

# Thermodynamica 1

**Bendiks Jan Boersma**

**Wiebren de Jong**

**Thijs Vlugt**

**Theo Woudstra**

**Afdeling Process en Energie**

**Sectie energietechniek**

**February 4, 2011**

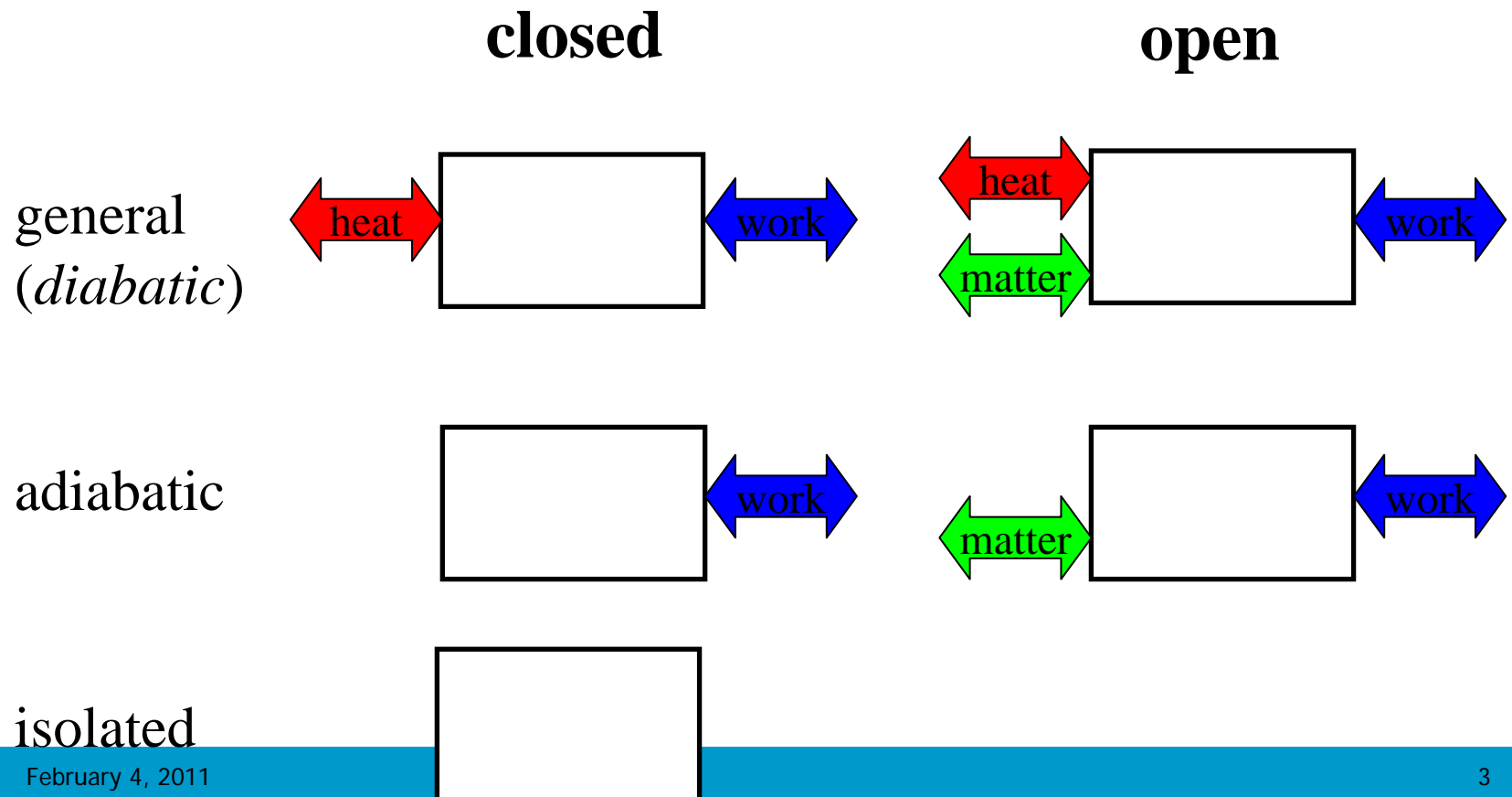
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**college 2 – boek hoofdstuk 1**

# summary lecture 1

- **system** (closed, open, adiabatic, isolated)
- **state** and **properties**
- **intensive**, **extensive** and **specific** properties
- **process**

# systems: summary

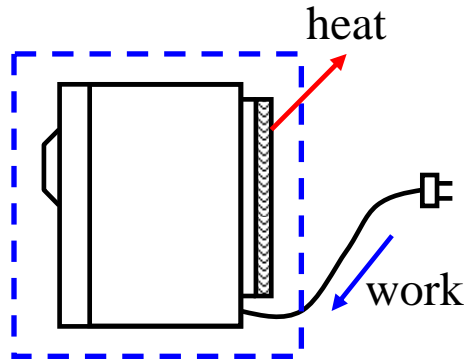


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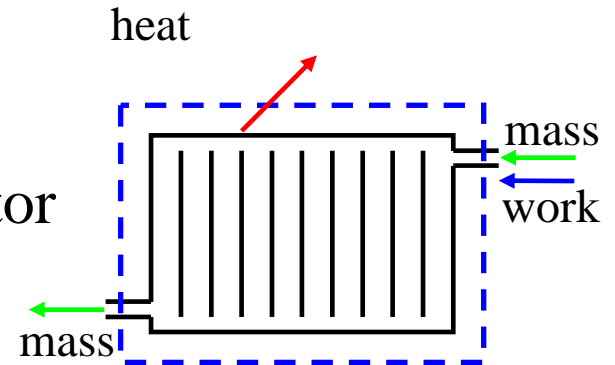
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# systems: examples

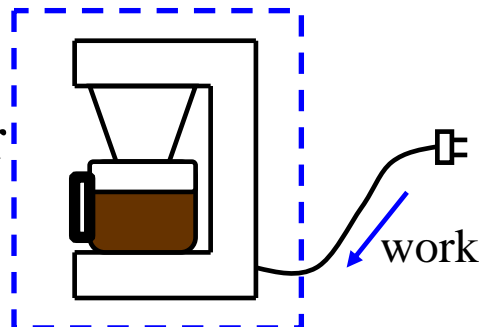
closed:  
refrigerator



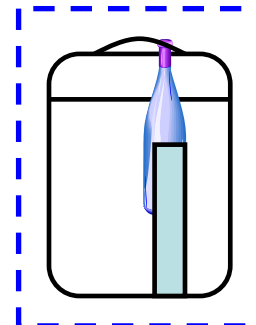
open:  
radiator



adiabatic:  
coffee maker



isolated:  
cooler with  
hot bottle and  
freezer pack



# process

A **process** is defined as the change of the state of a system.

We only consider changes from one equilibrium state to another

The state of a system has changed when the properties (in an equilibrium state) have changed. During the change the system is not in equilibrium.

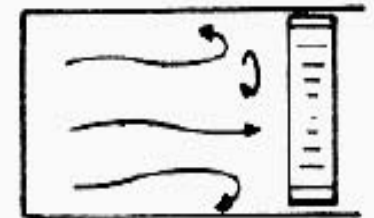
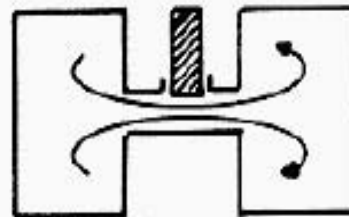
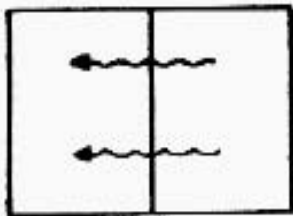
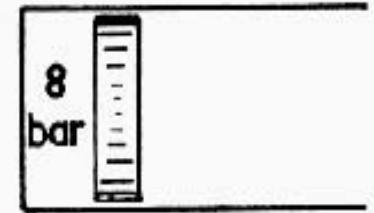
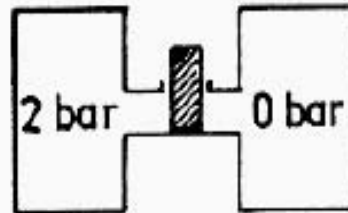
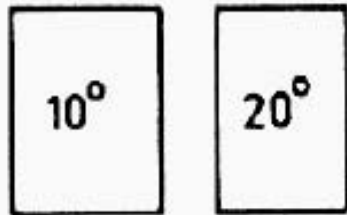
A (thermodynamic) **cycle** is a process where the initial and final states are identical.

adiabatic system → adiabatic process

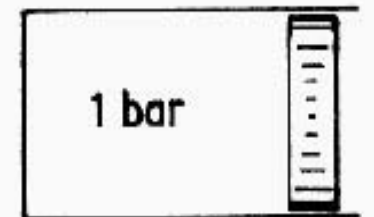
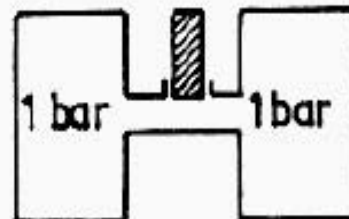
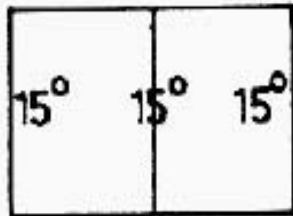
isolated system → isolated process

# process: examples A → B

A



B



a.

b.

c.

## Reversible/irreversible?

# Lecture 2

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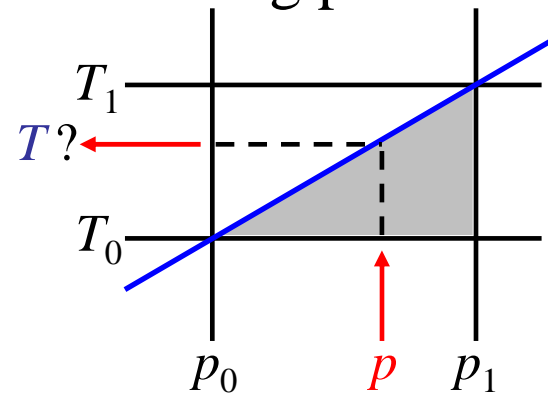
# interpolation

Properties of gases and liquids are given in tables (e.g., Table A-3).

TABLE A-3 Properties of Saturated Water (Liquid-Vapour): Pressure Table

Press. bars	Temp. °C	Specific Volume m <sup>3</sup> /kg	
		Sat. Liquid $v_f \times 10^3$	Sat. Vapour $v_g$
0.80	93.50	1.0380	2.087
0.90	96.71	1.0410	1.869
1.00	99.63	1.0432	1.694
1.50	111.4	1.0528	1.159
2.00	120.2	1.0605	0.8857

What is the boiling point at 1.3 bar?



Similar triangles:

$$\frac{T_1 - T_0}{p_1 - p_0} = \frac{T - T_0}{p - p_0} \Rightarrow$$

$$T = T_0 + \frac{T_1 - T_0}{p_1 - p_0} \times (p - p_0)$$

Answer:

$$T = 106.7^\circ \text{C}$$



TABLE A-3 Properties of Saturated Water (Liquid-Vapour): Pressure Table

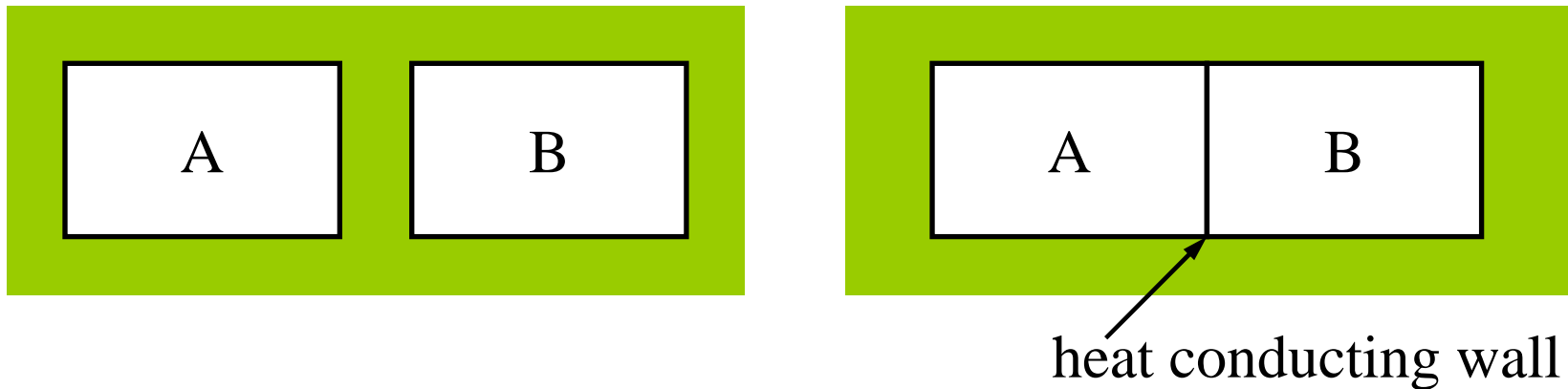
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106.7C

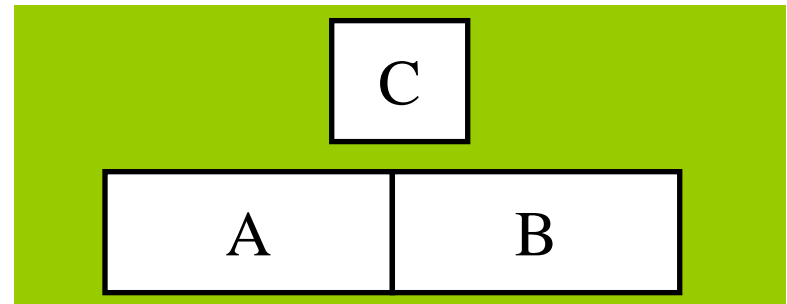
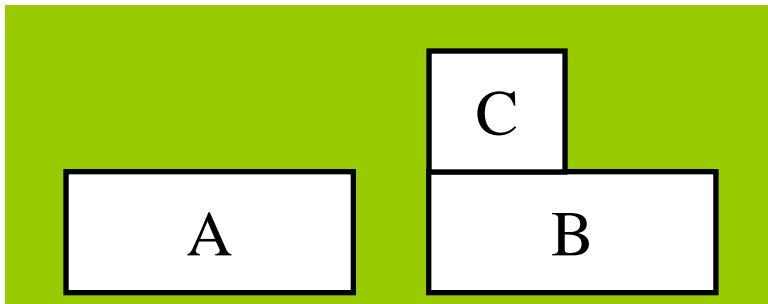
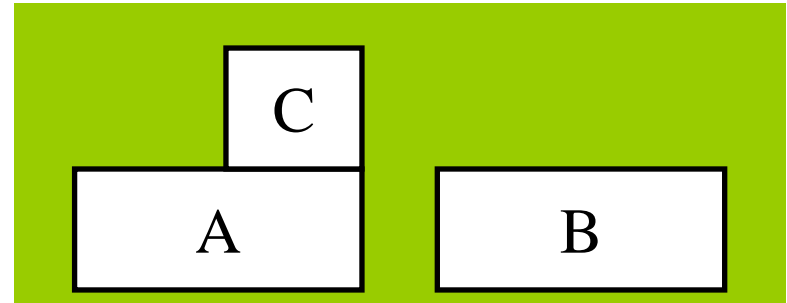
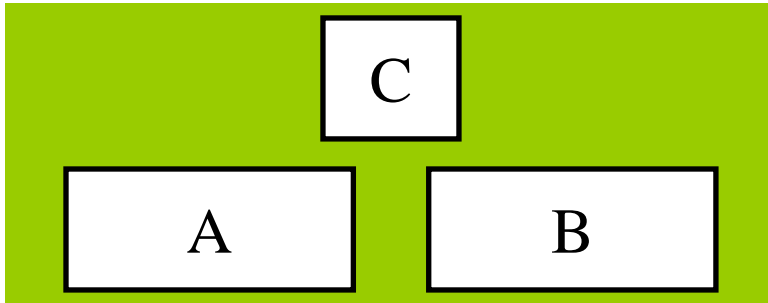
# thermal equilibrium



Two equilibrium systems that are brought into contact (via a heat-conducting wall) will eventually reach a new equilibrium. This new equilibrium is such that both systems feel 'equally warm/cold': they are said to have the same *temperature*.

How to quantify temperature?

# 0<sup>th</sup> Law of Thermodynamics



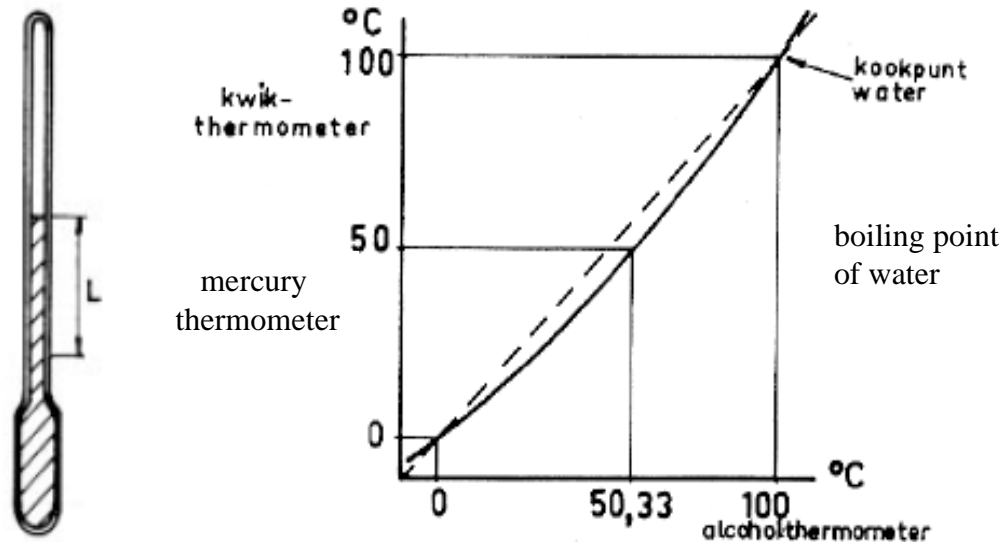
When C is in thermal equilibrium with A and B, then A and B are also in thermal equilibrium.

This defines the *experimental temperature* for 'thermometer C'

by measuring a property that uniquely depends on the temperature.<sup>11</sup>

# the experimental temperature

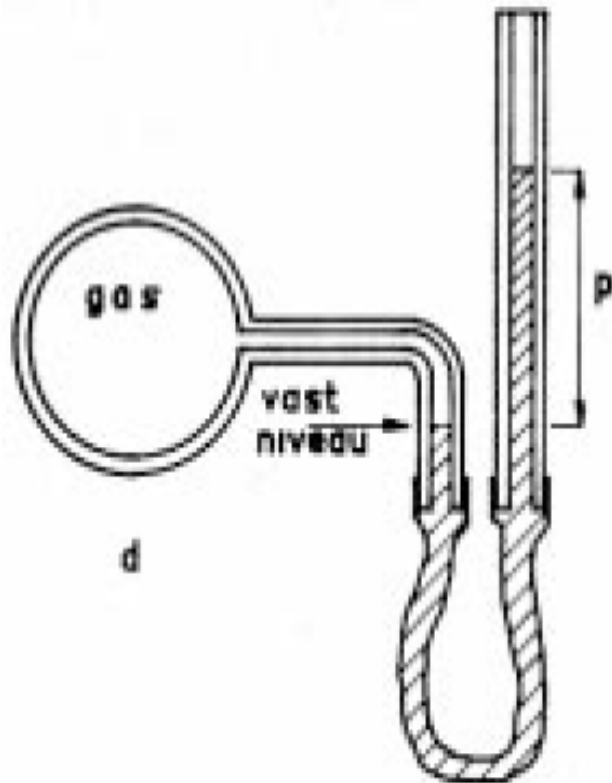
**Example:** the property is the expansion of a fluid (mercury or alcohol). The centigrade scale is obtained at atmospheric pressure (1.01325 bar) by calling the freezing point  $0^{\circ}\text{C}$  and the boiling point  $100^{\circ}\text{C}$ .



We have a problem: what is the correct value?

# the gas temperature scale (page 16-17)

for the gas temperature scale we use a constant-volume gas thermometer



The experimental gas temperature is defined as:  $T_{\text{exp}} = \alpha p$

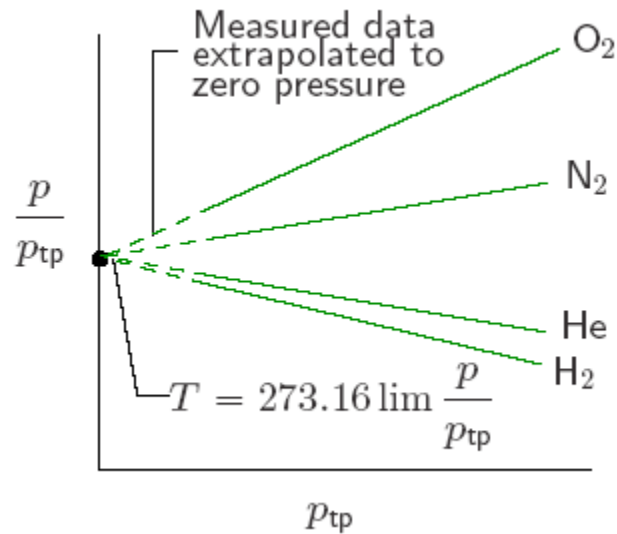
The constant  $\alpha$  is fixed for the water triple point ( $0.01^\circ \text{C}$ ) and refer to this value as 273.16 on the scale:

where  $p_{\text{tp}}$  is the triple point gas pressure

$$T_{\text{exp}} = 273.16 \frac{p}{p_{\text{tp}}}$$

# the gas temperature scale

when the amount of gas is reduced we find for different gases:



$$T_{\text{exp}} = 273.16 \lim_{p_{tp} \rightarrow 0} \frac{p}{p_{tp}}$$

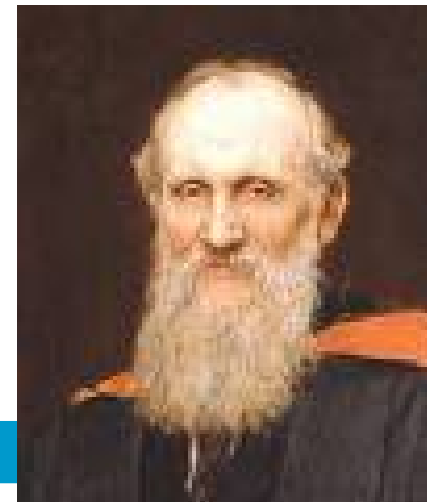
After consideration of the 2nd Law it will be shown that this scale is identical to the thermodynamic temperature scale when we use the triple point as a calibration point.

# Temperatuur

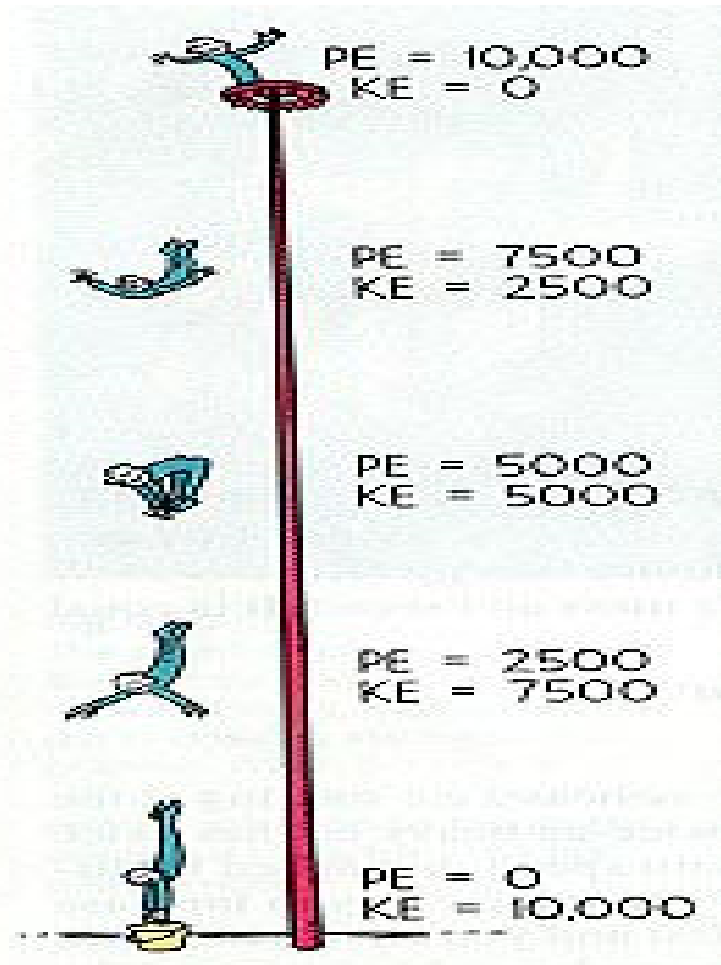
- Bij thermo berekeningen moet je onzettend opletten met de temperatuur schaal, Kelvin of Celsius.
- Celsius werkt soms, Kelvin werkt altijd.

**Reken alle temperaturen altijd eerst om naar Kelvin!!!**

**Wordt het antwoord gevraagd in Celsius reken dit dan pas helemaal op het eind om van Kelvin naar Celsius!!!**

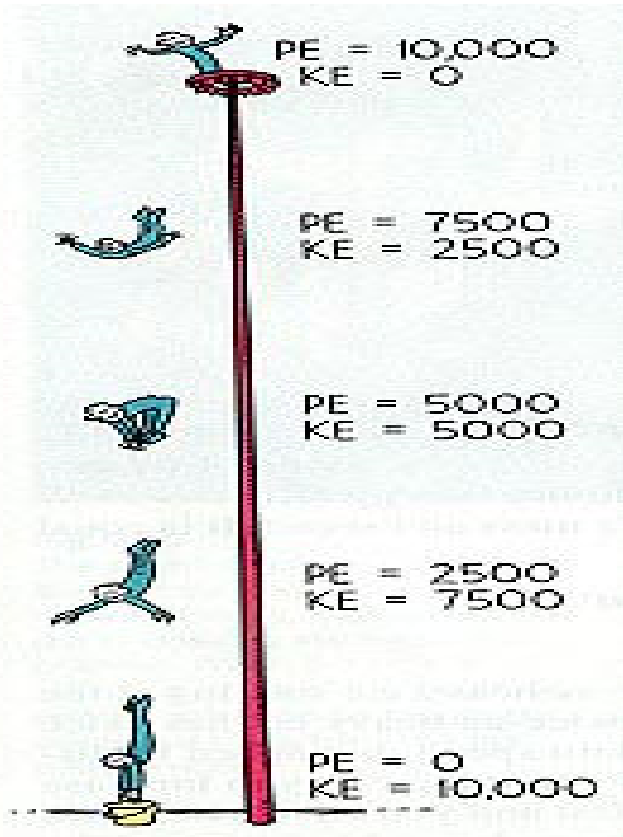


# Potential energy → Kinetic energy → ?





# Kinetic, potential energy and heat



$PE \rightarrow KE \rightarrow Heat$

$$mgh = \frac{1}{2}mV^2$$

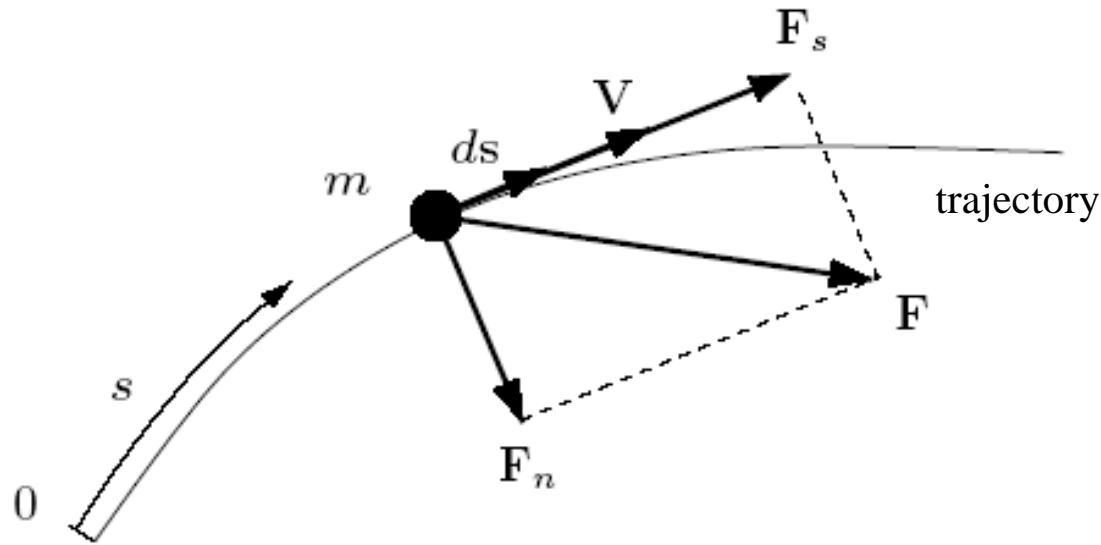
$$\frac{1}{2}mV^2 = mC_p\Delta T$$

$$PE \rightarrow .. \rightarrow Heat \Rightarrow \Delta T = \frac{gh}{C_p}$$

Experiment with small lead ( $C_p = 130J / Kg \cdot K$ )  
or brass ( $C_p = 380J / Kg \cdot K$ ) balls

$h = 20$  meters,  $\Delta T = ?$

# mechanical energy



Newton:  $\mathbf{F} = m \cdot \frac{d\vec{\mathbf{V}}}{dt}$

**V** (bold) is velocity vector

We find that:

$$\mathbf{F} \cdot \mathbf{V} = m \frac{d\mathbf{V}}{dt} \cdot \mathbf{V} = m \frac{d\left(\frac{1}{2} \mathbf{V} \cdot \mathbf{V}\right)}{dt} = m \frac{d\left(\frac{1}{2} V^2\right)}{dt} = \frac{d\left(\frac{1}{2} m V^2\right)}{dt}$$

and so:

$$\int_{t_1}^{t_2} \mathbf{F} \cdot \mathbf{V} dt = \frac{1}{2} m V_2^2 - \frac{1}{2} m V_1^2$$

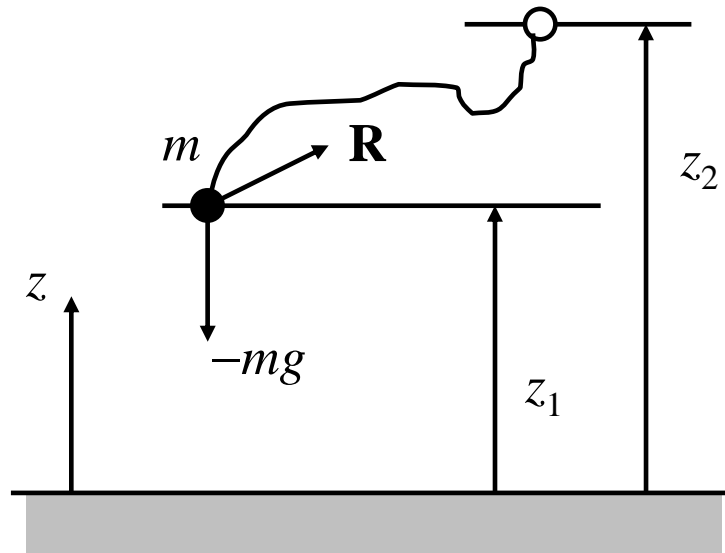
where:

$$\text{external work: } \int_{t_1}^{t_2} \mathbf{F} \cdot \mathbf{V} dt = \int_{s_1}^{s_2} \mathbf{F} \cdot d\mathbf{s} = \int_{s_1}^{s_2} F_s ds$$

$$\text{kinetic energy (KE): } \frac{1}{2} m V^2$$

thus:

$$\text{external work} = \text{KE}_2 - \text{KE}_1 = \Delta \text{KE}$$



$$\mathbf{F} = -mge_z + \mathbf{R}$$

External work:

$$\int_{s_1}^{s_2} \mathbf{F} \cdot d\mathbf{s} = -mgz_2 + mgz_1 + \int_{s_1}^{s_2} \mathbf{R} \cdot d\mathbf{s}$$

Substitute:

$$\int_{s_1}^{s_2} \mathbf{R} \cdot d\mathbf{s} = \frac{1}{2} mV_2^2 - \frac{1}{2} mV_1^2 + mgz_2 - mgz_1$$

where:

potential energy of gravity (PE):  $mgz$

thus:

$$\text{External work of } \mathbf{R} = \text{KE}_2 - \text{KE}_1 + \text{PE}_2 - \text{PE}_1 = \Delta\text{KE} + \Delta\text{PE}$$

When  $\mathbf{R} = \mathbf{0}$  :  $\Delta\text{KE} + \Delta\text{PE} = 0$  or  $\text{KE} + \text{PE} = \text{constant}$

# work

The work  $W$  is the work acted by the system on the surroundings

$W > 0$  : work is done *by* the system

$W < 0$  : work is done *on* the system

$$\Delta W_{1 \rightarrow 2} = \int_{t_1}^{t_2} \vec{F}_{\text{sur}} \cdot \vec{V} dt = \int_{s_1}^{s_2} \vec{F}_{\text{sur}} \cdot d\vec{s}$$

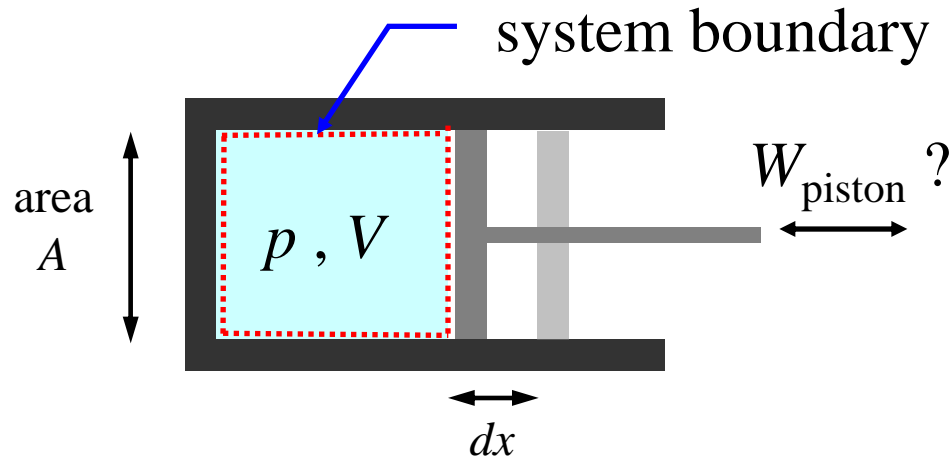
In general, the work  $W$  depends on the trajectory:

$$\Delta W_{1 \rightarrow 2} = \int_1^2 \delta W \neq W_2 - W_1 \quad \text{Work is **not** a *property*.}$$

Power (work per unit time):  $\dot{W} = \mathbf{F}_{\text{sur}} \cdot \mathbf{V}$

## example

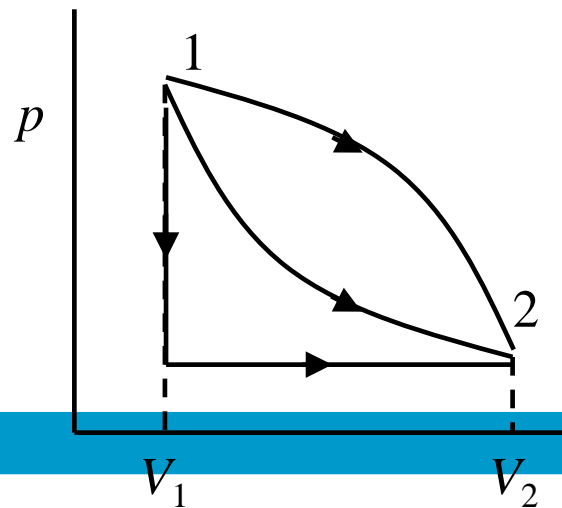
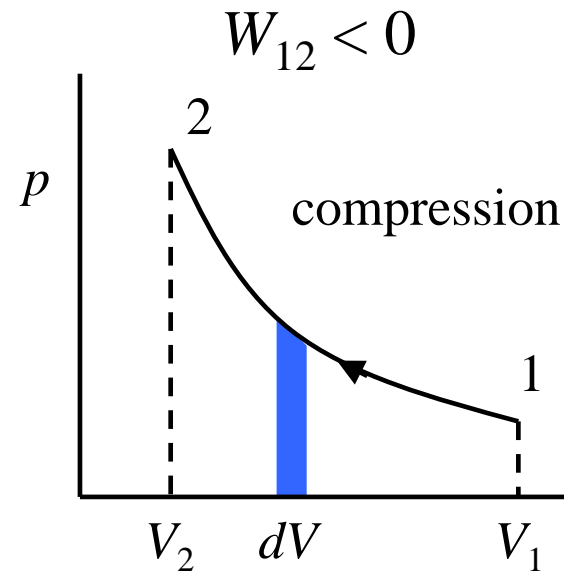
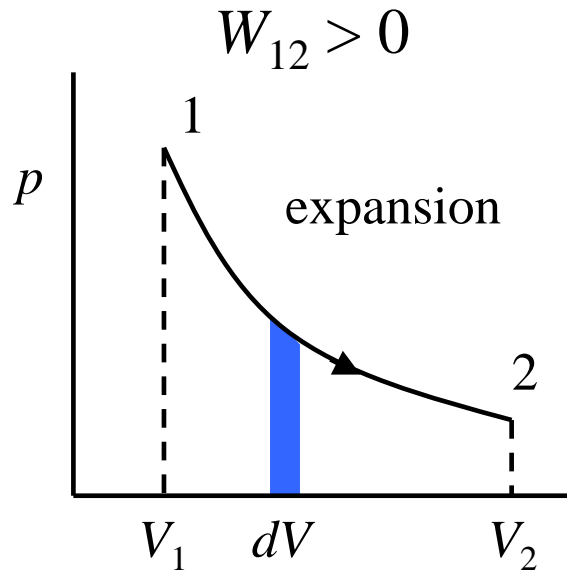
Work exerted by a gas on a piston. Consider a quasi-static process.



$$\delta W = F_{\text{ext}} dx = pAdx = pdV$$

$$W_{12} = \int_1^2 \delta W = \int_{V_1}^{V_2} pdV$$

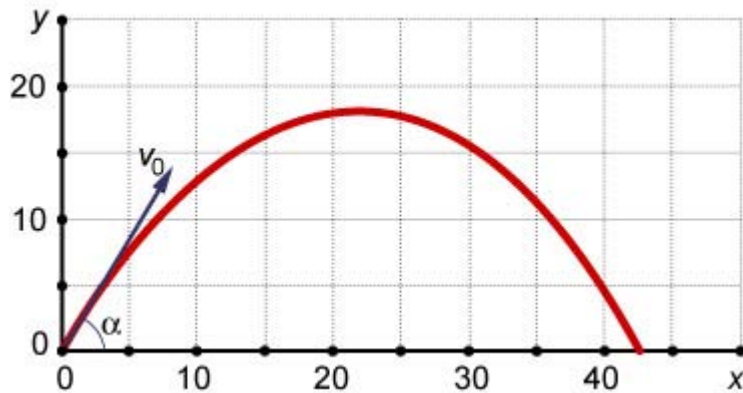
**Quasi-static  $\rightarrow$  P will be uniformly distributed**





# Water raket wedstrijd 25 maart, 2011 Mekelpark (voor de faculteit)

- Plastic cola fles (0.5 liter)
- Rubber stop of kurk
- Fiets pomp
- Prijs: 100 Euro voor grootste afstand (mits > 50 meter)
- 1 poging per deelnemer (team)



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## Question 2.18

- Gas expands from 500kPa to 100kPa, the initial volume is  $0.1\text{m}^3$ . Sketch the process in a P-V diagram and determine the work. (You can assume  $P V = \text{Const}$ ).

$$pV = C$$

$$p_1 V_1 = p_2 V_2$$

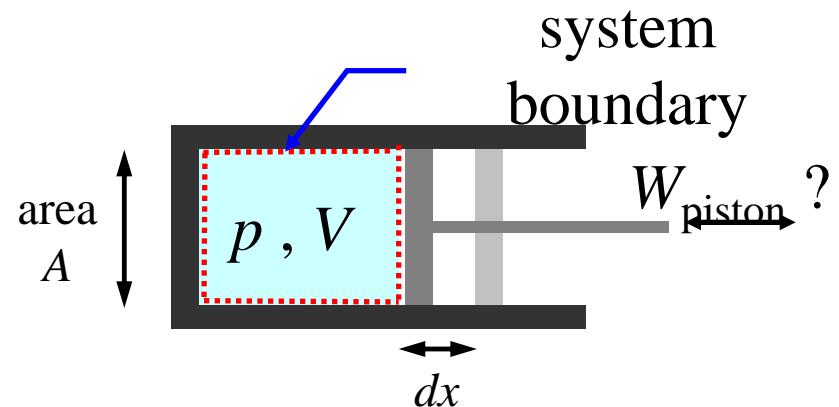
$$V_2 = V_1 \frac{p_1}{p_2} = 0.1 * 500 / 100 = 0.5\text{m}^3$$

$$W = \int_1^2 p dV = \int_1^2 \frac{C}{V} dV = C \int_1^2 \frac{1}{V} dV = C \ln \frac{V_2}{V_1} = 50 \cdot 10^3 * \ln(5) = 80.4\text{KJ}$$

let op  $C[\ln(V_2) - \ln(V_1)]$  is wiskundig gezien

het zelfde maar fysisch gezien niet. We kunnen

geen  $\ln(\cdot)$  nemen van een volume ivm dimensies



## •Question 2.18 (modified)

- Consider the expansion on the previous slide to be at  $T=500K$  and  $P V = C T \rightarrow C=100$
- Subsequently the same gas is compressed from 2 to 1 at a temperature of  $300K$  calculate the work for both steps.

$$\text{I: } pV = CT \rightarrow C = p_1 V_1 / T_1 = 100 \text{ Pa} \cdot \text{m}^3 / \text{K}$$

$$\Delta W_{1 \rightarrow 2} = \int_1^2 p dV = \int_1^2 \frac{CT}{V} dV = CT \ln \frac{V_2}{V_1} = 100 \cdot 500 * \ln(5) = 80.4 \text{ kJ}$$

$$\text{II: } pV = CT$$

$$\Delta W_{2 \rightarrow 1} = \int_2^1 p dV = \int_2^1 \frac{CT}{V} dV = CT \ln \frac{V_1}{V_2} = 100 * 300 * \ln\left(\frac{0.1}{0.5}\right) = -48 \text{ kJ}$$

$$\Delta W_{1 \rightarrow 2} + \Delta W_{2 \rightarrow 1} > 0 \text{ systeem levert netto arbeid} \Rightarrow \text{motor!!}$$

**•Verandering in temperatuur (toe of afvoer van warmte) geeft aanleiding tot netto arbeid!**

# Remark on work

$$\delta W = pdV \Rightarrow \Delta W_{1 \rightarrow 2} = \int_1^2 pdV$$

- **Alleen voor een gesloten systeem**

# instructions

- Ch. 1 & Ch. 2 up to §2.2 have been treated. Read this carefully before the next lecture.
- Make (some of) the exercises 2.1-2.10.
- Make one or more of the exercises 2.11-2.14 (work by a gas in a quasi-static equilibrium under compression or expansion)
- The next lecture will deal with the remainder of Ch. 2 (except §2.4.2, this will be done later) and Ch. 3 up to §3.2