

Thermodynamics 1

Lecture 13:
Kringprocessen
Gasturbines
Joule-Brayton

Bendiks Jan Boersma
Wiebren de Jong
Thijs Vlugt
Theo Woudstra

March 22, 2010

1

College 12

- Diesel process
- dual cycle

Recapitulation

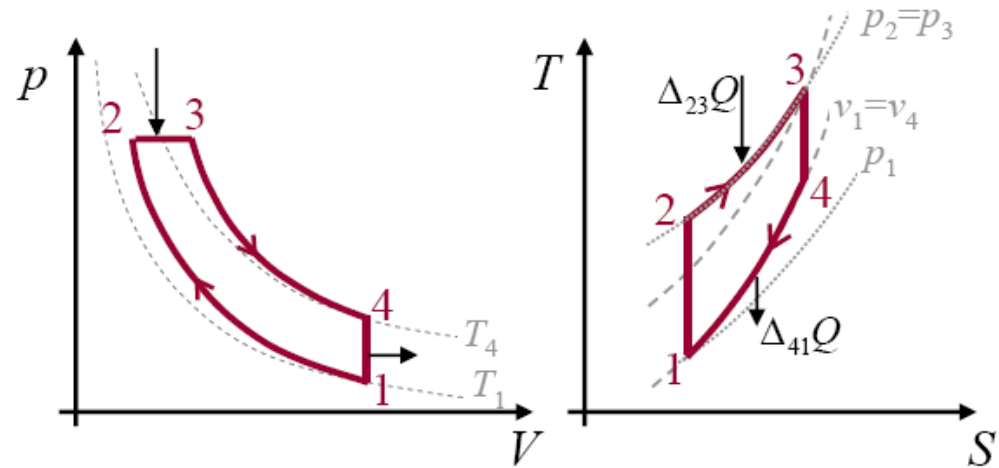
- Diesel cycle (s, p, s, v).

-> Compression ratio

$$r = \frac{V_1}{V_2}$$

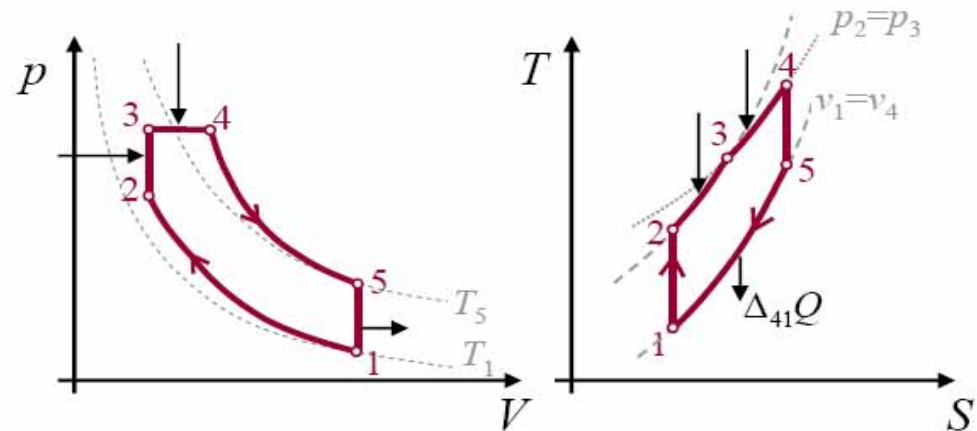
-> cut-off ratio

$$r_c = \frac{V_3}{V_2}$$



- Relation work per cycle and power.

- Dual cycle (s, v, p, s, v)

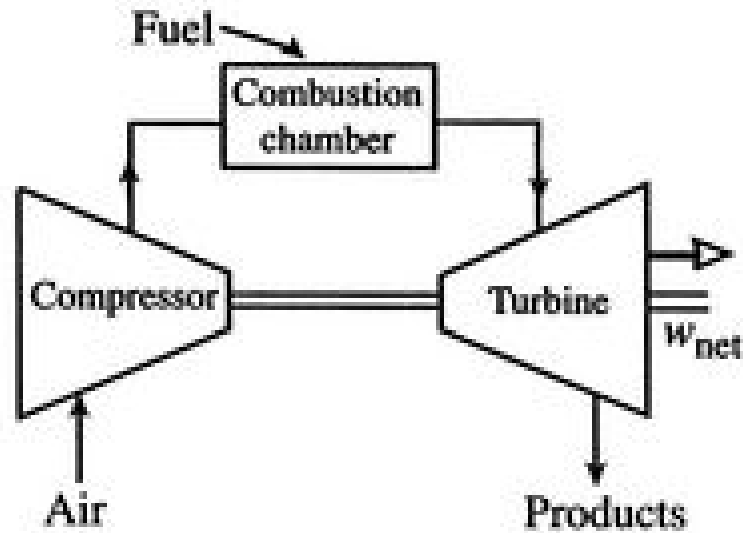


New

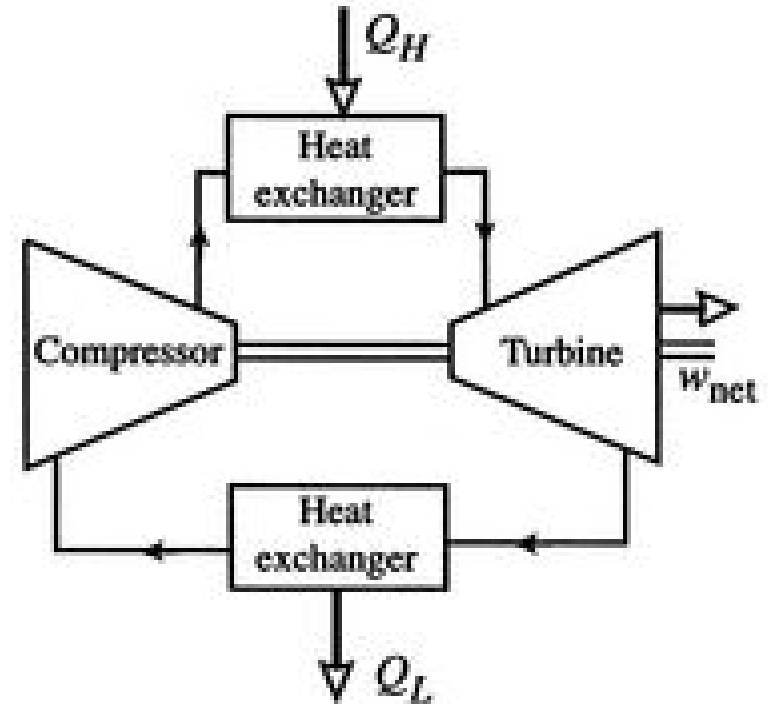
- Joule-Brayton-process (gas-turbine process)

Historisch	p <i>-const</i>	V <i>=const</i>	T <i>=const</i>	dQ <i>=0</i>		
Ericsson 1833 Joule 1852 Brayton 1867	p			dQ		
Ericsson 1853	p		T			
Otto 1867 (Barsanti - Matteucci 1854)		V		dQ		

Simple gas-turbine cycle: configurations



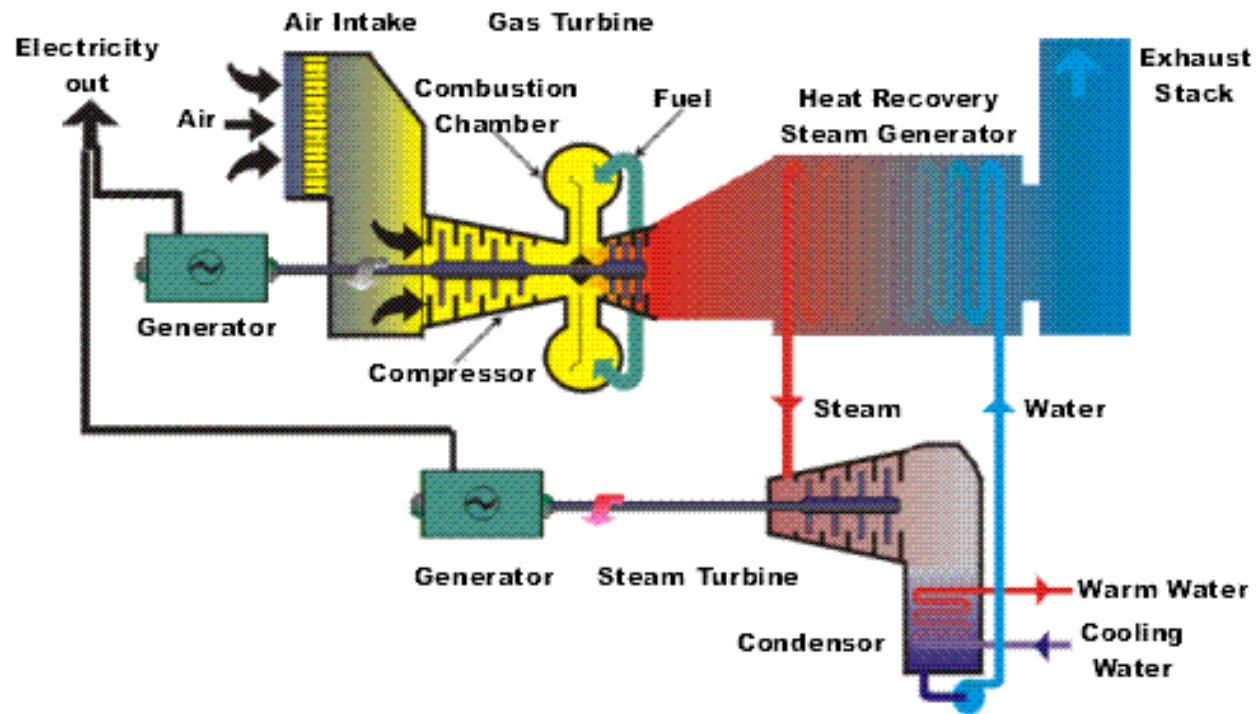
Open



Closed

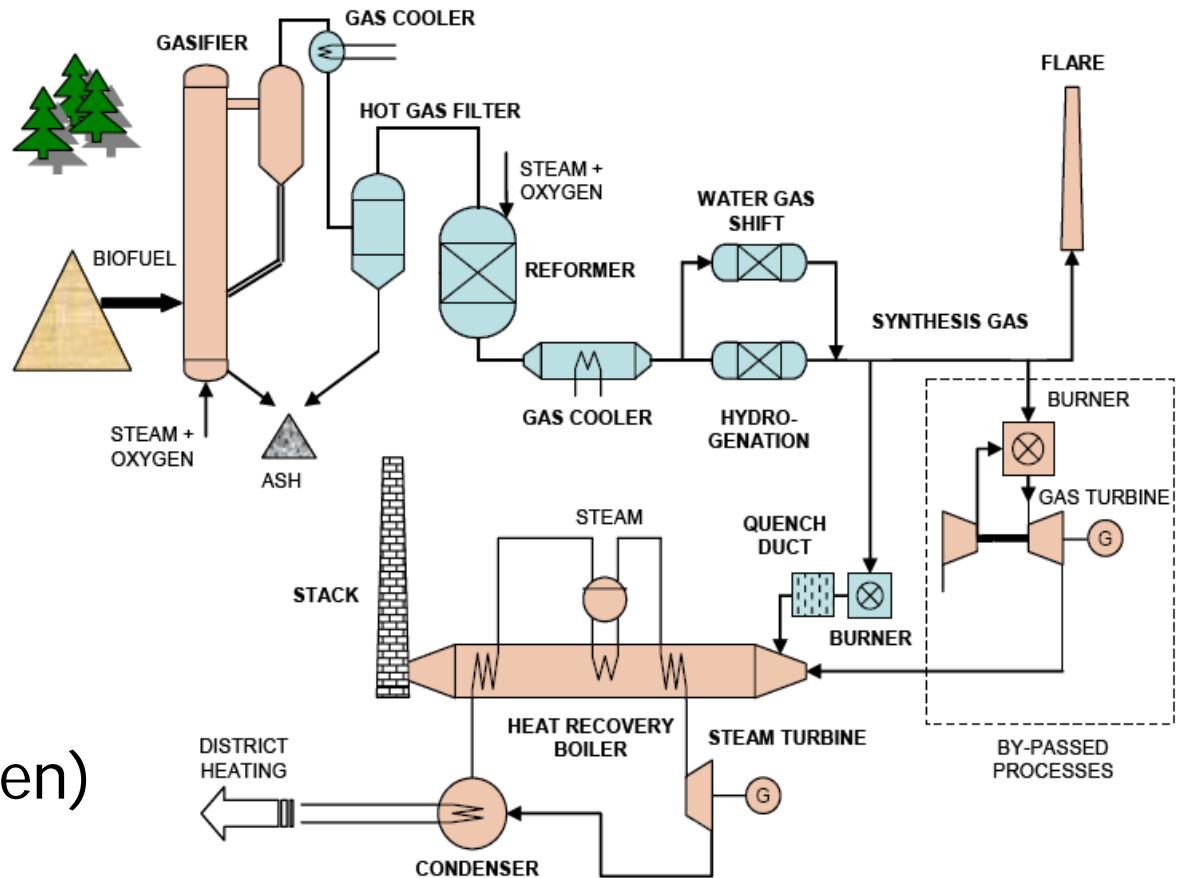
Advanced gas-turbine cycle: combined cycle

How a Combined Cycle Plant works



- Higher thermal efficiencies as hot flue gas from gas turbine is used as input heat for a steam cycle

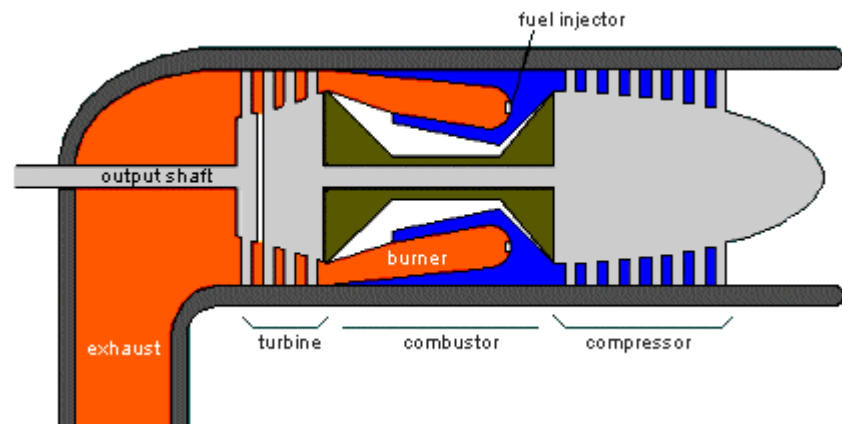
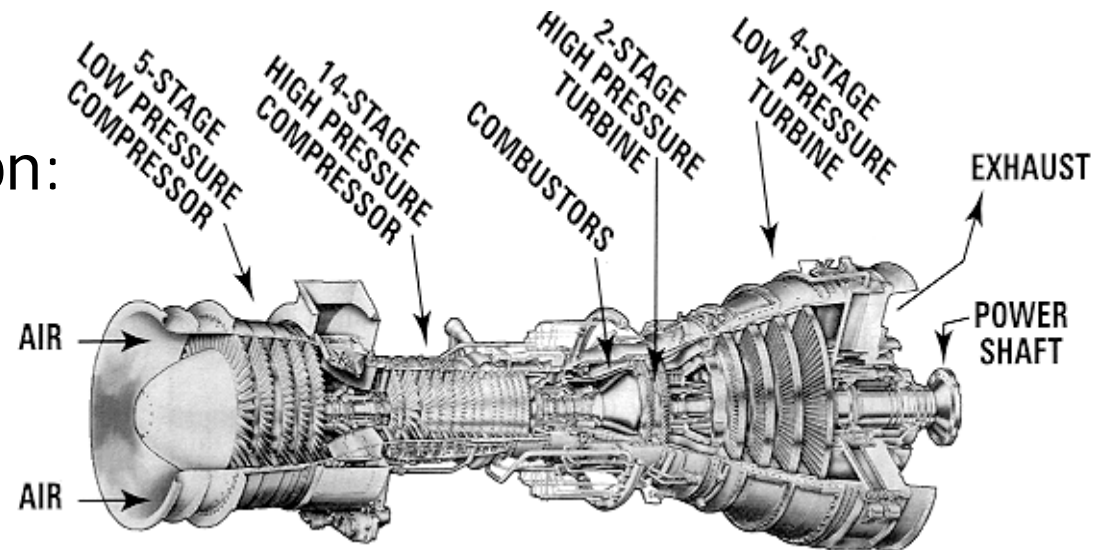
A biomass gasification integrated combined cycle (IGCC)



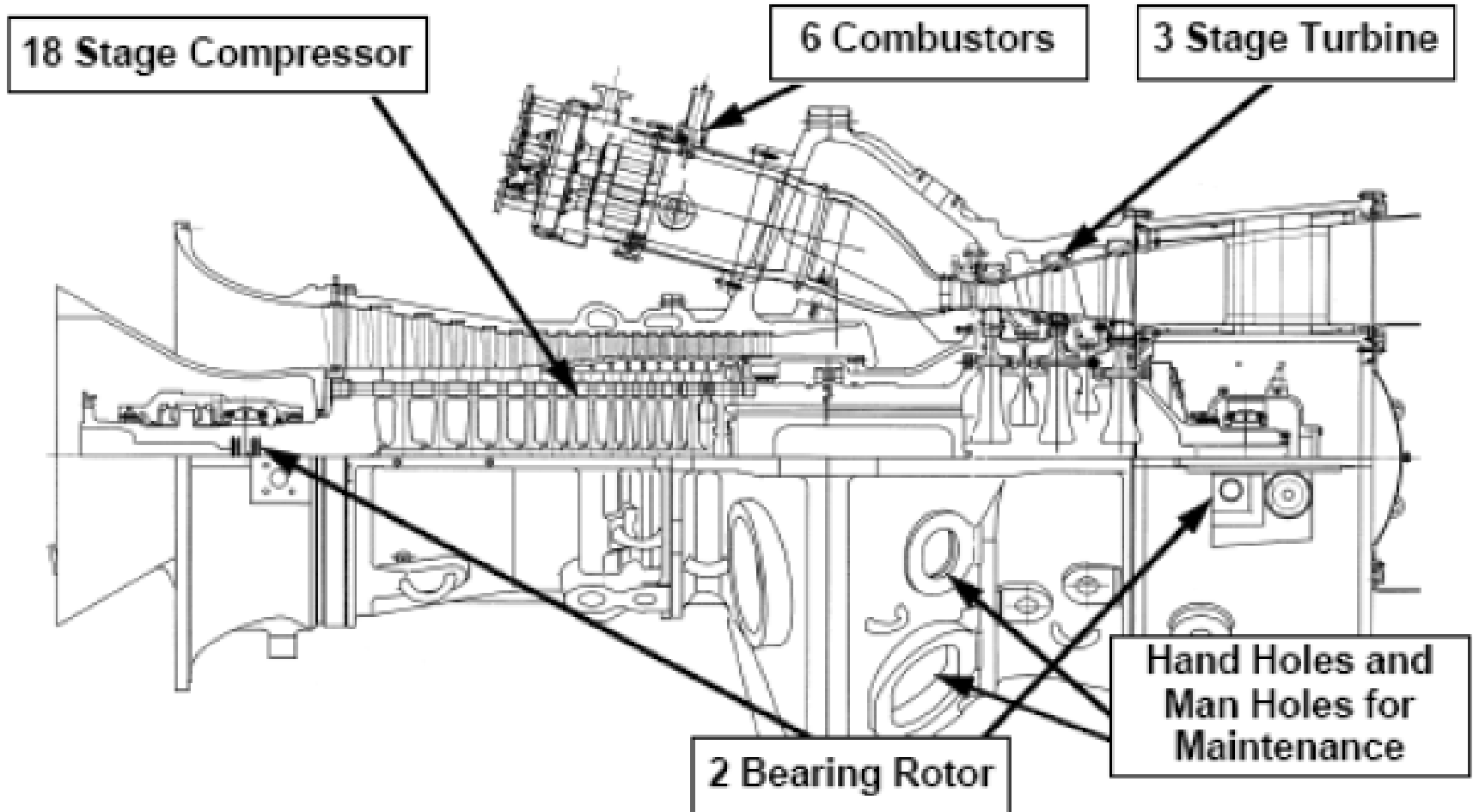
Varnamo (South Sweden)
18 MW_{th}

Gas-turbines: equipment

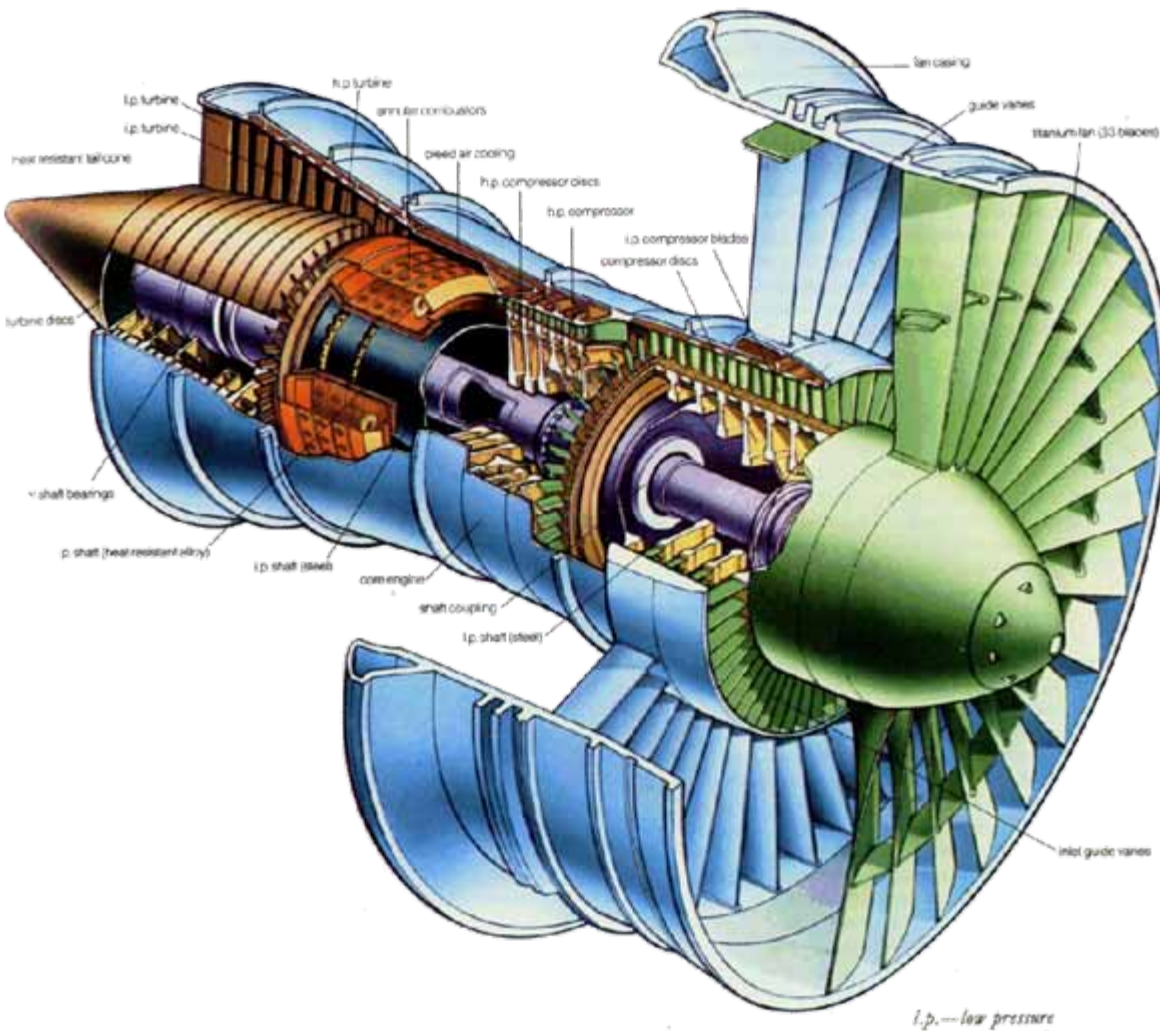
Marine application, propulsion:



Gas-turbines: equipment



Gas-turbines: equipment

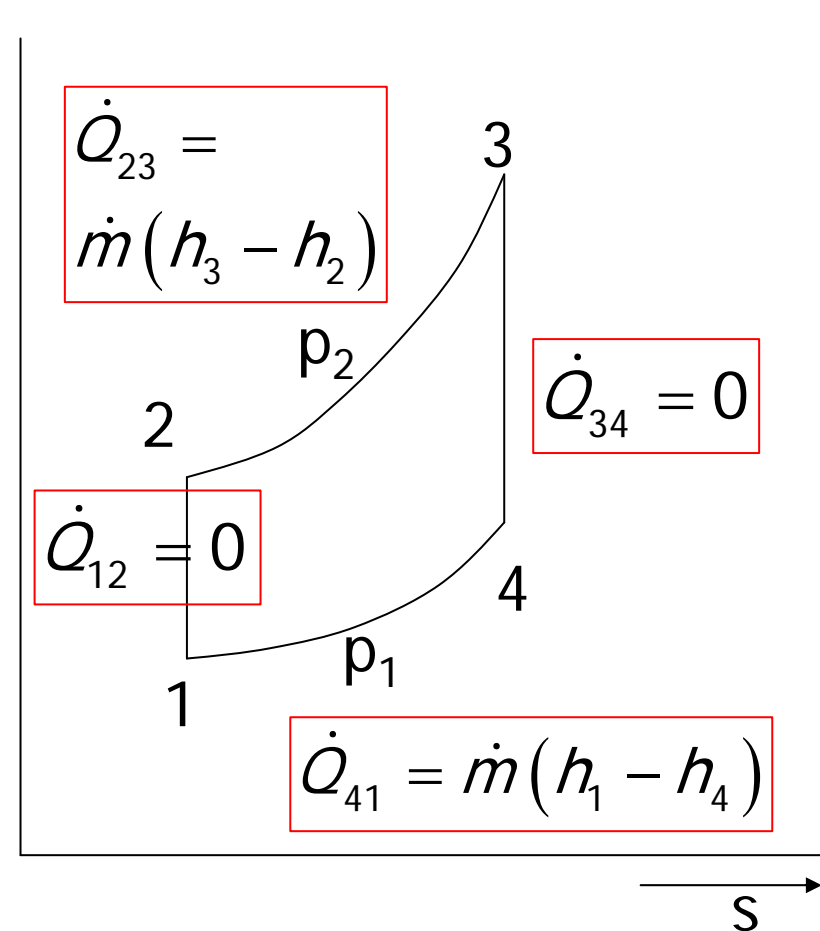
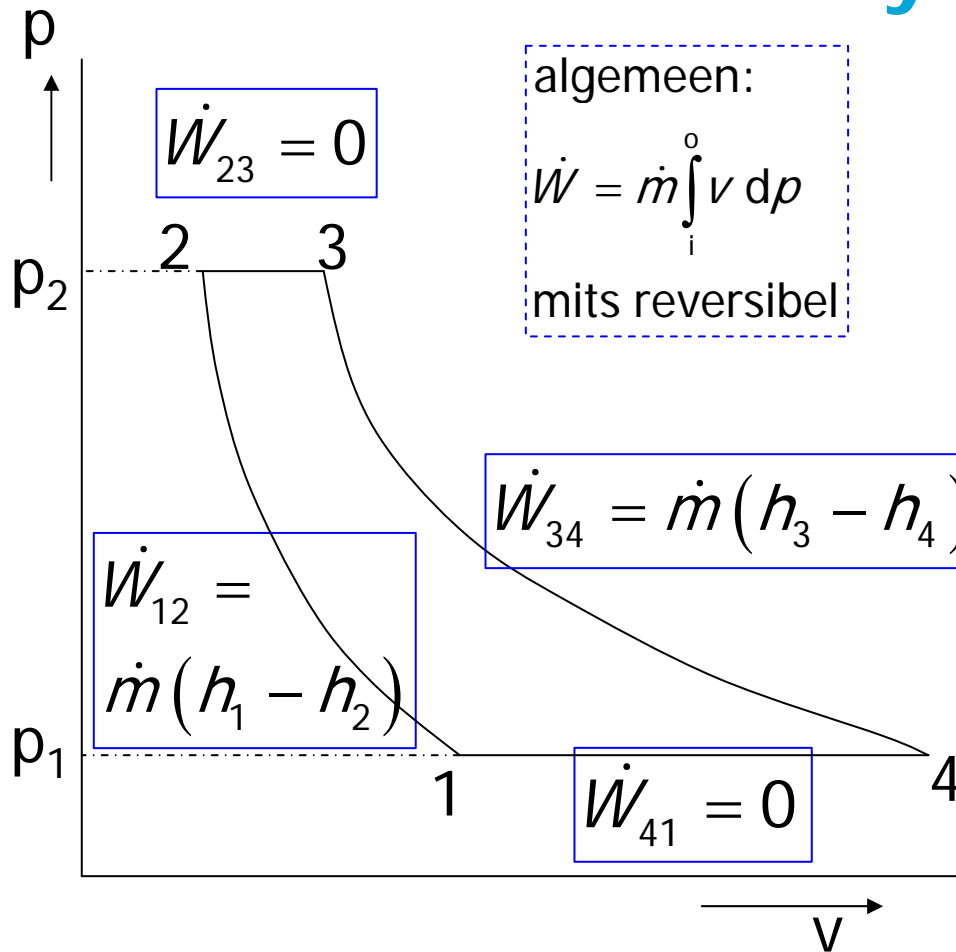


Aviation, important:

High power to mass ratio
Compact
Low emissions (CO, UHC)

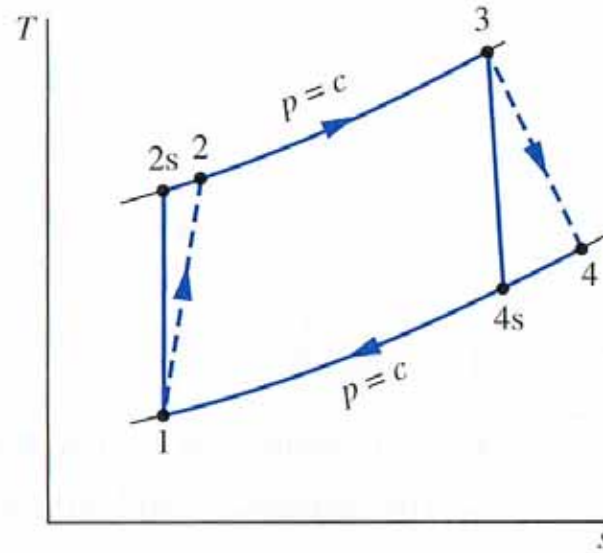
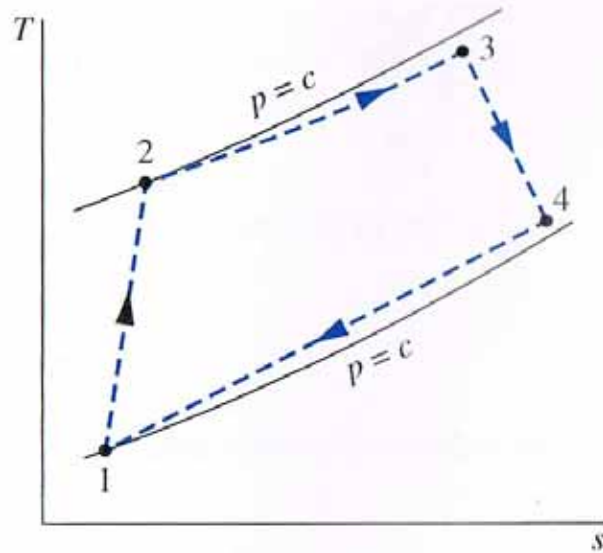


Joule – Brayton cycle (p,s)



$$\dot{W} = \dot{Q} + \dot{m} \left\{ (h_i - h_o) + \frac{1}{2} (V_i^2 - V_o^2) + g(z_i - z_o) \right\}$$

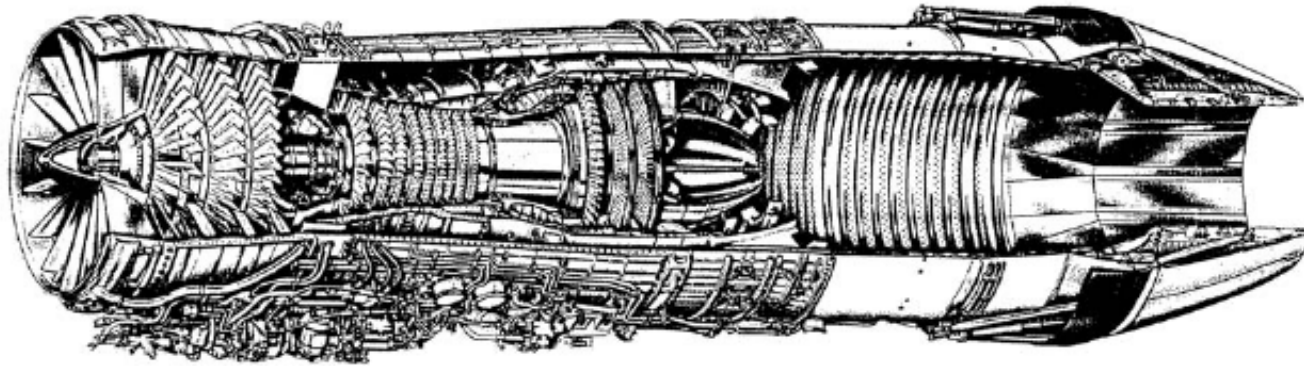
Irreversibilities in the cycle



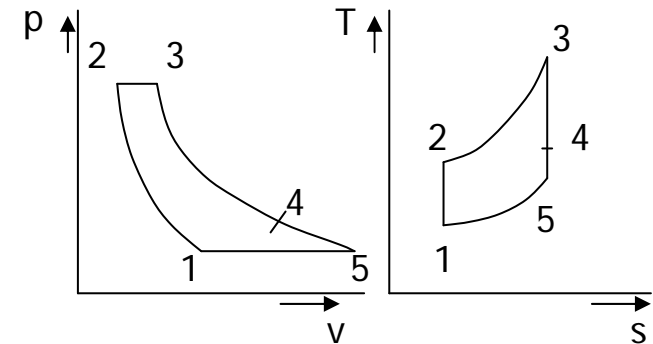
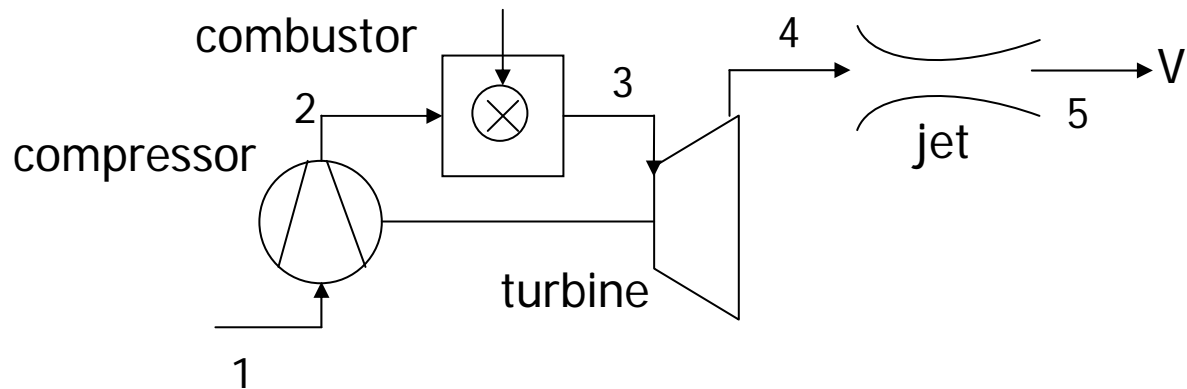
$$\eta_t = \frac{\left(\frac{W_t}{\dot{m}} \right)}{\left(\frac{W_t}{\dot{m}} \right)_s} = \frac{h_3 - h_4}{h_3 - h_{4s}}$$

$$\eta_c = \frac{\left(\frac{W_c}{\dot{m}} \right)_s}{\left(\frac{W_c}{\dot{m}} \right)} = \frac{h_{2s} - h_1}{h_2 - h_1}$$

Aircraft gas-turbine

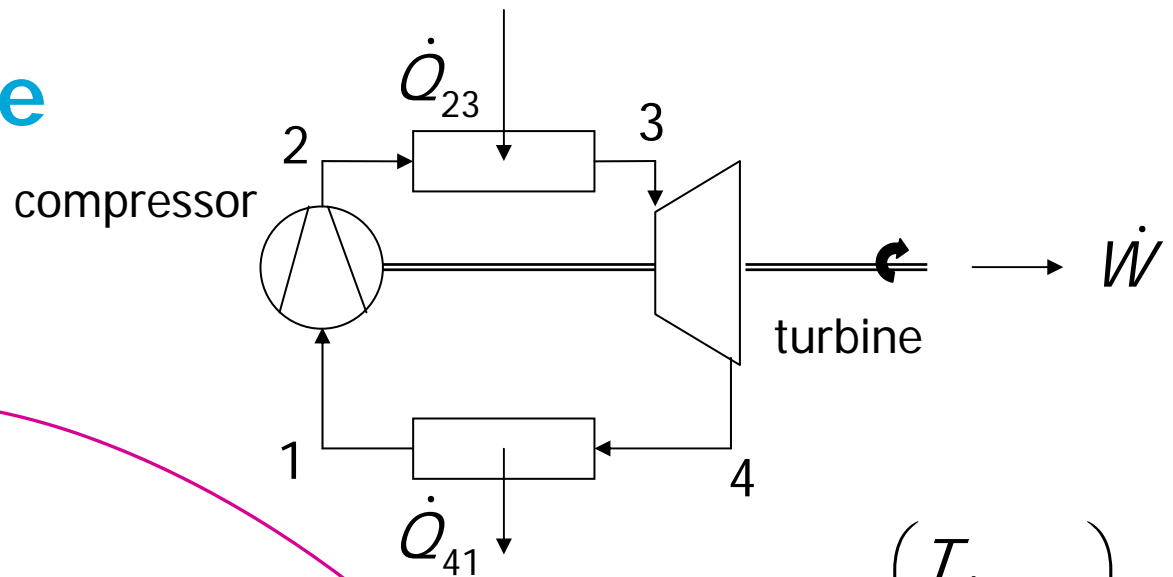


General Electric F110-GE-100 Augmented Turbofan Engine -> $T_2 \sim 600 \text{ }^\circ\text{C}$



Brayton-cycle

$$\dot{W} = \dot{Q}_{23} + \dot{Q}_{41}$$



Cold air standard

$$\eta = \frac{\dot{W}}{\dot{Q}_{23}} = 1 + \frac{\dot{Q}_{41}}{\dot{Q}_{23}} = 1 + \frac{T_1 - T_4}{T_3 - T_2} = 1 - \frac{T_1}{T_2} \frac{\left(\frac{T_4}{T_1} - 1 \right)}{\left(\frac{T_3}{T_2} - 1 \right)}$$

Poisson

$$\left. \begin{aligned} T_4 \rho_4^{\frac{\kappa-1}{\kappa}} &= T_3 \rho_3^{\frac{\kappa-1}{\kappa}} \\ T_1 \rho_1^{\frac{\kappa-1}{\kappa}} &= T_2 \rho_2^{\frac{\kappa-1}{\kappa}} \end{aligned} \right\}$$

$$\Rightarrow \frac{T_4}{T_1} = \frac{T_3}{T_2} \text{ en ook } \frac{T_3}{T_4} = \frac{T_2}{T_1}$$

Brayton cycle

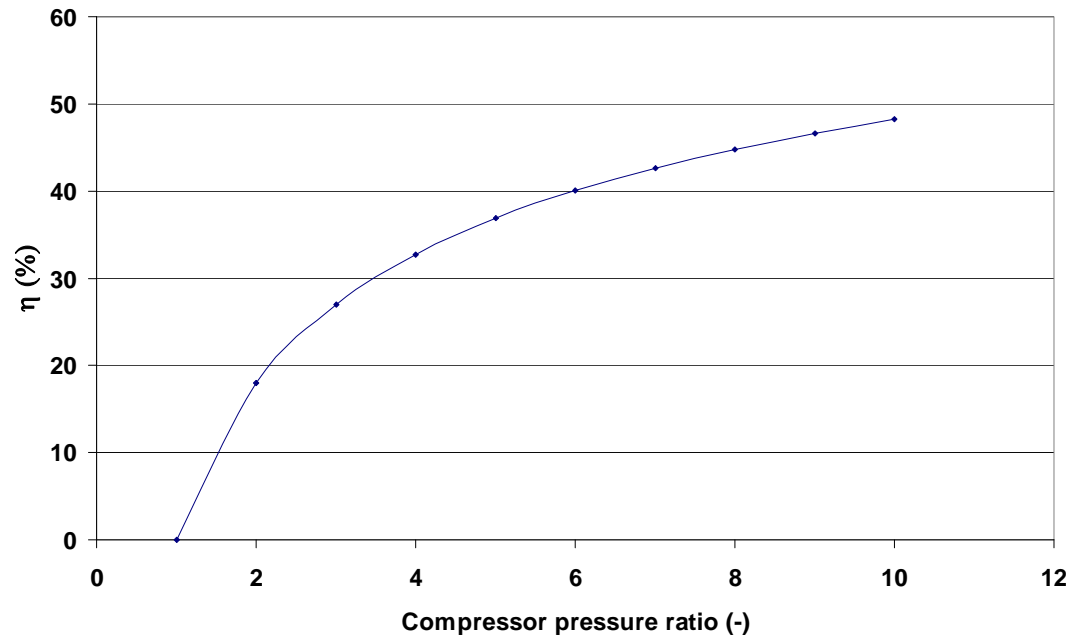
$$\eta = 1 - \frac{T_1}{T_2}$$

$$T_2 = T_1 \left(\frac{p_2}{p_1} \right)^{\frac{\kappa-1}{\kappa}} \rightarrow \text{derived in working class 4!!}$$

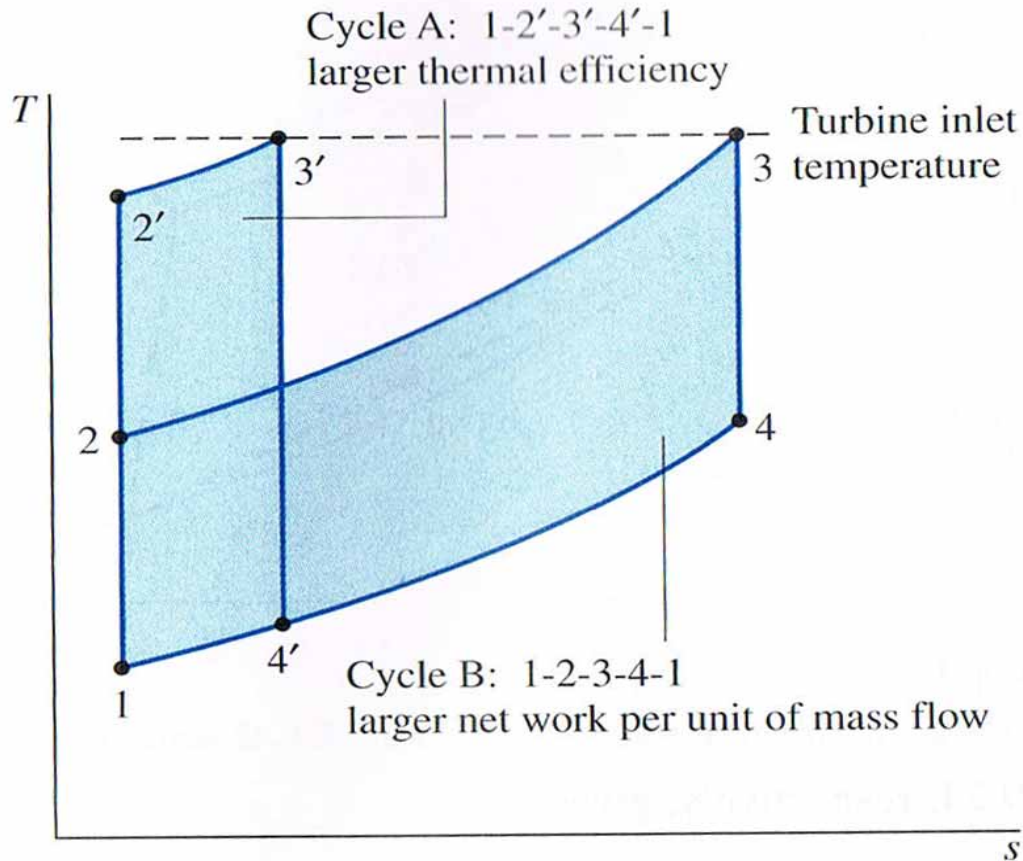
$$\frac{T_1}{T_2} = \left(\frac{p_2}{p_1} \right)^{\frac{-(\kappa-1)}{\kappa}}$$

$$\Rightarrow \eta = 1 - \frac{1}{\left(\frac{p_2}{p_1} \right)^{\frac{(\kappa-1)}{\kappa}}}$$

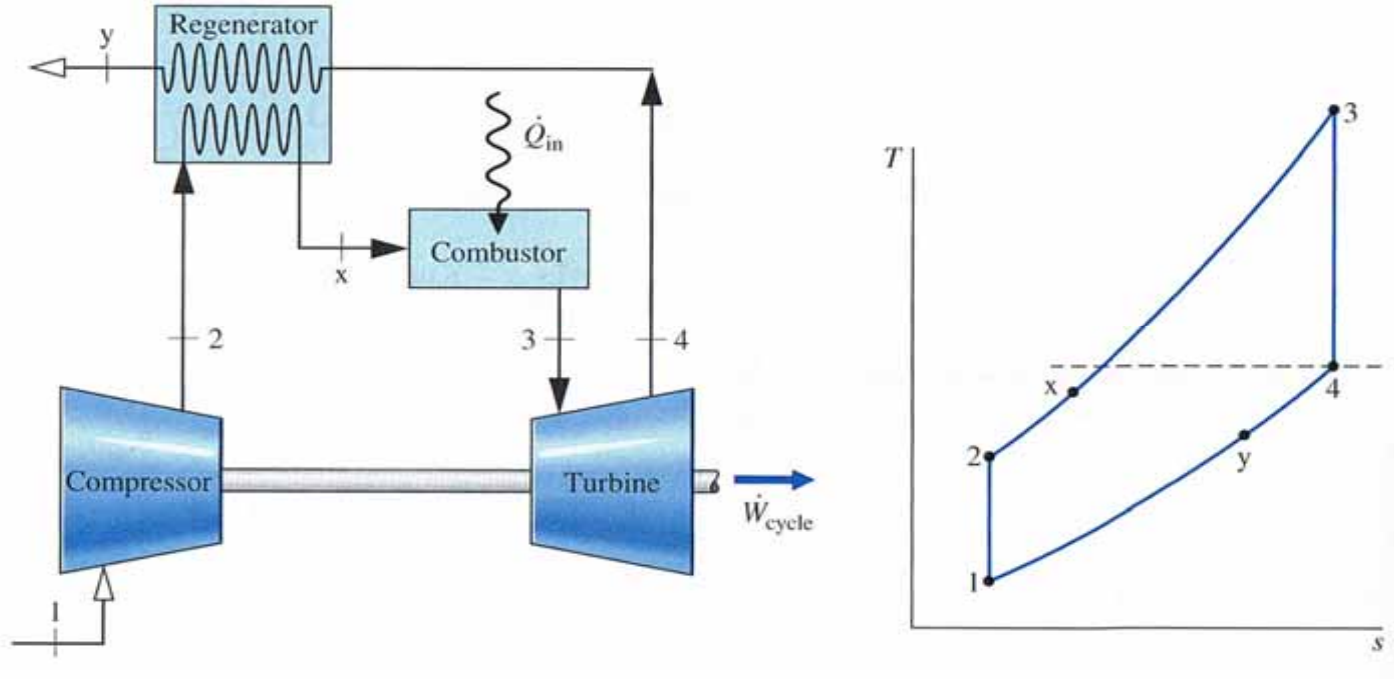
Practical limit:
Turbine inlet T_3



System design considerations



Regenerative Gas Turbines

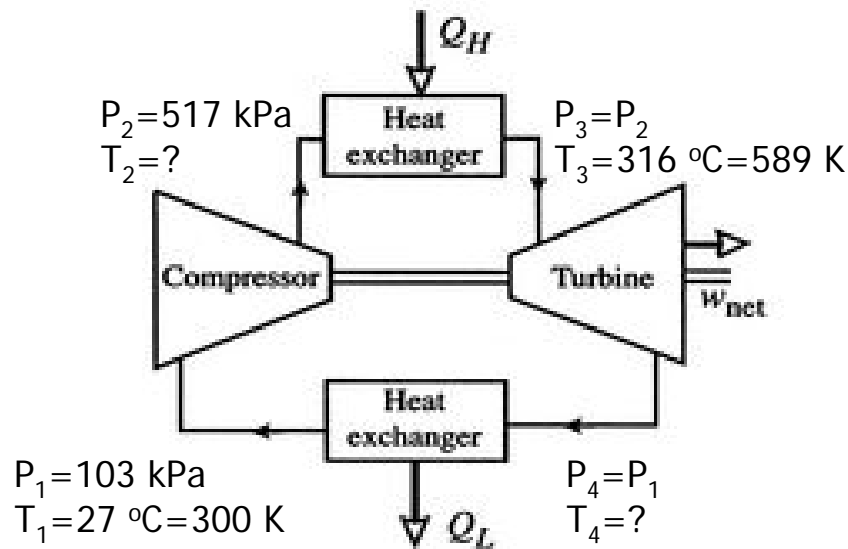


Regenerator effectiveness:
$$\eta_{reg} = \frac{h_x - h_2}{h_4 - h_2}$$

Typically, $60\% < \eta_{reg} < 80\%$

Example problem 1

An internally reversible air-standard Brayton cycle receives air at 27 °C and 103 kPa. The upper limits of pressure and temperature of the cycle are 517 kPa and 316 °C. Determine the thermal efficiency of the cycle, assuming constant specific heat, $C_p=1,0035 \text{ kJ}/(\text{kg}\cdot\text{K})$.



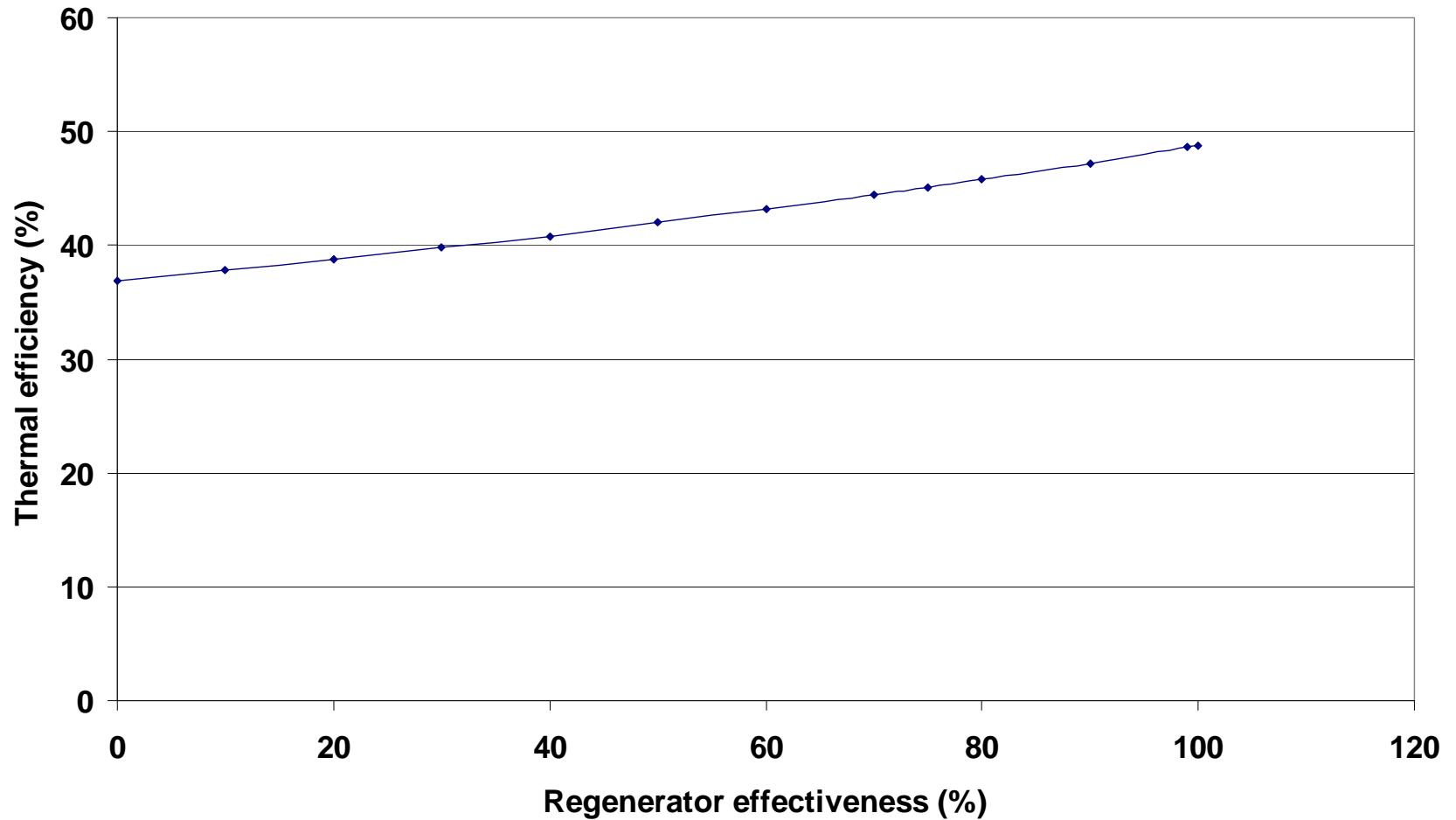
Example problem 2

A regenerator of 75% effectiveness is used in an air standard Brayton cycle working between pressures of 1030 hPa and 5,17 bar.

Determine the work per kg of air and the thermal efficiency of the cycle if the maximum and minimum temperatures of the cycle are 671,3 °C and 32,4 °C, respectively. Assume constant C_p of 1,004 kJ/(kg.K) and $\kappa=1,4$.

Sensitivity study on influence of regenerator effectiveness

(example problem 2)



Study-suggestions

- Study Chapter 9.1 - 9.8 and 9.11
- Do some of the exercises 9.28 - 9.35 (Brayton-cycles)
Especially: finish 9.28, do 9.29
- Exercises 9.36-9.39 regenerator
- Problems 9.40 - 9.44 reheat
- Problems 9.45 - 9.50 intercooling
- 9.51 intercooling and reheat
- 9.52 intercooling, reheat and regenerator