

## Lecture 7

Empirical Research Methods  
IN4304

### Quantitative Data analysis I – Differences

IN4304 Empirical Research Methods Spring 2010 Lecture 7

1



TU Delft

## Previous lecture

### Data Entry

Code data, direction scales,  
clear name, missing data,  
level

### Central tendency

Mean, median, mode, IQR, SD

### Explorative data analysis

- Boxplot
- Histogram
- Stem and leaf plot

### Normal distribution

1. Gives a good model of data for some real world data sets (e.g. large populations)
2. Good approximation of results of random outcomes (e.g. throwing a dice many times)
3. Large number of inferential statistics are based on normal distributions

*Check for Normality if you want to use parametric statistics*

IN4304 Empirical Research Methods Spring 2010 Lecture 7

2



TU Delft

## Today

- Hypothesis testing
- Chi-square test
- *t*-test
- ANOVA
- Mann-Whitney U-test
- MANOVA

IN4304 Empirical Research Methods Spring 2010 Lecture 7

3



TU Delft

## Learning outcomes of this lecture

After today's lecture you should be able :

- to explain the idea behind hypothesis testing
- to link conceptual models with specific statistical tests
- to perform a number of statistical tests in SPSS

IN4304 Empirical Research Methods Spring 2010 Lecture 7

4



TU Delft

## Idea behind hypothesis testing



- Is the difference between two samples a reflection of the difference of two different populations or simply caused by sampling error?

IN4304 Empirical Research Methods Spring 2010 Lecture 7

5



TU Delft

## Hypothesis testing

- **Null hypothesis:** observed difference in sample is caused by sampling error and when considering the whole population there is no difference
- **Alternative hypothesis:** observed difference in sample is a real effect plus some change variation
- **p-value:** if null hypothesis is true, than what is the probability of observing a difference at least as extreme as the one observed in the sample?
- Social Science:  $p < 0.05$  supports rejection of Null hypothesis

IN4304 Empirical Research Methods Spring 2010 Lecture 7

6



TU Delft

## Decision

Population

$H_0 = \text{True}$      $H_0 = \text{False}$

|        |              |                                       |                          |
|--------|--------------|---------------------------------------|--------------------------|
| Sample | Accept $H_0$ | No Error                              | Type II Error<br>$\beta$ |
|        | Reject $H_0$ | Type I Error<br>( $\alpha$ , p-value) | No Error                 |

Power =  $1 - \beta$

IN4304 Empirical Research Methods Spring 2010 Lecture 7

7



TU Delft

## Interpreting p-value

- p-value:** if null hypothesis is true, than what is the probability of observing a difference at least as extreme as the one observed in the sample?
- $p. < 0.05 \rightarrow$  reject  $H_0$
- $p. > 0.05$ 
  - Inconclusive
  - Or if there are no methodological problems, argue based on power analysis that the real difference can not be very large

IN4304 Empirical Research Methods Spring 2010 Lecture 7

8



TU Delft

## Statistical test and Scales of measurement

| Aim             | Samples                                | Data Level                             | Tests   |
|-----------------|--|--|---|
| Find difference | Single sample                          | Nominal<br>Ordinal<br>Interval / Ratio | Binominal test, $\chi^2$ goodness-of-fit<br>Wilcoxon signu-ranks test<br>z-test, One-Sample t-test                                    |
|                 | Independent                            | Nominal<br>Ordinal<br>Interval / Ratio | Fisher-Exact test, $\chi^2$<br>Mann-Whitney U test<br>z-test, two independent sample t-test,<br>ANOVA, MANOVA                         |
| Dependent       |  | Nominal<br>Ordinal<br>Interval / Ratio | McNemar<br>Sign Test, Wilcoxon matched-pairs signed-rank test, Friedman Test<br>Paired-Sample t-test, repeated measures ANOVA, MANOVA |
| Find relation   | Nominal<br>Ordinal<br>Interval / Ratio |  | Cramer's V, phi<br>Kendall, Spearman correlation<br>Pearson product moment correlation,<br>regression analysis                        |

IN4304 Empirical Research Methods Spring 2010 Lecture 7

9



TU Delft

## Chi-square test – Conceptual model

- Conceptual model**
- Assumptions
- Example
- Interpretation outcome
- Demo

User interface type



Task completed



IN4304 Empirical Research Methods Spring 2010 Lecture 7

10



TU Delft

## Chi-square test - example

- Conceptual model
- Assumptions
- Example**
- Interpretation outcome
- Demo

| Observed | UI A | UI B | UI C |     |     |  |
|----------|------|------|------|-----|-----|--|
| Yes      | 30   | 70   | 25   | 125 | 66% |  |
| No       | 35   | 10   | 20   | 65  | 34% |  |
|          | 65   | 80   | 45   | 190 |     |  |
|          | 34%  | 42%  | 24%  |     |     |  |
| Expected |      |      |      |     |     |  |
| Yes      | 43   | 53   | 30   |     |     |  |
| No       | 22   | 27   | 15   |     |     |  |

IN4304 Empirical Research Methods Spring 2010 Lecture 7

11



TU Delft

## Chi-square test - assumptions

- Conceptual model
  - Assumptions**
  - Example
  - Interpretation outcome
  - Demo
- Independence of observations
  - Nominal data
  - Each observed person (or case) must appear in only one of the frequency cells
  - No more than 20% of the expected frequency cell counts should be less than 5 in large contingency table. For small tables each expected frequency cell count should be greater than 5

IN4304 Empirical Research Methods Spring 2010 Lecture 7

12



TU Delft

## Chi-square test – interpretation outcomes

- Conceptual model
- Assumptions
- Example
- **Interpretation outcome**
- Demo

| Chi-Square Tests             |                     |    |                       |
|------------------------------|---------------------|----|-----------------------|
|                              | Value               | df | Asymp. Sig. (2-sided) |
| Pearson Chi-Square           | 29.983 <sup>a</sup> | 2  | .000                  |
| Likelihood Ratio             | 32.286              | 2  | .000                  |
| Linear-by-Linear Association | 2.726               | 1  | .099                  |
| N of Valid Cases             | 190                 |    |                       |

<sup>a</sup>. 0 cells (.0%) have expected count less than 5. The minimum expected count is 15.39.

IN4304 Empirical Research Methods Spring 2010 Lecture 7

13



TU Delft

## Chi-square test – SPSS Demo

- Conceptual model
- Assumptions
- Example
- Interpretation outcome
- **Demo**

File: examples\_chi.sav  
Var: UI-Type, Task\_complete

IN4304 Empirical Research Methods Spring 2010 Lecture 7

14



TU Delft

## Statistical test and Scales of measurement

| Aim             | Samples          | Data Level       | Tests   |
|-----------------|------------------|------------------|---|
| Find difference | Single sample    | Nominal          | Binominal test, $\chi^2$ goodness-of-fit                          |
|                 |                  | Ordinal          | Wilcoxon signed-ranks test  |
| Independent     | Interval / Ratio | Nominal          | $z$ -test, One-Sample $t$ -test                                   |
|                 |                  | Ordinal          | Fisher-Exact test, $\chi^2$                                       |
|                 |                  | Interval / Ratio | $z$ -test, two independent sample $t$ -test, ANOVA, MANOVA        |
| Dependent       | Interval / Ratio | Nominal          | McNemar   |
|                 |                  | Ordinal          | Sign Test, Wilcoxon matched-pairs signed-rank test, Friedman Test |
|                 |                  | Interval / Ratio | Paired-Sample $t$ -test, repeated measures ANOVA, MANOVA          |
| Find relation   | Interval / Ratio | Nominal          | Cramer's $V$ , phi  |
|                 |                  | Ordinal          | Kendall, Spearman correlation                                     |
|                 |                  | Interval / Ratio | Pearson product moment correlation, regression analysis           |

IN4304 Empirical Research Methods Spring 2010 Lecture 7

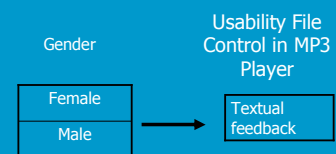
15



TU Delft

## Mann-Whitney U test – Conceptual model

- **Conceptual model**
- Assumptions
- Example
- Interpretation outcome
- Demo



IN4304 Empirical Research Methods Spring 2010 Lecture 7

16



TU Delft

## Mann-Whitney U test – example

- Conceptual model
- Assumptions
- **Example**
- Interpretation outcome
- Demo

(Rater total) rationale for score File Control \* Gender (female = 1, male = 2)  
Crosstabulation

| Count  |  | Gender (female = 1, male = 2) |      | Total |
|--|--|-------------------------------|------|-------|
|  |  | female                        | male |       |
| (Rater total) rationale for score File Control | missing or not relevant                                      | 3                             | 4    | 7     |
|  | Mainly negative comments, and/or improvement advice          | 1                             | 5    | 6     |
|  | Both negative and positive comments, and/or improvement advi | 2                             | 5    | 7     |
|  | Mainly positive or no negative comments and no improvement   | 8                             | 6    | 14    |
| Total  |  | 14                            | 20   | 34    |

IN4304 Empirical Research Methods Spring 2010 Lecture 7

17



TU Delft

## Mann-Whitney U test – assumptions

- Conceptual model
  - **Assumptions**
  - Example
  - Interpretation outcome
  - Demo
1. Independence of observations
  2. At least ordinal level

IN4304 Empirical Research Methods Spring 2010 Lecture 7

18



TU Delft

## Mann-Whitney U test – interpretation outcomes

- Conceptual model
- Assumptions
- Example
- **Interpretation outcome**
- Demo

| Ranks  |                 |    |           |              |
|--|-----------------|----|-----------|--------------|
| (Rater total) rationale for score File Control | Gender (female) | N  | Mean Rank | Sum of Ranks |
| female   |                 | 11 | 17.09     | 187.50       |
| male   |                 | 16 | 11.91     | 190.50       |
| Total  |                 | 27 |           |              |

| Test Statistics <sup>a</sup>   |  | (Rater total) rationale for score File Control |
|--------------------------------|--|--|
| Mann-Whitney U                 |  | 54.500   |
| Wilcoxon W                     |  | 190.500  |
| Z                              |  | -1.811   |
| Asymp. Sig. (2-tailed)         |  | .070   |
| Exact Sig. [2*(1-tailed Sig.)] |  | .093 <sup>b</sup>                              |

a. Not corrected for ties.  
b. Grouping Variable: Gender (female = 1, male = 2)

IN4304 Empirical Research Methods Spring 2010 Lecture 7

19



TU Delft

## Mann-Whitney U test – SPSS Demo

- Conceptual model
- Assumptions
- Example
- Interpretation outcome
- **Demo**

File: mp3playersurvey.sav  
Var: gender, fileRateTotal

IN4304 Empirical Research Methods Spring 2010 Lecture 7

20



TU Delft

## Statistical test and Scales of measurement

| Aim             | Samples          | Data Level       | Tests  |
|-----------------|------------------|------------------|--|
| Find difference | Single sample    | Nominal          | Binominal test, $\chi^2$ goodness-of-fit   |
|                 |                  | Ordinal          | Wilcoxon signed-ranks test<br>$z$ -test $\leftarrow$ One-Sample $t$ -test              |
| Independent     | Interval / Ratio | Nominal          | Fisher's Exact test  |
|                 |                  | Ordinal          | Mann-Whitney U test  |
|                 |                  | Interval / Ratio | $z$ -test, two independent sample $t$ -test, ANOVA, MANOVA                             |
| Dependent       | Nominal          | Ordinal          | McNemar  |
|                 |                  | Interval / Ratio | Sign Test, Wilcoxon matched-pairs signed-rank test, Friedman Test                      |
| Find relation   | Nominal          | Ordinal          | Paired-Sample $t$ -test, repeated measures ANOVA, MANOVA                               |
|                 |                  | Interval / Ratio | Cramer's V, phi  |
|                 |                  | Interval / Ratio | Kendall, Spearman correlation, Pearson product moment correlation, regression analysis |

IN4304 Empirical Research Methods Spring 2010 Lecture 7

21



TU Delft

## One-sample $t$ -test – Conceptual model

- **Conceptual model**
  - Assumptions
  - Example
  - Interpretation outcome
  - Demo
- Single Condition
  - Compare results with a norm or standard

IN4304 Empirical Research Methods Spring 2010 Lecture 7

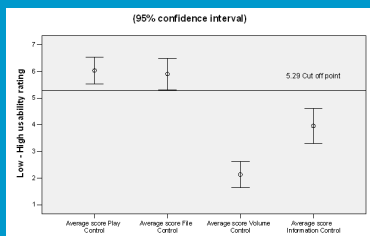
22



TU Delft

## One-sample $t$ -test - example

- Conceptual model
- Assumptions
- **Example**
- Interpretation outcome
- Demo



Usability rating of 4 UI components, with Cut of point 5.29

IN4304 Empirical Research Methods Spring 2010 Lecture 7

23



TU Delft

## One-sample $t$ -test - assumptions

- Conceptual model
  - **Assumptions**
  - Example
  - Interpretation outcome
  - Demo
1. Independence of observations
  2. Interval (or ratio) data
  3. Data are from normally distributed population

IN4304 Empirical Research Methods Spring 2010 Lecture 7

24



TU Delft

## One-sample t-test – interpretation outcomes

- Conceptual model
- Assumptions
- Example
- **Interpretation outcome**
- Demo

| One-Sample Test                   |         |    |                 |                 |
|-----------------------------------|---------|----|-----------------|-----------------|
| Test Value = 5.29                 |         |    |                 |                 |
|                                   | t       | df | Sig. (2-tailed) | Mean Difference |
| Average score Play Control        | 3.013   | 33 | .005            | .74922          |
| Average score File Control        | 2.120   | 33 | .042            | .61196          |
| Average score Volume Control      | -13.126 | 33 | .000            | -3.15765        |
| Average score Information Control | -4.102  | 33 | .000            | -1.33412        |

IN4304 Empirical Research Methods Spring 2010 Lecture 7

25



## One-sample t-test – SPSS Demo

- Conceptual model
- Assumptions
- Example
- Interpretation outcome
- **Demo**

File: mp3playersurvey.sav  
Var: fileAvg, VolumeAvg, InfAvg, PlayAvg

IN4304 Empirical Research Methods Spring 2010 Lecture 7

26



## Statistical test and Scales of measurement

| Aim             | Samples          | Data Level       | Tests   |
|-----------------|------------------|------------------|---|
| Find difference | Single sample    | Nominal          | Binominal test, $\chi^2$ goodness-of-fit                          |
|                 |                  | Ordinal          | Wilcoxon signed-ranks test  |
| Independent     | Interval / Ratio | Interval / Ratio | z-test, One-Sample t-test   |
|                 |                  | Nominal          | Fisher-Exact test, $\chi^2$                                       |
|                 |                  | Ordinal          | Mann-Whitney U test   |
|                 |                  | Interval / Ratio | z-test, <b>two independent sample t-test</b> , ANOVA, MANOVA      |
| Dependent       | Interval / Ratio | Nominal          | McNemar   |
|                 |                  | Ordinal          | Sign Test, Wilcoxon matched-pairs signed-rank test, Friedman Test |
|                 |                  | Interval / Ratio | Paired-Sample t-test, repeated measures ANOVA, MANOVA             |
| Find relation   | Interval / Ratio | Nominal          | Cramer's V, phi   |
|                 |                  | Ordinal          | Kendall, Spearman correlation                                     |
|                 |                  | Interval / Ratio | Pearson product moment correlation, regression analysis           |

IN4304 Empirical Research Methods Spring 2010 Lecture 7

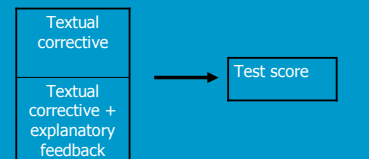
27



## Independent-sample t-test – Conceptual model

- **Conceptual model**
- Assumptions
- Example
- Interpretation outcome
- Demo

Feedback type in e-learning module



Score in post test

IN4304 Empirical Research Methods Spring 2010 Lecture 7

28



## Independent-sample t-test – assumptions

- Conceptual model
  - **Assumptions**
  - Example
  - Interpretation outcome
  - Demo
1. Independence of observations
  2. Interval (or ratio) data
  3. Data are from normally distributed population
  4. Homogeneity of variance (variances in populations are roughly equal)\*

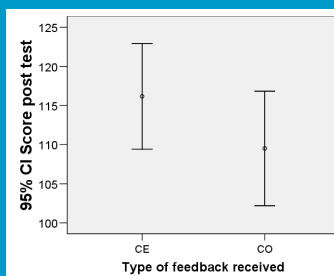
IN4304 Empirical Research Methods Spring 2010 Lecture 7

29



## Independent-sample t-test – example

- Conceptual model
- Assumptions
- **Example**
- Interpretation outcome
- Demo



IN4304 Empirical Research Methods Spring 2010 Lecture 7

30



## Independent-sample t-test – interpretation outcomes

- Conceptual model
- Assumptions
- Example
- **Interpretation outcome**
- Demo

|                 |                             | Levene's Test for Equality of Variances |      | t-test for Equality of Means |        |                 |                 |
|-----------------|-----------------------------|---|------|------------------------------|--------|-----------------|-----------------|
|                 |                             | F                                       | Sig. | t                            | df     | Sig. (2-tailed) | Mean Difference |
| Score post test | Equal variances assumed     | .040                                    | .841 | 1.365                        | 59     | .177            | 6.651           |
|                 | Equal variances not assumed |   |      | 1.367                        | 58.741 | .177            | 6.651           |

IN4304 Empirical Research Methods Spring 2010 Lecture 7

31



## Independent-sample t-test – SPSS Demo

- Conceptual model
- Assumptions
- Example
- Interpretation outcome
- **Demo**

File: Feedback experiment.sav  
 Var: feedback (1,2), postscore  
 Note: Filter feedback <> 3

IN4304 Empirical Research Methods Spring 2010 Lecture 7

32



## Statistical test and Scales of measurement

| Aim             | Samples          | Data Level       | Tests   |
|-----------------|------------------|------------------|---|
| Find difference | Single sample    | Nominal          | Binominal test, $\chi^2$ goodness-of-fit                          |
|                 |                  | Ordinal          | Wilcoxon signed-ranks test  |
| Independent     | Interval / Ratio | Ordinal          | z-test, One-Sample t-test   |
|                 |                  | Ordinal          | Fisher-Exact test, $\chi^2$ Mann-Whitney U test                   |
|                 |                  | Interval / Ratio | z-test, two independent sample t-test, ANOVA, MANOVA              |
|                 |                  | Ordinal          | McNemar   |
| Dependent       | Interval / Ratio | Nominal          | Sign Test, Wilcoxon matched-pairs signed-rank test, Friedman Test |
|                 |                  | Ordinal          | Paired-Sample t-test, repeated measures ANOVA, MANOVA             |
|                 |                  | Interval / Ratio | ANOVA, MANOVA   |
| Find relation   | Interval / Ratio | Nominal          | Cramer's V, phi   |
|                 |                  | Ordinal          | Kendall, Spearman correlation                                     |
|                 |                  | Interval / Ratio | Pearson product moment correlation, regression analysis           |

IN4304 Empirical Research Methods Spring 2010 Lecture 7

33



## Paired-sample t-test – Conceptual model

- **Conceptual model**
- Assumptions
- Example
- Interpretation outcome
- Demo



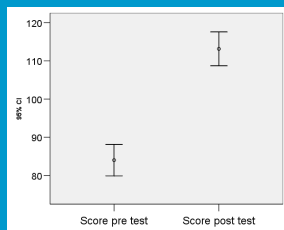
IN4304 Empirical Research Methods Spring 2010 Lecture 7

34



## Paired-sample t-test – example

- Conceptual model
- Assumptions
- **Example**
- Interpretation outcome
- Demo



IN4304 Empirical Research Methods Spring 2010 Lecture 7

35



## Paired-sample t-test – assumptions

- Conceptual model
  - **Assumptions**
  - Example
  - Interpretation outcome
  - Demo
1. Independence of observations
  2. Interval (or ratio) data
  3. Difference data are from a normally distributed population

IN4304 Empirical Research Methods Spring 2010 Lecture 7

36



## Paired-sample $t$ -test – interpretation outcomes

- Conceptual model
- Assumptions
- Example
- **Interpretation outcome**
- Demo

| Paired Samples Test |                                  |                    |                |                 |   |           |         |    |                 |
|---------------------|----------------------------------|--------------------|----------------|-----------------|---|-----------|---------|----|-----------------|
|                     |                                  | Paired Differences |                |                 | 95% Confidence Interval of the Difference |           | t       | df | Sig. (2-tailed) |
|                     |                                  | Mean               | Std. Deviation | Std. Error Mean | Lower                                     | Upper     |         |    |                 |
| Pair 1              | Score pre test - Score post test | -29.12088          | 22.02074       | 2.30640         | -33.70692                                 | -24.53484 | -12.615 | 0  | .000            |

IN4304 Empirical Research Methods Spring 2010 Lecture 7

37



TU Delft

## Paired-sample $t$ -test – SPSS Demo

- Conceptual model
- Assumptions
- Example
- Interpretation outcome
- **Demo**

File: Feedback experiment.sav  
Var: pre\_score, post\_score  
Note: Filter out

IN4304 Empirical Research Methods Spring 2010 Lecture 7

38



TU Delft

## Statistical test and Scales of measurement

| Aim             | Samples       | Data Level                             | Tests  |
|-----------------|---------------|--|--|
| Find difference | Single sample | Nominal<br>Ordinal<br>Interval / Ratio | Binominal test, $\chi^2$ goodness-of-fit<br>Wilcoxon signed-ranks test<br>$z$ -test, One-Sample $t$ -test                                |
|                 | Independent   | Nominal<br>Ordinal<br>Interval / Ratio | Fisher-Exact test, $\chi^2$<br>Mann-Whitney $U$ test<br>$z$ -test, two independent sample $t$ -test,<br><b>ANOVA, MANOVA</b>             |
| Dependent       |               | Nominal<br>Ordinal<br>Interval / Ratio | McNemar<br>Sign Test, Wilcoxon matched-pairs signed-rank test, Friedman Test<br>Paired-Sample $t$ -test, repeated measures ANOVA, MANOVA |
| Find relation   |               | Nominal<br>Ordinal<br>Interval / Ratio | Cramer's $V$ , phi<br>Kendall, Spearman correlation<br>Pearson product moment correlation, regression analysis                           |

IN4304 Empirical Research Methods Spring 2010 Lecture 7

39



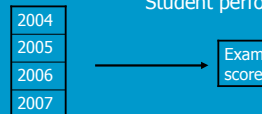
TU Delft

## One-way ANOVA – Conceptual model

- **Conceptual model**
- Assumptions
- Example
- Interpretation outcome
- posthoc
- Demo

Exam year

Student performance



IN4304 Empirical Research Methods Spring 2010 Lecture 7

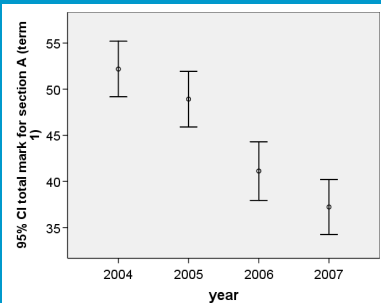
40



TU Delft

## One-way ANOVA – example

- Conceptual model
- Assumptions
- **Example**
- Interpretation outcome
- posthoc
- Demo



IN4304 Empirical Research Methods Spring 2010 Lecture 7

41



TU Delft

## One-way ANOVA – assumptions

- Conceptual model
  - **Assumptions**
  - Example
  - Interpretation outcome
  - posthoc
  - Demo
1. Independence of observations
  2. Interval (or ratio) data
  3. data are from a normally distributed population
  4. Homogeneity of variance

IN4304 Empirical Research Methods Spring 2010 Lecture 7

42



TU Delft

## One-way ANOVA – interpretation outcomes

- Conceptual model
- Assumptions
- Example
- **Interpretation outcome**
- posthoc
- Demo

| ANOVA                             |                |     |             |        |      |
|-----------------------------------|----------------|-----|-------------|--------|------|
| total mark for section A (term 1) |                |     |             |        |      |
|                                   | Sum of Squares | df  | Mean Square | F      | Sig. |
| Between Groups                    | 22481.424      | 3   | 7493.808    | 19.933 | .000 |
| Within Groups                     | 236000.9       | 628 | 375.941     |        |      |
| Total                             | 258572.3       | 631 |             |        |      |

IN4304 Empirical Research Methods Spring 2010 Lecture 7

43



## One-way ANOVA – Post-Hoc

- Conceptual model
- Assumptions
- Example
- Interpretation outcome
- **Post-hoc**
- Demo

| Multiple Comparisons                                  |          |                       |            |      |                         |             |
|---|----------|-----------------------|------------|------|-------------------------|-------------|
| Dependent Variable: total mark for section A (term 1) |          |                       |            |      |                         |             |
| Tukey HSD   |          |                       |            |      |                         |             |
| (I) year  | (J) year | Mean Difference (I-J) | Std. Error | Sig. | 95% Confidence Interval |             |
|   |          |                       |            |      | Lower Bound             | Upper Bound |
| 2004  | 2005     | 3.266                 | 2.181      | .440 | -2.25                   | 8.89        |
|   | 2006     | 11.057*               | 2.181      | .000 | 5.44                    | 16.68       |
|   | 2007     | 14.956*               | 2.181      | .000 | 9.34                    | 20.57       |
| 2005  | 2004     | -3.266                | 2.181      | .440 | -8.89                   | 2.35        |
|   | 2006     | 7.791*                | 2.181      | .002 | 2.17                    | 13.41       |

- Instead of separate t-tests, post-hoc test control for Type I error
- Keeps family-wise error rate down to 0.05
- Tukey's Honestly Significant Difference (HSD) test

IN4304 Empirical Research Methods Spring 2010 Lecture 7

44



## One-way ANOVA – SPSS Demo

- Conceptual model
- Assumptions
- Example
- Interpretation outcome
- Post-Hoc
- **Demo**

File: exam\_marks2004-2007\_equal\_year\_sample.sav  
Var: Year, t\_term1  
Tukey posthoc

IN4304 Empirical Research Methods Spring 2010 Lecture 7

45



## Statistical test and Scales of measurement

| Aim             | Samples          | Data Level  | Tests   |
|-----------------|------------------|---|---|
| Find difference | Single sample    | Nominal   | Binominal test, $\chi^2$ goodness-of-fit                          |
|                 |                  | Ordinal   | Wilcoxon signed-ranks test  |
|                 | Interval / Ratio | z-test, One-Sample t-test                               |   |
| Independent     | Independent      | Nominal   | Fisher-Exact test, $\chi^2$                                       |
|                 |                  | Ordinal   | Mann-Whitney U-test   |
|                 | Interval / Ratio | z-test, two independent sample t-test, ANOVA, MANOVA    |   |
| Dependent       | Dependent        | Nominal   | McNemar   |
|                 |                  | Ordinal   | Sign Test, Wilcoxon matched-pairs signed-rank test, Friedman Test |
|                 | Interval / Ratio | Paired-Sample t-test, repeated measures ANOVA, MANOVA   |   |
| Find relation   | Independent      | Nominal   | Cramer's V, phi   |
|                 |                  | Ordinal   | Kendall, Spearman correlation                                     |
|                 | Interval / Ratio | Pearson product moment correlation, regression analysis |   |

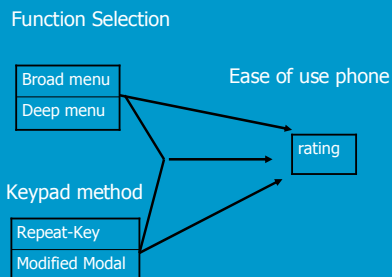
IN4304 Empirical Research Methods Spring 2010 Lecture 7

46



## Two-way ANOVA – Conceptual model

- **Conceptual model**
- Assumptions
- Example
- Interpretation outcome
- Demo



IN4304 Empirical Research Methods Spring 2010 Lecture 7

47



## Two-way ANOVA – assumptions

- Conceptual model
  - **Assumptions**
  - Example
  - Interpretation outcome
  - Demo
1. Independence of observations
  2. Interval (or ratio) data
  3. data are from a normally distributed population
  4. Homogeneity of variance

File: mobile Phone (Interaction with Computers)  
Var: Keypad, function, qamobile

IN4304 Empirical Research Methods Spring 2010 Lecture 7

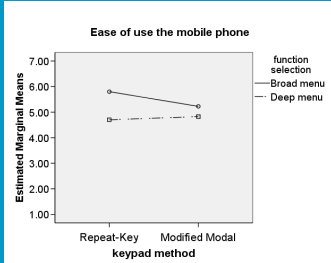
48





## Two-way ANOVA – example

- Conceptual model
- Assumptions
- **Example**
- Interpretation outcome
- Demo



IN4304 Empirical Research Methods Spring 2010 Lecture 7

49



## Two-way ANOVA – interpretation outcomes

- Conceptual model
- Assumptions
- Example
- **Interpretation outcome**
- Demo

Tests of Between-Subjects Effects

Dependent Variable: Average of questions about ease of use of the mobile phone

| Source            | Type III Sum of Squares | df | Mean Square | F        | Sig. |
|-------------------|-------------------------|----|-------------|----------|------|
| Corrected Model   | 14.713 <sup>a</sup>     | 3  | 4.904       | 5.094    | .003 |
| Intercept         | 2111.513                | 1  | 2111.513    | 2193.363 | .000 |
| keypad            | 1.013                   | 1  | 1.013       | 1.052    | .308 |
| function          | 11.250                  | 1  | 11.250      | 11.686   | .001 |
| keypad * function | 2.450                   | 1  | 2.450       | 2.545    | .115 |
| Error             | 73.164                  | 76 | .963        |          |      |
| Total             | 2199.389                | 80 |             |          |      |
| Corrected Total   | 87.876                  | 79 |             |          |      |

<sup>a</sup>. R Squared = .167 (Adjusted R Squared = .135)

IN4304 Empirical Research Methods Spring 2010 Lecture 7

50



## Two-way ANOVA – SPSS Demo

- Conceptual model
- Assumptions
- Example
- Interpretation outcome
- **Demo**

File: mp3playerSurvey.sav  
 Within factor: Component (4)  
 (1) playAvg  
 (2) FileAvg  
 (3) VolumeAvg  
 (4) InfAvg

IN4304 Empirical Research Methods Spring 2010 Lecture 7

51



## Statistical test and Scales of measurement

| Aim             | Samples          | Data Level  | Tests  |
|-----------------|------------------|---|--|
| Find difference | Single           | Nominal   | Binomial test, $\chi^2$ goodness-of-fit              |
|                 | sample           | Ordinal   | Wilcoxon signed-ranks test                           |
| Independent     | Interval / Ratio | Nominal   | z-test, One-Sample t-test                            |
|                 |                  | Ordinal   | Fisher-Exact test, $\chi^2$                          |
|                 | Interval / Ratio | Nominal   | Mann-Whitney U-test                                  |
|                 |                  | Ordinal   | z-test, two independent sample t-test, ANOVA, MANOVA |
| Dependent       | Nominal          | McNemar   |  |
|                 | Ordinal          | Sign Test, Wilcoxon matched-pairs signed-rank test, Friedman Test |  |
|                 | Interval / Ratio | Paired-Sample t-test, repeated measures ANOVA, MANOVA             |  |
| Find relation   | Nominal          | Cramer's $\chi^2$ test  |  |
|                 | Ordinal          | Kendall, Spearman correlation                                     |  |
|                 | Interval / Ratio | Pearson product moment correlation, regression analysis           |  |

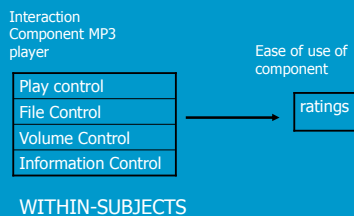
IN4304 Empirical Research Methods Spring 2010 Lecture 7

52



## ANOVA with repeated measures – Conceptual model

- **Conceptual model**
- Assumptions
- Example
- Interpretation outcome
- Demo



IN4304 Empirical Research Methods Spring 2010 Lecture 7

53



## ANOVA with repeated measures – assumptions

- Conceptual model
  - **Assumptions**
  - Example
  - Interpretation outcome
  - Demo
1. Independence of observations
  2. Interval (or ratio) data
  3. data are from a normally distributed population
  4. Sphericity (1. homogeneity of variance, 2. variances of the differences between levels are similar to one another)

IN4304 Empirical Research Methods Spring 2010 Lecture 7

54



### ANOVA with repeated measures - example

- Conceptual model
- Assumptions
- Example
- Interpretation outcome
- Demo

(95% confidence interval)

Low - High usability rating

Average score Fly Control    Average score File Control    Average score Volume Control    Average score Information Control

5.29 Out of point

IN4304 Empirical Research Methods Spring 2010 Lecture 7 55

### ANOVA with repeated measures - interpretation outcomes

- Conceptual model
- Assumptions
- Example
- Interpretation outcome**
- Demo

Mauchly's Test of Sphericity

| Measure: MEASURE_1               | Approx. Chi-Square | df    | Sig. |
|----------------------------------|--------------------|-------|------|
| Within Subjects Effect component | .836               | 5,673 | .340 |

Tests of Within-Subjects Effects

| Source           | Type III Sum of Squares | df      | Mean Square | F       | Sig.   |      |
|------------------|-------------------------|---------|-------------|---------|--------|------|
| component        | Sphericity Assumed      | 336.948 | 3           | 112.316 | 67.363 | .000 |
|                  | Greenhouse-Geisser      | 336.948 | 2.727       | 123.553 | 67.363 | .000 |
|                  | Huynh-Feldt             | 336.948 | 2.997       | 112.434 | 67.363 | .000 |
|                  | Lower-bound             | 336.948 | 1.000       | 336.948 | 67.363 | .000 |
| Error(component) | Sphericity Assumed      | 165.066 | 99          | 1.667   |        |      |

IN4304 Empirical Research Methods Spring 2010 Lecture 7 56

### ANOVA with repeated measures - SPSS Demo

- Conceptual model
- Assumptions
- Example
- Interpretation outcome
- Demo**

File: mobile phone (IwC)  
Var: function (IV), DV: tokey, Tot\_time, qamobile

IN4304 Empirical Research Methods Spring 2010 Lecture 7 57

### Statistical test and Scales of measurement

| Aim             | Samples          | Data Level  | Tests   |
|-----------------|------------------|---|---|
| Find difference | Single sample    | Nominal   | Binomial test, $\chi^2$ goodness-of-fit                           |
|                 |                  | Ordinal   | Wilcoxon signed-ranks test  |
|                 | Interval / Ratio | Nominal   | z-test, One-Sample t-test   |
|                 |                  | Ordinal   | Fisher-Exact test, $\chi^2$                                       |
| Find relation   | Independent      | Nominal   | Mann-Whitney U test   |
|                 |                  | Interval / Ratio  | z-test, two independent sample t-test, ANOVA, MANOVA              |
|                 | Dependent        | Nominal   | McNemar   |
|                 |                  | Ordinal   | Sign Test, Wilcoxon matched-pairs signed-rank test, Friedman Test |
| Find relation   | Interval / Ratio | Paired-Sample t-test, repeated measures ANOVA, MANOVA   |   |
|                 | Nominal          | Cramer's V, phi   |   |
| Find relation   | Ordinal          | Kendall, Spearman correlation                           |   |
|                 | Interval / Ratio | Pearson product moment correlation, regression analysis |   |

IN4304 Empirical Research Methods Spring 2010 Lecture 7 58

### MANOVA - Conceptual model

- Conceptual model
- Assumptions
- Example
- Interpretation outcome
- Demo

Usability

Function Selection

Broad menu    Deep menu

Number of keystrokes

Task time

Subjective ease of use

IN4304 Empirical Research Methods Spring 2010 Lecture 7 59

### MANOVA - example

- Conceptual model
- Assumptions
- Example
- Interpretation outcome
- Demo

Number of Keystrokes

Task time

Ease of Use

IN4304 Empirical Research Methods Spring 2010 Lecture 7 60

## MANOVA – assumptions

- Conceptual model
- **Assumptions**
- Example
- Interpretation outcome
- Demo

1. Independence of observations
2. Interval (or ratio) data
3. Multivariate normality\*
4. Homogeneity of covariance matrices\*

\*(see Fields, 2005, p.593 for checking assumptions)

IN4304 Empirical Research Methods Spring 2010 Lecture 7

61



## MANOVA – interpretation outcomes

- Conceptual model
- Assumptions
- Example
- **Interpretation outcome**

| Multivariate Tests <sup>b</sup> |                    |        |                       |               |          |      |
|---------------------------------|--------------------|--------|-----------------------|---------------|----------|------|
| Effect                          |                    | Value  | F                     | Hypothesis df | Error df | Sig. |
| Intercept                       | Pillai's Trace     | .981   | 1328.630 <sup>a</sup> | 3.000         | 76.000   | .000 |
|                                 | Wilks' Lambda      | .019   | 1328.630 <sup>a</sup> | 3.000         | 76.000   | .000 |
|                                 | Hotelling's Trace  | 52.446 | 1328.630 <sup>a</sup> | 3.000         | 76.000   | .000 |
|                                 | Roy's Largest Root | 52.446 | 1328.630 <sup>a</sup> | 3.000         | 76.000   | .000 |
| function                        | Pillai's Trace     | .323   | 12.078 <sup>a</sup>   | 3.000         | 76.000   | .000 |
|                                 | Wilks' Lambda      | .677   | 12.078 <sup>a</sup>   | 3.000         | 76.000   | .000 |
|                                 | Hotelling's Trace  | .477   | 12.078 <sup>a</sup>   | 3.000         | 76.000   | .000 |
|                                 | Roy's Largest Root | .477   | 12.078 <sup>a</sup>   | 3.000         | 76.000   | .000 |

IN4304 Empirical Research Methods Spring 2010 Lecture 7

62



## MANOVA – SPSS Demo

- Conceptual model
- Assumptions
- Example
- Interpretation outcome
- **Demo**

IN4304 Empirical Research Methods Spring 2010 Lecture 7

63



## Summary

### Idea behind hypothesis testing

- Is the difference between two samples a reflection of the difference of two different populations or simply caused by sampling error?

### Conceptual models with specific statistical tests

- Different tests depending on: level, number of independent and dependent variables, between or within subjects set up

### Statistical tests in SPSS

- See the recording of this lecture

IN4304 Empirical Research Methods Spring 2010 Lecture 7

64



## This week in practicum

Working on project coursework

- Chi-square,
- Error-bars,
- One-sample t-test,
- independent-sample t-test,
- paired-sample t-test,
- Mann-Whitney U test

IN4304 Empirical Research Methods Spring 2010 Lecture 7

65



## Next time

### Week 4.1 (20/4/2010) Quantitative Data analysis II - Relations

- Correlation
- Regression
- (Robson ch. 13)

EWI lecture room B, Tuesday 15:45 - 17:45

IN4304 Empirical Research Methods Spring 2010 Lecture 7

66



## References

- Coolican, H., (2004). *Research methods and statistics in psychology* (4<sup>th</sup> ed). London, UK: Hodder Arnold.
- Fields, A. (2005). *Discovering statistics using SPSS* (2<sup>nd</sup> ed). London: UK, Sage.

IN4304 Empirical Research Methods Spring 2010 Lecture 7

67

