

Thermodynamica 1

Otto, Diesel & dual cycle

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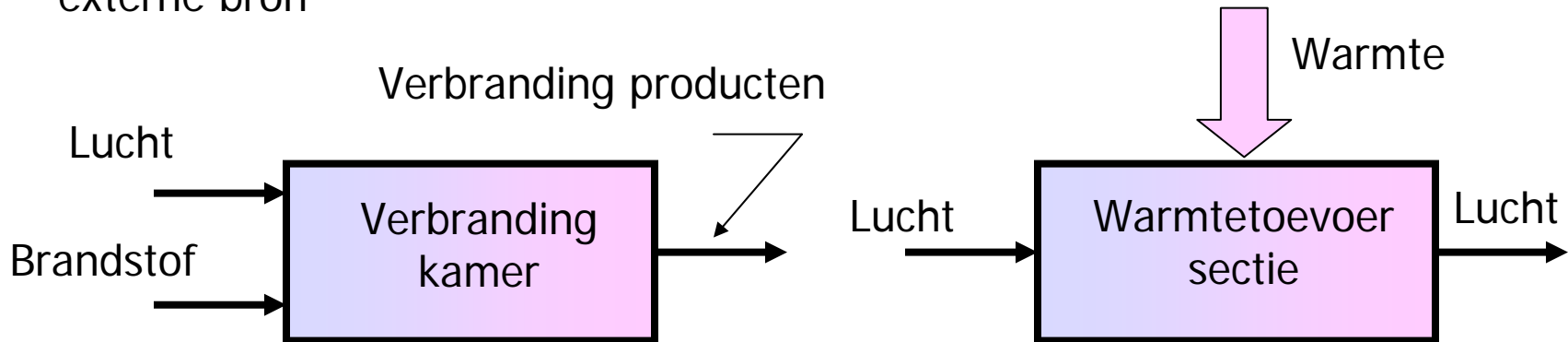
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lecture 12

Standaard-lucht aannames / Koude-lucht standaard

Standaard lucht aannames

- Werkmedium is lucht met ideaal gas gedrag
- Kringproces is gesloten
- Deel processen zijn inwendig reversibel
- Verbrandingsprocessen worden vervangen door warmte toevoer vanuit een externe bron



- Uitdrijfproces wordt vervangen door warmteafvoer proces waardoor werkmedium in oorspronkelijke toestand terugkomt

Koude-lucht standaard aannames

- Soortelijke warmte (c_p, c_v) constant bij kamer temperatuur (25°C)

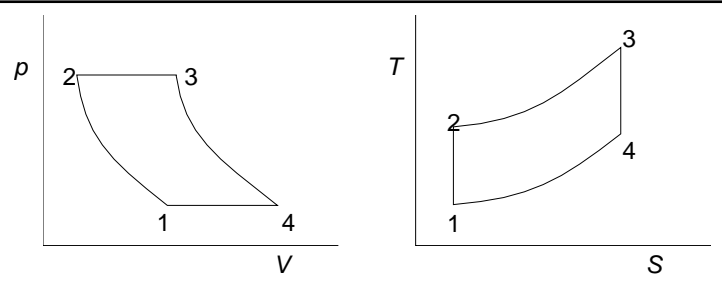
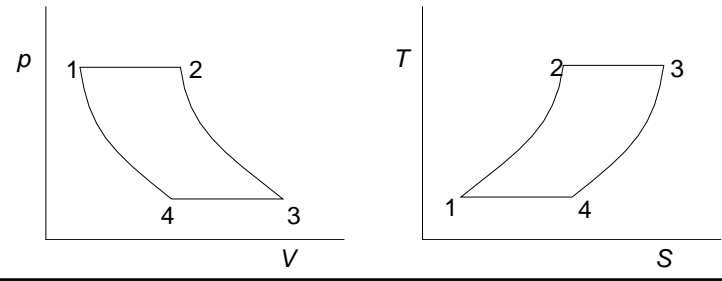
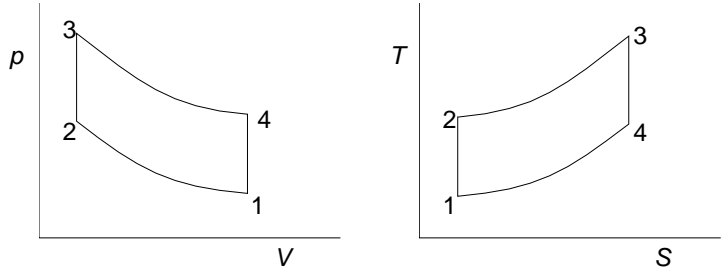
then $k = \frac{c_p}{c_v}$ also constant

Cycle processes



Historisch	p =const	V =const	T =const	dQ =0		
Papin 1690	p	V				
Stirling (Robert) James 1815		V	T			
Carnot 1824 (Diesel, 1893/7)			T	dQ		

Cycle processes

Historisch	p =const	V =const	T =const	dQ =0	
Ericsson 1833 Joule 1852 Brayton 1867	p			dQ	 <p>The Ericsson cycle consists of four states: 1 (bottom-left), 2 (top-left), 3 (top-right), and 4 (bottom-right). The p-V diagram shows a horizontal line from 2 to 3 (isobaric expansion), a curve from 3 to 4 (adiabatic expansion), a horizontal line from 4 to 1 (isobaric compression), and a curve from 1 to 2 (adiabatic compression). The T-S diagram shows a horizontal line from 2 to 3 (isobaric expansion), a curve from 3 to 4 (adiabatic expansion), a horizontal line from 4 to 1 (isobaric compression), and a curve from 1 to 2 (adiabatic compression).</p>
Ericsson 1853	p		T		 <p>The Ericsson cycle consists of four states: 1 (bottom-left), 2 (top-left), 3 (top-right), and 4 (bottom-right). The p-V diagram shows a horizontal line from 1 to 2 (isobaric expansion), a curve from 2 to 3 (adiabatic expansion), a horizontal line from 3 to 4 (isobaric compression), and a curve from 4 to 1 (adiabatic compression). The T-S diagram shows a horizontal line from 2 to 3 (isobaric expansion), a curve from 3 to 4 (adiabatic expansion), a horizontal line from 4 to 1 (isobaric compression), and a curve from 1 to 2 (adiabatic compression).</p>
Otto 1867 (Barsanti - Matteucci 1854)		V		dQ	 <p>The Otto cycle consists of four states: 1 (bottom-right), 2 (top-right), 3 (top-left), and 4 (bottom-left). The p-V diagram shows a curve from 1 to 2 (adiabatic compression), a horizontal line from 2 to 3 (isobaric expansion), a curve from 3 to 4 (adiabatic expansion), and a horizontal line from 4 to 1 (isobaric compression). The T-S diagram shows a curve from 1 to 2 (adiabatic compression), a horizontal line from 2 to 3 (isobaric expansion), a curve from 3 to 4 (adiabatic expansion), and a horizontal line from 4 to 1 (isobaric compression).</p>

Recap: reversible process steps in closed systems

	$\Delta_{12}Q$	$\Delta_{12}W = m \int_{v_1}^{v_2} p dv$
isotherm ($T=const.$)	ideal gas $-RT \ln \frac{p_2}{p_1} = +RT \ln \frac{v_2}{v_1}$	ideal gas $\Delta_{12}W = \Delta_{12}Q$
isochor ($v=const.$)	$m \int_{T_1}^{T_2} c_v dT = m(u_2 - u_1)$	0
isobar ($p=const.$)	$m \int_{T_1}^{T_2} c_p dT = m(h_2 - h_1)$	$m p_1 (v_2 - v_1)$
adiabatic ($dQ=0$)	0	$-m(u_2 - u_1)$
polytropic ($pv^n=const.$)	$m(u_2 - u_1) - \Delta_{12}W$	$-\frac{m}{n-1} (p_2 v_2 - p_1 v_1)$

Recap: reversible process steps in closed systems

	$\Delta_{12}Q$	$\Delta_{12}W$
isotherm ($T=const.$)		
isochor ($v=const.$)		
isobar ($p=const.$)		
adiabatic ($dQ=0$)		
polytropic ($pv^n=const.$)		

Ideal gas (cold air standard)

$$\left. \begin{array}{l} PV^\kappa = \text{Const} \\ P = mRT / V \end{array} \right\} TV^{\kappa-1} = \text{Const}^*$$

$$T_1 V_1^{\kappa-1} = T_2 V_2^{\kappa-1}$$

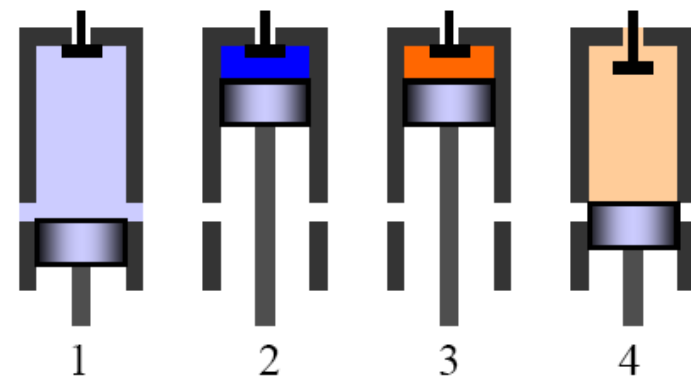
$$\frac{T_1}{T_2} = \left(\frac{V_2}{V_1} \right) = \left(\frac{V_1}{V_2} \right)^{\frac{1}{\kappa-1}}$$

$$\left. \begin{array}{l} PV^\kappa = \text{Const} \\ V = mRT / P \end{array} \right\} P^{\kappa-1} T^\kappa = \text{Const}^{**}$$

$$\frac{P_1}{P_2} = \left(\frac{T_1}{T_2} \right)^{\frac{\kappa}{\kappa-1}}$$

Otto motor

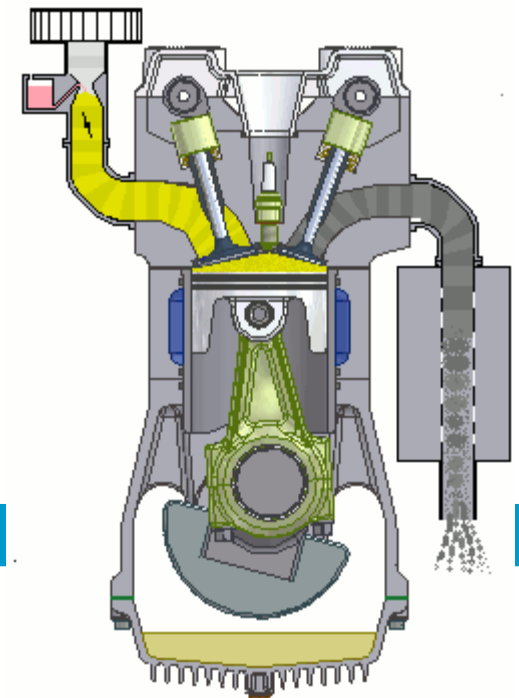
$$\eta^{rev} = 1 - \frac{1}{r^{k-1}}; \text{ met } r = V_1 / V_2$$



Rendement hangt alleen af van de compressie verhouding

Brandstof wordt samen met lucht gecomprimeerd

Beperkende factor is de vroegtijdige ontbranding "knock"



Diesel



Rudolf Diesel



Werkspoor diesel 1951



Cilinderboring (diameter doorsnee)	390mm
Slag (op- en neergaande beweging)	680mm
Aantal cilinders	10
Omwentelingen per minuut (maximaal)	275
Vermogen in epk (bij vol vermogen)	2100 pk /1500 kW



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Moderne diesel

WÄRTSILÄ 38

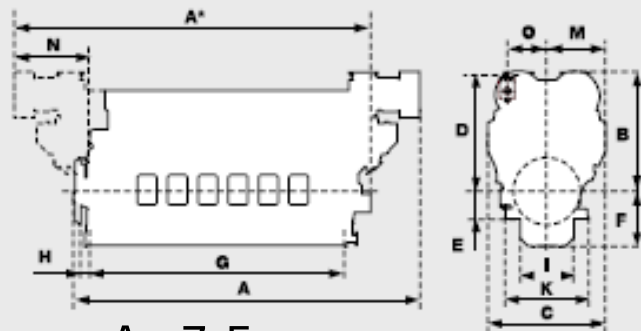
Marine engines

Cylinder bore	380 mm
Piston stroke	475 mm
Cylinder output	725 kW/cyl
Engine speed	600 rpm
Mean effective pressure	26.9 bar

Rated power: Propulsion engines

Engine type

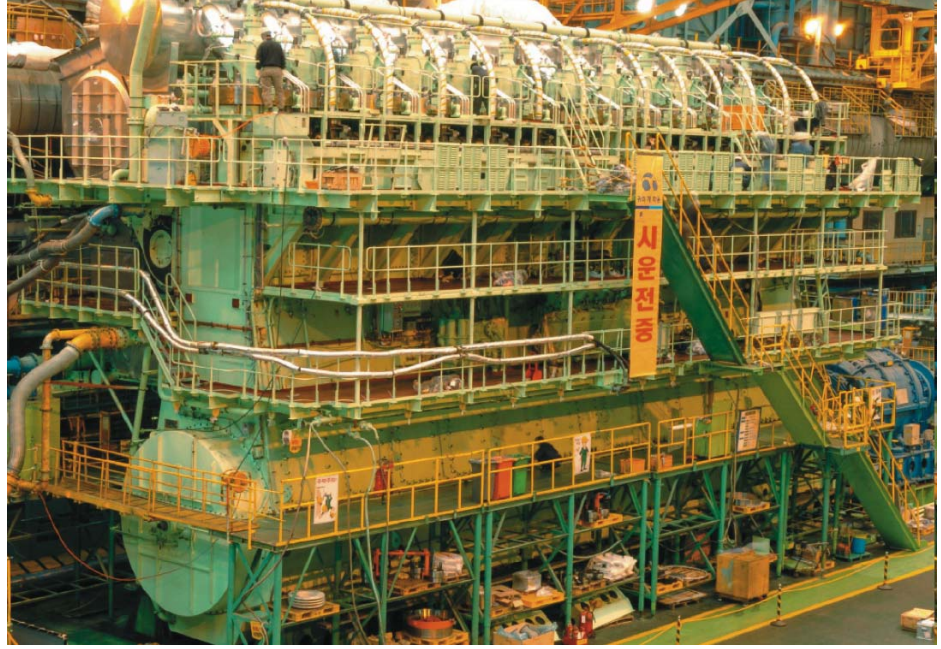
	KW
6L38	4 350
8L38	5 800
9L38	6 625
12V38	8 700
16V38	11 800



A=7.5m

B+F=4.3m



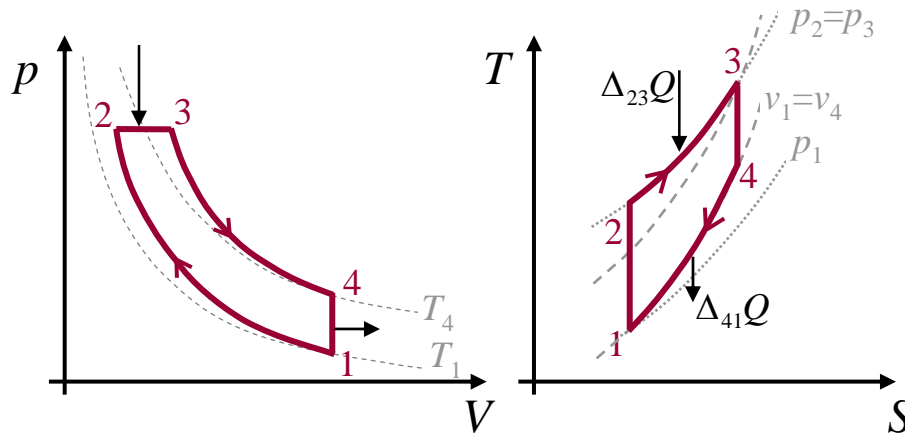


Length: 89 feet (27 meter)
Height: 44 feet (13 meter)
Maximum power: 108,920 hp at 102 rpm
80MW

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Diesel process

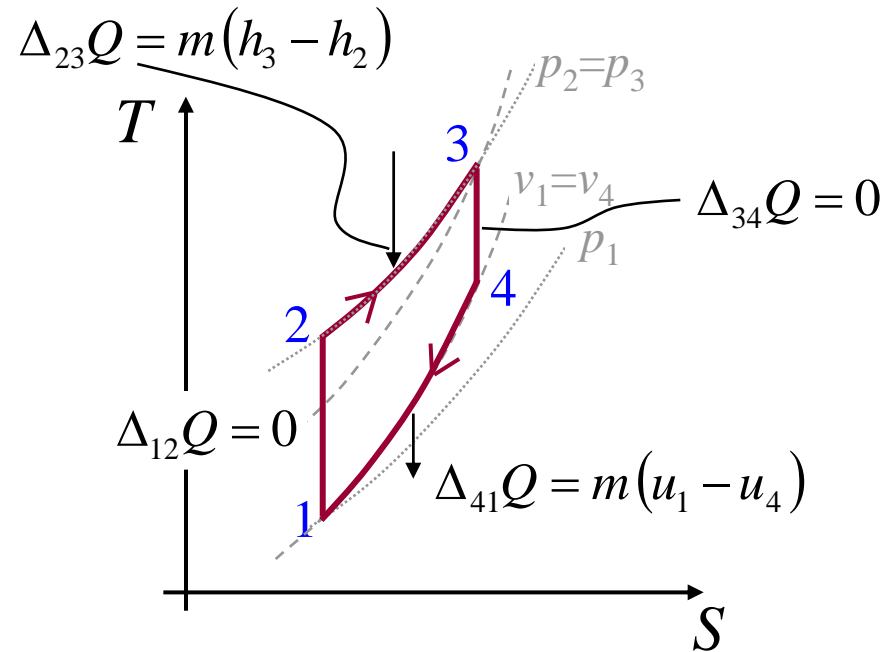
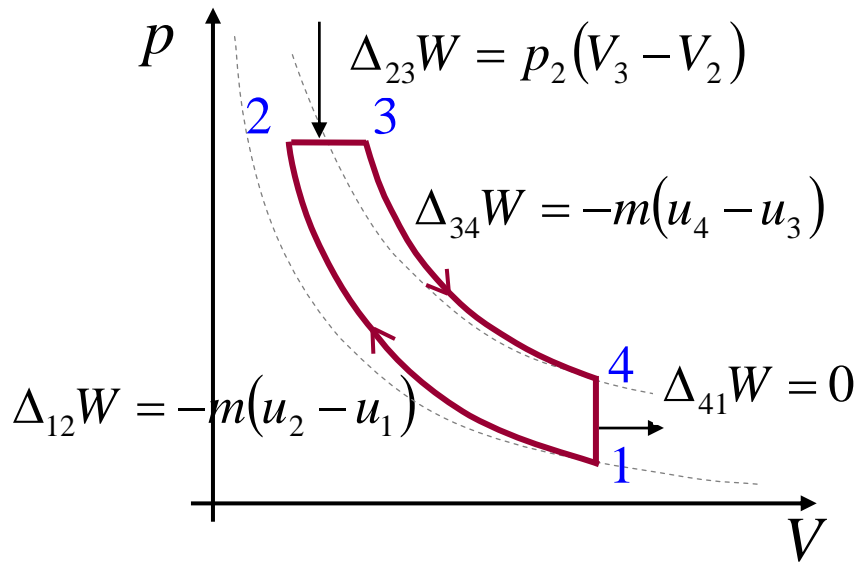


De lucht wordt gecomprimeerd en de temperatuur neemt daardoor toe. Als de cilinder op het hoogste punt is wordt brandstof ingespoten die dan spontaan gaat ontbranden. Door de constructie heeft de motor geen "knock"

internally reversible processes

- 1-2 **adiabatic compression** of the air as the piston moves from bottom dead center to top dead center
- $$\Delta_{12}Q = 0 \qquad \Delta_{12}W = -m(u_2 - u_1)$$
- 2-3 first part of power stroke: **isobaric heating** of air from external source – to mimic ignition and oxidation of fuel-air mixture
- $$\Delta_{23}Q = m(h_3 - h_2) \qquad \Delta_{23}W = p_2(V_3 - V_2)$$
- 3-4 second part of power stroke: **adiabatic expansion**
- $$\Delta_{34}Q = 0 \qquad \Delta_{34}W = -m(u_4 - u_3)$$
- 4-1 **isochoric heat transfer** to external reservoir – to mimic the release of hot exhaust and uptake of fresh (cool) fuel-air mixture
- $$\Delta_{41}Q = m(u_1 - u_4) \qquad \Delta_{41}W = 0$$

Diesel process (s, p, s, v)



the ratio V_3/V_2 is called **cut-off ratio** r_c , with

$$r_c := \frac{V_3}{V_2}$$

\Leftrightarrow

$$r_c = \frac{T_3}{T_2}$$

ideal gas with $p_2=p_3$

$$\left\{ \begin{array}{l} \frac{T_2}{V_2} = \frac{p_2}{mR} = \frac{T_3}{V_3} \end{array} \right.$$

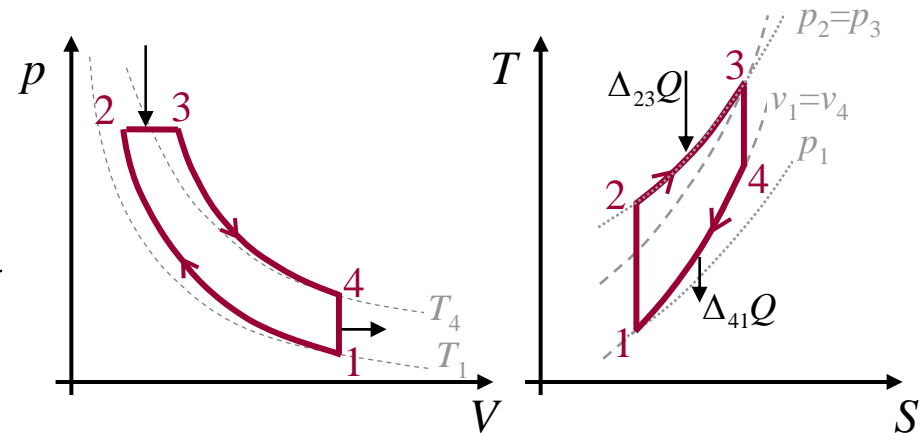
the ratio V_1/V_2 is the **compression ratio** r , with

$$r := \frac{V_1}{V_2}$$

Efficiency of the Diesel engine (s, p, s, v)

$$\eta^{rev} = \frac{W^{cyc}}{\Delta_{23}Q} = \frac{\Delta_{12}W + \Delta_{34}W + \Delta_{23}W}{\Delta_{23}Q}$$

$$\eta^{rev} = \frac{\Delta_{23}Q + \Delta_{41}Q}{\Delta_{23}Q} = 1 + \frac{\Delta_{41}Q}{\Delta_{23}Q} = 1 + \frac{u_1 - u_4}{h_3 - h_2}$$



cold air standard

$$\eta^{rev} = 1 + \frac{c_v(T_1 - T_4)}{c_p(T_3 - T_2)} = 1 + \frac{1}{k} \frac{T_1 - T_4}{T_3 - T_2}$$

$$\eta^{rev} = 1 - \frac{1}{k} \frac{T_1(T_4/T_1 - 1)}{T_2(T_3/T_2 - 1)}$$

with

$$\frac{T_1}{T_2} = \left(\frac{V_2}{V_1}\right)^{k-1} = \frac{1}{r^{k-1}}$$

$$\frac{T_3}{T_2} = \frac{V_3}{V_2} = r_c$$

$$\frac{p_4}{p_3} = \left(\frac{V_3}{V_4}\right)^k$$

$$\frac{p_1}{p_2} = \left(\frac{V_2}{V_1}\right)^k$$

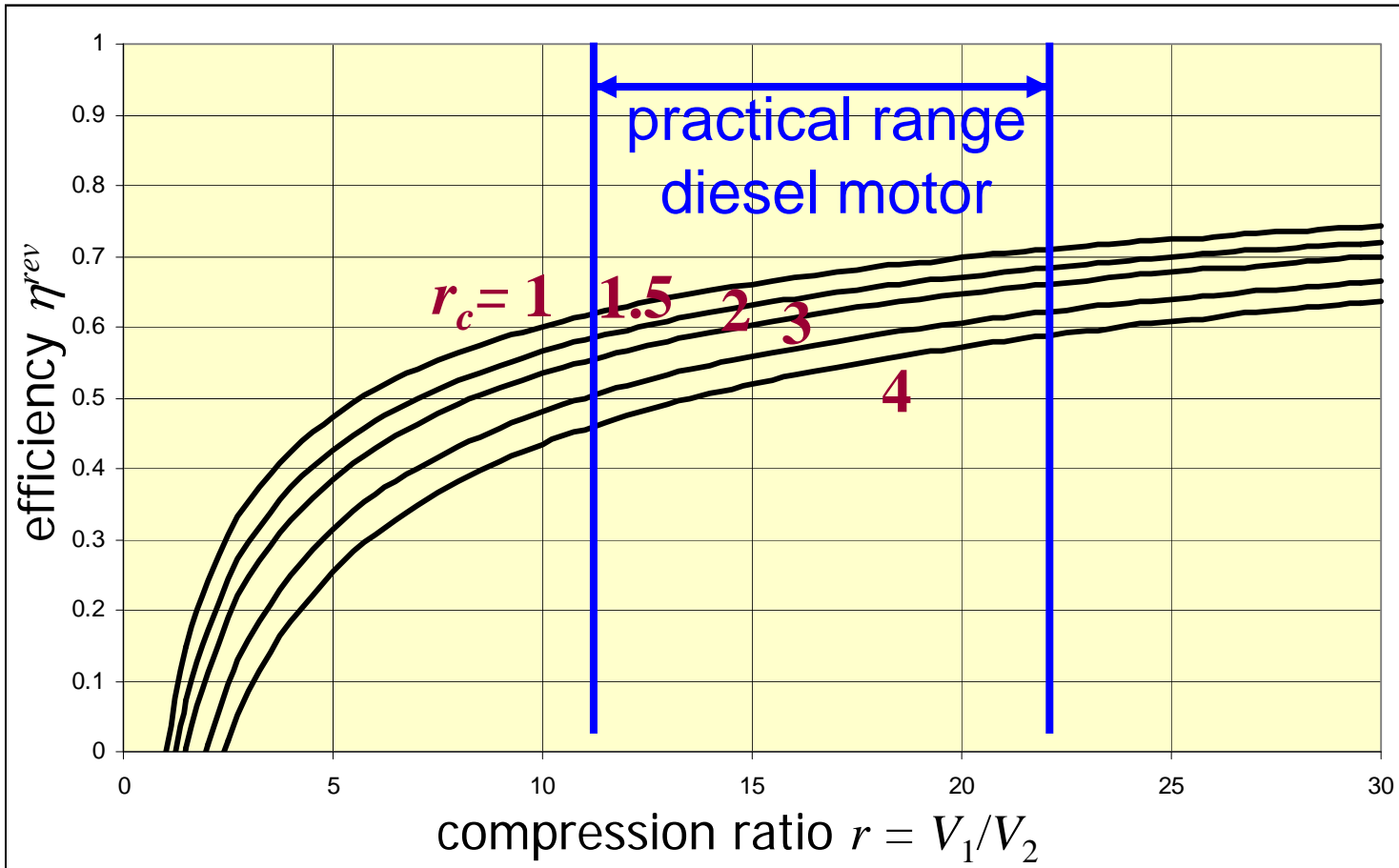
$$\frac{p_4}{p_1} = \left(\frac{V_3}{V_2}\right)^k = r_c^k$$

with $p_2=p_3$
and $V_1=V_4$

$$\frac{T_4}{T_1} = \frac{p_4}{p_1}$$

$$\eta^{rev} = 1 - \frac{1}{r^{k-1}} \left[\frac{r_c^k - 1}{k(r_c - 1)} \right]$$

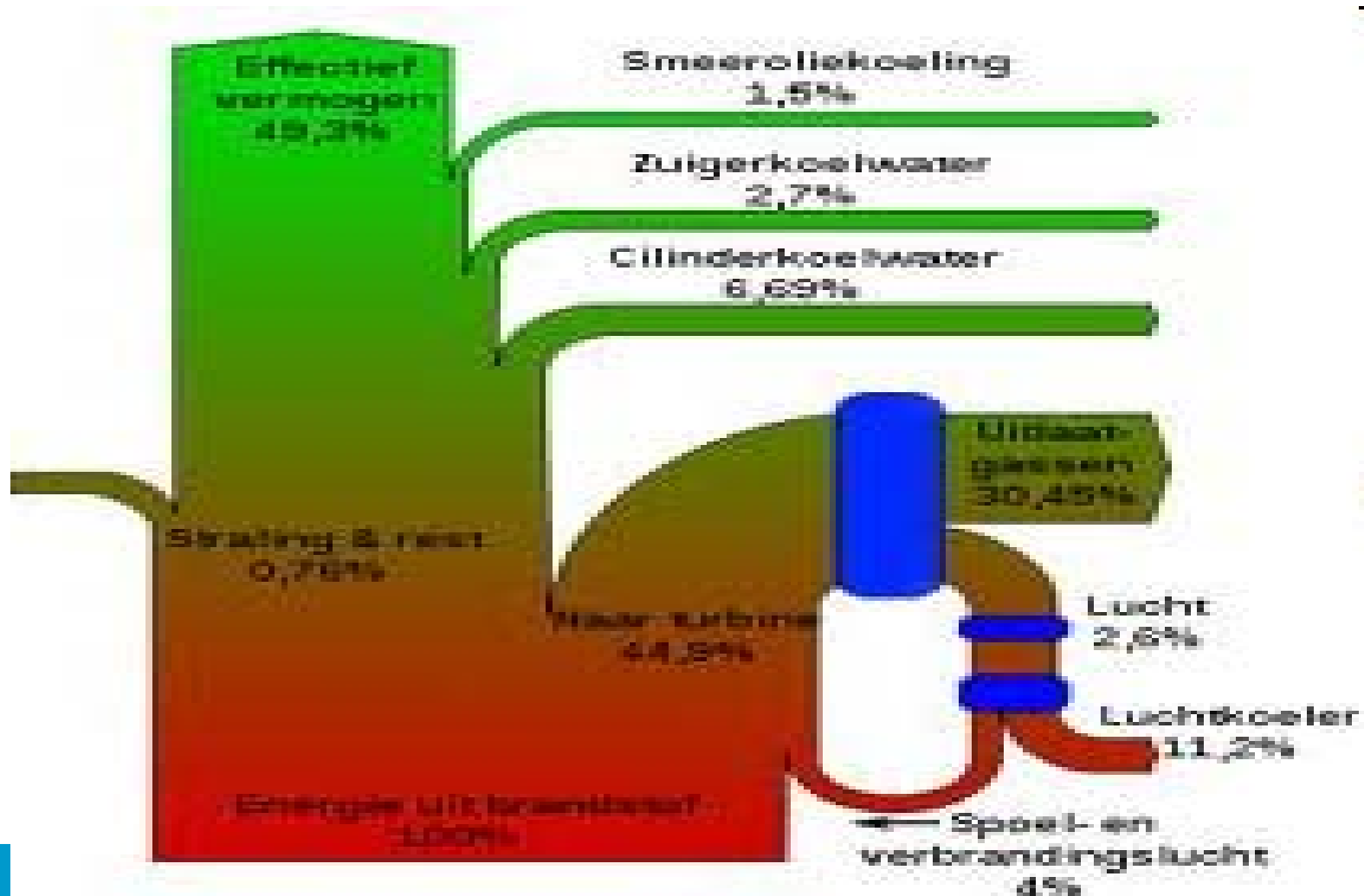
Efficiency of the Diesel engine



$$\eta^{rev} = 1 - \frac{1}{r^{k-1}} \left[\frac{r_c^k - 1}{k(r_c - 1)} \right]$$

\Rightarrow for a given compression ratio r , the efficiency of Diesel is lower than Otto (because the square bracket is >1). But higher compression ratios are realized for Diesel engines.

Diesel waar blijft de rest?



Diesel motor (opgave 9.17)

De slagvolume van een inwendige verbrandingsmotor is 5.60 liter . De processen in de verschillende cilinders van de motor worden gemodelleerd als een standaard-lucht Diesel kringproces met een "cutoff ratio" van 2.4. De luchttoestand bij start van de compressie fase is $p_1=95 \text{ kPa}$, $T_1=300\text{K}$, en $V_1=6.0 \text{ liter}$

- Bereken de netto arbeid per cyclus, in kJ
- Het vermogen geleverd door de motor, in kW , als 1500 cycli worden uitgevoerd per minuut
- Het thermisch rendement

Diesel motor (opgave 9.17)

- Standard air
- Cold air standard

$$h_2 - h_1 = \int_1^2 C_p dT$$

$$\text{Cold air standard} \Rightarrow C_p = \text{const} \Rightarrow \underline{h_2 - h_1} = C_p \int_1^2 dT = \underline{C_p (T_2 - T_1)}$$

$$\text{Air standard} \Rightarrow C_p = f(T) \Rightarrow h_2 - h_1 = \int_1^2 C_p dT \Rightarrow \text{Tabel A22}$$

Entropy op soortgelijke wijze

Diesel motor (opgave 9.17)

berekenpad 1

netto arbeid per cyclus

$$\Delta^{cyc}W = \Delta_{12}W + \Delta_{23}W + \Delta_{34}W$$

$$\Delta_{12}W = -m(u_2 - u_1)$$

$$\Delta_{23}W = p_2(V_3 - V_2)$$

$$\Delta_{34}W = -m(u_4 - u_3)$$

thermisch rendement

$$\Delta_{23}Q = m(h_3 - h_2)$$

$$\eta^{therm} = \frac{\Delta^{cyc}W}{\Delta_{23}Q}$$

berekenpad 2

netto arbeid per cyclus

$$\Delta^{cyc}W = \Delta^{cyc}Q$$

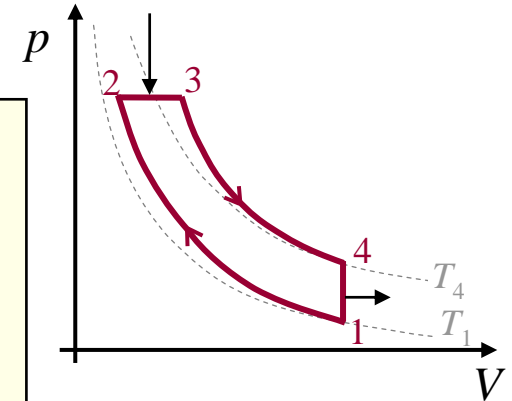
$$\Delta^{cyc}W = \Delta_{23}Q + \Delta_{41}Q$$

$$\Delta_{23}Q = m(h_3 - h_2)$$

$$\Delta_{41}Q = m(u_1 - u_4)$$

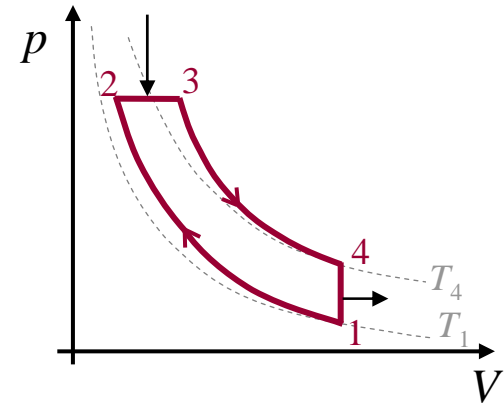
thermisch rendement

$$\eta^{therm} = \frac{\Delta^{cyc}W}{\Delta_{23}Q}$$



Diesel motor (opgave 9.17)

#	T / K	p / bar	V / m^3	$u / kJ/kg$	$h / kJ/kg$
1	300.	0.95	$6.0 \cdot 10^{-3}$	214.07	
2	843.2		$0.4 \cdot 10^{-3}$		869.6
3	2024.		$0.96 \cdot 10^{-3}$		2282.1
4	1146.		$6.0 \cdot 10^{-3}$	885.6	



volume

$$V_1 - V_2 = 5.6 \cdot 10^{-3} m^3$$

$$V_1 = 6.0 \cdot 10^{-3} m^3 \Rightarrow \underline{V_2 = 0.4 \cdot 10^{-3} m^3}$$

$$\underline{V_4 = V_1 = 6.0 \cdot 10^{-3} m^3}$$

$$r_c = 2.4 \Rightarrow \frac{V_3}{V_2} = 2.4 \Rightarrow \underline{V_3 = 2.4 \cdot V_2 = 0.96 \cdot 10^{-3} m^3}$$

massa (punt 1)

$$p_1 V_1 = m R T_1 \Rightarrow m = \frac{p_1 V_1}{R T_1} = \frac{95 \frac{kJ}{m^3} \cdot 0.006 m^3}{8.314 \frac{kJ}{kmol K} \cdot 300 K}$$

$$\frac{28.97 \frac{kg}{kmol}}$$

$$\underline{m = 0.00662 kg}$$

rood: in opgave gespecificeerd
 zwart: hier berekend
 grijs: later berekend

Diesel motor (opgave 9.17)

temperatuur punt 2

$$\frac{V_2}{V_1} = \frac{v_2}{v_1} = \frac{v_{r2}}{v_{r1}}$$

Tabel A22: $T_1 = 300K \Rightarrow v_r(T_1 = 300K) = 621.2$

$$v_r(T_2) = v_r(T_1) \frac{v_2}{v_1} = 621.2 \frac{0.4}{6.0} = 41.41$$

$$\Rightarrow T_2 = \frac{843.2K}{\text{geïnterpoleerd}} \quad (\text{Tabel A-22}) \quad T_2 = 840K + \frac{860K - 840K}{v_r(860K) - v_r(840K)} (v_r(T_2) - v_r(840K))$$

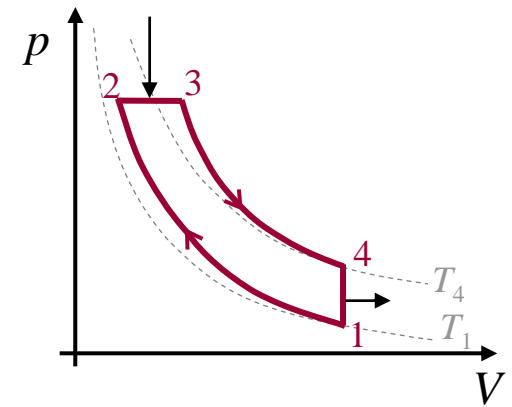
$$\Rightarrow h_2 = h(T_2 = 843.2K) = \frac{869.6kJ/kg}{\text{geïnterpoleerd}}$$

temperatuur punt 3

$$\frac{V_2}{T_2} = \frac{mR}{p_2} = \frac{mR}{p_3} = \frac{V_3}{T_3} \quad \text{met } p_2 = p_3$$

$$T_3 = T_2 \frac{V_3}{V_2} = 843.3K \cdot 2.4 = 2024.K$$

$$\Rightarrow h_3 = h(T_3 = 2024K) = \frac{2282.1kJ/kg}{\text{geïnterpoleerd}}$$



Diesel motor (opgave 9.17)

temperatuur punt 4

$$\frac{V_4}{V_3} = \frac{v_r(T_4)}{v_r(T_3)}$$

$$v_r(T_4) = v_r(T_3) \frac{V_4}{V_3} = 2.670 \frac{6.0}{\text{geïnterpoleerd } 0.96} = 16.69$$

$$\Rightarrow T_4 = \text{geïnterpoleerd } 1146. K$$

$$\Rightarrow u_4 = u(T_4 = 1146 K) = \text{geïnterpoleerd } 885.6 \text{ kJ/kg}$$

netto arbeid per cyclus

$$W^{cyc} = Q^{cyc}$$

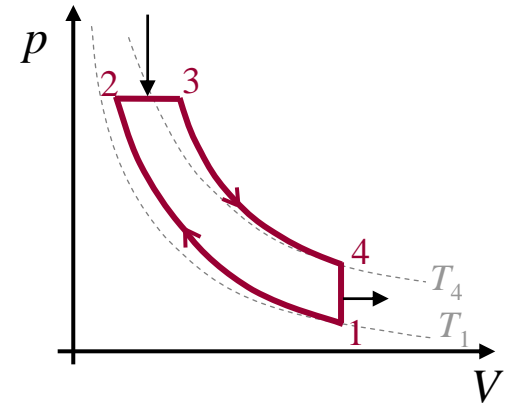
$$W^{cyc} = \Delta_{23}Q + \Delta_{41}Q$$

$$\Delta_{23}Q = m(h_3 - h_2)$$

$$\Delta_{41}Q = m(u_1 - u_4)$$

$$W^{cyc} = 0.00662 \text{ kg} \cdot (2282.1 - 869.6 + 214.07 - 885.6) \frac{\text{kJ}}{\text{kg}}$$

$$W^{cyc} = 4.91 \text{ kJ}$$



Diesel motor (opgave 9.17)

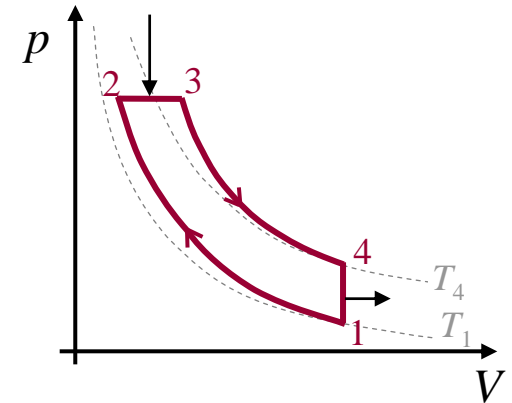
vermogen motor

$$\dot{W} = W^{cyc} \cdot \frac{\text{cycli}}{\text{tijdseenheid}}$$

$$\dot{W} = 4.91 \text{ kJ} \cdot \frac{1500}{60 \text{ s}} = 123 \text{ kW}$$

thermisch rendement

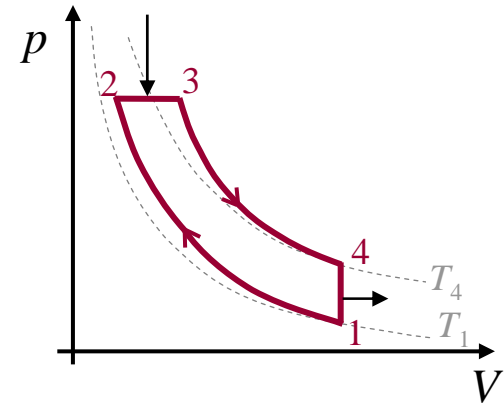
$$\eta = \frac{W^{cyc}}{\Delta_{23}Q} = \frac{4.91 \text{ kJ}}{0.00662 \text{ kg} (2282.1 - 869.6) \text{ kJ/kg}} = \frac{4.91 \text{ kJ}}{9.35 \text{ kJ}} = 0.525$$



Zelfde opgave met cold air standard

Volume identiek aan air standard

#	T / K	p / bar	V / m^3	$u / kJ/kg$	$h / kJ/kg$
1	300.	0.95	$6.0 \cdot 10^{-3}$	214.07	
2	843.2		$0.4 \cdot 10^{-3}$		869.6
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volume

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$$V_1 = 6.0 \cdot 10^{-3} m^3 \Rightarrow \underline{V_2 = 0.4 \cdot 10^{-3} m^3}$$

$$\underline{V_4 = V_1 = 6.0 \cdot 10^{-3} m^3}$$

$$r_c = 2.4 \Rightarrow \frac{V_3}{V_2} = 2.4 \Rightarrow \underline{V_3 = 2.4 \cdot V_2 = 0.96 \cdot 10^{-3} m^3}$$

massa (punt 1)

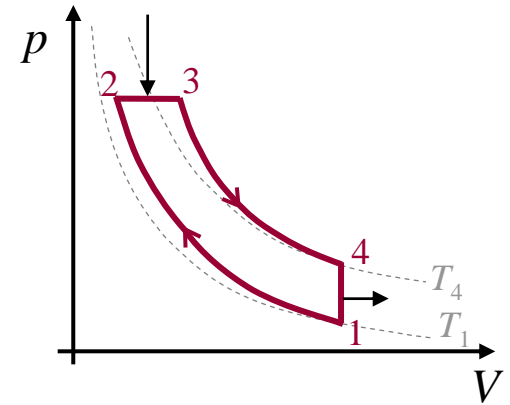
$$p_1 V_1 = m R T_1 \Rightarrow m = \frac{p_1 V_1}{R T_1} = \frac{95 \frac{kJ}{m^3} \cdot 0.006 m^3}{\frac{8.314 \frac{kJ}{kmol K}}{28.97 \frac{kg}{kmol}} \cdot 300 K}$$

$$\underline{m = 0.00662 kg}$$

rood: in opgave gespecificeerd
 zwart: hier berekend
 grijs: later berekend

Diesel motor (opgave 9.17)

punt 2 $T_2 = T_1 \left(\frac{V_1}{V_2} \right)^{\kappa-1} = 300 * 15^{0.4} = 886K \quad (843K)$



punt 3 $\frac{V_2}{T_2} = \frac{V_3}{T_3} \Rightarrow T_3 = T_2 \cdot 2.4 = 2127K \quad (2024K)$

$$\Delta Q_{23} = mc_p (T_3 - T_2) = 0.0066 \cdot 1005 \cdot (2127 - 886) = 8.23kJ$$

$$T_4 = T_3 \left(\frac{V_3}{V_4} \right)^{0.4} = 2127 (0.96/6)^{0.4} = 1022K \quad (1146K)$$

punt 4

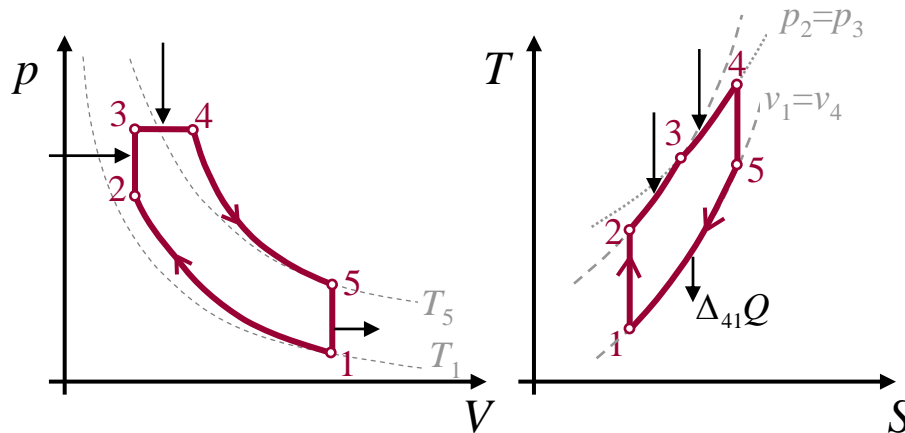
$$\Delta Q_{41} = mc_p (T_1 - T_4) = 0.0066 * 0.718 * (300 - 1022) = 3.42kJ$$

$$W_{cyc} = 8.23 - 3.42 = 4.8kJ$$

$$\eta = 4.8 / 8.23 = 58.4\%$$

$$\eta^{rev} = 1 - \frac{1}{r^{k-1}} \left[\frac{r_c^k - 1}{k(r_c - 1)} \right] = 0.584$$

Dual process



the Otto cycle and the Diesel cycle are strongly idealized. The dual process cycle can better approximate real combustion engines

internally reversible processes

1-2 **adiabatic compression** of the air

$$\Delta_{12}Q = 0$$

$$\Delta_{12}W = -m(u_2 - u_1)$$

2-3 1st part of power stroke: **isochoric heating**

$$\Delta_{23}Q = m(u_3 - u_2) \quad \Delta_{23}W = 0$$

3-4 2nd part of power stroke: **isobaric expansion**

$$\Delta_{34}Q = m(h_4 - h_3) \quad \Delta_{34}W = p_3(V_4 - V_3)$$

4-5 3rd part of power stroke: **adiabatic expansion**

$$\Delta_{45}Q = 0 \quad \Delta_{45}W = -m(u_5 - u_4)$$

5-1 **isochoric heat transfer** to external reservoir

$$\Delta_{51}Q = m(u_1 - u_5) \quad \Delta_{51}W = 0$$

Duaal kringproces (opgave 9.26)

Een standaard lucht duaal kringproces heeft een compressieverhouding van 16 en een cutoff ratio van 1.15. Aan het begin van de compressieproces $p_1=95 \text{ kPa}$ en $T_1=300 \text{ K}$. De druk wordt 2.2 keer zo groot gedurende het isochoor warmte toevoer proces. Als de massa van lucht 0.04 kg bedraagt, bereken:

- a) de toegevoerde warmte gedurende de twee warmte toevoer processen
- b) de netto arbeid van het kringproces, in kJ
- c) de afgevoerde warmte, in kJ
- d) het thermisch rendement

Duaal kringproces (opgave 9.26)

berekenpad

nodig

nodig

a) toegevoerde warmte

$$\Delta^{in} Q = \Delta_{23} Q + \Delta_{34} Q$$

$$\Delta_{23} Q = m(u_3 - u_2)$$

$$T_2, T_3$$

$$\Delta_{34} Q = m(h_4 - h_3)$$

$$T_4$$

b) netto arbeid per cyclus

$$\Delta^{cyc} W = \Delta^{cyc} Q$$

$$\Delta^{cyc} W = \Delta_{23} Q + \Delta_{34} Q + \Delta_{51} Q$$

$$\Delta_{51} Q = m(u_1 - u_5)$$

$$T_5$$

c) afgevoerde warmte

$$\Delta_{51} Q$$

d) thermisch rendement

$$\eta^{therm} = \frac{\Delta^{cyc} W}{\Delta^{in} Q}$$

Duaal kringproces (opgave 9.26)

#	T / K	p / kPa	V / m^3	$u / kJ/kg$	$h / kJ/kg$
1	300.	95	0.03625	214.07	
2	862.3		0.002266	643.3	
3	1897.		0.002266	1580.	2124.
4	2182.		0.002606		2480.
5	955.4		0.03625	721.1	

volume

$$V_1 = \frac{mRT_1}{p_1} = \frac{0.04 \text{ kg} \cdot 287 \frac{\text{J}}{\text{kg K}} \cdot 300 \text{ K}}{95 \cdot 10^3 \frac{\text{J}}{\text{m}^3}}$$

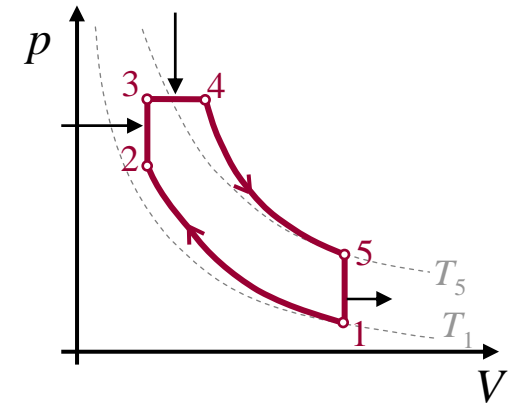
$$V_1 = 0.03625 \text{ m}^3$$

$$r = 16 = \frac{V_1}{V_2} \quad V_2 = \frac{V_1}{16} = 0.002266 \text{ m}^3$$

$$V_3 = V_2 = 0.002266 \text{ m}^3$$

$$r_c = 1.15 = \frac{V_4}{V_3} \quad V_4 = 1.15 \cdot V_3 = 0.002606 \text{ m}^3$$

$$V_5 = V_1 = 0.03625 \text{ m}^3$$



temperature T_1 $T_1 = 300 \text{ K}$
 pressure p_1 $p_1 = 95 \text{ kPa}$
 compression ratio $r = 16$
 cut-off ratio $r_c = 1.15$
 pressure ratio $p_3 = 2.2 \cdot p_2$
 mass $m = 0.04 \text{ kg}$

$$R = \frac{\bar{R}}{M} = \frac{8.314 \frac{\text{kJ}}{\text{kmol K}}}{28.97 \frac{\text{kg}}{\text{kmol}}} = 0.287 \frac{\text{kJ}}{\text{kg K}}$$

Duaal kringproces (opgave 9.26)

punt 2

$$\frac{V_2}{V_1} = \frac{v_2}{v_1} = \frac{v_r(T_2)}{v_r(T_1)}$$

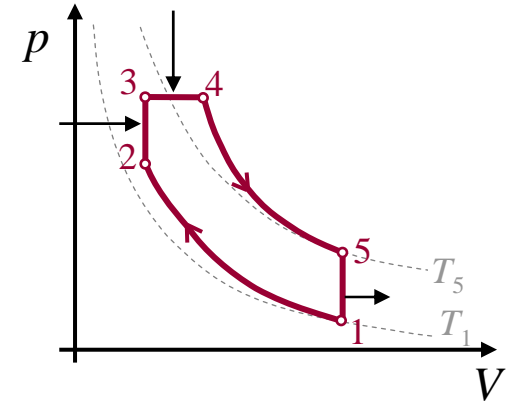
$$\text{Tabel A22: } T_1 = 300\text{K} \Rightarrow v_r(T_1 = 300\text{K}) = 621.2$$

$$v_r(T_2) = v_r(T_1) \frac{V_2}{V_1} = 621.2 \frac{1}{16} = 38.83$$

$$\Rightarrow T_2 = \frac{862.3\text{K}}{\text{geïnterpoleerd}} \quad (\text{Tabel A-22})$$

$$T_2 = 860\text{K} + \frac{880\text{K} - 860\text{K}}{v_r(880\text{K}) - v_r(860\text{K})} (v_r(T_2) - v_r(860\text{K}))$$

$$\Rightarrow u_2 = u(T_2 = 862.3\text{K}) = \frac{643.3\text{kJ/kg}}{\text{geïnterpoleerd}}$$



Duaal kringproces (opgave 9.26)

punt 3

stap 2→3: isochoor ($V_3=V_2$) met $p_3=2.2 p_2$

met $pV = mRT$ is $\frac{p_3}{T_3} = \frac{mR}{V_3} = \frac{mR}{V_2} = \frac{p_2}{T_2}$

$$\Rightarrow \frac{T_3}{T_2} = \frac{p_3}{p_2} = 2.2$$

$$\Rightarrow T_3 = 2.2 \cdot T_2 = 2.2 \cdot 862.3K$$

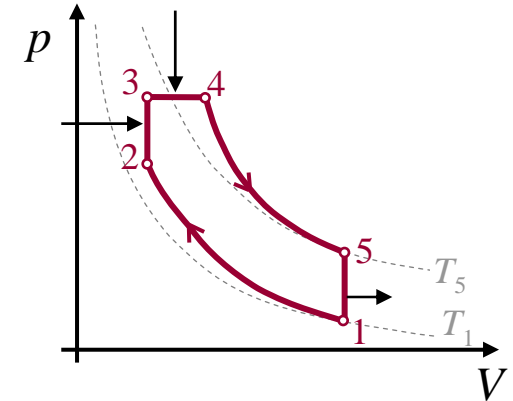
$$\Rightarrow T_3 = 1897.K$$

$$\Rightarrow u_3 = u(T_3 = 1897.K) = \underline{\underline{1580.kJ/kg}}$$

geïnterpoleerd

$$\Rightarrow h_3 = h(T_3 = 1897.K) = \underline{\underline{2124.kJ/kg}}$$

geïnterpoleerd



Duaal kringproces (opgave 9.26)

punt 4

stap 3→4: isobaar ($p_4=p_3$) met $V_4=1.15 V_3$

met $pV = mRT$ is $\frac{V_4}{T_4} = \frac{mR}{p_4} = \frac{mR}{p_3} = \frac{V_3}{T_3}$

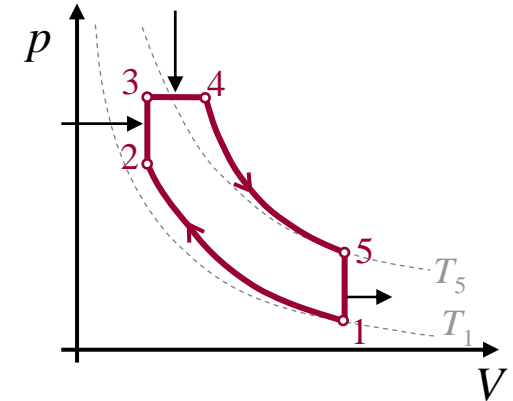
$$\Rightarrow \frac{T_4}{T_3} = \frac{V_4}{V_3} = 1.15$$

$$\Rightarrow T_4 = T_3 \frac{V_4}{V_3} = T_3 \cdot 1.15 = 1897.K \cdot 1.15$$

$$\Rightarrow T_4 = 2182.K$$

$$\Rightarrow h_4 = h(T_4 = 2182.K) = \underline{\underline{2480.kJ/kg}}$$

geïnterpoleerd



Duaal kringproces (opgave 9.26)

punt 5

$$\frac{V_5}{V_4} = \frac{v_5}{v_4} = \frac{v_r(T_5)}{v_r(T_4)}$$

$$T_4 = 2182.K \quad \Rightarrow \quad v_r(T_4 = 2182K) = 2.072$$

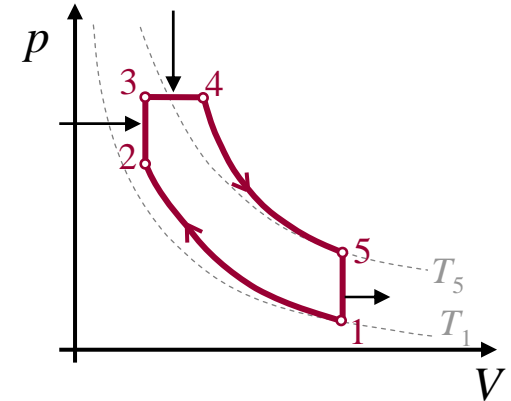
$$v_r(T_5) = v_r(T_4) \frac{V_5}{V_4} = 2.072 \frac{0.03625 m^3}{0.002606 m^3} = 28.82$$

$$\Rightarrow T_5 = \underline{\underline{955.4 K}}$$

geïnterpoleerd

$$\Rightarrow u_5 = u(T_5 = 955.4K) = \underline{\underline{721.1 kJ/kg}}$$

geïnterpoleerd



Duaal kringproces (opgave 9.26)

toegevoerde warmte

$$\Delta^{in} Q = \Delta_{23} Q + \Delta_{34} Q$$

$$\Delta_{23} Q = m(u_3 - u_2) = 0.04 \text{ kg} (1580. - 643.3) \text{ kJ/kg} = 37.5 \text{ kJ}$$

$$\Delta_{34} Q = m(h_4 - h_3) = 0.04 \text{ kg} (2480 - 2124) \text{ kJ/kg} = 14.2 \text{ kJ}$$

$$\Delta^{in} Q = 37.5 \text{ kJ} + 14.2 \text{ kJ} = 51.7 \text{ kJ}$$

netto arbeid per cyclus

$$\Delta^{cyc} W = \Delta^{cyc} Q$$

$$\Delta^{cyc} W = \Delta_{23} Q + \Delta_{34} Q + \Delta_{51} Q$$

$$\Delta_{51} Q = m(u_1 - u_5) = 0.04 \text{ kg} (214.07 - 721.1) \text{ kJ/kg} = -20.3 \text{ kJ}$$

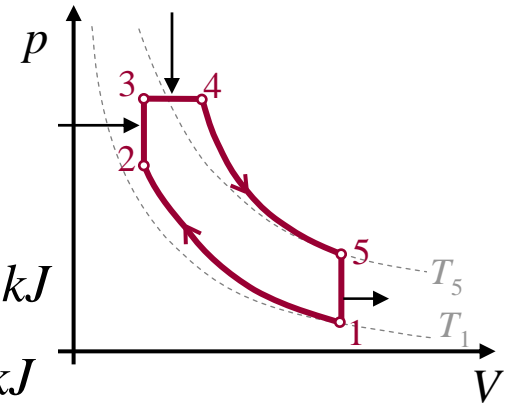
$$\Delta^{cyc} W = (37.5 + 14.2 - 20.3) \text{ kJ} = 31.4 \text{ kJ}$$

afgevoerde warmte

$$\Delta_{51} Q = -20.3 \text{ kJ}$$

thermisch rendement

$$\eta^{therm} = \frac{\Delta^{cyc} W}{\Delta^{in} Q} = \frac{31.3}{51.7} = 0.608$$



Aanwijzingen voor zelfstudie

- H9.3 en H9.4 nu behandeld. Dit voor de volgende keer goed doorlezen – ook de 'examples' in tekst
- Maak enkele van de opgaven 9.13 t/m 9.21 (Diesel kringproces)
- Maak enkele van de opgaven 9.22 t/m 9.27 (lucht dual kringprocessen)