

# Fluid mechanics

## Instruction 7


# Week 7

Van onderstaande vraagstukken zal tijdens de instructie er een aantal behandeld worden. Het is een goede voorbereiding er doorheen te kijken, en te proberen of je ze zelf kan oplossen.

Let op: vraagstuknummering is niet altijd uniform door de verschillende edities van 'White'.

Bron: alle opgaven komen van het boek *Fluid Mechanics* van Frank M. White (McGraw-Hill Series in Mechanical Engineering)

# Grenslagen

**P7.36**  A ship is 125 m long and has a wetted area of 3500 m<sup>2</sup>. Its propellers can deliver a maximum power of 1.1 MW to seawater at 20°C. If all drag is due to friction, estimate the maximum ship speed, in kn.

Hint: Een 'kn' is uiteraard geen kilo-newton, maar een knot = 'knoop'.  
1 knoop = 1 nmi/hr = 1 nautic mile / hour = 1 zeemijl per uur  
1 zeemijl = 10 kabellengtes = 1852 meter.

# Aerodynamica

Hint: 'landmijl' is geen 'zeemijl',  
maar slechts 1609 m.

**P7.57** The main cross-cable between towers of a coastal suspension bridge is 60 cm in diameter and 90 m long. Estimate the total drag force on this cable in crosswinds of 50 mi/h. Are these laminar-flow conditions?

Andere Mijl eenheden:

- Duitse (of geografische) mijl - 7407,41 meter
- Hollandse mijl - 5555,6 meter (1/20 graden)
- Zweedse en Noorse mijl - 10 kilometer
- Spaanse mijl - bijna 7 kilometer
- Oude Romeinse mijl - bijna 2,5 kilometer.

# Aerodynamica

Hint: 'standard atmosphere' staat hieronder.

Los de differentiaalvergelijking niet op, maar bepaal (eerst) voor de gemiddelde dichtheid. Bekijk dat later wel kritisch!

**P7.64** A parachutist jumps from a plane, using an 8.5-m-diameter chute in the standard atmosphere. The total mass of the chutist and the chute is 90 kg. Assuming an open chute and quasi-steady motion, estimate the time to fall from 2000- to 1000-m altitude.

**\*P2.29** Under some conditions the atmosphere is *adiabatic*,  $p \approx (\text{const})(\rho^k)$ , where  $k$  is the specific heat ratio. ~~Show that, for an adiabatic atmosphere,~~ the pressure variation is given by

$$p = p_0 \left[ 1 - \frac{(k-1)gz}{kRT_0} \right]^{k/(k-1)}$$

Compare this formula for air at  $z = 5000$  m with the standard atmosphere in Table A.6.

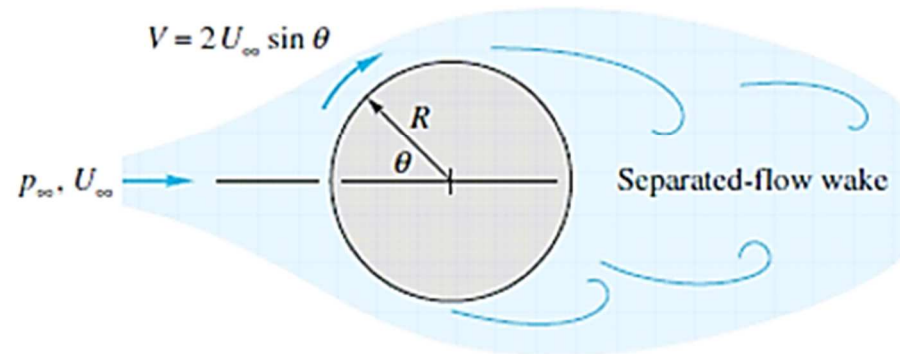
# Aerodynamica: de actualiteit!

Hint: 'standard atmosphere':  
Als in vorige opgave.

**P7.79** Assume that a radioactive dust particle approximates a sphere of density  $2400 \text{ kg/m}^3$ . How long, in days, will it take such a particle to settle to sea level from an altitude of 12 km if the particle diameter is (a)  $1 \mu\text{m}$  or (b)  $20 \mu\text{m}$ ?

# Aerodynamica

**P7.63** The cross section of a cylinder is shown in Fig. P7.63. Assume that on the front surface the velocity is given by potential theory (Sec. 8.4),  $V = 2U_\infty \sin \theta$ , from which the surface pressure is computed by Bernoulli's equation. In



the separated flow on the rear, the pressure is assumed equal to its value at  $\theta = 90^\circ$ . Compute the theoretical drag coefficient and compare with Table 7.2.

# Aerodynamica

**P7.87** A tractor-trailer truck has a drag-area  $C_D A = 8 \text{ m}^2$  bare and  $6.7 \text{ m}^2$  with an aerodynamic deflector (Fig. 7.18*b*). Its rolling resistance is 50 N for each mile per hour of speed. Calculate the total horsepower required at sea level with and without the deflector if the truck moves at (a) 55 mi/h and (b) 75 mi/h.

Om van de lastige definitie van 'aanstroomoppervlak'  $A$  af te komen wordt in de voertuigaerodynamica geregeld het  $C_D \cdot A$  product gebruikt.



# Aerodynamica

**P7.115** An airplane weighs 180 kN and has a wing area of 160 m<sup>2</sup> and a mean chord of 4 m. The airfoil properties are given by Fig. 7.25. If the airplane cruises at 250 mi/h at 3000-m standard altitude, what propulsive power is required to overcome wing drag?

# Gasdynamica

**P9.19** The Concorde aircraft flies at  $Ma \approx 2.3$  at 11-km standard altitude. Estimate the temperature in  $^{\circ}\text{C}$  at the front stagnation point. At what Mach number would it have a front stagnation-point temperature of  $450^{\circ}\text{C}$ ?

De Concorde was de enige supersone lijnvlucht; tussen Parijs/London en New York. Lees de historie op bijv. [http://nl.wikipedia.org/wiki/Concorde\\_\(vliegtuig\)](http://nl.wikipedia.org/wiki/Concorde_(vliegtuig))

# Gasdynamica

**P9.33** Air flows isentropically from a reservoir, where  $p = 300$  kPa and  $T = 500$  K, to section 1 in a duct, where  $A_1 = 0.2$  m<sup>2</sup> and  $V_1 = 550$  m/s. Compute (a)  $Ma_1$ , (b)  $T_1$ , (c)  $p_1$ , (d)  $\dot{m}$ , and (e)  $A^*$ . Is the flow choked?

Hint: 'Gasdynamica-sommen' zijn meestal puzzels: Welke parameters ken ik, welke nog niet. Kan ik relateren?

Hier: bepaal eerst uit de energievergelijking,  $c_p T + \frac{1}{2} V^2 = C_{st}$ , de temperatuur  $T_1$

# Gasdynamica

**P9.52** A converging-diverging nozzle exits smoothly to sea-level standard atmosphere. It is supplied by a  $40\text{-m}^3$  tank initially at  $800\text{ kPa}$  and  $100^\circ\text{C}$ . Assuming isentropic flow in the nozzle, estimate (a) the throat area and (b) the tank pressure after  $10\text{ s}$  of operation. The exit area is  $10\text{ cm}^2$ .

Hint: 'smooth' = 'aangepast'.

Hint 2: de initiële massa in de tank is erg groot t.o.v. 10 seconde leegloop. Check!

# Gasdynamica

**P9.55** Air, supplied by a reservoir at 450 kPa, flows through a converging-diverging nozzle whose throat area is  $12 \text{ cm}^2$ . A normal shock stands where  $A_1 = 20 \text{ cm}^2$ . (a) Compute the pressure just downstream of this shock. Still farther downstream, at  $A_3 = 30 \text{ cm}^2$ , estimate (b)  $p_3$ , (c)  $A_3^*$ , and (d)  $Ma_3$ .

Ook een typische 'puzzel'. (b..d) zijn lastiger dan je denkt;  $A_3^*$  is ongelijk aan  $A^*$ !  
Als ná  $A_3$  de diffusor geleidelijk en verliesvrij uitwaaiert naar reservoir<sub>4</sub>;  
schets dan vanaf reservoir<sub>1</sub> t/m reservoir<sub>4</sub> het verloop van druk en temperatuur.