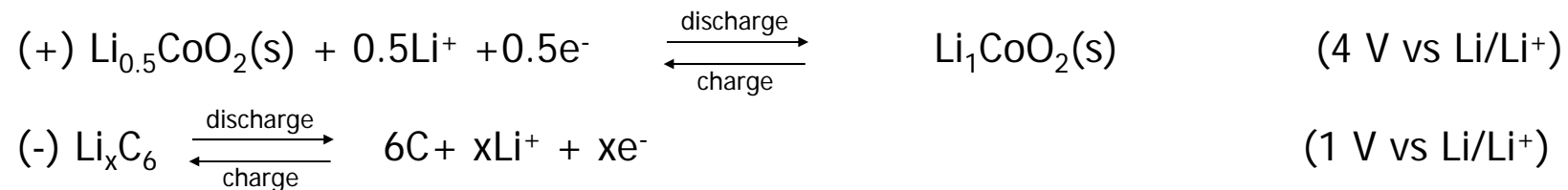
SEI: Solid electrolyte interface: forms during first (dis)charge cycles, decomposed electrolyte



Structural changes of the electrode Insertion-reactions

Electrode material serves as a host, also phase changes possible (structural changes):

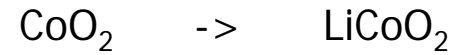
Example: LiCoO_2 :



Such reactions lead in most cases to mechanical failure after many cycles due to swelling-shrinking associated with the structural changes.

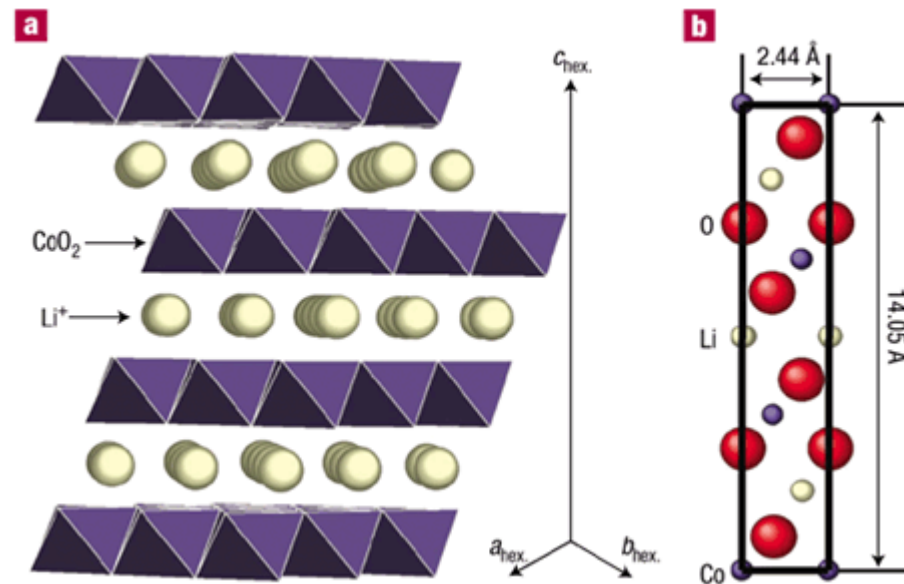
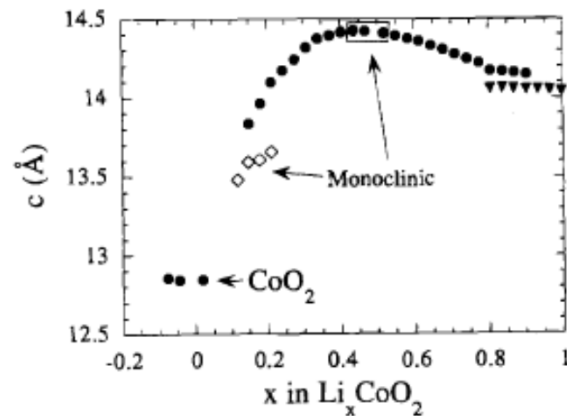
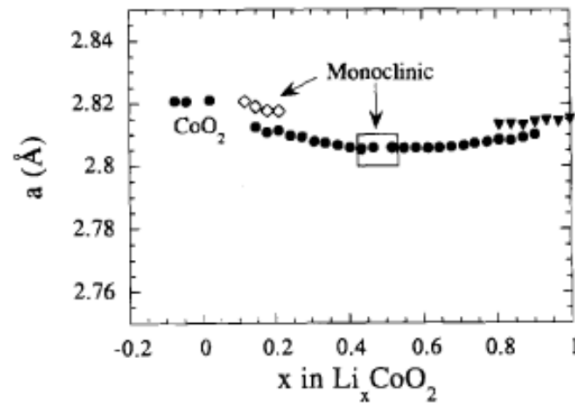
Structural changes of the electrode

Insertion-reactions: LiCoO_2



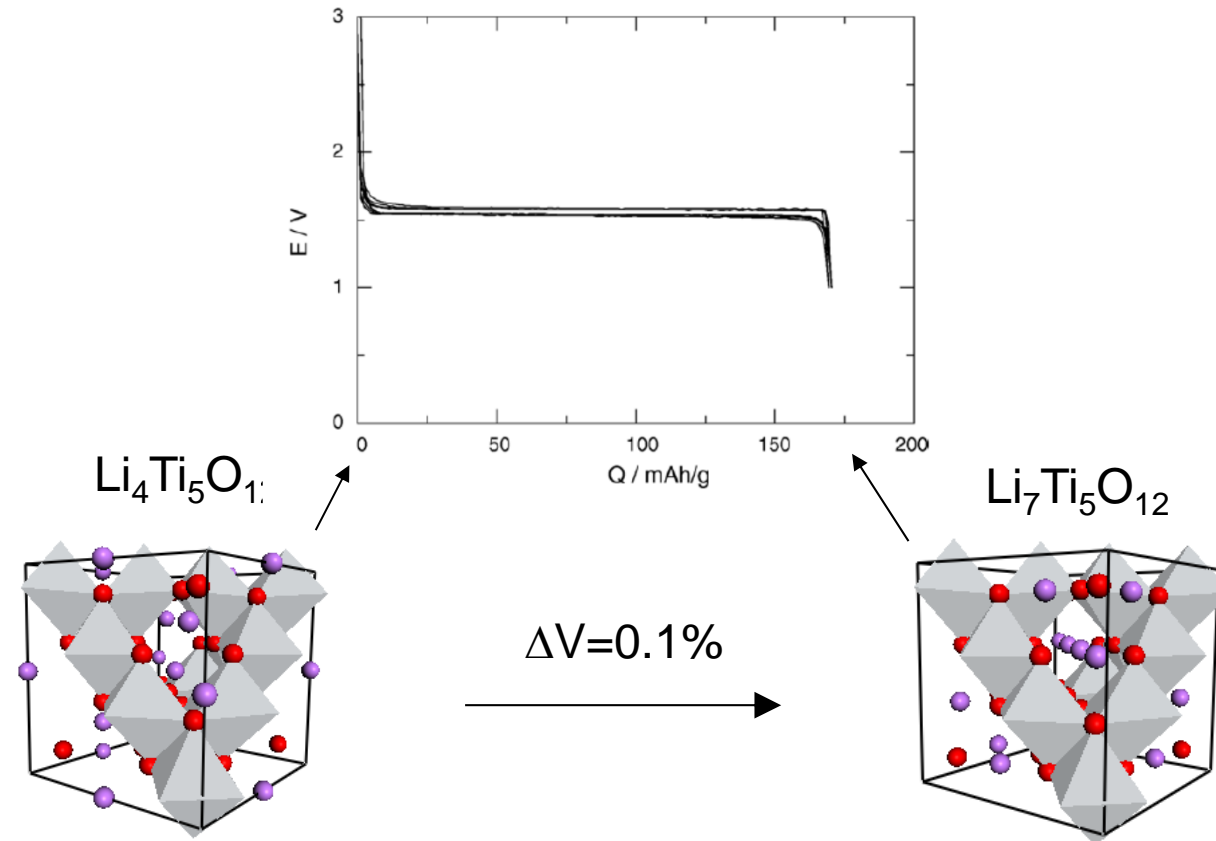
a:	2.822	2.819 Å (10^{-10} m)
b:	2.822	2.819 Å
c:	12.879	14.05 Å

V:	102.56	111.65 Å ³	$\Delta V = 8.9\%$
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Structural changes of the electrode

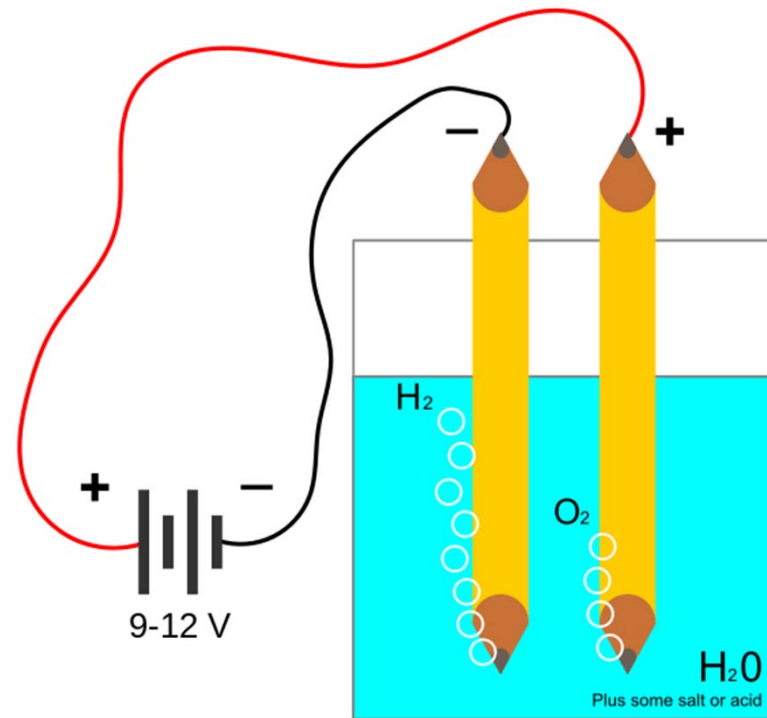
Insertion-reactions: $\text{Li}_4\text{Ti}_5\text{O}_{12}$



-2-

Thermodynamic instability electrode-electrolyte leading to decomposition of the electrolyte

Decomposition of the electrolyte



Electrochemical cells, driving force

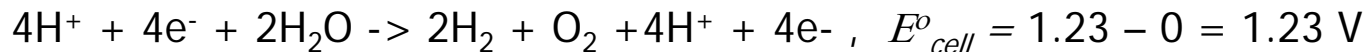
Standard reduction potentials are commonly denoted by the symbol ε° . (means under standard conditions 293 K and 1 bar, 1 molair concentrations) ε° values for hundreds of electrodes have been determined and are usually tabulated in order of increasing tendency to accept electrons (increasing oxidizing power.)

The more positive the half-cell EMF, the smaller the tendency of the reductant to donate electrons, and the larger the tendency of the oxidant to accept electrons

oxidant (electron acceptor)	reductant (electron donor)	E° , volts
$\text{Na}^+ + \text{e}^- \rightarrow$	$\text{Na}(s)$	-2.71
$\text{Zn}^{2+} + 2\text{e}^- \rightarrow$	$\text{Zn}(s)$	-.76
$\text{Fe}^{2+} + 2\text{e}^- \rightarrow$	$\text{Fe}(s)$	-.44
$\text{Cd}^{2+} + 2\text{e}^- \rightarrow$	$\text{Cd}(s)$	-.40
$\text{Pb}^{2+} + 2\text{e}^- \rightarrow$	$\text{Pb}(s)$	-.126
$2\text{H}^+ + 2\text{e}^- \rightarrow$	$\text{H}_2(g)$	0.000
$\text{AgCl}(s) + \text{e}^- \rightarrow$	$\text{Ag}(s) + \text{Cl}^-(aq)$	+.222
$\text{Hg}_2\text{Cl}_2(s) + 2\text{e}^- \rightarrow$	$2\text{Cl}^-(aq) + 2\text{Hg}(l)$	+.268
$\text{Cu}^{2+} + 2\text{e}^- \rightarrow$	$\text{Cu}(s)$	+.337
$\text{I}_2(s) + 2\text{e}^- \rightarrow$	$2\text{I}^-(s)$	+.535
$\text{Fe}^{3+} + \text{e}^- \rightarrow$	$\text{Fe}^{2+}(aq)$	+.771
$\text{Ag}^+ + \text{e}^- \rightarrow$	$\text{Ag}(s)$	+.799
$\text{O}_2(g) + 4\text{H}^+ + 4\text{e}^- \rightarrow$	$2\text{H}_2\text{O}(l)$	+1.23
$\text{Cl}_2(g) + 2\text{e}^- \rightarrow$	$2\text{Cl}^-(g)$	+1.36

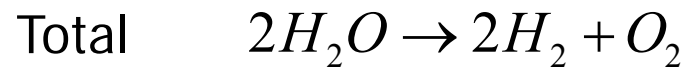
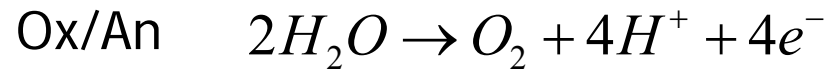
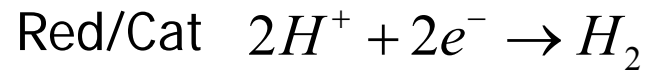
More noble
More likely to run to the right

What is the potential difference we need to split water? Charge!

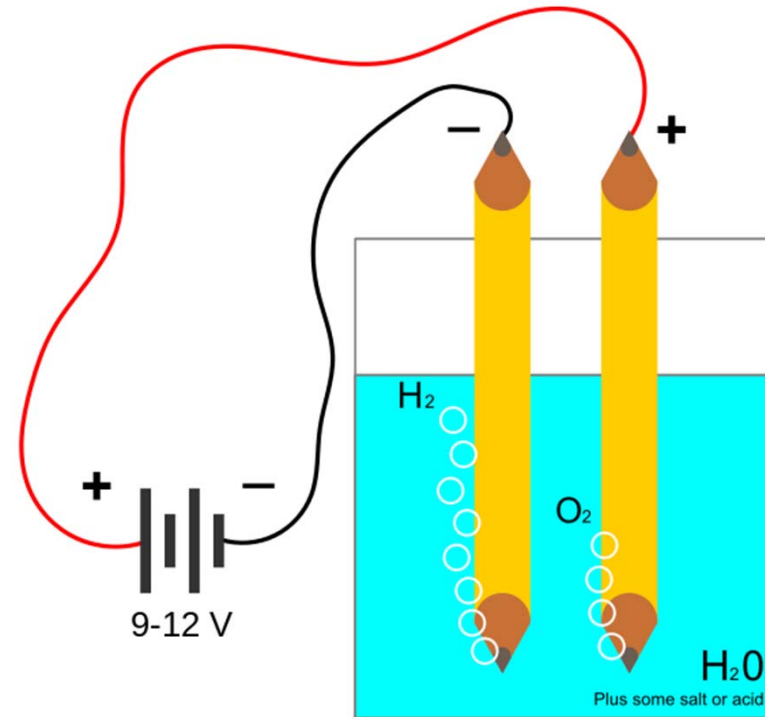
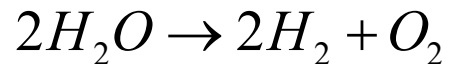
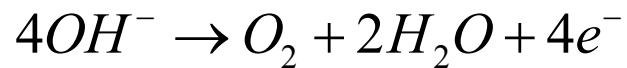
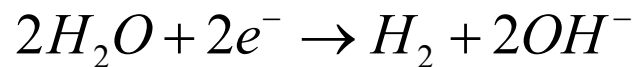


Decomposition of the electrolyte

Splitting of water



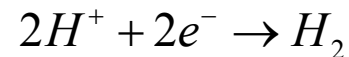
$$E_{Cell}^{\circ} = 1.23 \text{ V}$$



Decomposition of water

Depends on concentrations H^+/OH^- (pH) of water => Nernst

$$E_{Cell} = E^0 - \frac{RT}{zF} \ln \prod c_j^{\nu} = E^0 - \frac{RT}{zF} \ln(K)$$

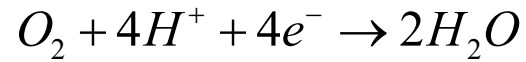


$$E_H = E_{H^+/H_2}^0 - \frac{RT}{zF} \ln \frac{[H_2]}{[H^+]^2} = E_{H^+/H_2}^0 - \frac{RT}{zF} \ln \frac{p_{H_2} / p_0}{[H^+]^2} = E_{H^+/H_2}^0 - \frac{2.303RT}{zF} \log \frac{p_{H_2} / p_0}{[H^+]^2}$$

$$E_{H^+/H_2}^0 = 0, \quad p_{H_2} = p_0, \quad pH = -\log[H^+]$$

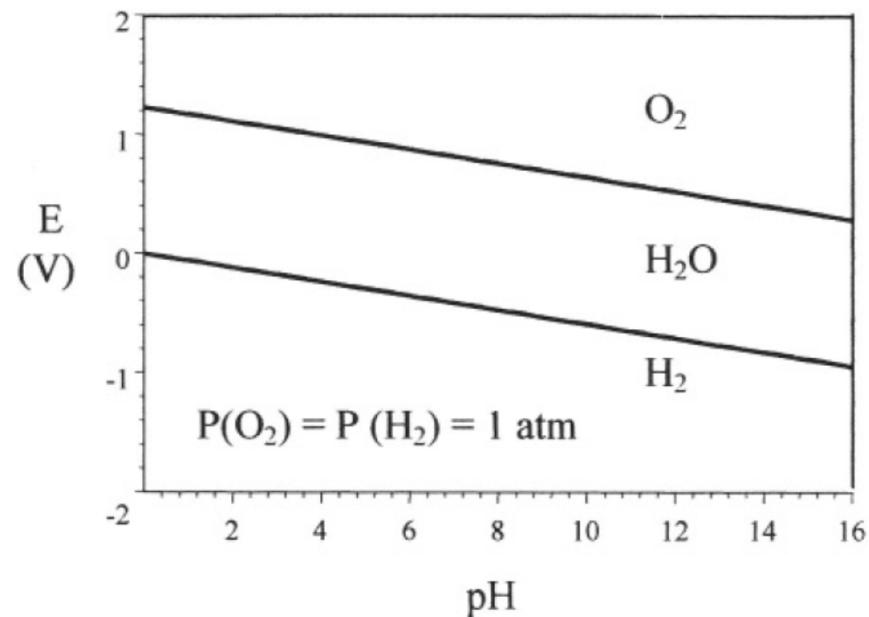
$$E_H = -\frac{2.303RT}{2F} \left[\log \left[\frac{p_{H_2}}{p_0} \right] - 2 \log [H^+] \right] = -\frac{2.303RT}{F} pH$$

Decomposition of water



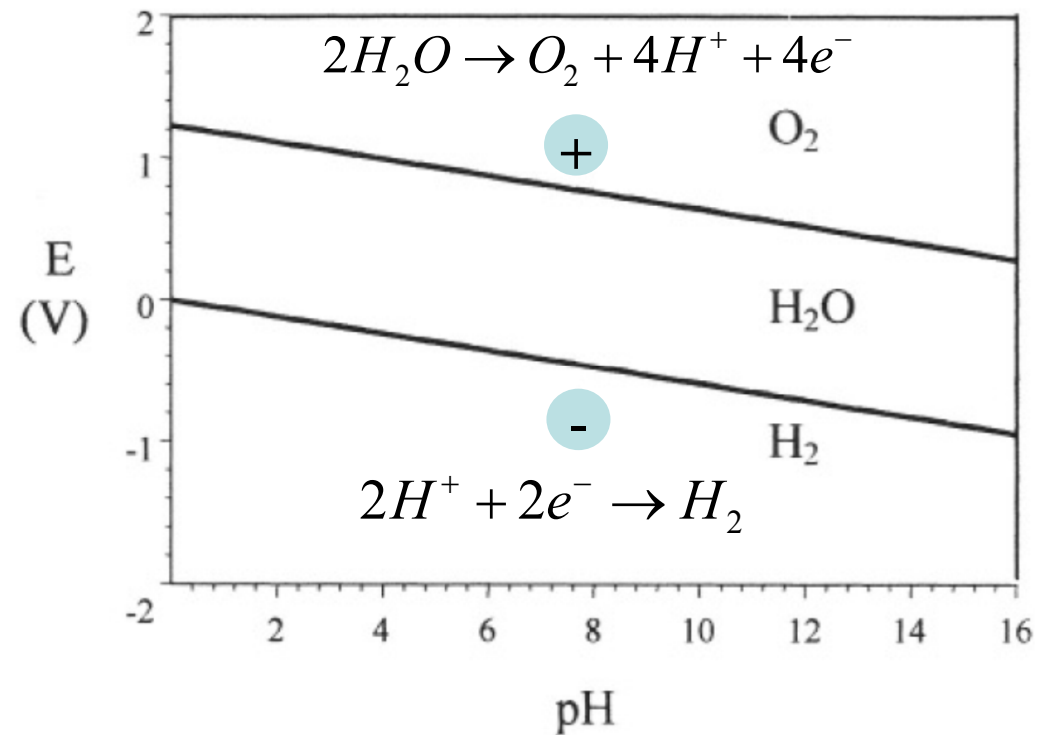
$$E_{O_2} = E_{O_2}^{\circ} - \frac{RT}{zF} \ln \frac{[H_2O]^2}{[O_2][H^+]^4} = 1.229 - \frac{2.303RT}{F} pH$$

Pourbaix Diagram



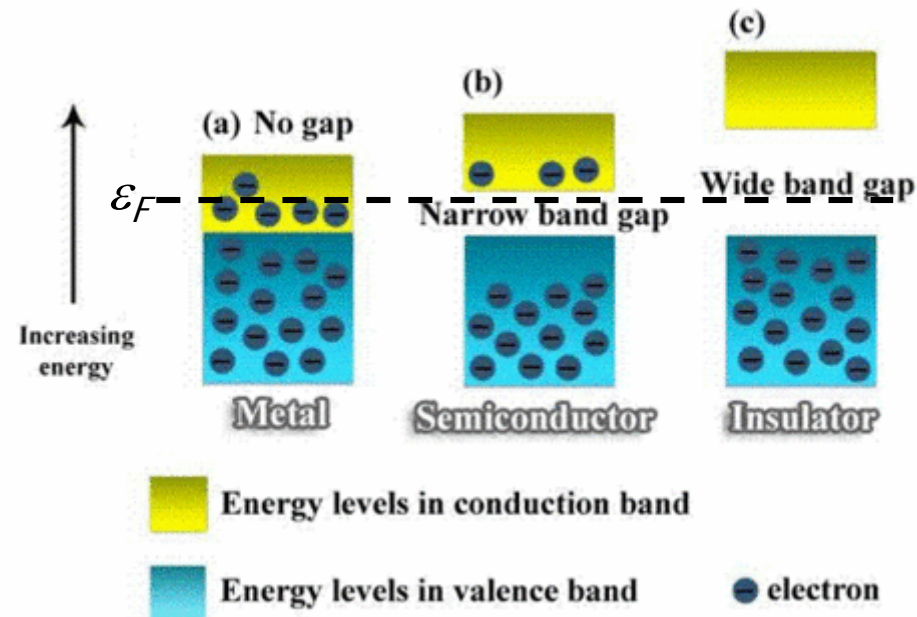
Decomposition of water

Pourbaix Diagram



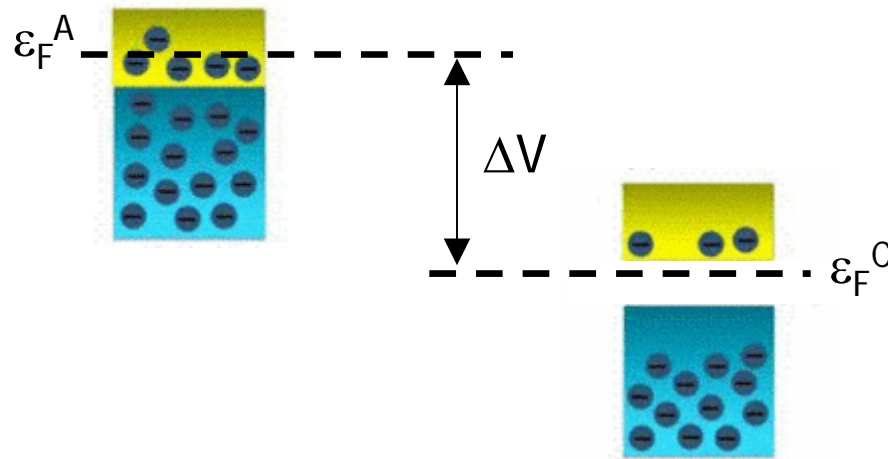
A more general way to look at it: band structure

Band structure of solids

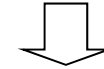


ε_F : Fermi level, potential energy of an electron in a solid defined as the chemical potential of the electron: $\varepsilon_F = \mu_{e^-}$

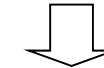
Relation battery voltage and Fermi level



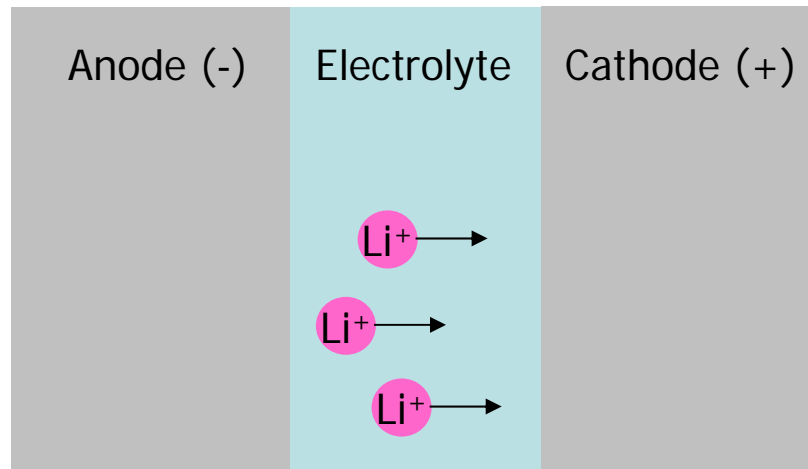
Difference in Fermi level



Difference in electron
chemical potential

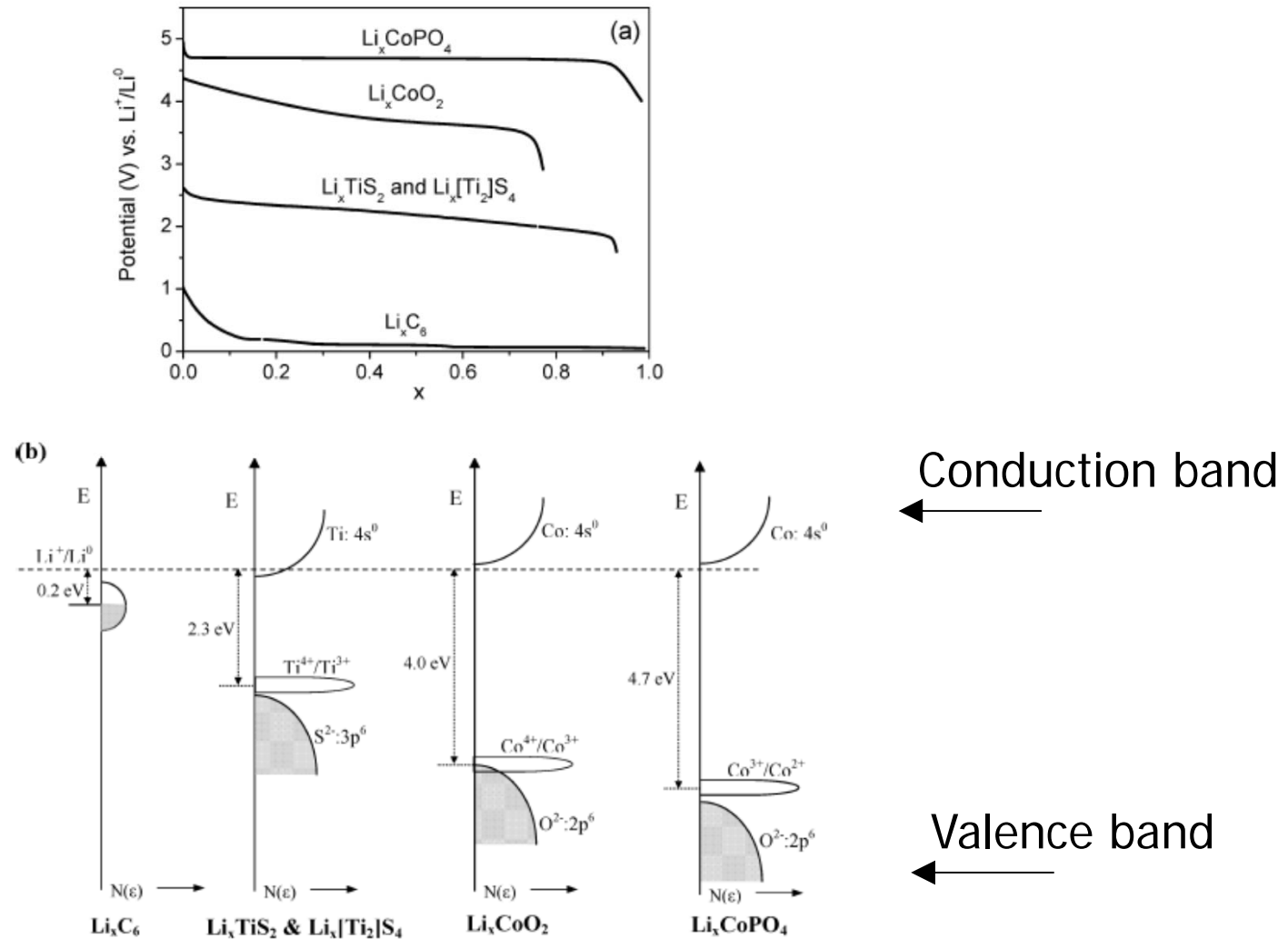


Difference in potential

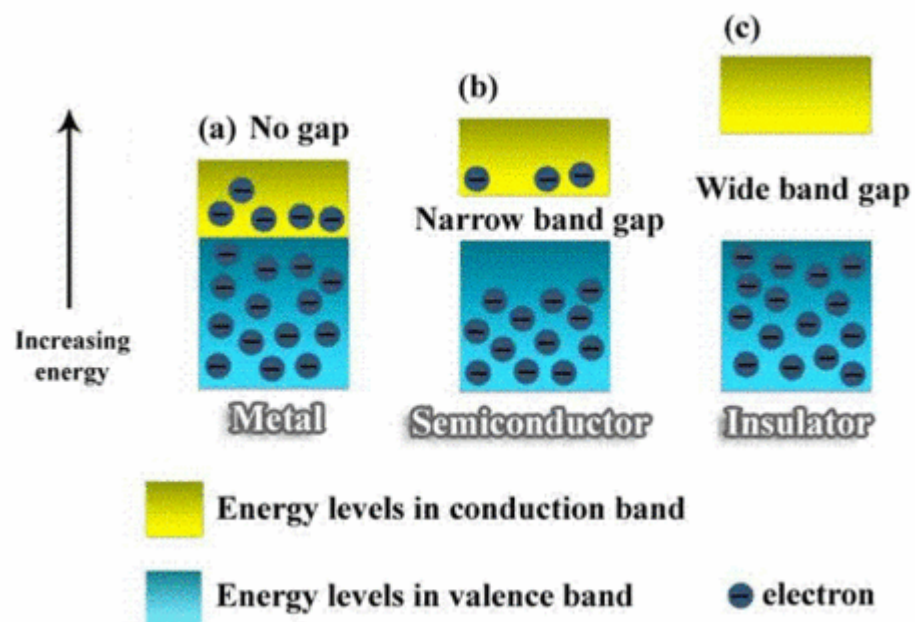


$$E_{Cell} = \mu_{e^-}^A - \mu_{e^-}^C = \varepsilon_F^A - \varepsilon_F^C$$

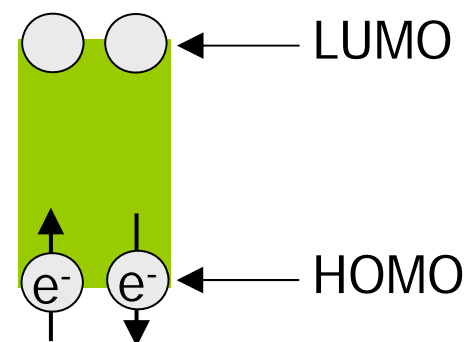
Relation battery voltage and Fermi level



LUMO and HOMO inorganic materials

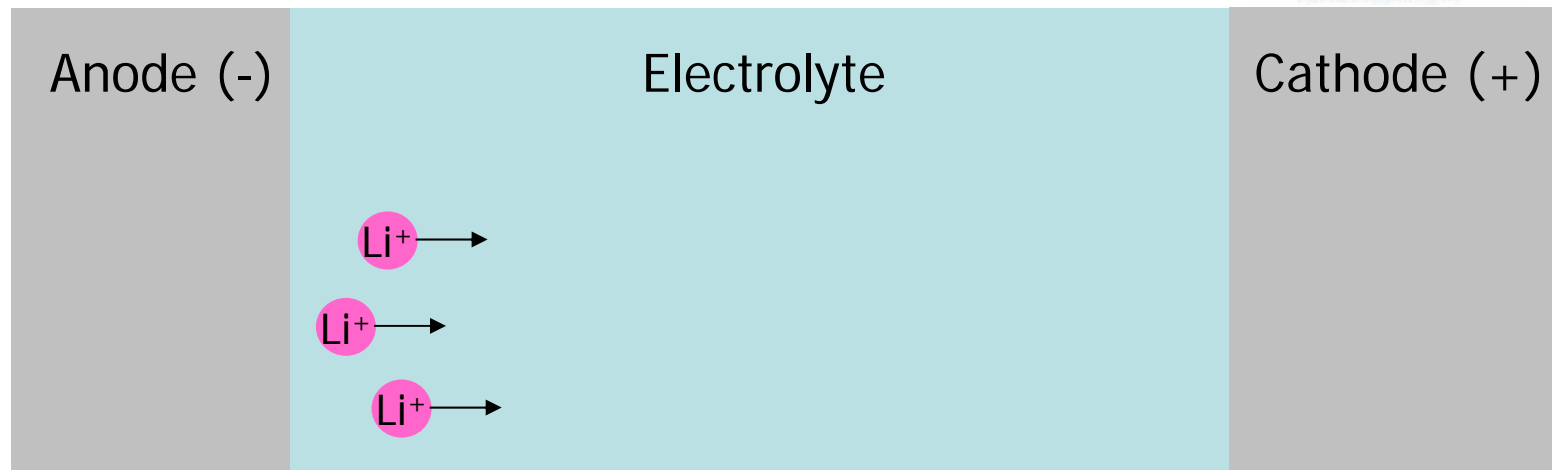
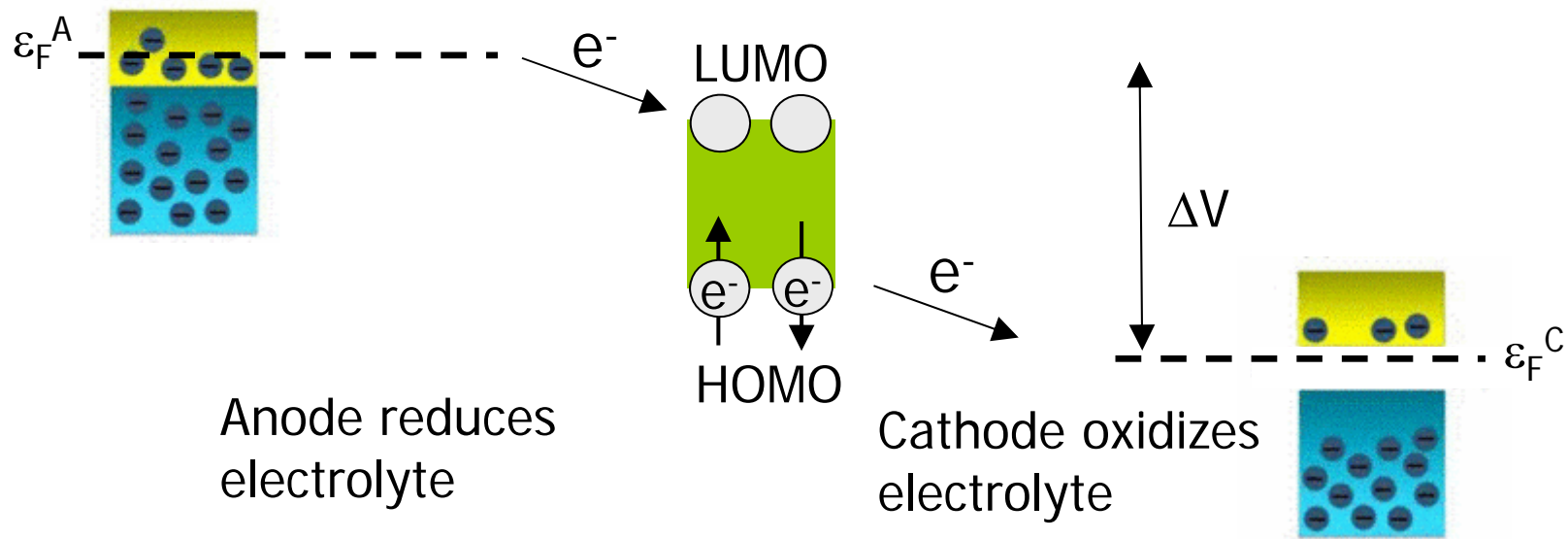


Inorganic material

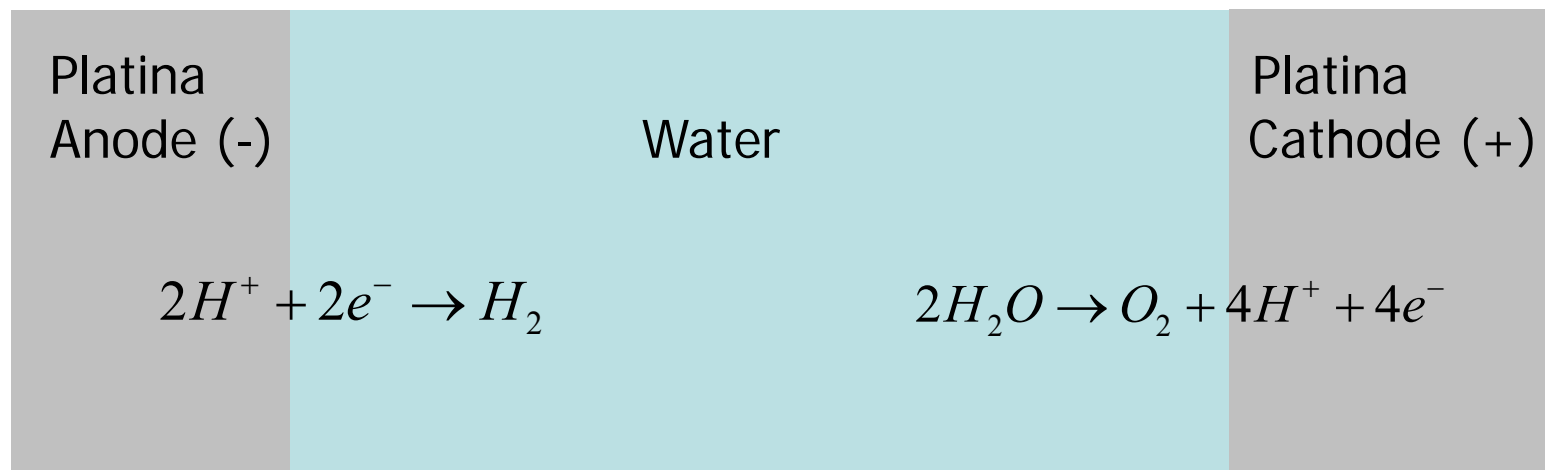
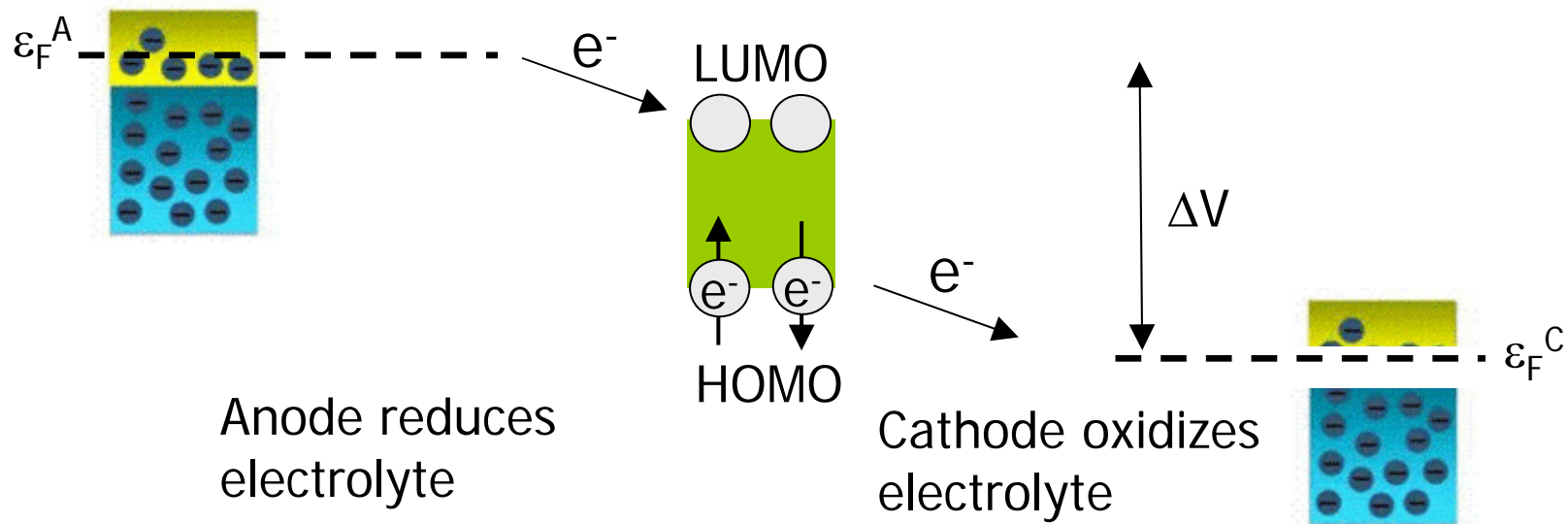


LUMO: Lowest Unoccupied Molecular Orbital (in conduction "band")
HOMO: Highest Occupied Molecular Orbital (in valence "band")

Electrolyte stability

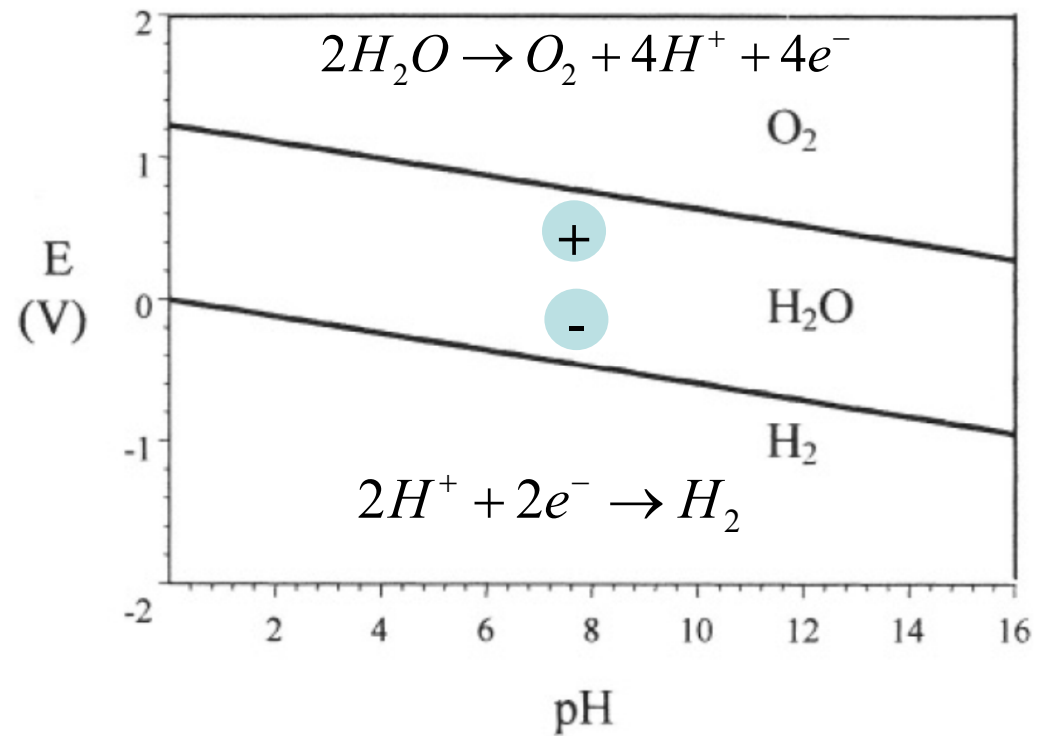


Electrolyte stability

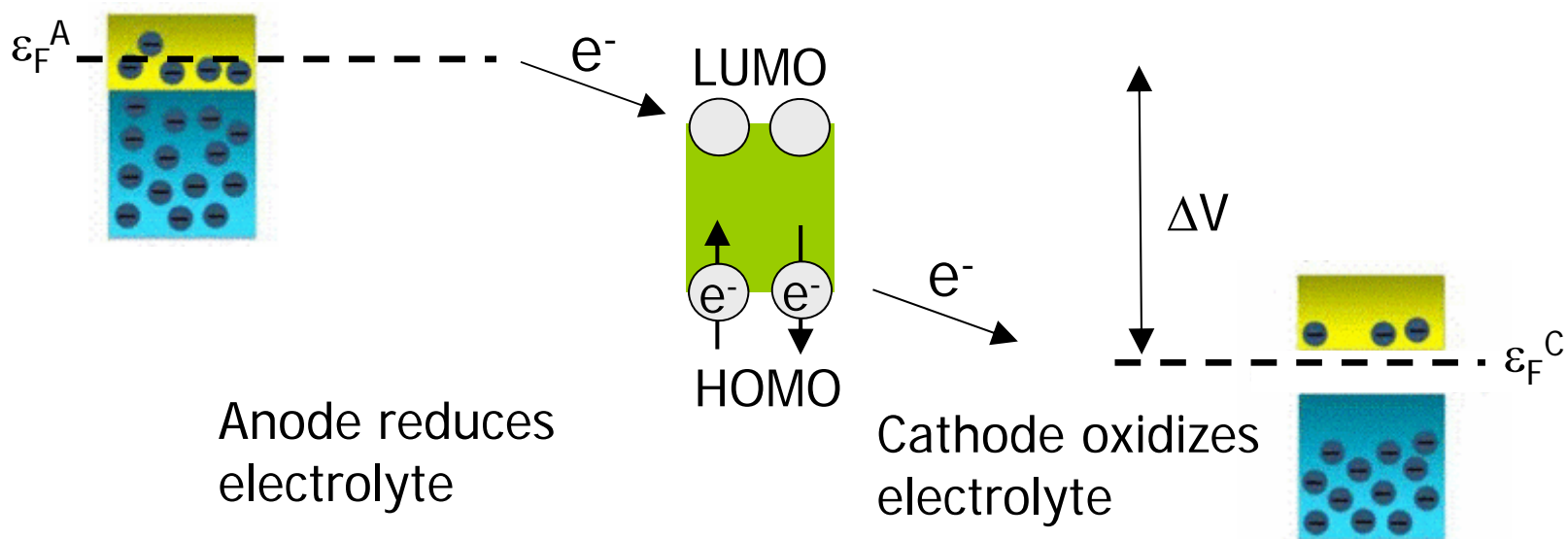


Decomposition of water

Pourbaix Diagram



Question electrolyte stability 1

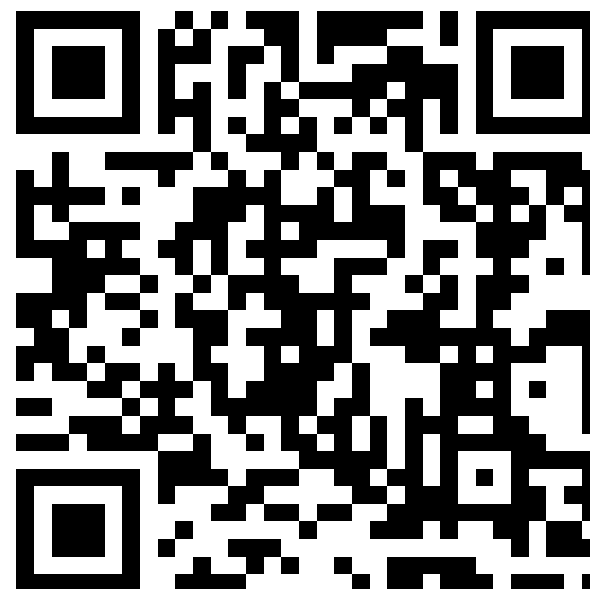


24. To prevent electrolyte decomposition:

- a) The difference between the LUMO and HOMO should be as small as possible
- b) $\text{LUMO-HOMO} > \varepsilon_F^A - \varepsilon_F^C$
- c) $\text{LUMO-HOMO} < \varepsilon_F^A - \varepsilon_F^C$
- d) $\text{LUMO} > \varepsilon_F^A$ and $\varepsilon_F^C > \text{HOMO}$
- e) no clue

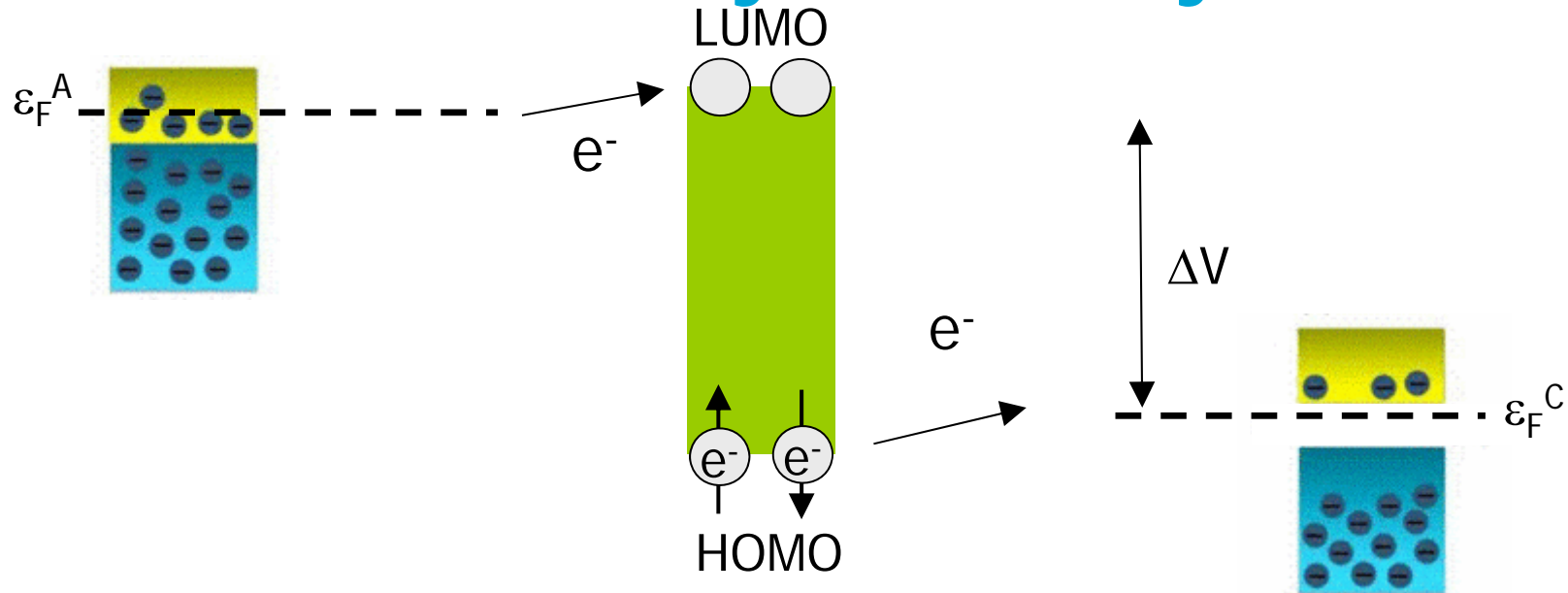
<http://www.edupinion.nl/c619>

Result





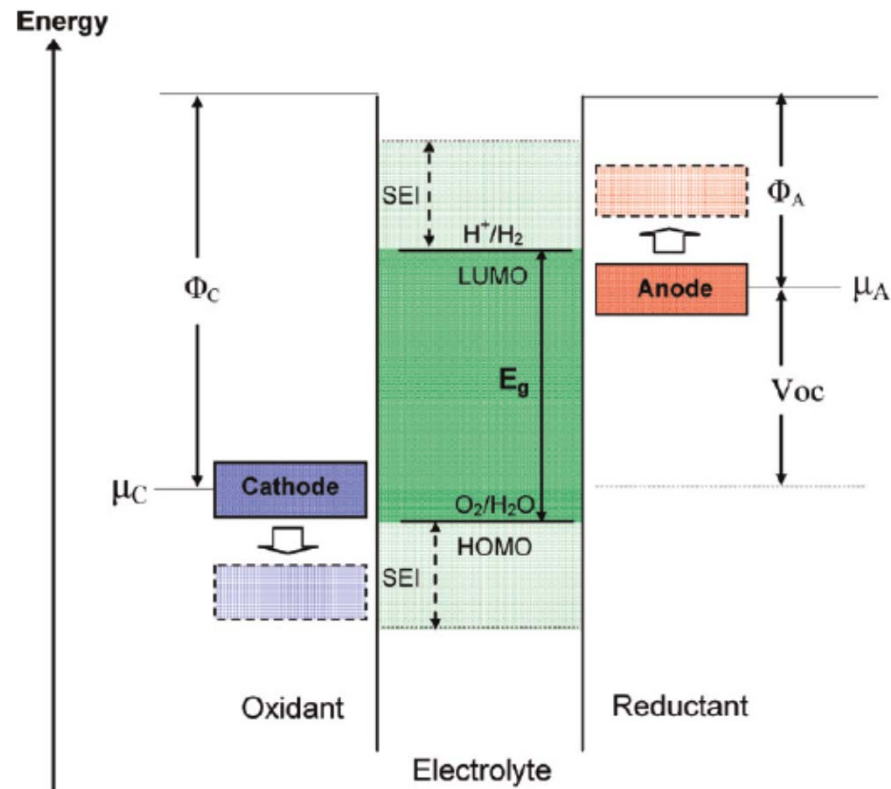
Question electrolyte stability 1



24. To prevent electrolyte decomposition:

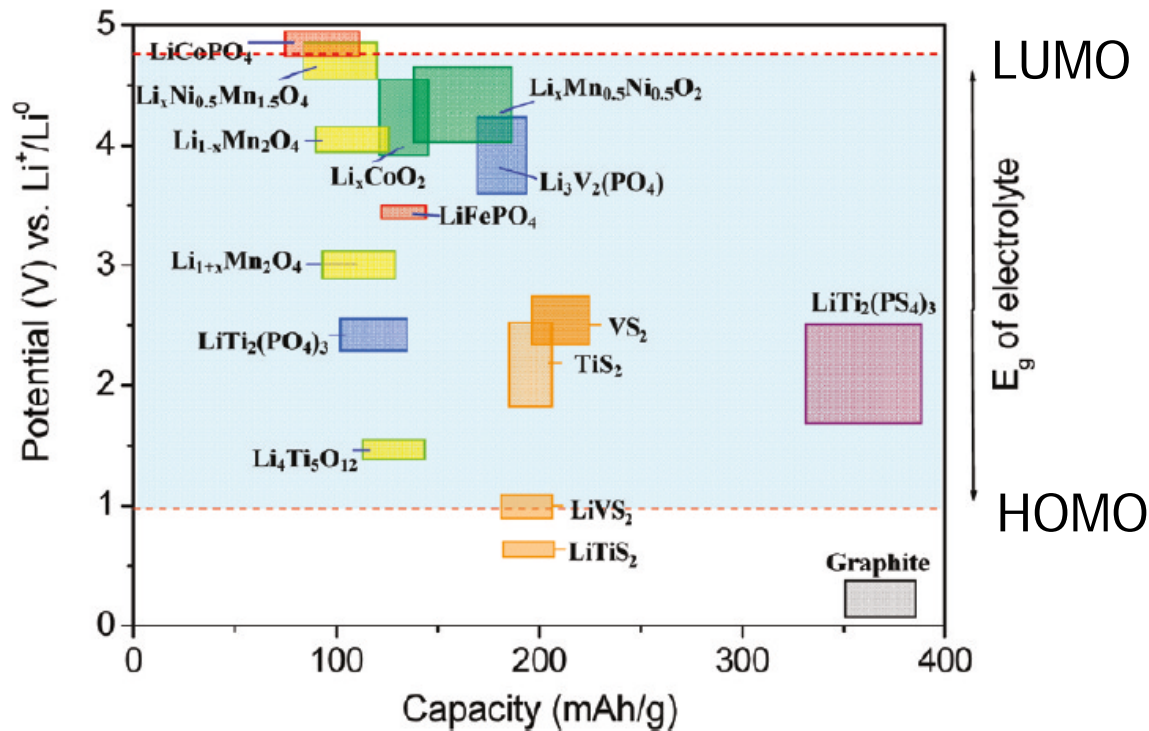
- a) The difference between the LUMO and HOMO should be as small as possible
- b) $\text{LUMO-HOMO} > \epsilon_F^A - \epsilon_F^C$
- c) $\text{LUMO-HOMO} < \epsilon_F^A - \epsilon_F^C$
- d) $\text{LUMO} > \epsilon_F^A$ and $\epsilon_F^C > \text{HOMO}$**
- e) no clue

Electrolyte-electrode stability diagram



$$E_{Cell} = \phi_C - \phi_A = \mu_e^A - \mu_e^C = \varepsilon_F^A - \varepsilon_F^C$$

Question electrolyte stability 2



25. The highest energy density electrode combination that will not result in electrolyte decomposition is:

- a) LiCoPO_4 vs Graphite
- b) $\text{LiNi}_{0.5}\text{Mn}_{1.5}\text{O}_4$ vs LiVS_2
- c) $\text{Li}_3\text{V}_2(\text{PO}_4)_3$ vs $\text{LiTi}_2(\text{PS}_4)_3$
- d) LiCoPO_4 vs LiVS_2
- e) no clue

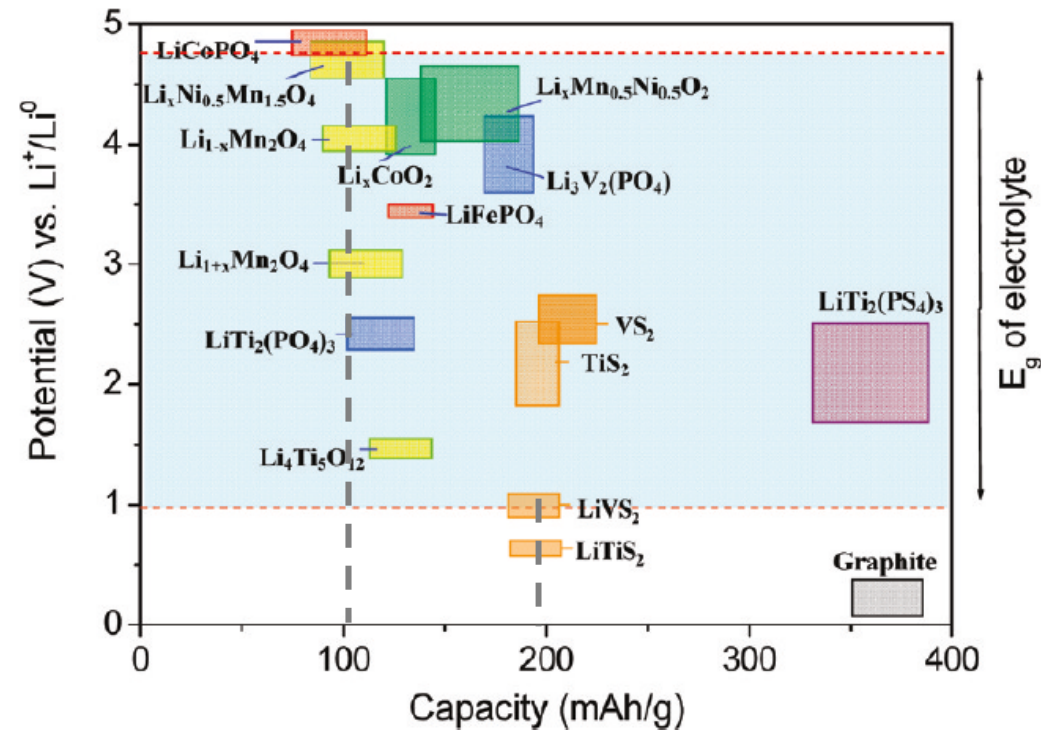
<http://www.edupinion.nl/c863>

Result



Question electrolyte stability 2

Energy = Capacity x Voltage
 (1 mAh/g = 3.6 C, [V] = [J/C])

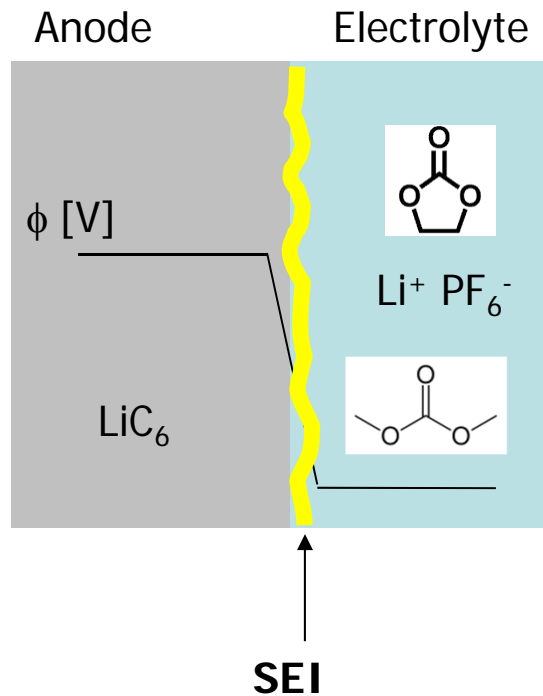


25. The highest energy density electrode combination that will not result in electrolyte decomposition is:

- a) LiCoPO_4 vs Graphite:
- b) $\text{LiNi}_{0.5}\text{Mn}_{1.5}\text{O}_4$ vs LiVS_2 : $\sim 150 \times 3.5 = 525$
- c) $\text{Li}_3\text{V}_2(\text{PO}_4)_3$ vs $\text{LiTi}_2(\text{PS}_4)_3$ $\sim 270 \times 2 = 545$
- d) LiCoPO_4 vs LiVS_2
- e) no clue

SEI Formation

Formation of the Solid Electrolyte Interface (SEI) at the negative electrode



Side reactions take mainly place at the interface between electrolyte and anode

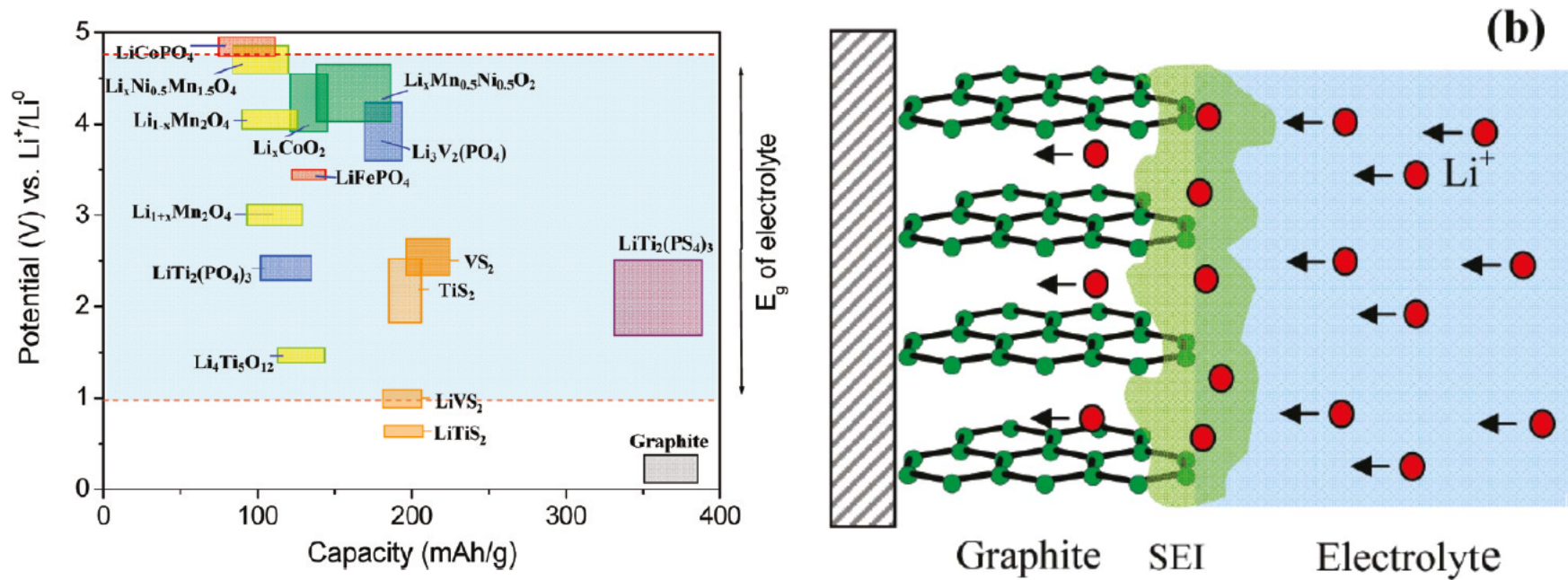
At low voltage (0-0.8 V versus Li metal) the inorganic solvents are thermodynamically unstable versus the anode

Leads to the formation of a Solid Electrolyte Interface (SEI) layer (Li_2CO_3 , alkyl-carbonates, polymers...)

Ethylene Carbonate (EC):

Dimethyl Carbonate (DMC):

Example SEI Formation: Graphite

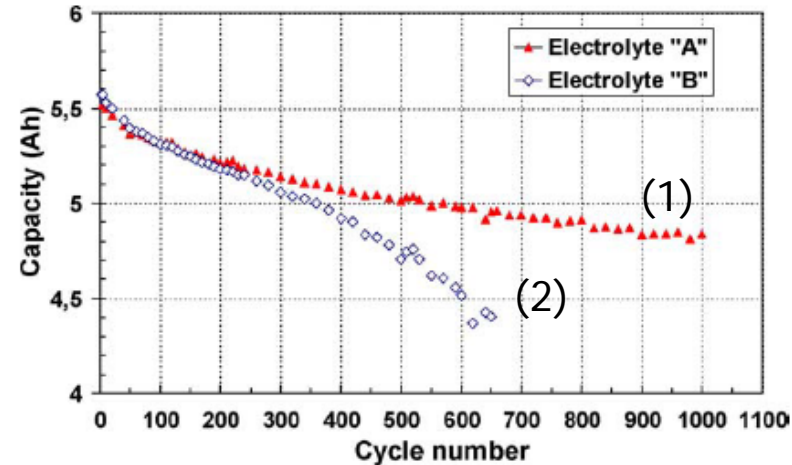
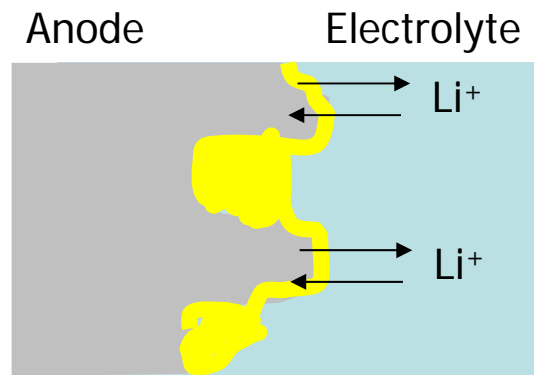
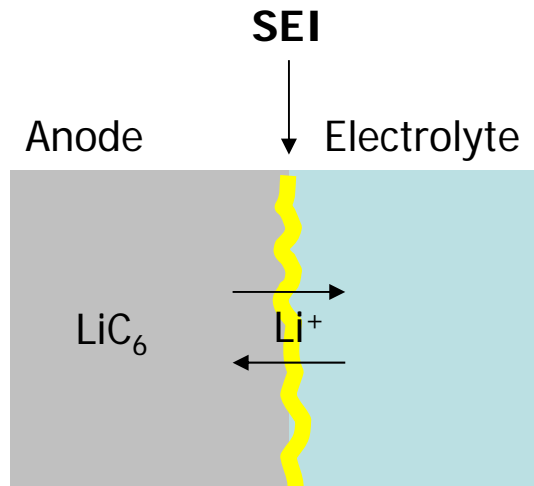


SEI Formation

Depending on the electrolyte, interface and salt the SEI can:

(1) Form a stable electronic isolating layer (but ionic conducting) passivating further side reactions -> long cycle life

(2) Grow extensively blocking Li-transfer and reducing active surface area -> increasing the current density -> higher over potentials -> more SEI formation -> avalanche effect -> short cycle life

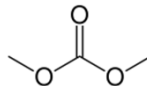
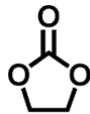


Demands Li-ion Electrolyte

- Good (Li⁺) ionic conductor
- Electronic Isolator
- Stability window 5 V (depends on sys.)
- Stable up to ~ 70 degree celcius
- Cheap
- Non toxic

Mostly applied: Non aqueous solvents:

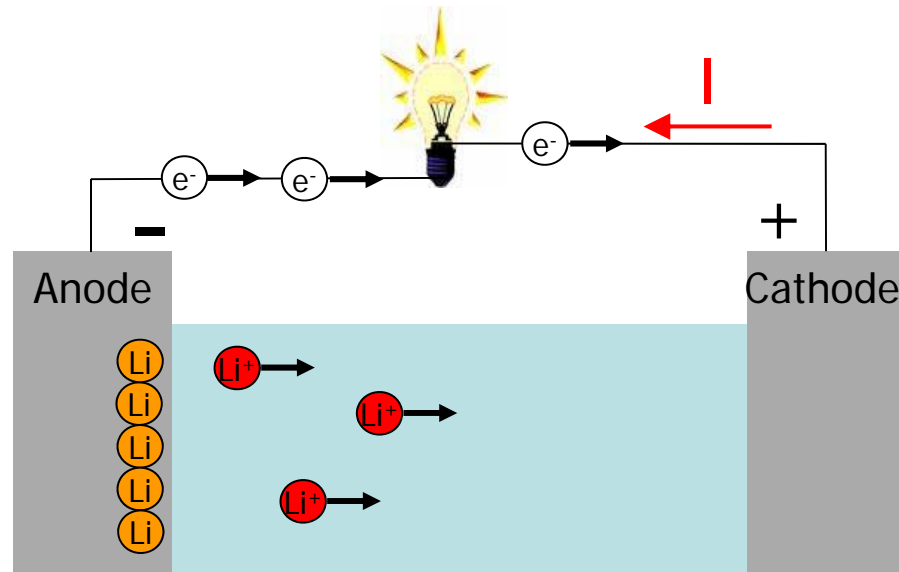
Ethylene Carbonate (EC), Dimethyl Carbonate (DMC)



Good ionic conduction, stability ~ 0.8-4.5 V (vs Li/Li⁺)

Medium toxic, flammable, unstable etc -> Casing battery should be very good (=expensive)

Li salts: LiClO₄ or LiPF₆: Toxic and expensive



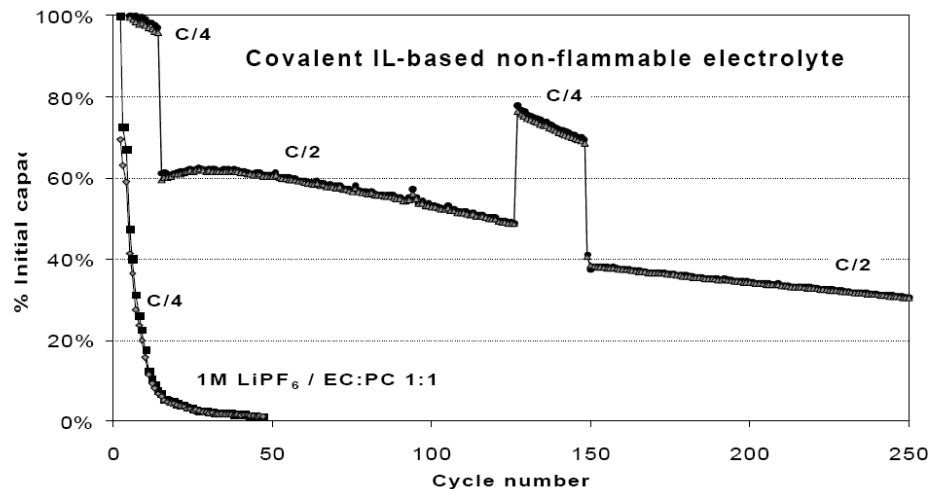
Li-ion batteries, ionic liquids

Ionic liquid: salt in the liquid state:

electronic isolator
good ionic conductor
thermal stability
non-flammable
chemically stable (large stability window)
cheap?

} safe

Li-ion Cycling Performance at 100°C

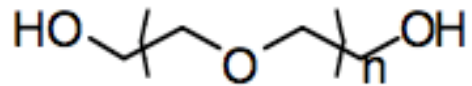


Li-ion batteries, solid electrolytes

Solid electrolytes:

Less difficulty/cost associated with long term encapsulating liquid electrolytes (that may start leaking), freedom design of batteries, high temp.

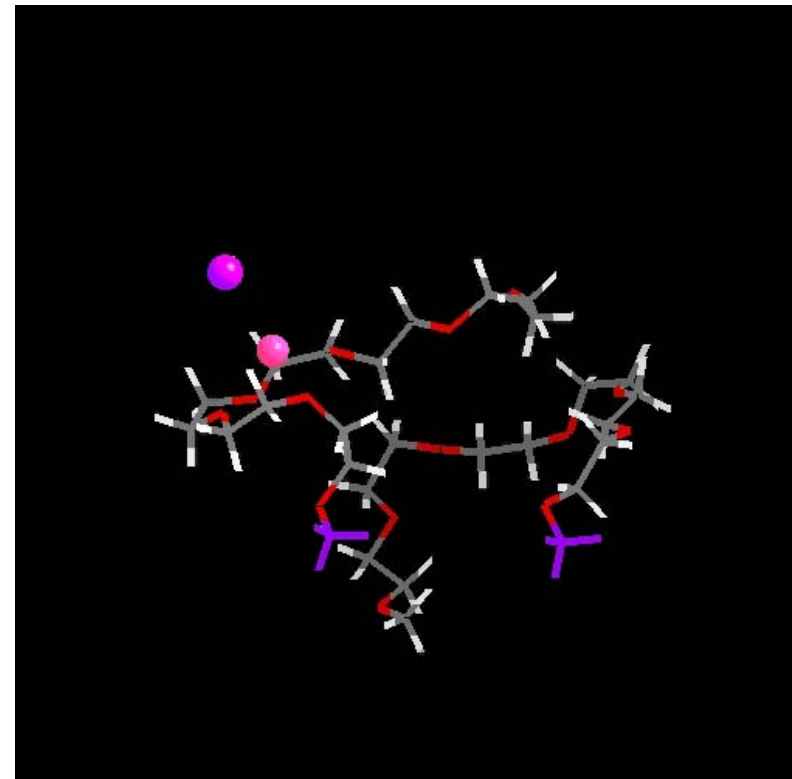
Example: polymer electrolytes like polyethyleneoxide



Because polymers can have intrinsic mobility of the polymer chains, a dissolved Li salt can also move through it. However, solid electrolytes show much lower Li^+ conductivities (low power density)

Application limited to large systems that can be maintained at high temperatures

Poor ionic mobility, PEO LiI



Li-ion batteries, electrolytes

Other strategy:

Adding nano-particles increases the Conductivity in PEO-LiClO₄

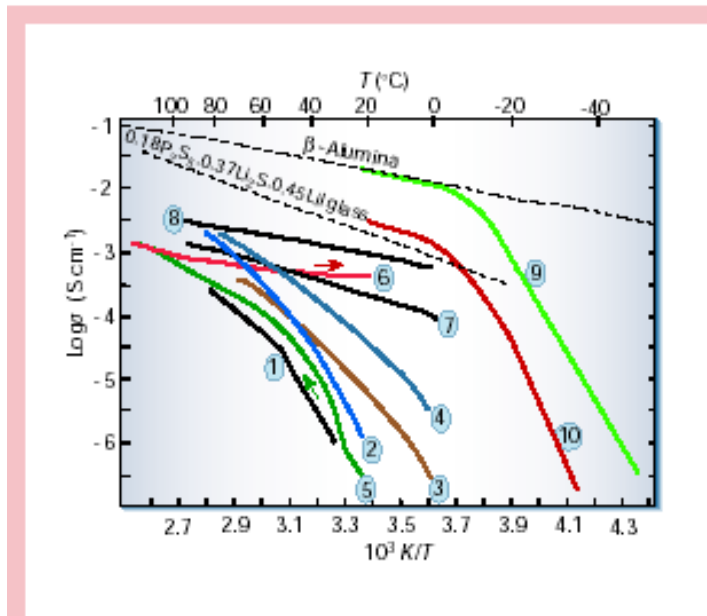
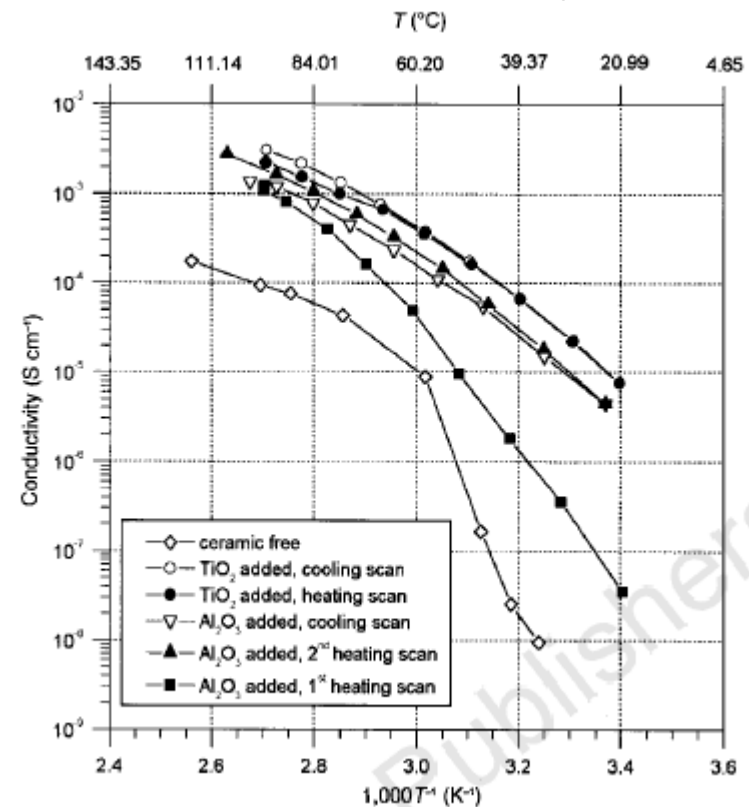
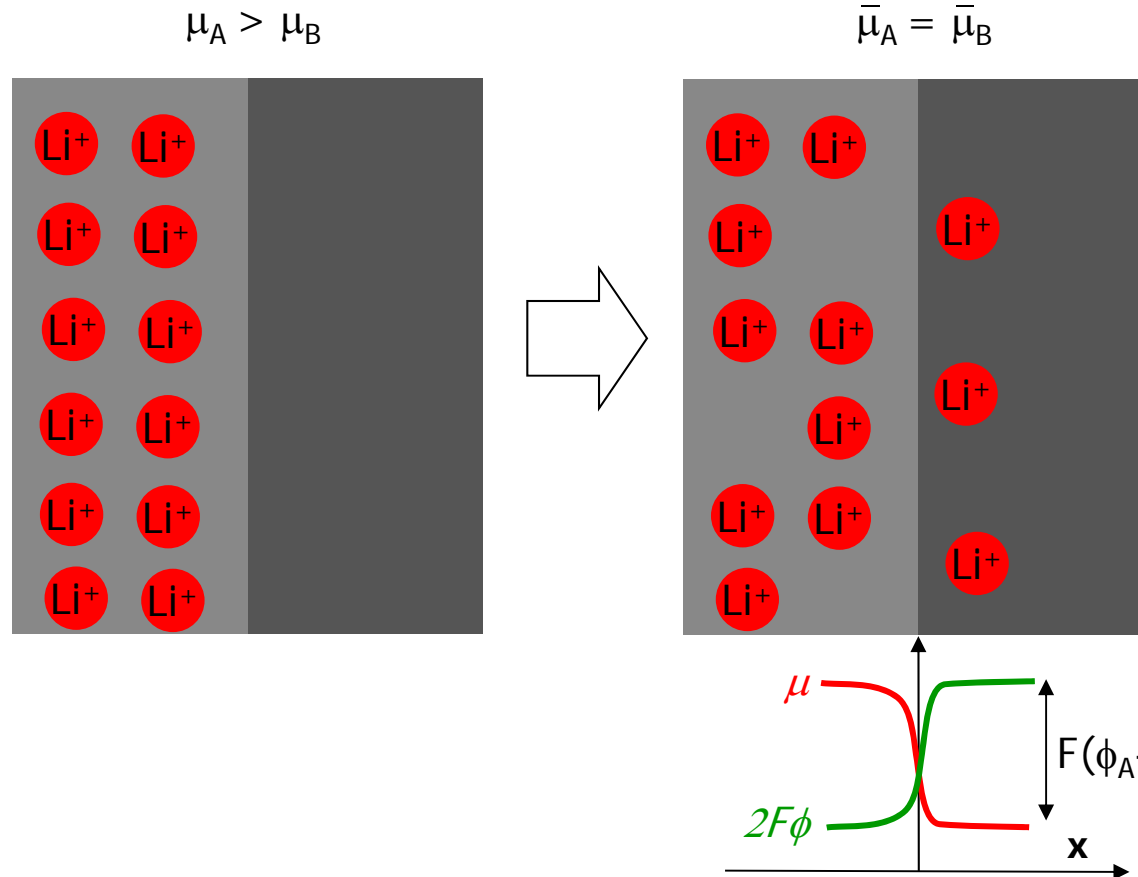


Figure 8 Arrhenius plot of conductivity for various solid electrolytes. 1, First-generation PEO-LiCF₃SO₃; 2, new solutes with high-dissociation PEO-Li[(CF₃SO₂)₂N]; 3, low-*T*_g combination polymer; 4, plasticized polymer electrolyte PEO-Li[(CF₃SO₂)₂N] + 25% w/w PEG-dimethylether (molecular weight, 250); liquid crystalline polymer electrolytes; 5, heating curves; 6, cooling curve⁶⁴; 7, gel-type polymer (X-linked PEO-dimethacrylate-Li[(CF₃SO₂)₂N]-PC 70%); 8, liquid electrolyte PC/DME LiCF₃SO₃; 9, liquid electrolyte EC/DMC-LiPF₆ at low temperature⁶¹; 10, gel electrolyte P(VDF-HFP)/EC/DMC-LiPF₆ (ref. 61).



Space charges

Two ion conductors and poor electronic isolators:



$$(\phi_A - \phi_B) = -\frac{(\mu_A - \mu_B)}{F}$$

$$\mu_A + F\phi_A = \mu_B + F\phi_B$$

$$\bar{\mu}_A = \bar{\mu}_B$$

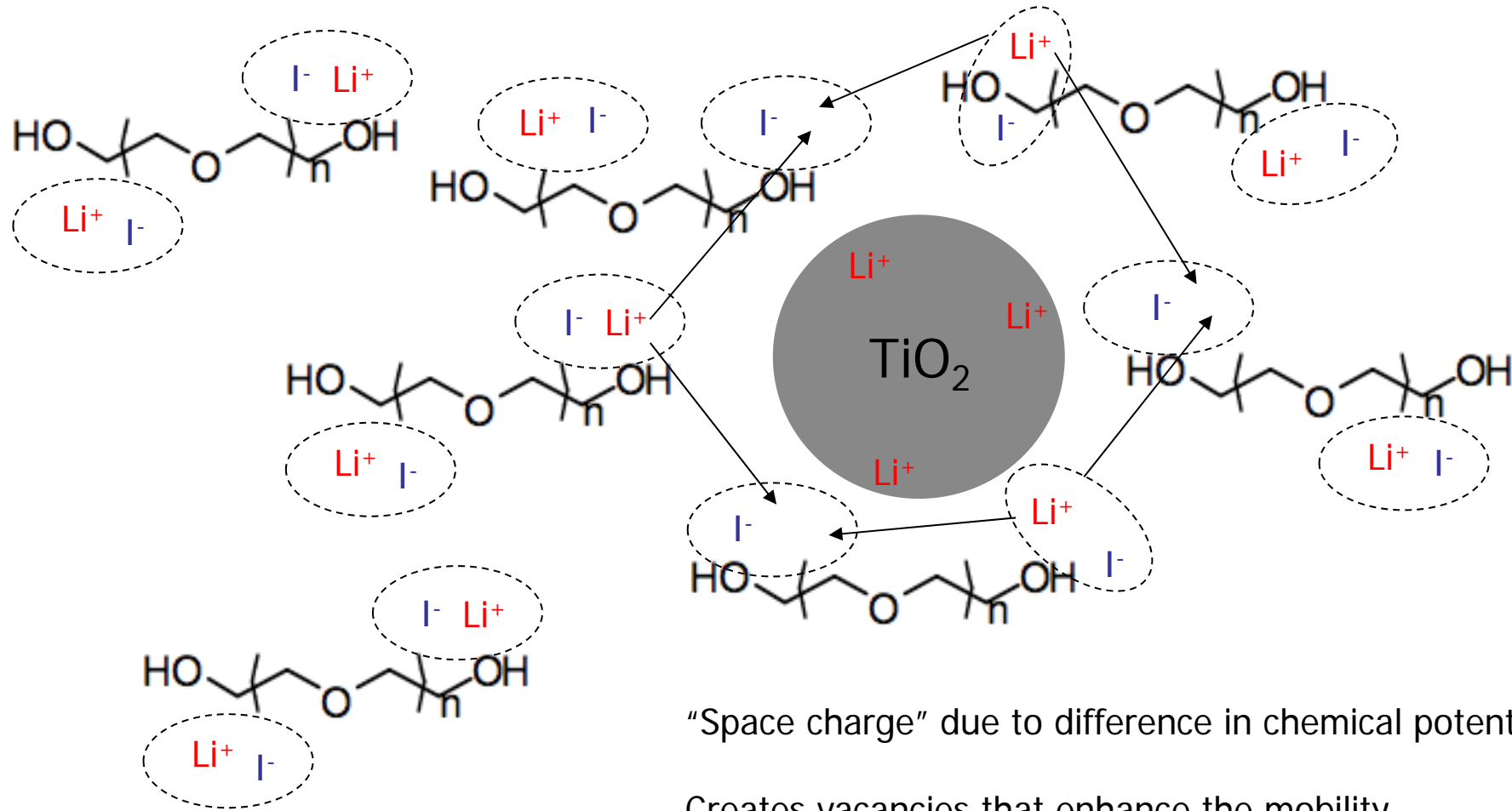
Creates vacancies in A!

Is called "Space Charge"

For diffusion you need vacancies



Li-ion batteries, electrolytes



"Space charge" due to difference in chemical potential

Creates vacancies that enhance the mobility

Practical questions



What is the direction of a redox reaction?



What is the voltage that a redox reaction can deliver?



What is the energy density of a battery?



What determines the cycle life of a battery

What is the power density of a battery? -> kinetics

Practical Energy Density

Energy density only exists for a combination of electrodes, capacity times voltage:

$$\text{EnergyDensity}[J / g] = \frac{xzF \varepsilon_{\text{Cell}}}{M}$$

x : Fractional occupancy host materials Li_xM

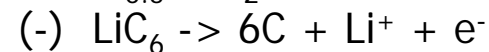
F : Faraday's constant [C/mol]

z : number of electrons involved in the reaction (=1 for Li^+)

$\varepsilon_{\text{Cell}}$: cell potential [V]

M : mass of the electrodes (sum of both!) [g/mol]

Example:



0.5 Li^+ stored per unit CoO_2 , this requires 0.5 C_6

\Rightarrow For $x = 0.5$ $M = M_{3\text{C}} + M_{\text{CoO}_2} = 127 \text{ g/mol}$

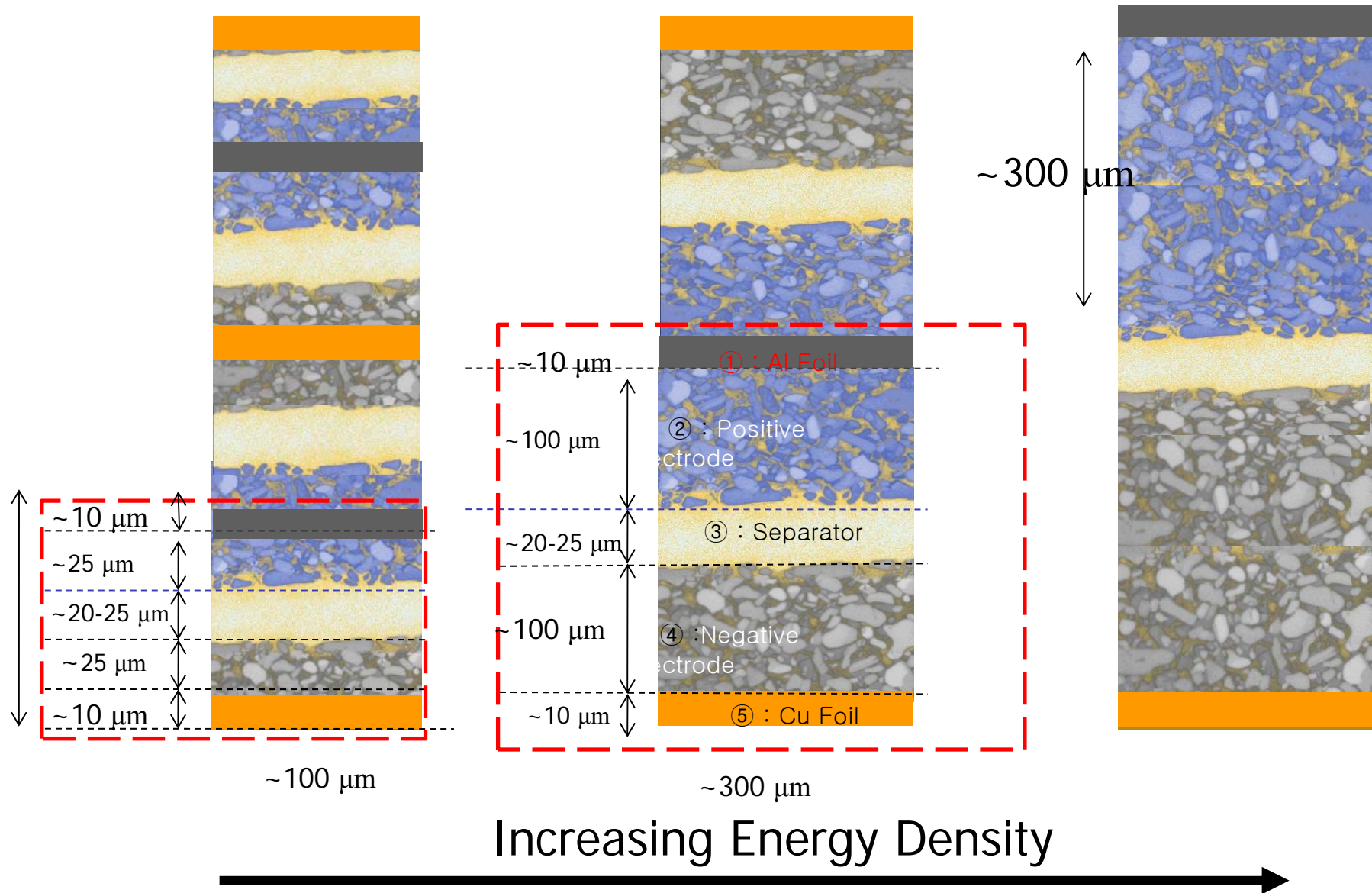
\Rightarrow Using $\varepsilon_{\text{Cell}} = 3.6 \text{ V}$ it follows that $\text{Energy density} = 1370 \text{ J/g} = 380 \text{ Wh/kg}$

This is only taking into account the weight of the electrodes,

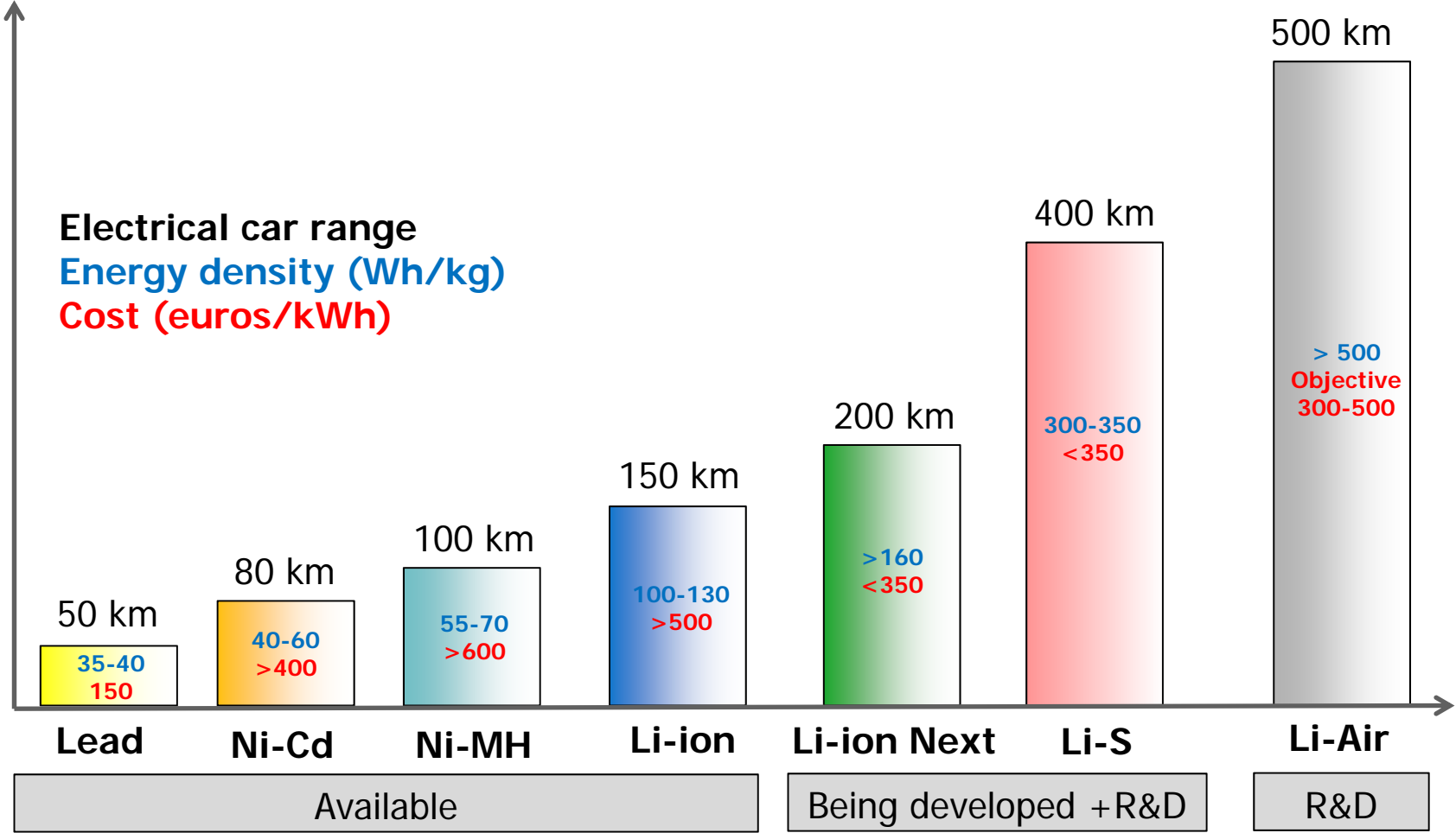
Electrode additives, Electrolyte, separator, current collectors and packing:

Energy density complete battery $\sim 110 \text{ Wh/kg}$ ($\sim 30\%$)

Energy density: amount of active material



Energy density for mobility



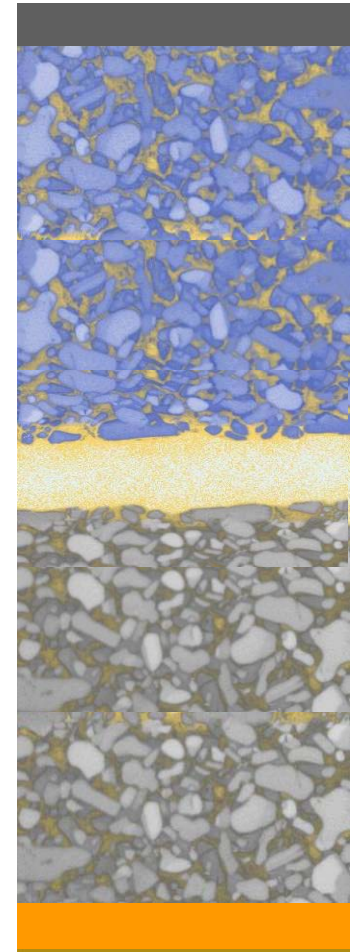
Question Energy Density

26. Why do you think batteries in practice have relatively thin (\sim max $50 \mu\text{m}$) electrodes?

- a) Difficult to make
- b) Long (dis)charge times
- c) Shorter cycle life
- d) No clue



$\sim 300 \mu\text{m}$





Question Energy Density

26 Why do you think batteries have in practice relatively thin electrodes?

- a) Difficult to make
- b) Long (dis)charge times
- c) Shorter cycle life
- d) No clue

L : diffusion length:

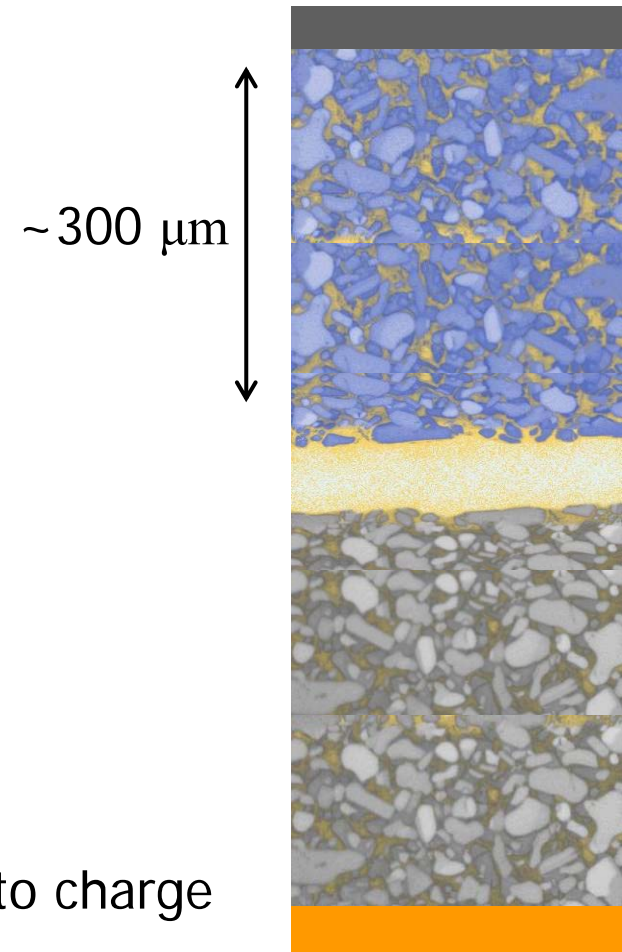
D : diffusion coefficient

t : diffusion time

$$L \approx \sqrt{\pi Dt}$$

$$t \approx \frac{L^2}{\pi D}$$

Electrode 6 times thicker => takes 36 times longer to charge



Practical questions



What is the direction of a redox reaction?



What is the voltage that a redox reaction can deliver?



What is the energy density of a battery?



What determines the cycle life of a battery

What is the power density of a battery? -> kinetics

Program Batteries

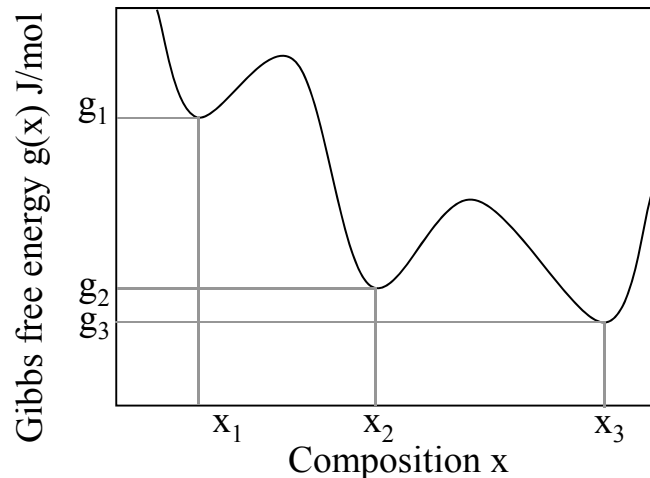
- Lecture 1: History, Applications, basic Electrochemistry and thermodynamics of batteries: Redox reactions, Gibbs free energy, chemical potential, Nernst.
Feb 27
- Lecture 2: Solid state electrode reaction mechanisms, phase diagrams, phase rule, Gibbs Free energy, voltage profiles, capacities and energy densities. Li-ion batteries
March 6
- Lecture 3: Continue topics Lecture 2. Electrolyte stability: Pourbaix diagram, band structure solids, Cycle life.
March 13
- Lecture 4: Kinetics, Buttlar-Volmer, diffusion, solid state diffusion
March 20
Discussion on Science paper 6 seconds discharge.
- Lecture 5: Super capacitors
March 27
Future systems: Li-air, Li-sulphur
Flow-cells
Batteries for static storage, NaS, Na aqueous.
Costs and Performance comparison batteries/systems
Material Abundance

Home assignments

Read Chapters 3.1-3.3 Electrochemistry

Read Paper Ceder et al. Science (bb)

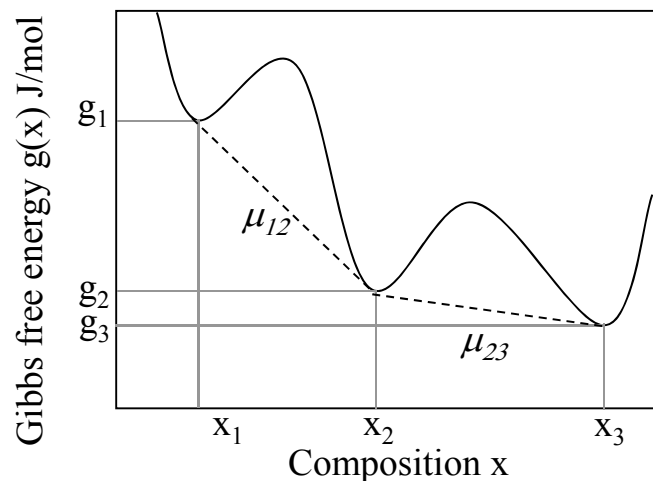
Exercise:



$g(x)$ is the Gibbs Free energy of the cathode during discharge, assume the potential of the anode to be 0 and constant

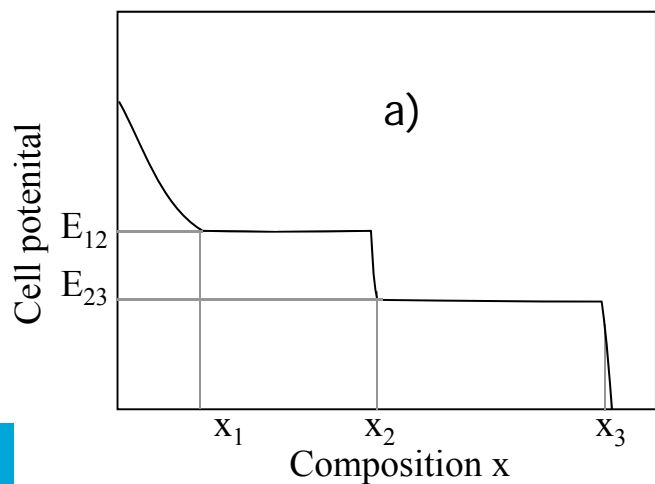
- Sketch the voltage profile resulting from the Gibbs Free energy diagram
- In which direction with this reaction proceed
- Calculate the voltage of the voltage plateau('s) if any.
- Sketch a phase diagram that could represent this Gibbs Free energy diagram

Home assignment



$g(x)$ is the Gibbs Free energy of the cathode during discharge, assume the potential of the anode to be 0 and constant

- Sketch the voltage profile resulting from the Gibbs Free energy diagram
- Which direction will this reaction proceed?
- Calculate the voltage of the voltage plateau('s) if any.
- Sketch a phase diagram that could represent this Gibbs Free energy diagram



- In the direction of decreasing Gibbs Free energy: right